

November 12th 2024

Pizza Seminar 2024  
University of Texas at Austin, TX

# Free-streaming neutrinos & the cosmic microwave background

Gabriele Montefalcone

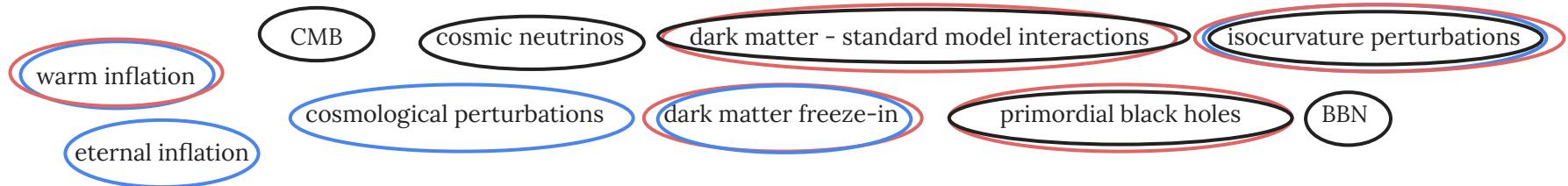
Weinberg Institute for Theoretical Physics, University of Texas at Austin



# My Research Journey at UT

## MY RESEARCH INTERESTS:

primordial cosmology - cosmological probes to constrain fundamental physics - the dark sector



## MY COLLABORATORS AT UT:



Prof. Katherine Freese



Dr. Barmak Shams



Dr. Evangelos Sfikanakis



Prof. Kimberly Boddy



Dr. Subhajit Ghosh



Dr. Gilly Elor



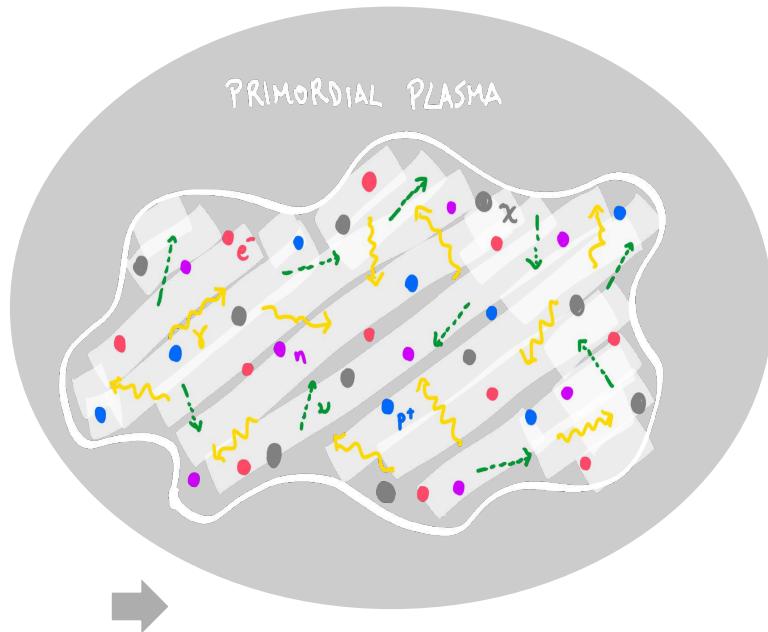
Joshua Ziegler

Jonathan Lozano

Robert Everett

# The Big Picture

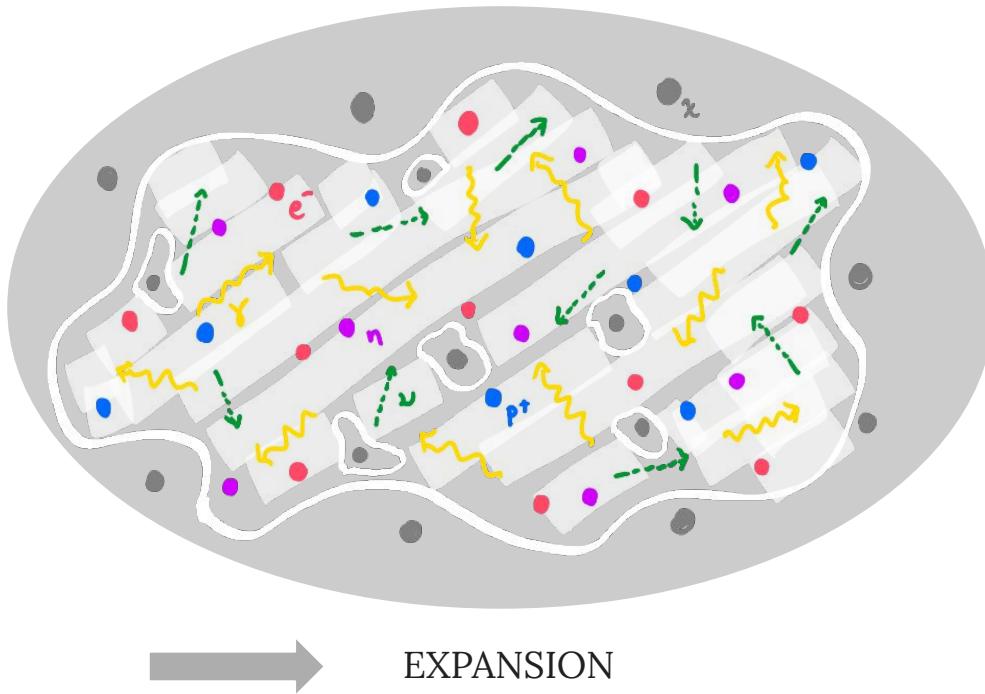
## The Hot Big Bang



All SM particles species\* are in thermal equilibrium at a temperature  $T$

\*possibly even dark matter

# The Big Picture



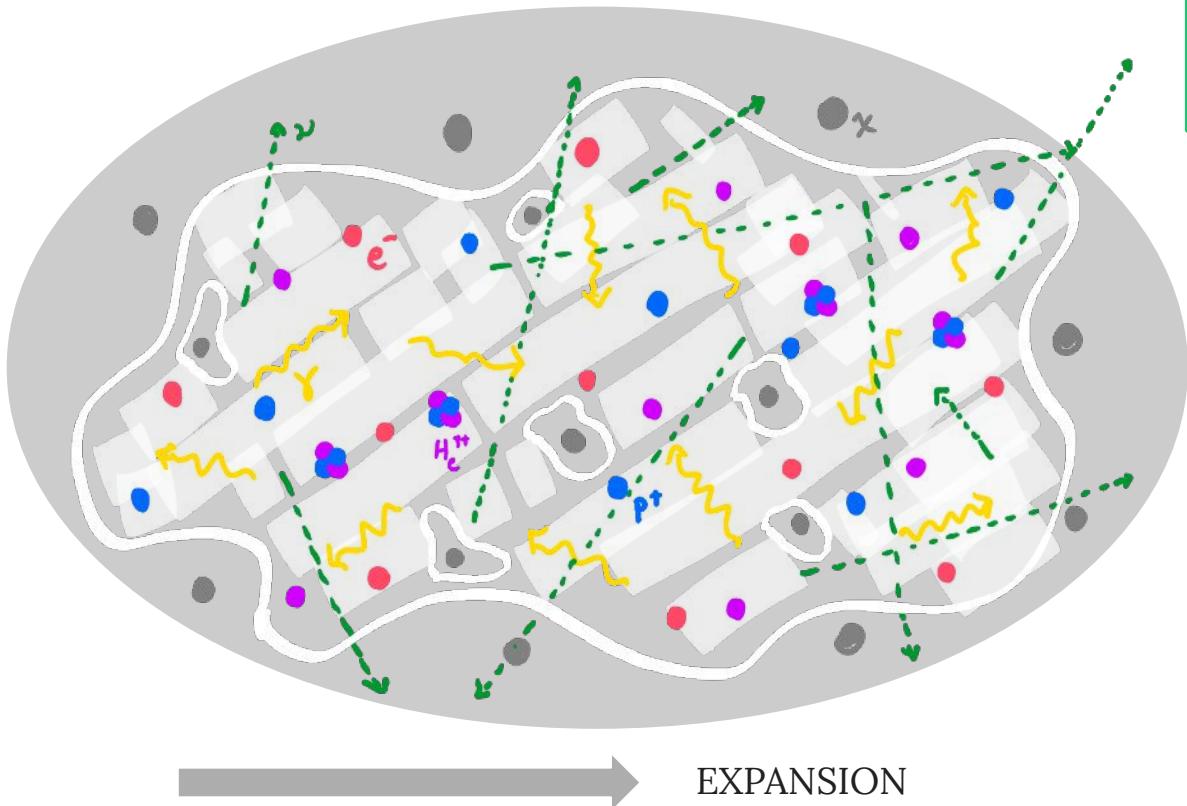
$$(T_{\text{dec}}) \approx H(T_{\text{dec}})$$

interaction rate      expansion rate

As the Universe expands, it **cools** and different species **decouple** from the primordial plasma

- The first one to go is dark matter

# The Big Picture



$$(T_{\text{dec}}) \approx H(T_{\text{dec}})$$

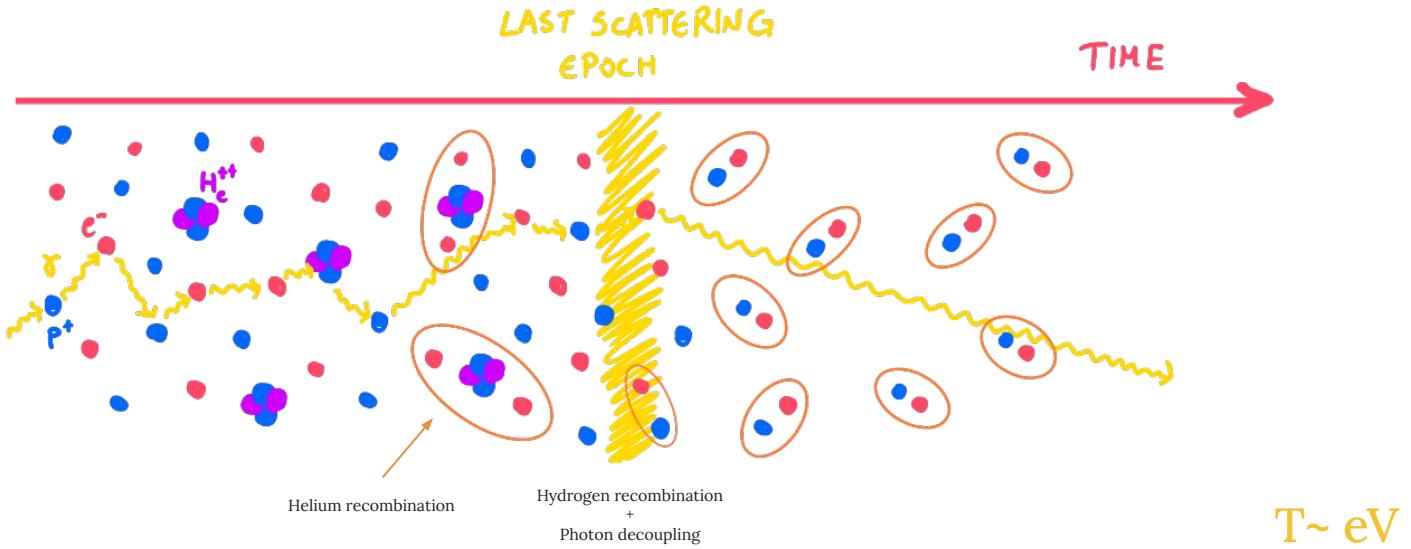
interaction rateexpansion rate

Then **neutrinos decouple**, and shortly after **nuclei form** in the process known as Big Bang Nucleosynthesis

- Mainly  ${}^4\text{He}$
- Also  ${}^3\text{He}$ ,  ${}^2\text{H}$ ,  ${}^7\text{Li}$

**T ~ MeV**

# The Big Picture



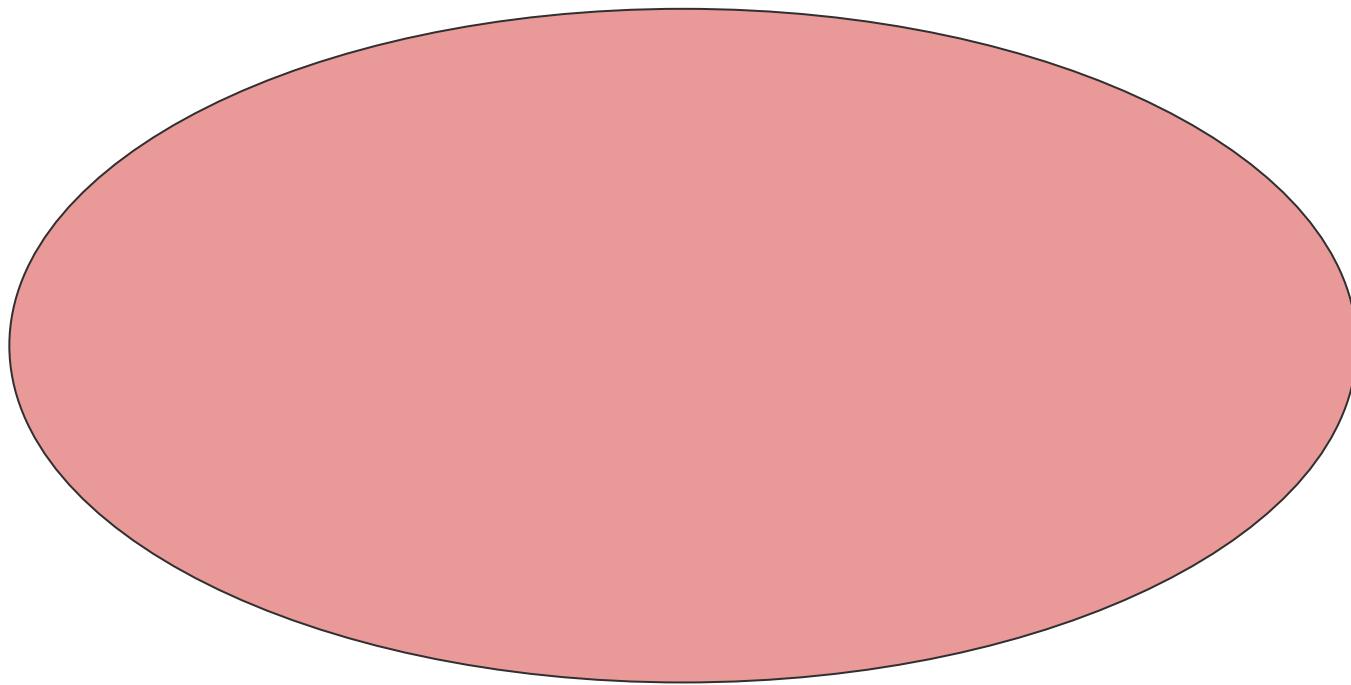
Once the universe is cool enough for neutral Hydrogen to form,  
photons are finally free to travel across the universe, reaching us today

EXPANSION

If the **Big Bang picture** is correct, we expect the universe  
to be filled by a **Cosmic Background** of photons,  
all roughly at the **same temperature**.

# The Cosmic Microwave Background

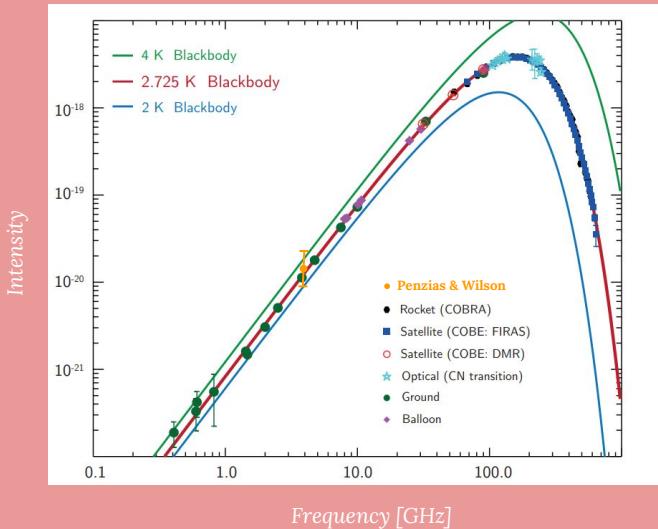
An almost perfect black-body spectrum at a temperature of  $T_0 = 2.7255 \text{ K}$  today



# The Cosmic Microwave Background

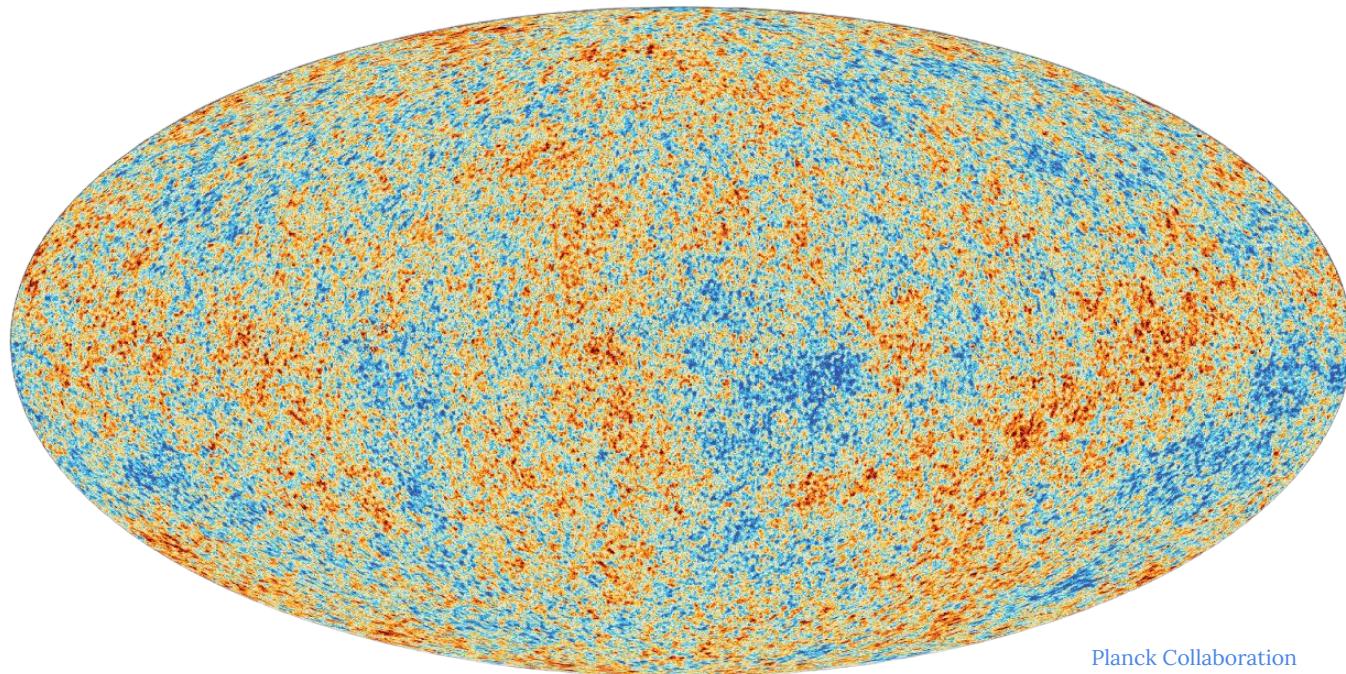
An almost perfect black-body spectrum at a temperature of  $T_0 = 2.7255 \text{ K}$  today

- Discovered by Penzias & Wilson (1965)
- First spectrum measurement by the **COBE FIRAS** instrument (1990)



# The Cosmic Microwave Background

Small temperature anisotropies in the order of  $\Delta T/T \sim 10^{-4}$



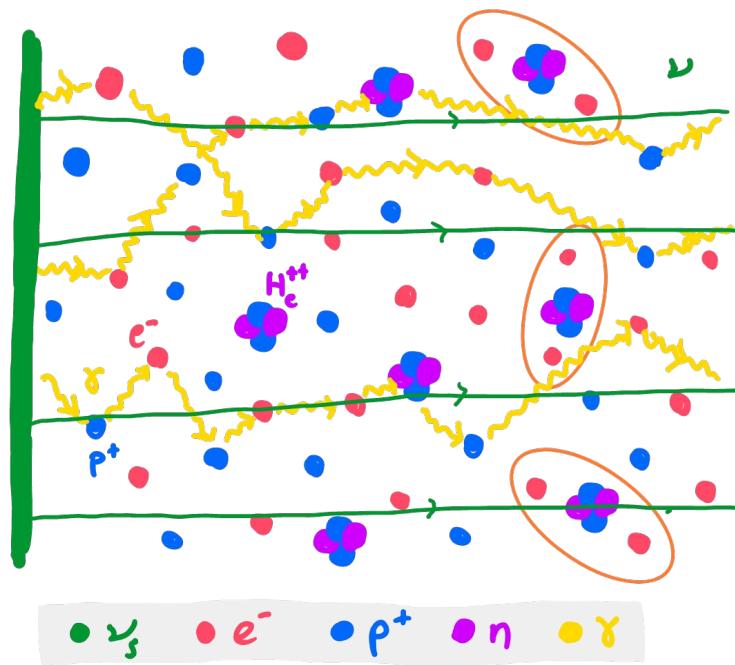
Planck Collaboration

# Neutrinos & the CMB

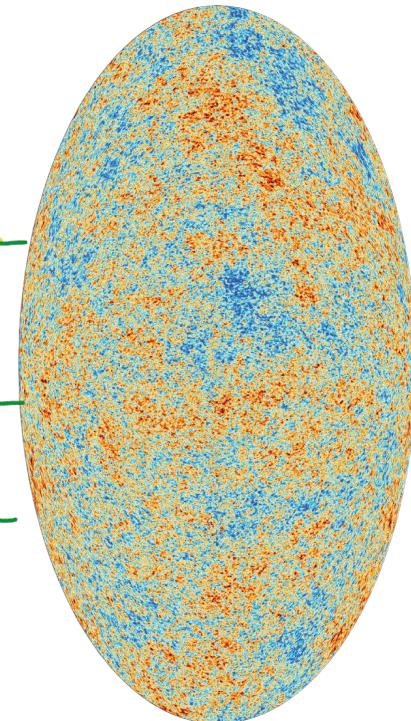
Small temperature anisotropies in the order of  $\Delta T/T \sim 10^{-4}$

- Significant fraction of **energy density** in neutrinos
- **Free-streaming** since their decoupling at  $t \sim 1$  s

Cosmic Neutrino Background



$\Delta T/T \sim 10^{-4}$



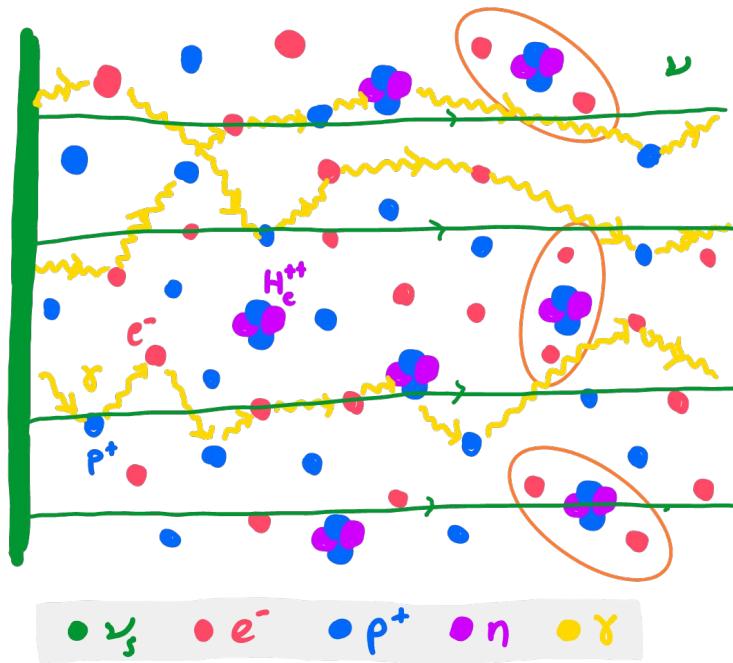
# Neutrinos & the CMB

The background radiation associated with the **decoupling** of photons from the primordial plasma

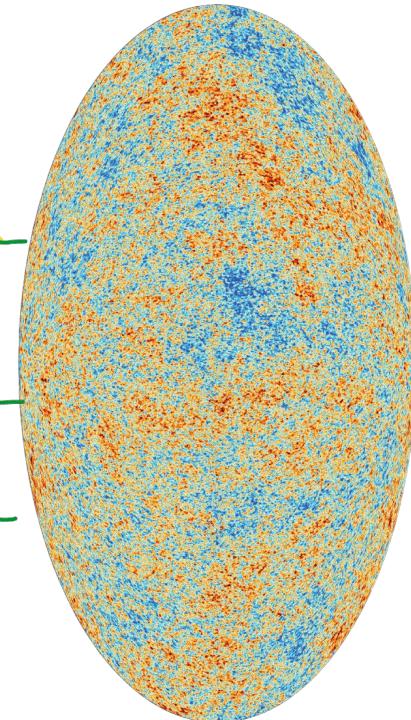
- Significant fraction of **energy density** in neutrinos
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Can we detect this?

Cosmic Neutrino Background



$$\Delta T/T \sim 10^{-4}$$

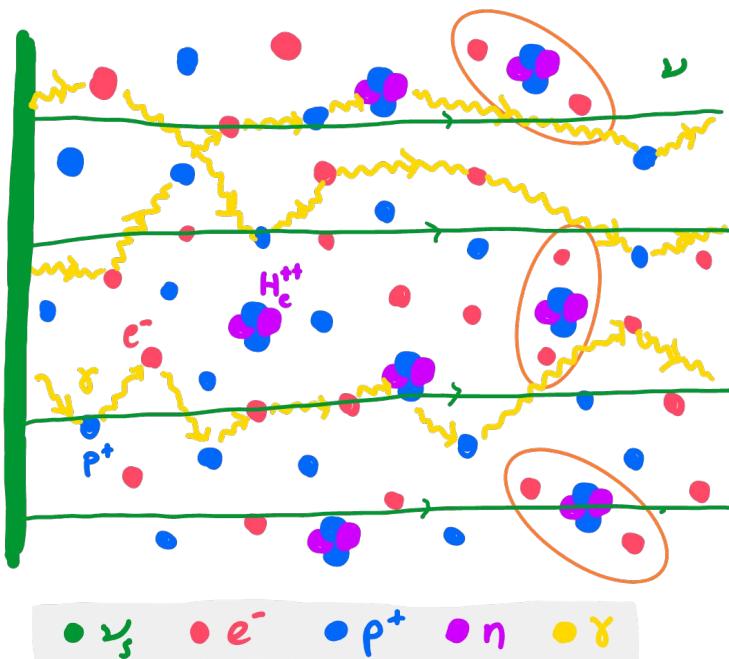


# Neutrinos & the CMB

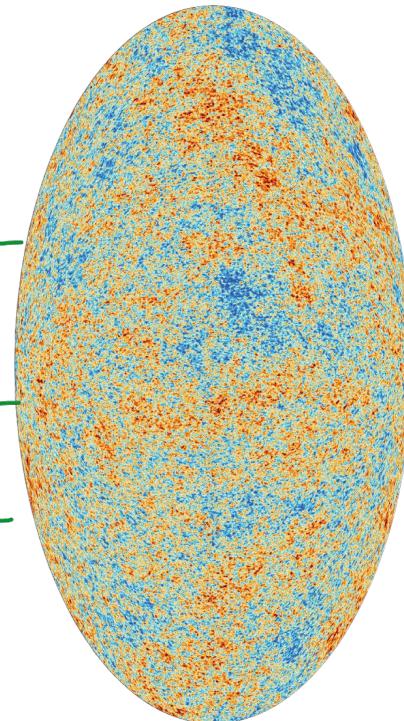
The background radiation associated with the **decoupling** of photons from the primordial plasma

- Significant fraction of **energy density** in neutrinos
  - **Free-streaming** since their decoupling at  $t \sim 1$  s
- Can we detect this?
- Neutrino masses  $m_\nu$ ?  
no detection but **unimportant** in the early universe

Cosmic Neutrino Background

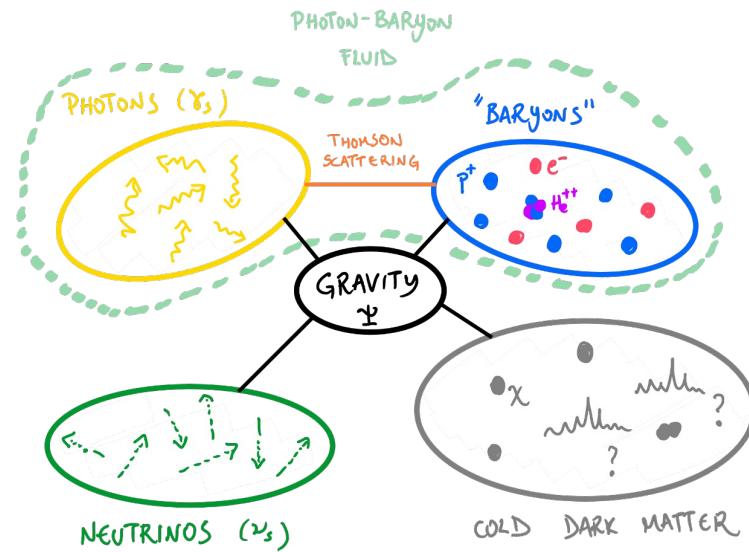


$$\Delta T/T \sim 10^{-4}$$



# Cosmic sound waves

- Photons and baryons are **tightly coupled**
- **Initial fluctuations** excited sound waves in the primordial plasma
- **Gravity** sources the fluctuations in the photon-baryon fluid



$$\ddot{\delta}_\gamma - c_\gamma^2 \nabla^2 \delta_\gamma = \nabla^2 \Psi_+$$

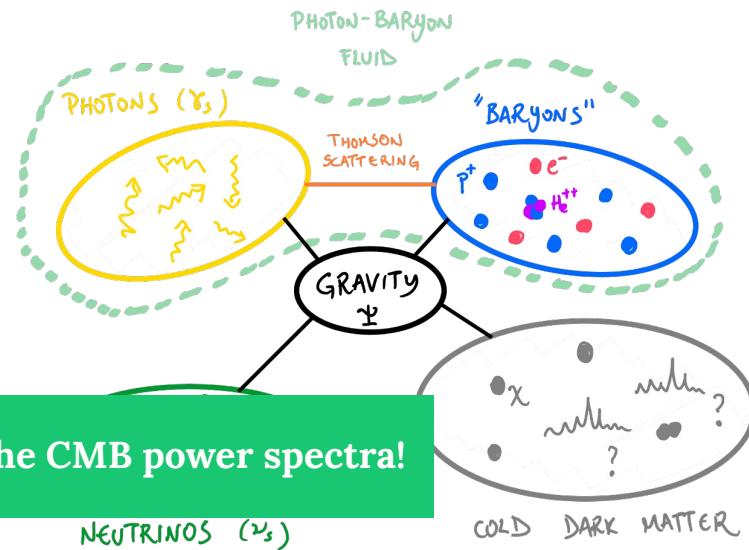
$\underbrace{\hspace{100px}}$   
Photon Pressure
 $\underbrace{\hspace{100px}}$   
Gravity

$$\delta_\gamma \sim \underbrace{A_{\vec{k}}}_{\text{Initial condition (inflation)}} \cos(c_s k \tau),$$

$$c_s^2 \sim \frac{c^2}{3(1 + R_b)} \} R_b \equiv 3\bar{\rho}_b/(4\bar{\rho}_\gamma) \quad \text{Baryons add inertia to the fluid}$$

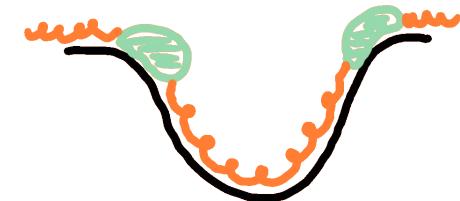
# Cosmic sound waves

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- **Gravity** We observe these acoustic oscillations in the CMB power spectra!



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$\underbrace{\phantom{...}}_{\text{Photon Pressure}}$ 
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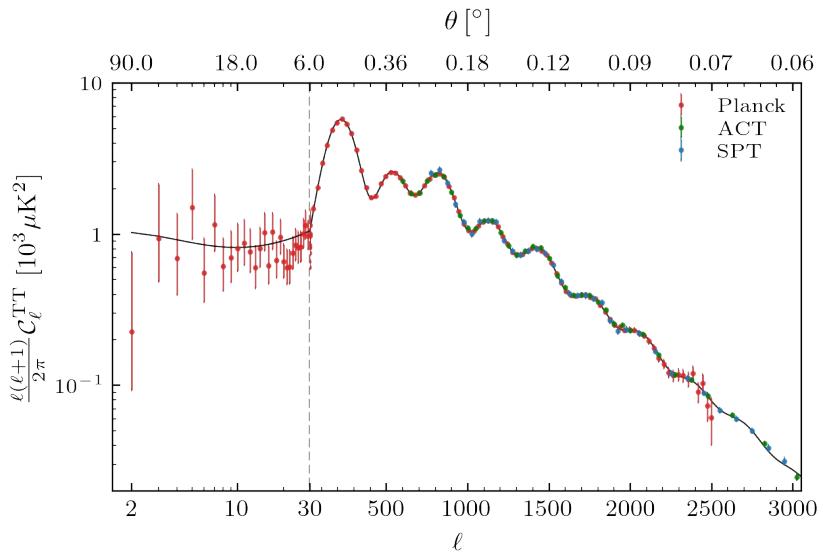


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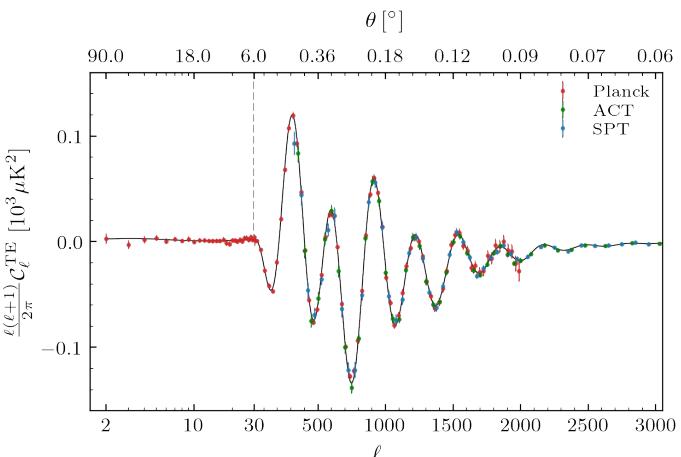
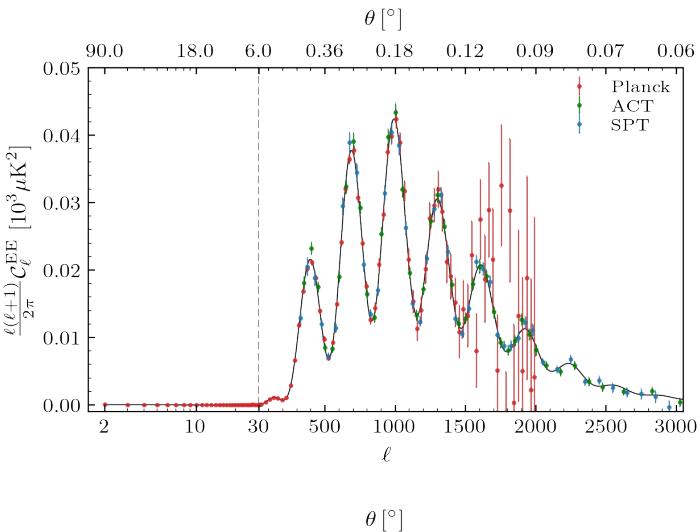
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# The CMB power spectra

Temperature spectrum traces **density** perturbations,  
roughly the gravitational potential



TE spectrum roughly tells us how the plasma is moving into the gravitational potential wells



# Cosmic neutrinos

- 41% of the radiation density in the universe
- Parametrized by the observable  $N_{\text{eff}}$ , known as *the effective number of relativistic species*
  - In the SM,  $N_{\text{eff}} = 3.044$  [Akita1, Yamaguchi \(2020\)](#)
- Cosmology is sensitive to their gravitational effects
  - CMB measurements are **consistent with SM value** of  $N_{\text{eff}}$

$$\rho_r = \rho_\gamma \left( 1 + \underbrace{\frac{7}{8} \left( \frac{4}{11} \right)^{\frac{4}{3}} N_{\text{eff}} }_{\text{Neutrino contribution}} \right)$$

$$N_{\text{eff}} = 2.92 \pm 0.18$$

Planck 2018

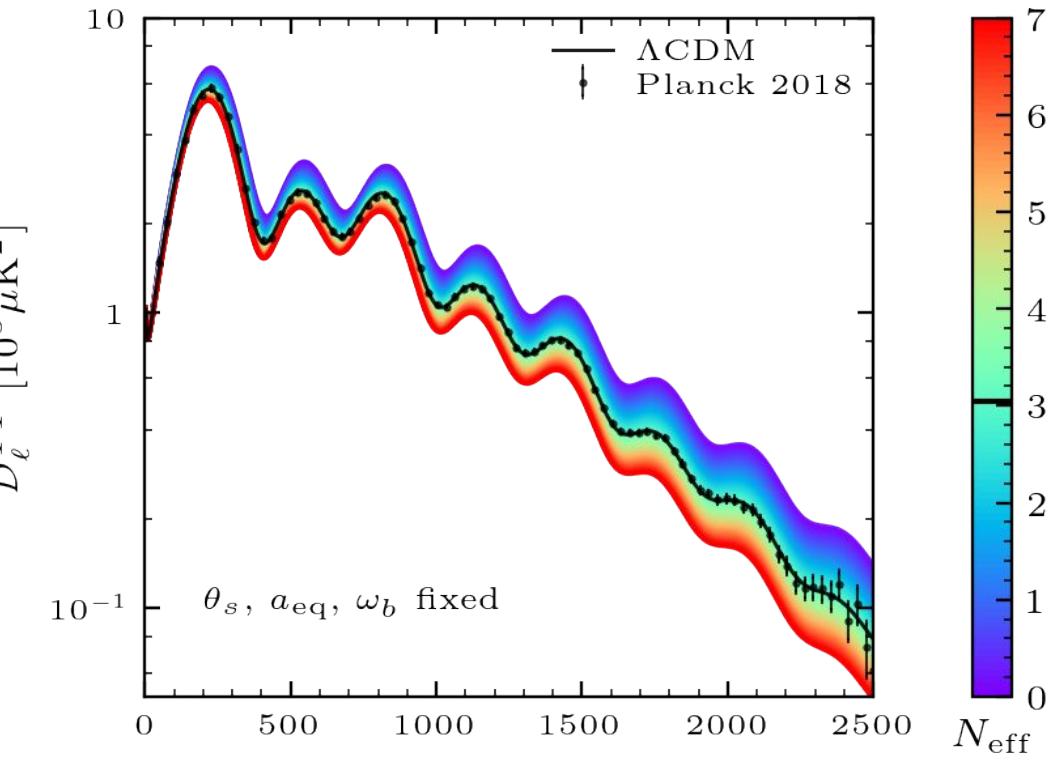
# Cosmic neutrinos in the CMB energy density

- Main effect in the damping tail of the CMB TT power spectrum, via their effect on the expansion rate

$$\theta_d \propto (H/n_e)^{1/2} \theta_s$$

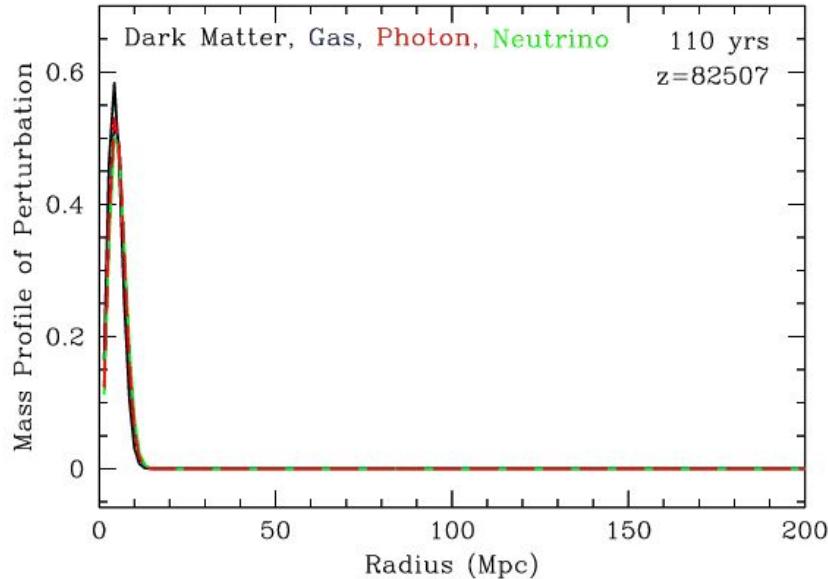
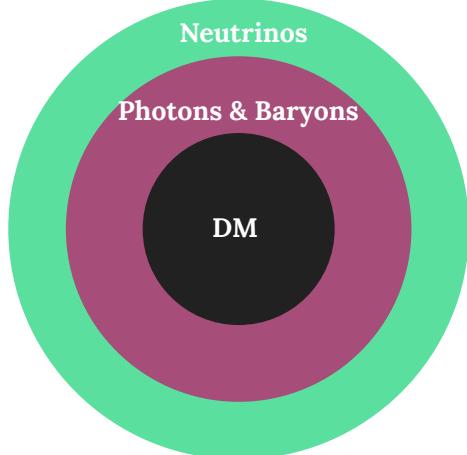
- For fixed  $a_{\text{eq}}$  and  $\theta_s$ , **larger  $N_{\text{eff}}$  means more damping**

$$\mathcal{D}_\ell^{XY} \equiv \frac{\ell(\ell+1)}{2\pi} \mathcal{C}_\ell^{XY}$$



# Cosmic neutrinos in the CMB free-streaming nature

- Perturbations from free-streaming neutrinos induce **metric perturbations ahead of the sound horizon**
- The photon-baryon fluid is **pulled** by such perturbations, shifting their perturbations peaks to larger radii.



Eisenstein, Seo and White

# Cosmic neutrinos in the CMB free-streaming nature

- This results in a **phase shift in the acoustic peaks of the CMB**

Bashinsky & Seljak (2003)

- Larger radii  $\rightarrow$  smaller multipoles
- Small effect, prop. to:  $\epsilon_\nu \equiv \rho_\nu / \rho_r$

- Difficult to reproduce in the absence of **free-streaming**

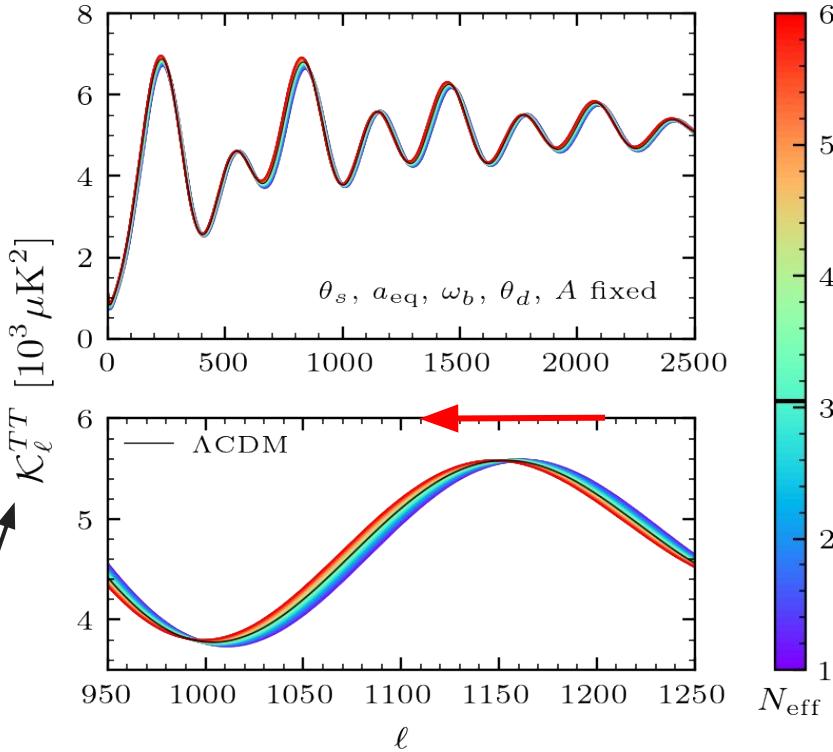
- Either free-streaming or non-adiabatic fluctuations

Baumann, Green, Meyers & Wallisch (2015)

$$\mathcal{K}_\ell^{XY} \equiv \frac{\ell(\ell+1)}{2\pi} \mathcal{C}_\ell^{XY} \exp \{a(\ell\theta_d)^\kappa\}$$

Undamped temperature power spectrum

$$\delta_\gamma(\vec{k}) \approx A(\vec{k}) \cos(kr_s + \phi)$$



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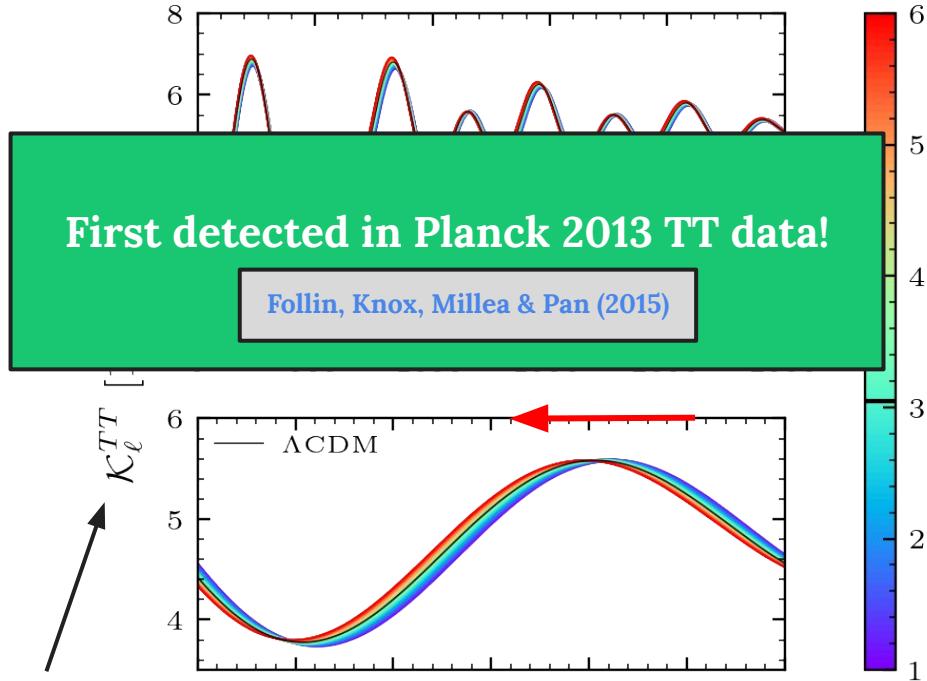
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First detected in Planck 2013 TT data!

Follin, Knox, Millea & Pan (2015)

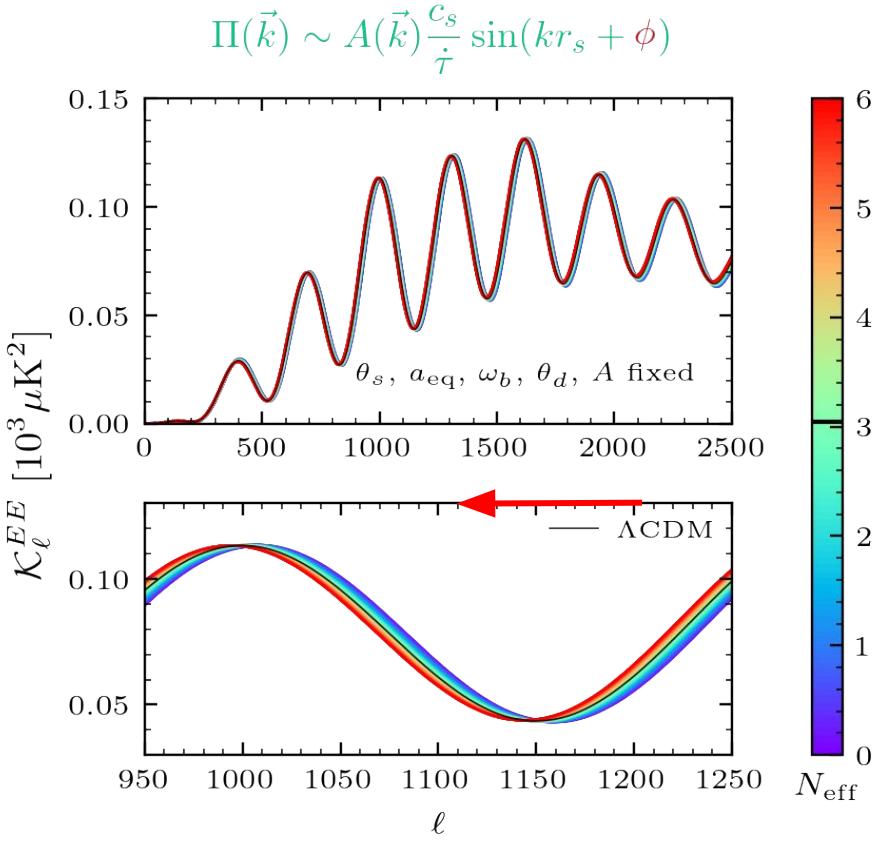
# Cosmic neutrinos in the CMB free-streaming nature

- Same shift both in temperature and polarization spectrum

$$\Pi(k, \eta) \sim \frac{d}{d\eta} \delta_\gamma(k, \eta)$$

- polarization provides cleaner signal

$$\mathcal{K}_\ell^{XY} \equiv \frac{\ell(\ell+1)}{2\pi} \mathcal{C}_\ell^{XY} \exp \{a(\ell\theta_d)^\kappa\}$$



# The phase shift in the CMB power spectra

Following Follin, Knox, Millea & Pan (2015)

- A new parameter to control the shift

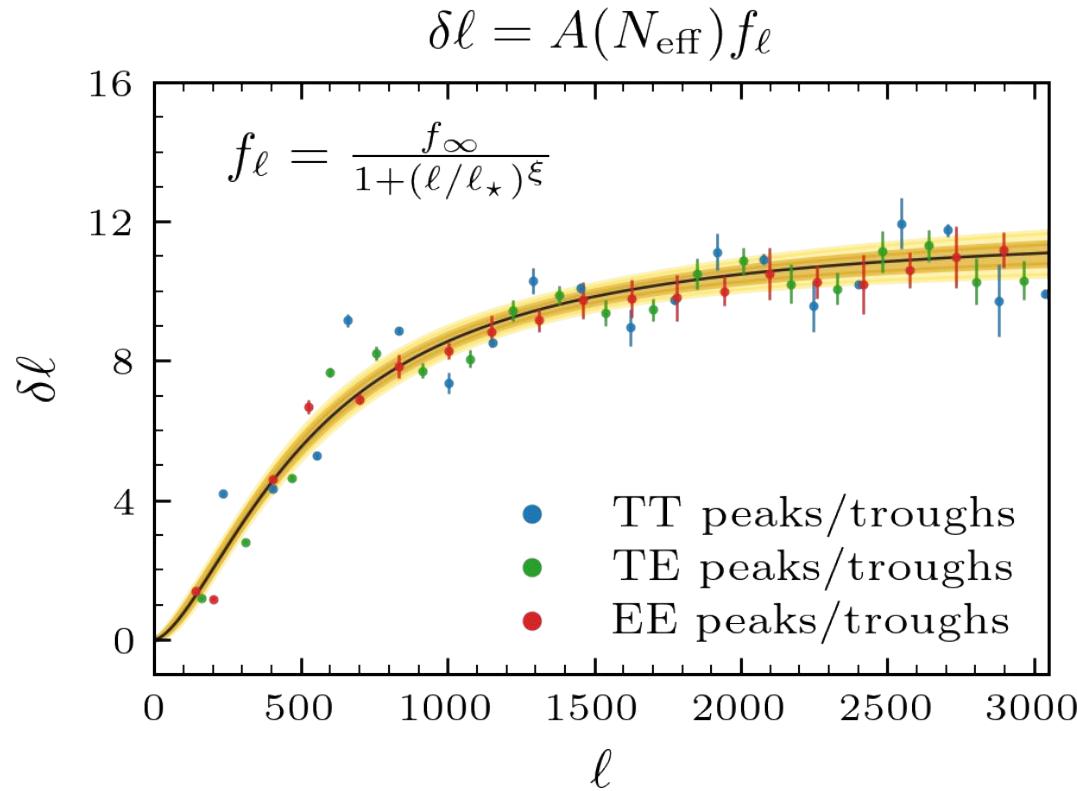
$$N_{\text{eff}}^{\delta\ell}$$

$$\delta\ell = \left[ A(N_{\text{eff}}^{\delta\ell}) - A(N_{\text{eff}}) \right] f_\ell$$

$$\mathcal{C}_\ell \rightarrow \mathcal{C}_{\ell+\delta\ell}$$

## Our Contributions:

- A new analytic form of the template
- Test with both temperature and polarization data



# Phase-shift constraints spectrum-based analysis

- Based on Planck 2013 temperature only:

$$N_{\text{eff}}^{\delta\ell} = 2.3^{+1.1}_{-0.4} \quad \text{Follin et al. (2015)}$$

$( N_{\text{eff}} = N_{\nu} = 3.044 )$

- Work in Progress (preliminary)

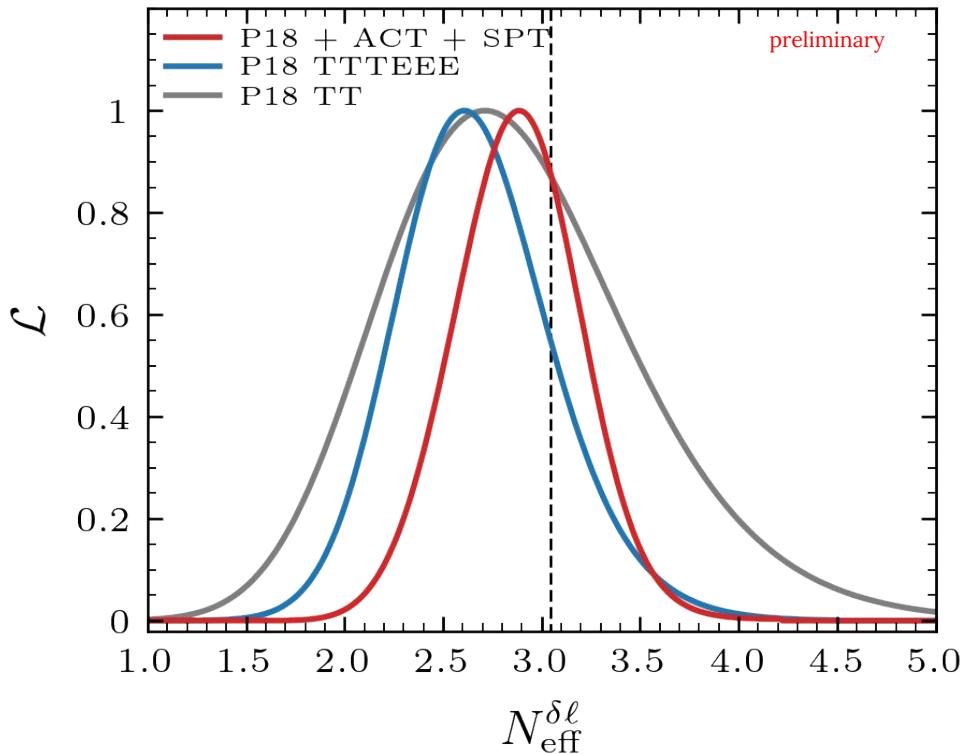
- Planck 2018 TT only:  $N_{\text{eff}}^{\delta\ell} = 2.9^{+0.7}_{-0.6}$

- Including polarization:

**Planck 2018:**  $N_{\text{eff}}^{\delta\ell} = 2.7^{+0.5}_{-0.4}$

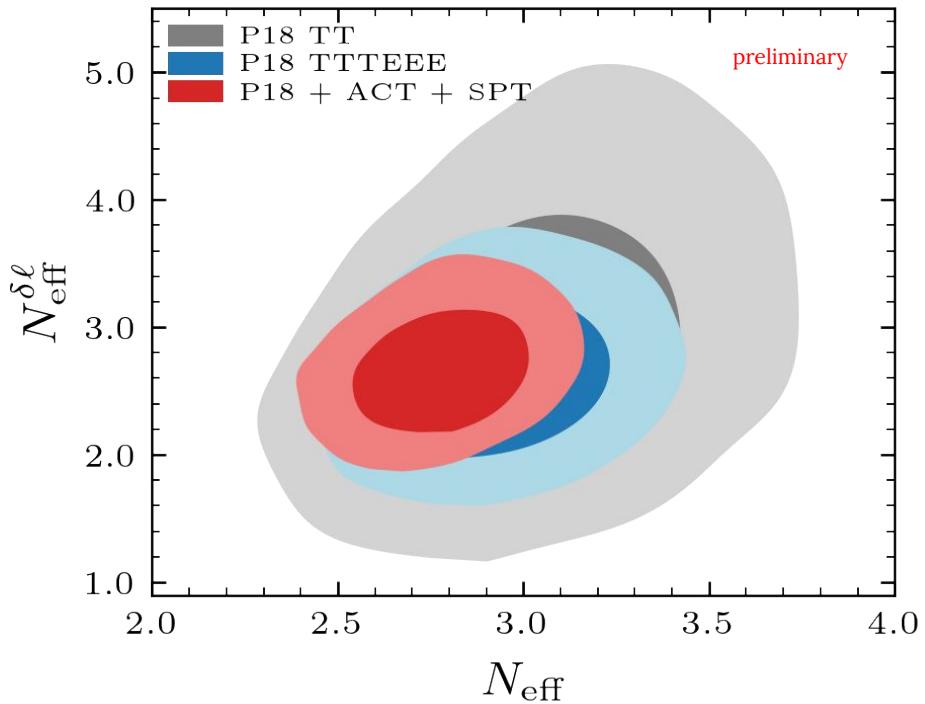
**+ ACT + SPT:**  $N_{\text{eff}}^{\delta\ell} = 2.9^{+0.3}_{-0.3}$

$( N_{\text{eff}} = N_{\nu} = 3.044 )$



# Phase-shift constraints spectrum-based analysis

- Strong evidence of **free-streaming nature** of neutrinos
- Current CMB data is compatible with the **Standard Model** prediction for free-streaming neutrinos



# Main Takeaways

- The CMB is consistent with **a black-body spectrum** at a temperature of **2.7255 K**, providing strong evidence that the early universe was in **near-perfect thermal equilibrium**, thereby confirming the Big Bang Theory.
- The **patterns of fluctuations** in the CMB encode a wealth of information about the **universe's composition** and the physics that governed its **evolution**
- **Neutrinos** leave a sizable **gravitational imprint** in the CMB, which we can use to **constrain their properties**
  - The **phase shift** is a robust probe of **free-streaming neutrinos**
  - Current data are **compatible** with the **Standard Model**, constraining non-standard neutrino physics.

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Grazie per l'attenzione!



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# Back-up Slides

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Gabriele Montefalcone

Weinberg Institute for Theoretical Physics, University of Texas at Austin

# Cosmic timeline

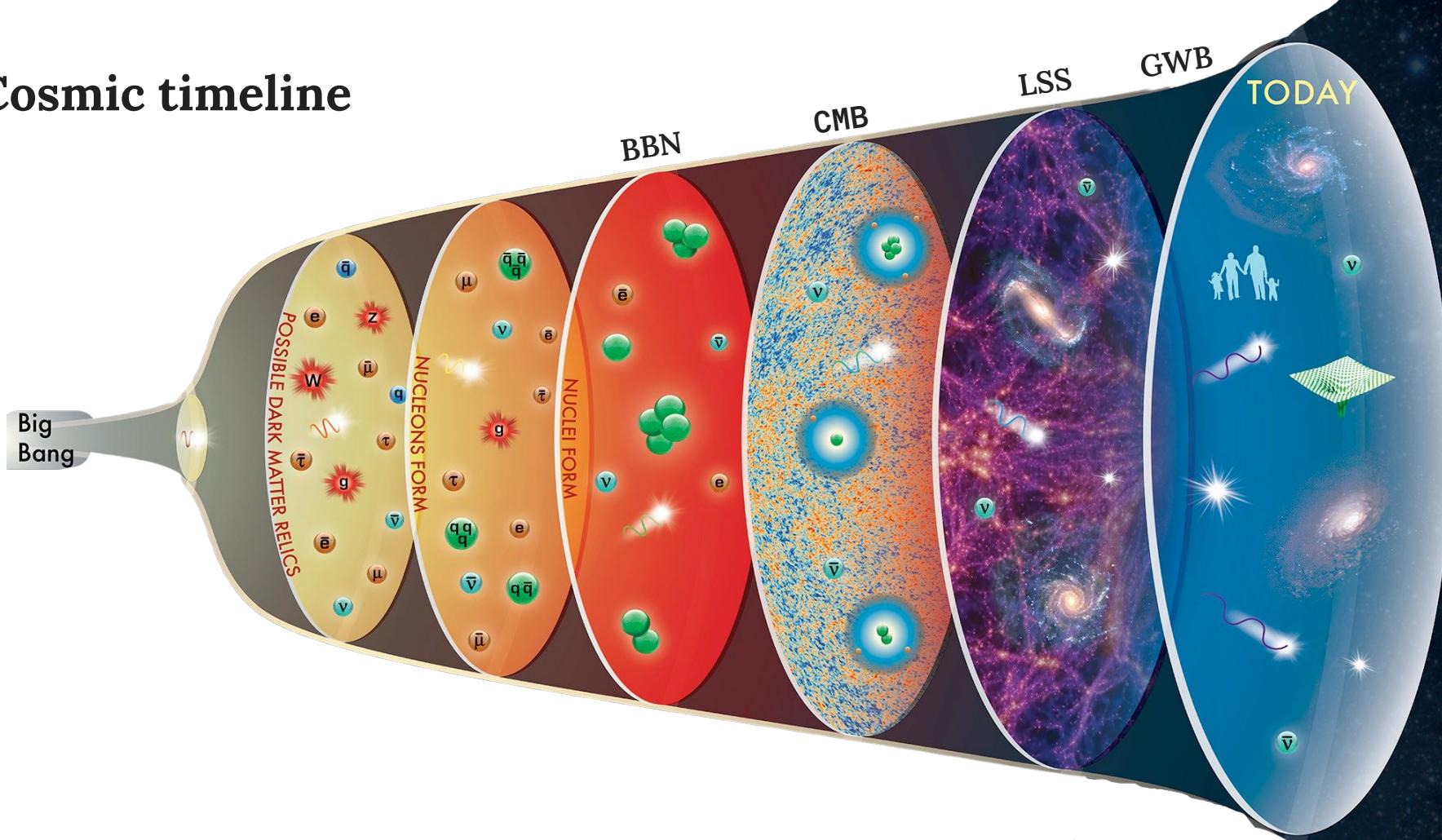


Figure from PDG

# Cosmic timeline

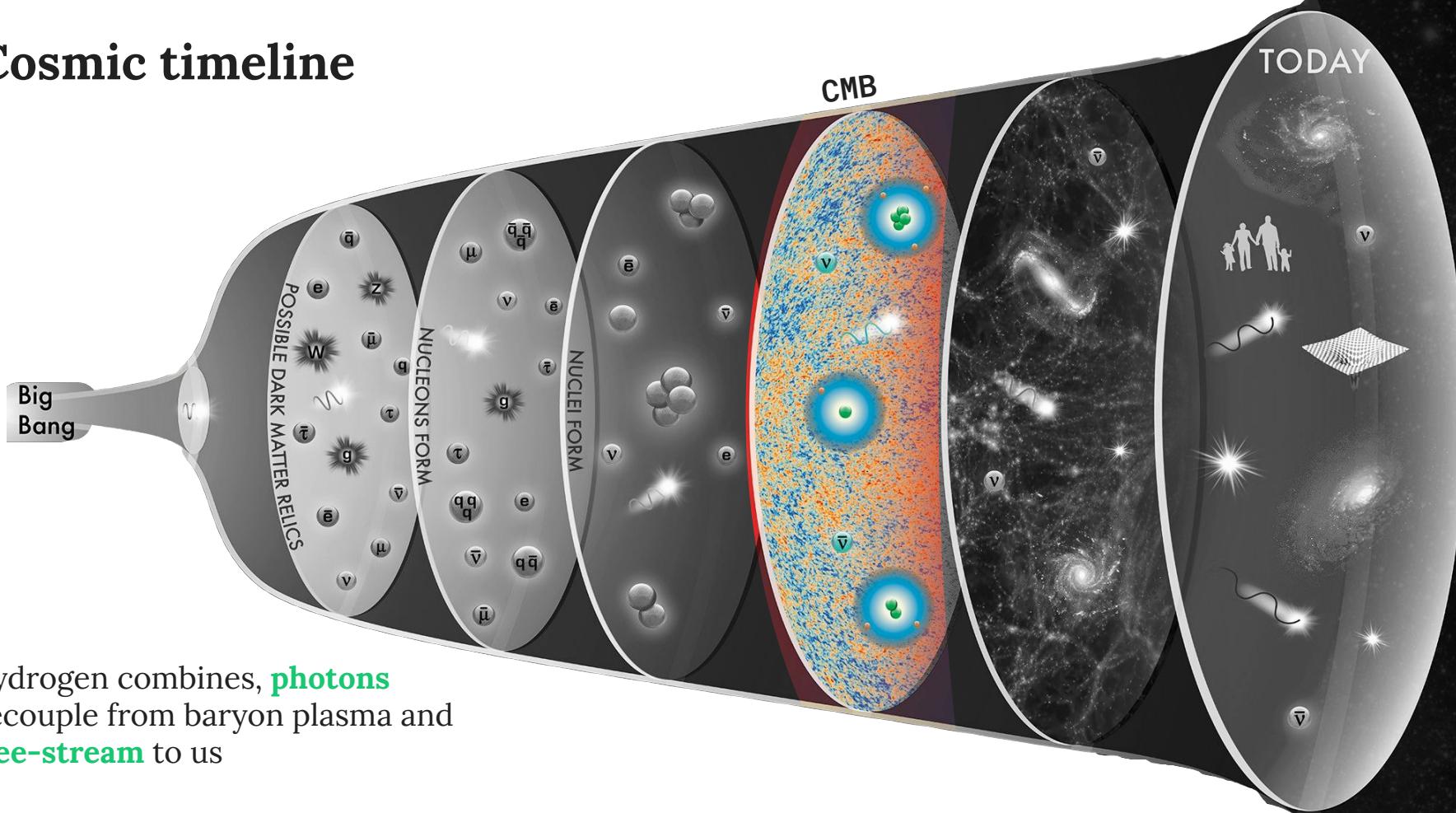


Figure from PDG

# Cosmic timeline

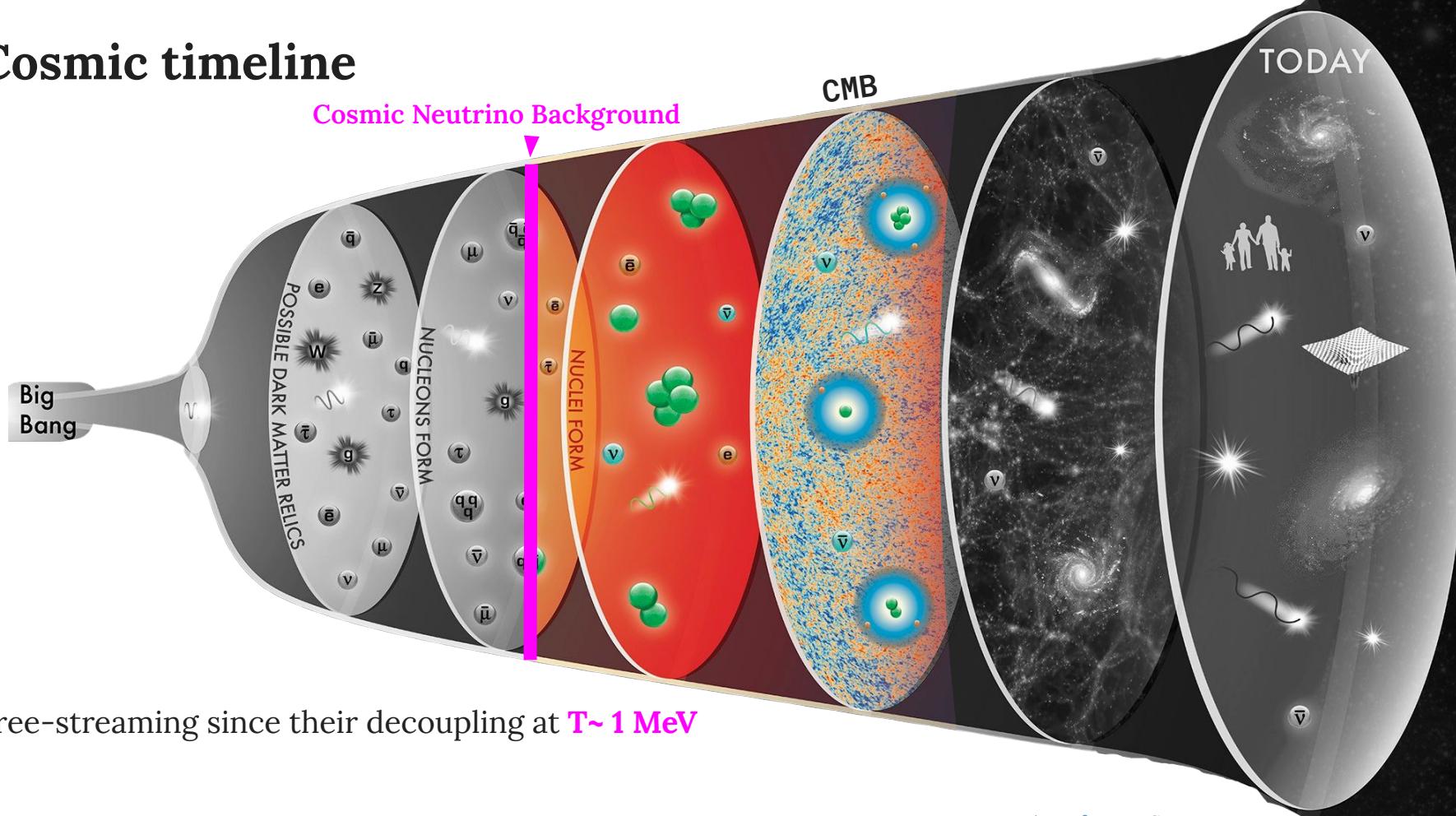
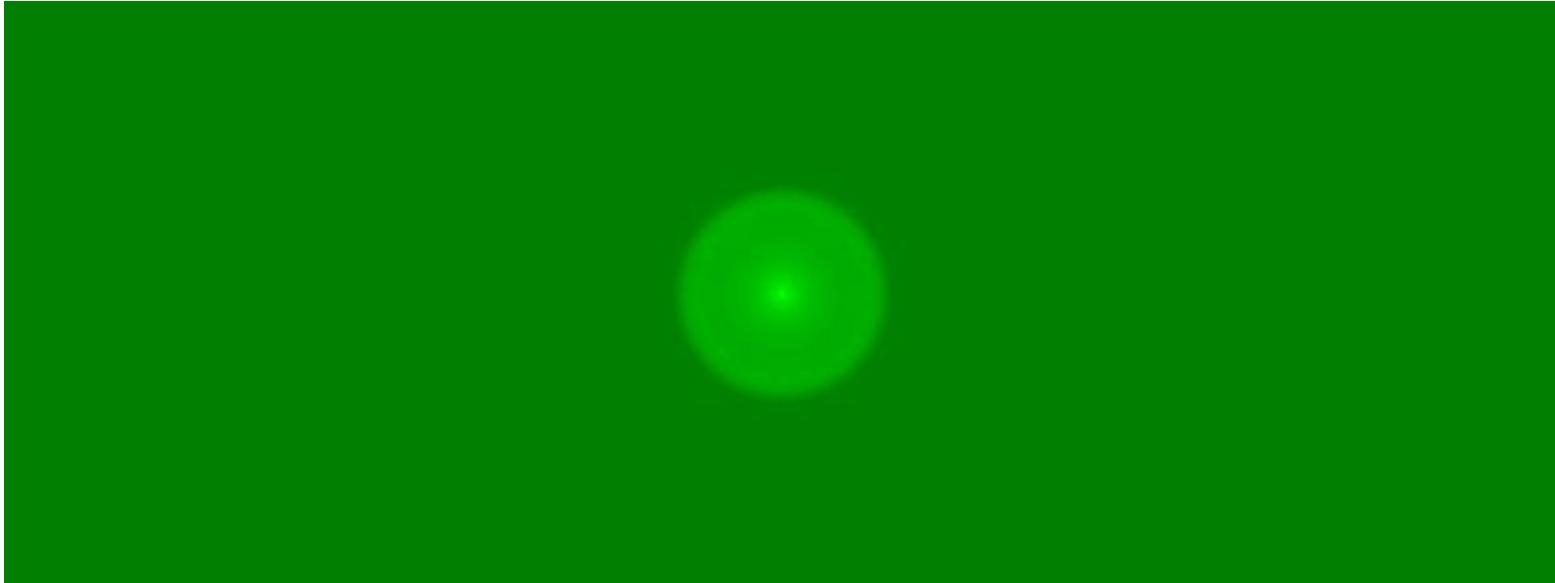


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# Cosmic sound waves

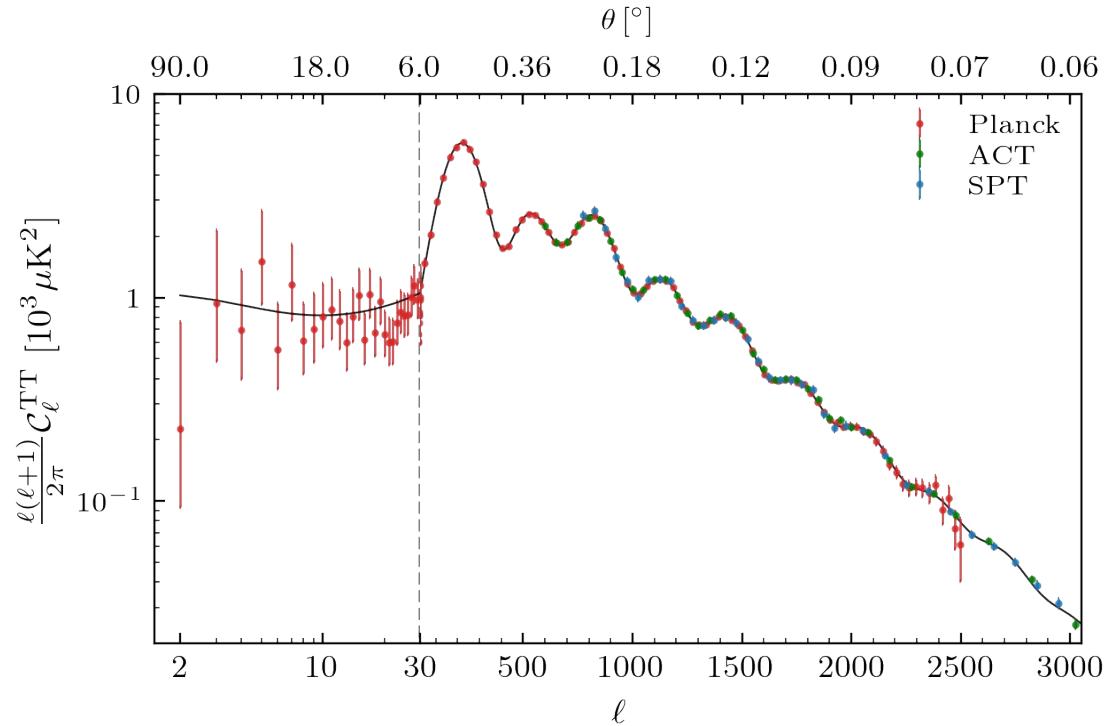
The CMB is the final snapshot of the **superposition of many incoherent sound waves**, that have been oscillating for ~400,000 years



The state of these oscillations is **frozen** at recombination when the **baryons release the photons**.

# The CMB power spectra

The CMB angular temperature power spectrum represents the variance of temperature fluctuations as a function of angular scale



$$\delta_\gamma \sim A_{\vec{k}} \cos(c_s k \tau)$$



$$C_\ell^{TT} \propto \cos^2(\theta_s \ell)$$

# The CMB Power Spectrum

The CMB angular power spectrum represents the variance of temperature fluctuations as a function of angular scale

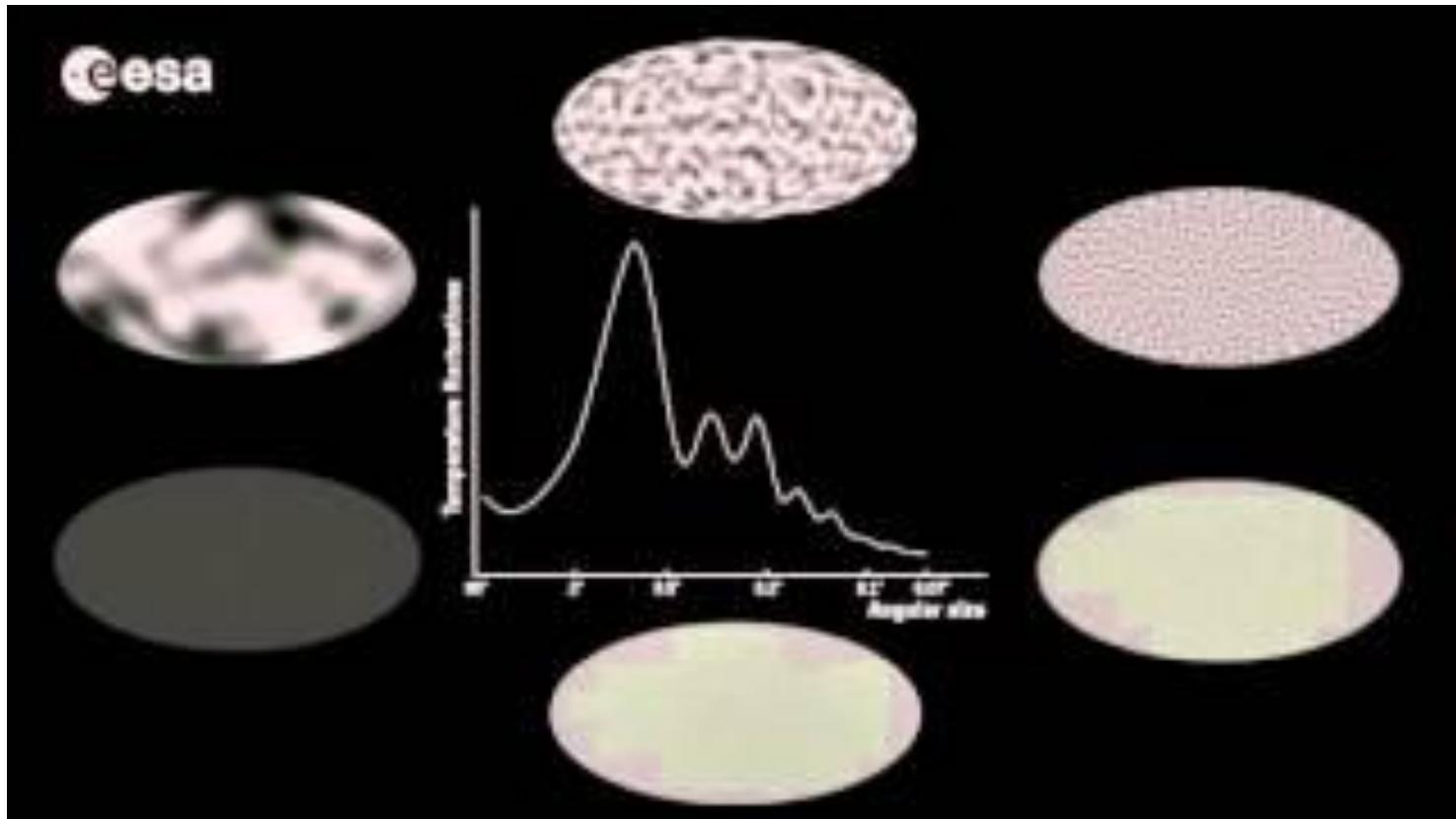
A spherical harmonic expansion of the temperature field

$$\Theta(\hat{\mathbf{n}}) \equiv \frac{\Delta T(\hat{\mathbf{n}})}{\bar{T}} = \sum_{\ell m} \Theta_{\ell m} Y_{\ell m}(\hat{\mathbf{n}})$$

$$\mathcal{C}_\ell \equiv \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |\Theta_{\ell m}|^2$$

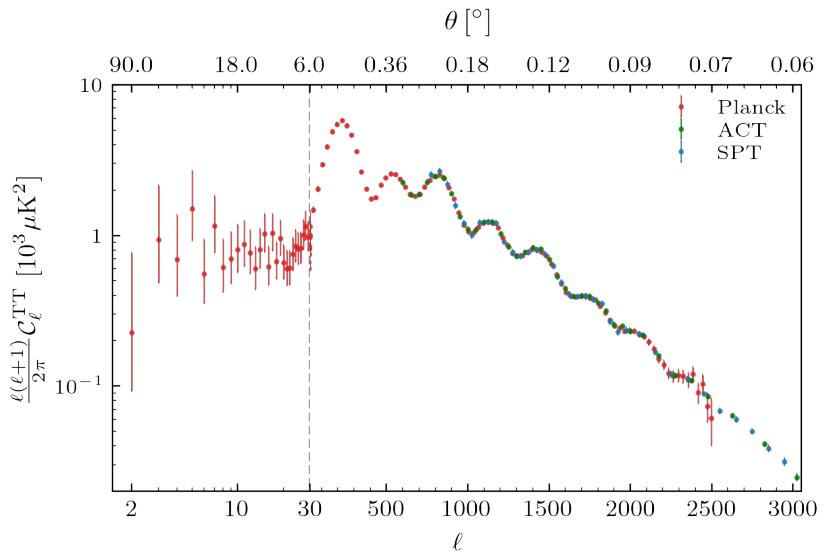
This compresses  $10^7$  pixels of the CMB map into  $10^3$  multipole moments

# CMB Power Spectrum

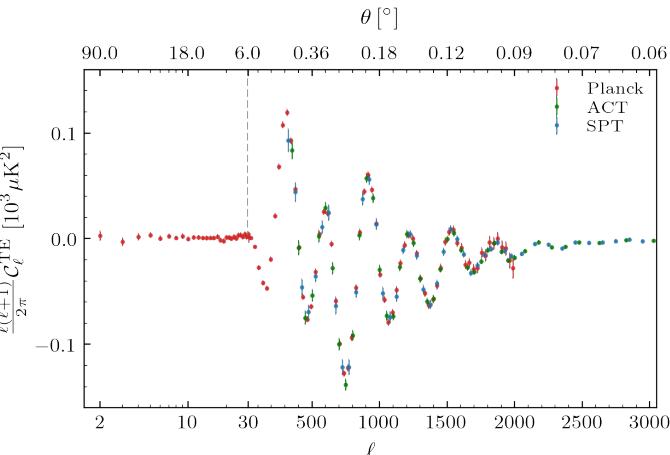
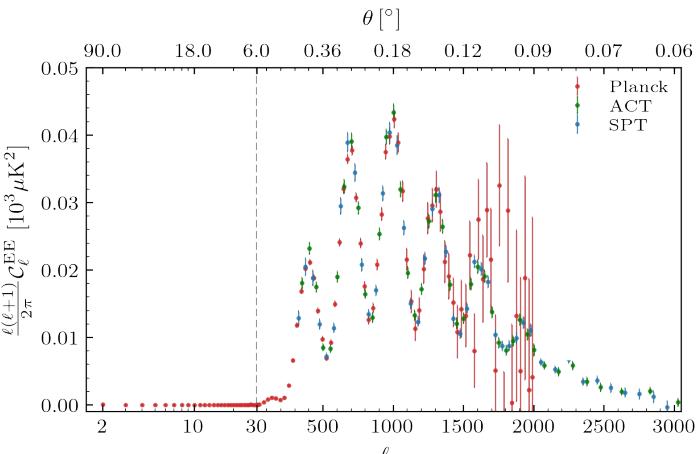


# The CMB power spectra

Temperature spectrum traces **density** perturbations,  
roughly the gravitational potential

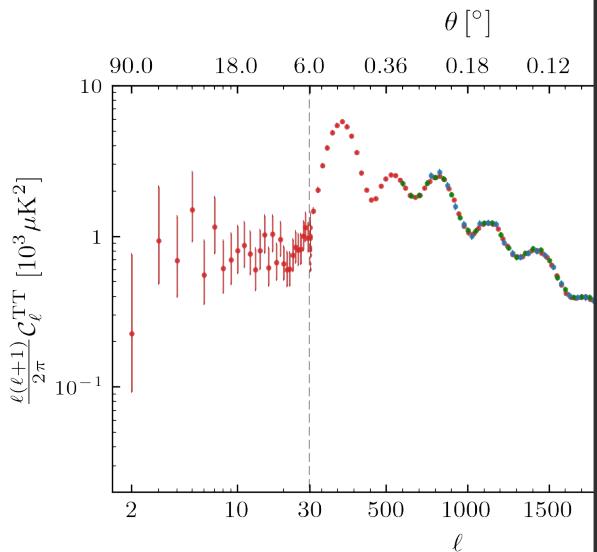


TE spectrum roughly tells us how the plasma is moving into the gravitational potential wells

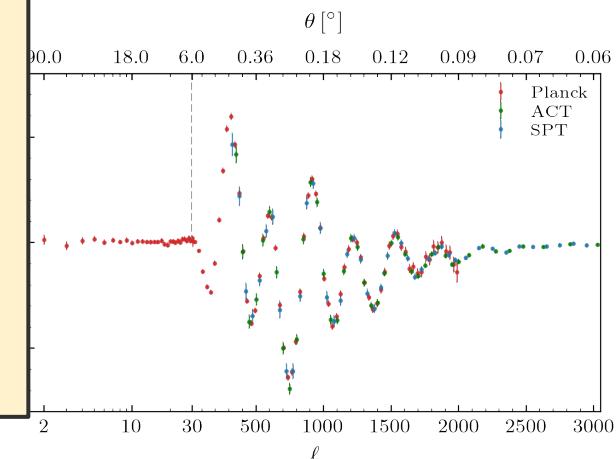
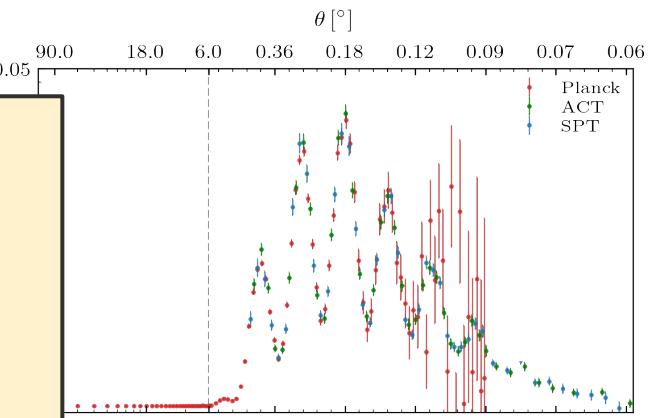
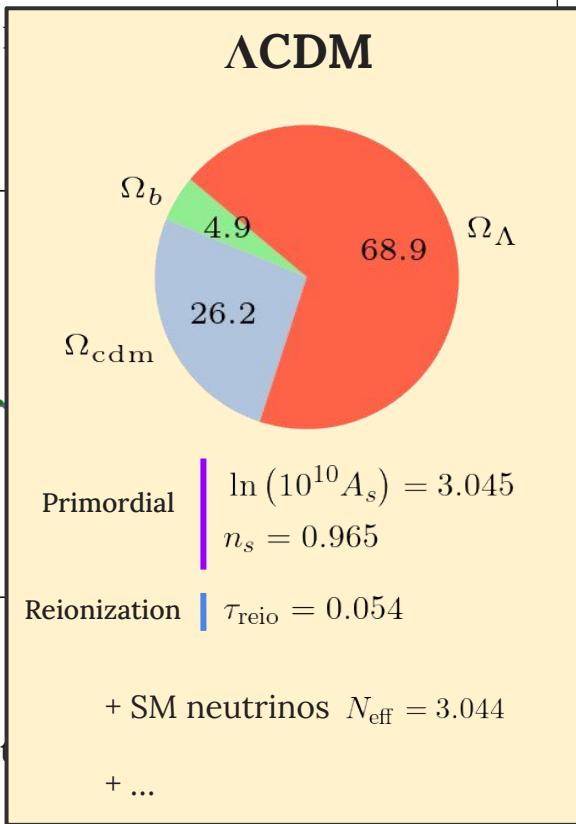


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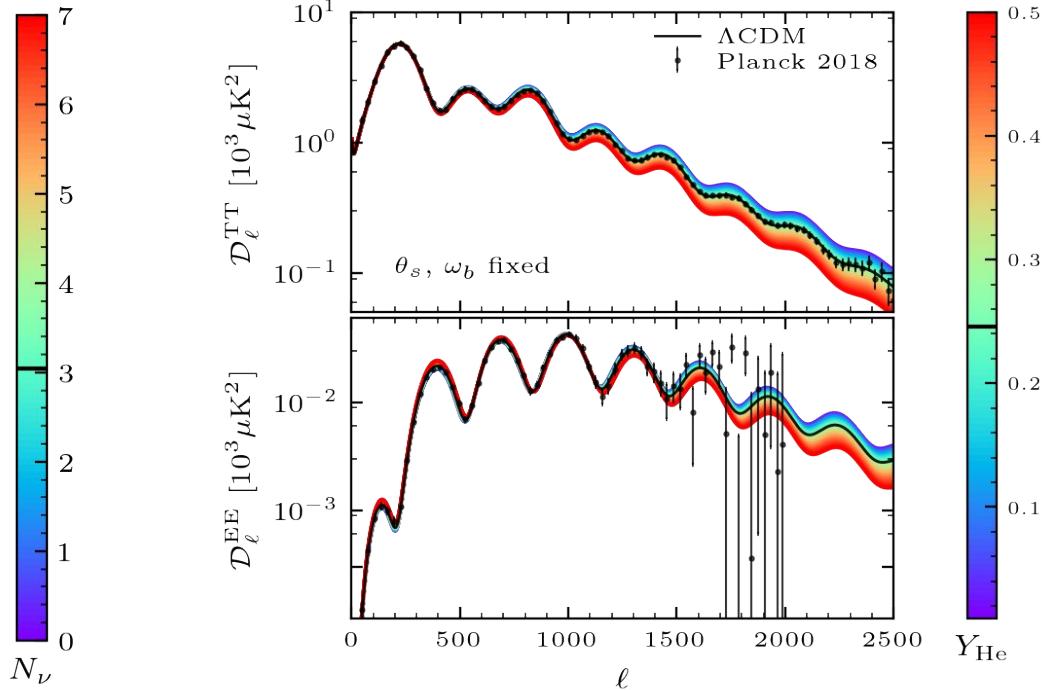
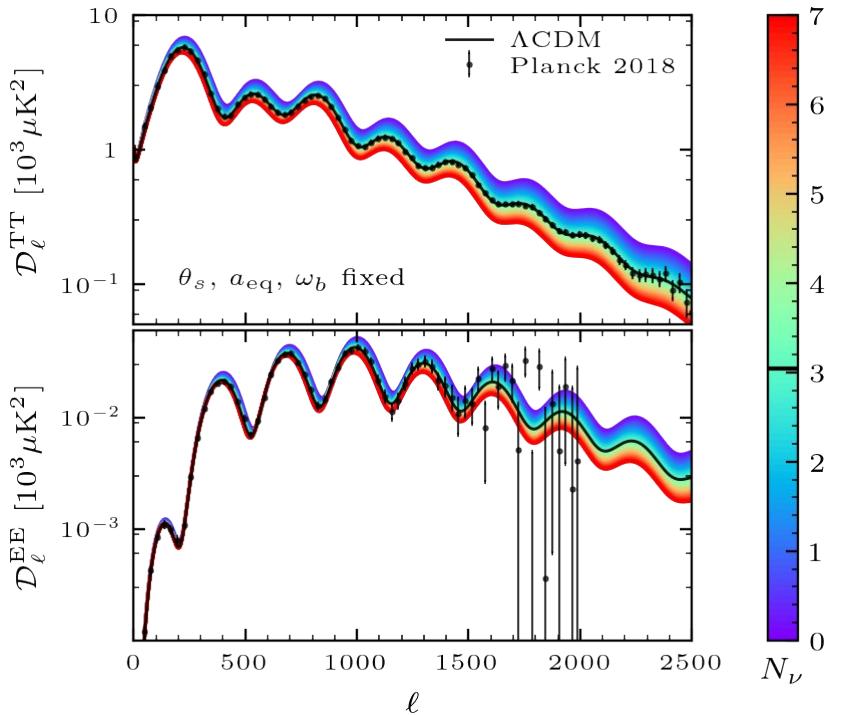


TE spectrum roughly  
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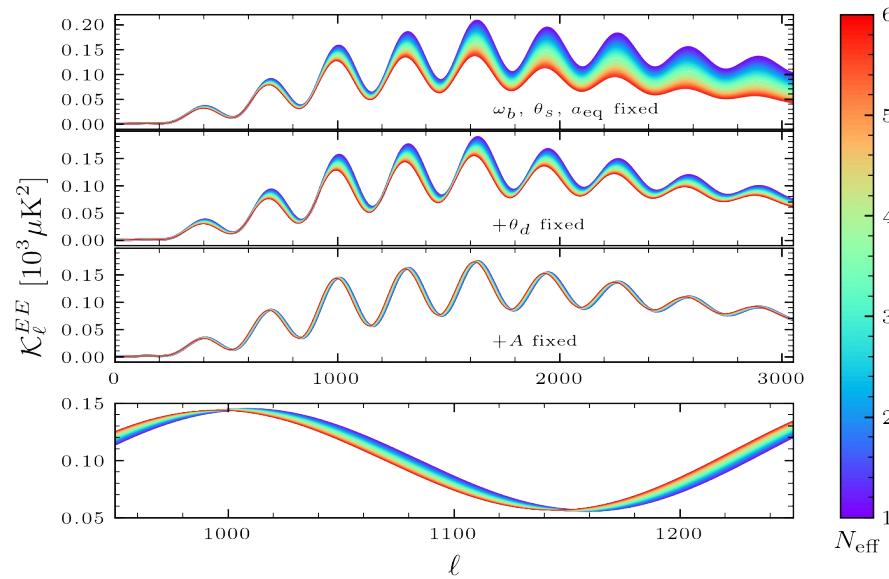
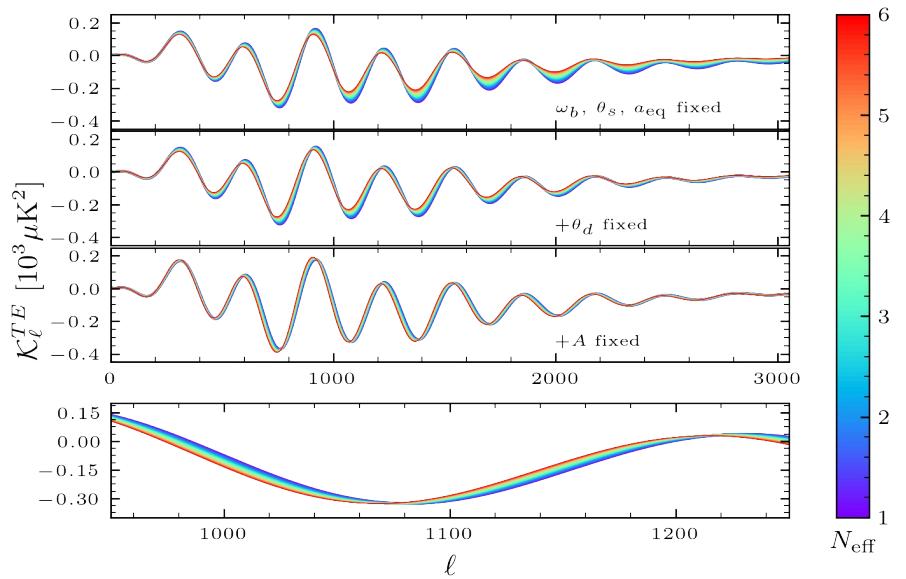
# Cosmic neutrinos in the CMB energy density

$$\theta_d \propto (H/n_e)^{1/2} \theta_s$$



Degeneracy with primordial Helium fraction  $Y_{\text{He}}$  via  $n_e$

# Cosmic neutrinos in the CMB free-streaming nature



# The phase shift in the CMB perturbations

- Extract the **phase shift** at the **perturbations** level, instead of the CMB power spectra
  - **Cleaner** signature: avoids projection and smearing effects

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X Physical Source Term

$$S_X(k, \eta)$$



X Anisotropies

$$\Delta_\ell^X = \int_0^{\eta_0} d\eta S_X(k, \eta) P_{X\ell}(k[\eta_0 - \eta])$$



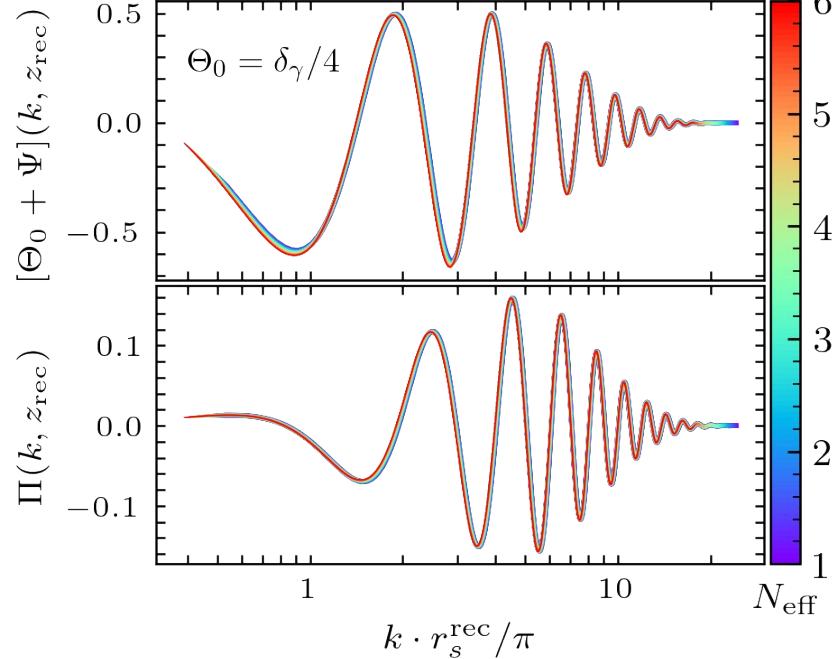
XY Power Spectra

$$c_\ell^{XY} = \frac{2}{\pi} \int k^2 dk \underbrace{\Delta_\ell^2(k)}_{\text{Primordial Spectrum}} \Delta_\ell^X(k) \Delta_\ell^Y(k)$$

$$\begin{cases} S_T(k, \eta) = g_\gamma (\delta_\gamma/4 + \Psi) + \dots \\ S_E(k, \eta) = \sqrt{6}/2 \cdot g_\gamma \Pi \end{cases}$$

$$\delta_\gamma(\vec{k}) \approx A(\vec{k}) \cos(kr_s + \phi)$$

$$\Pi(\vec{k}) \sim A(\vec{k}) \frac{c_s}{\tau} \sin(kr_s + \phi)$$



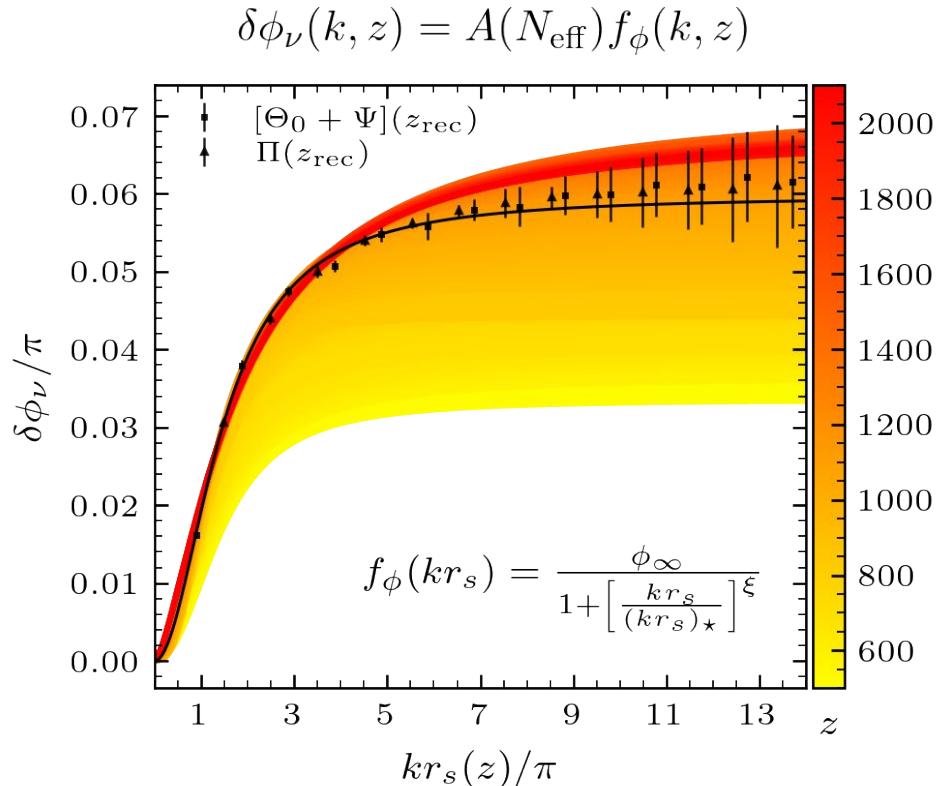
# The phase shift in the CMB perturbations

- The neutrino induced phase shift is **redshift** and mode dependent
- A new parameter to control the shift

$$N_{\text{eff}}^{\delta\phi}$$

$$\delta\phi_\nu = \left[ A(N_{\text{eff}}^{\delta\phi}) - A(N_{\text{eff}}) \right] f_\phi$$

$$S_X(k, \eta) \rightarrow S_X(k + \delta\phi_\nu/r_s, \eta)$$



# The phase shift in the CMB perturbations

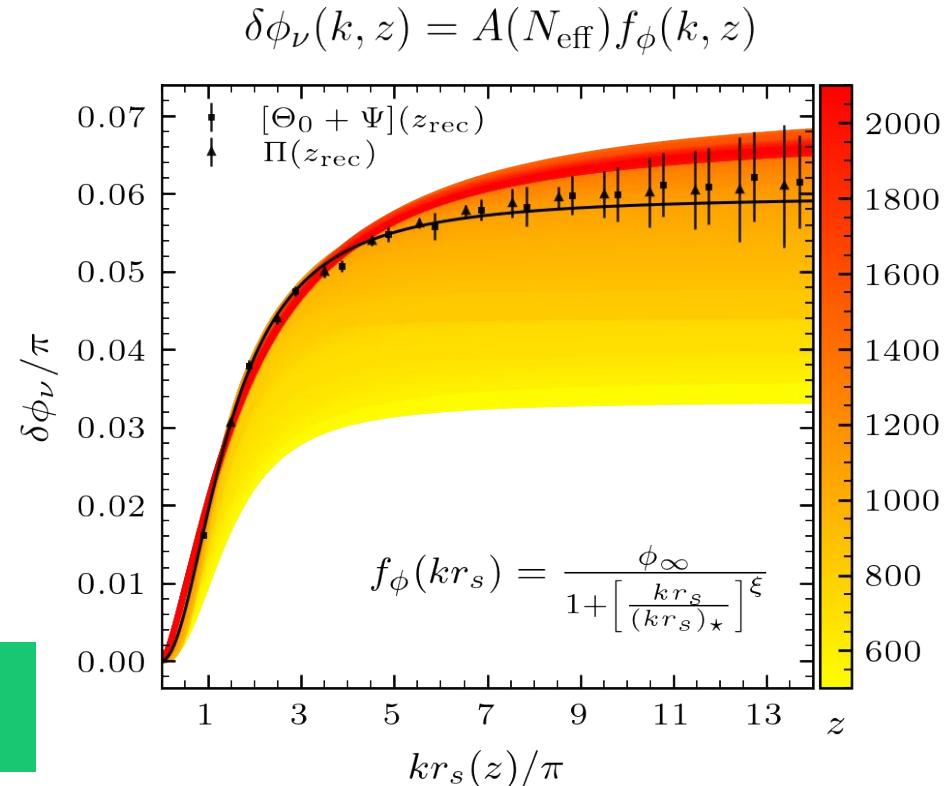
- The neutrino induced phase shift is **redshift** and mode dependent
- A new parameter to control the shift

$$N_{\text{eff}}^{\delta\phi}$$

$$\delta\phi_\nu = \left[ A(N_{\text{eff}}^{\delta\phi}) - A(N_{\text{eff}}) \right] f_\phi$$

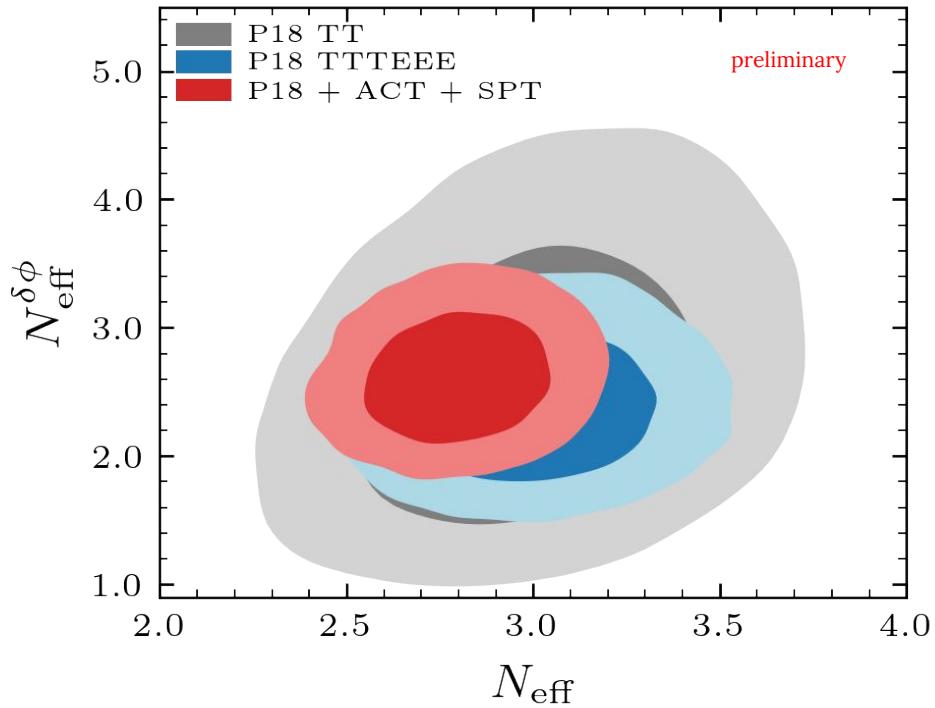
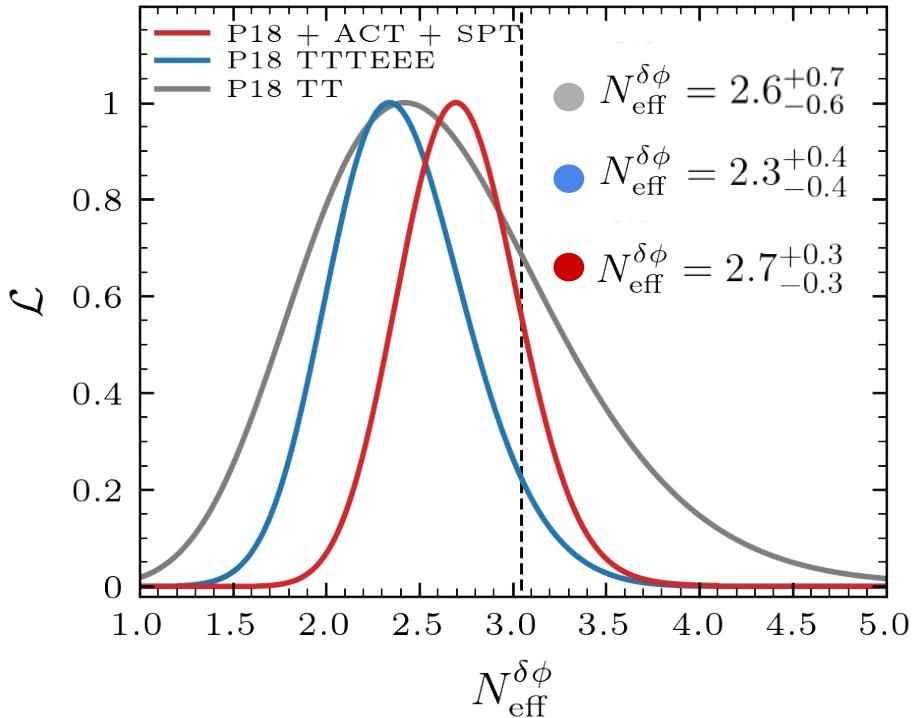
$$S_X(k, \eta) \rightarrow S_X(k + \delta\phi_\nu/r_s, \eta)$$

It results in the observed neutrino induced multipole shift in the CMB spectra



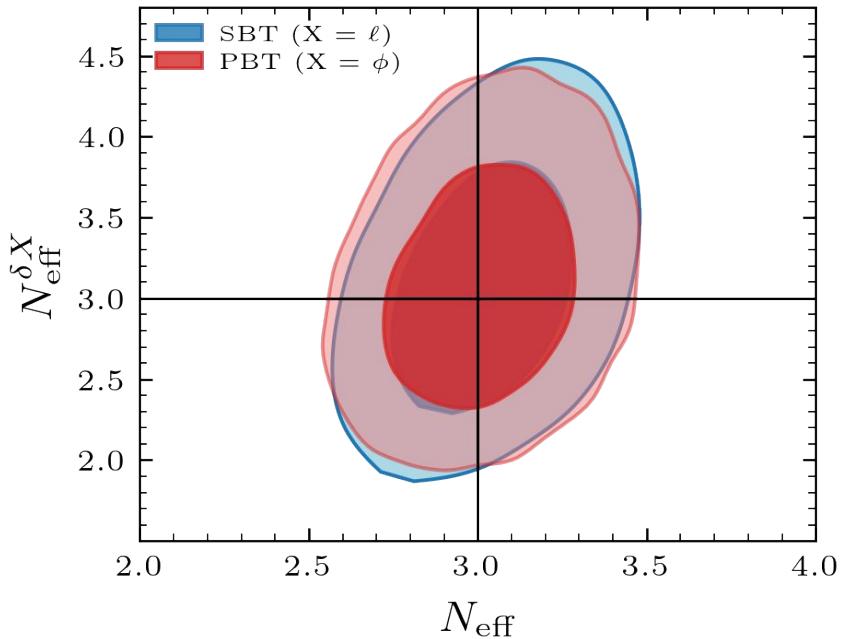
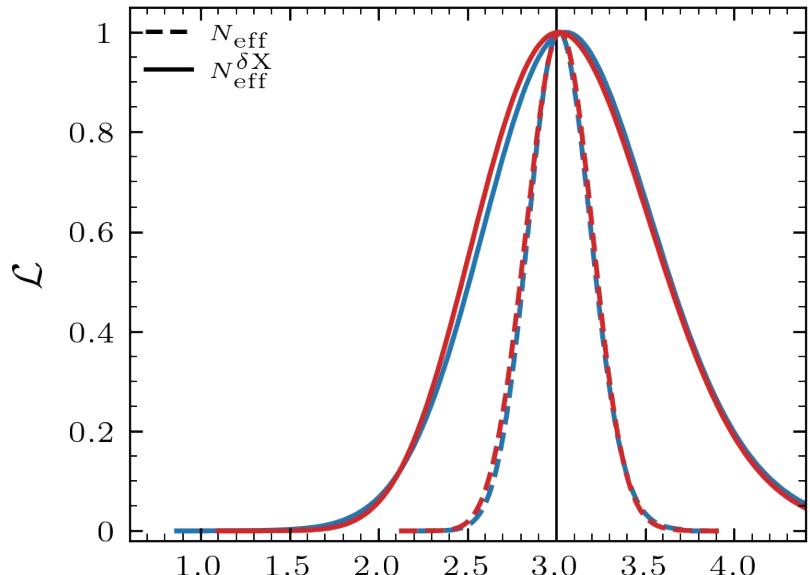
# Phase-shift constraints perturbations-based analysis

(  $N_{\text{eff}} = N_{\nu} = 3.044$  )



# Phase-shift constraints validation of phase shift extraction

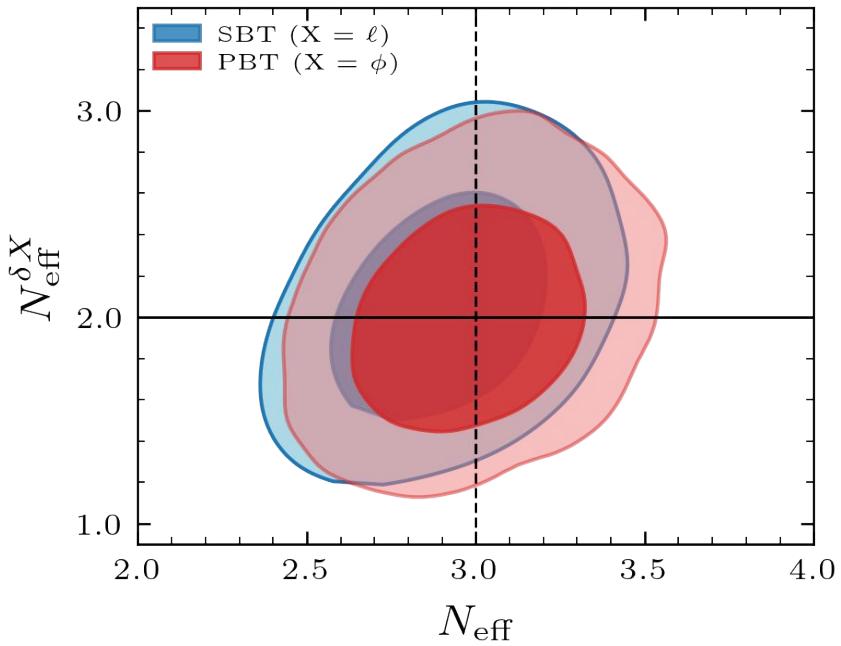
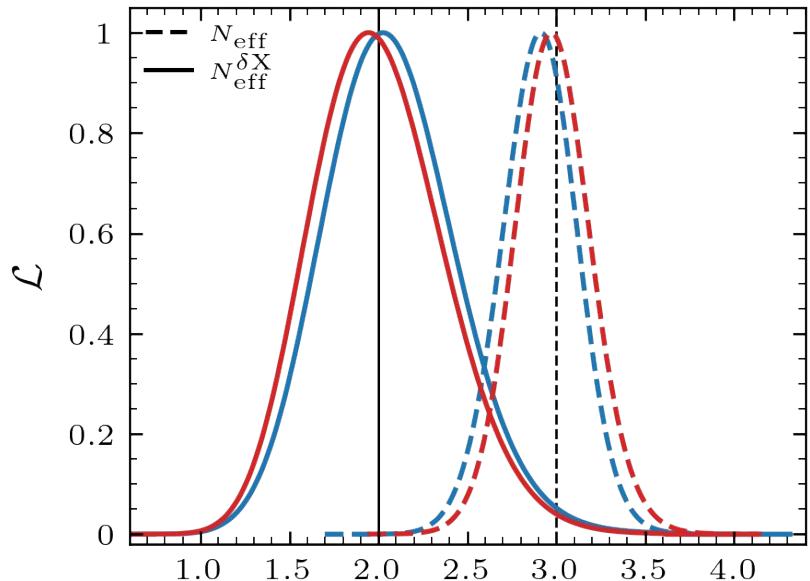
Planck 2018 Forecast:  $\Lambda\text{CDM} + N_{\text{eff}} = 3$  ( $M_\nu = 0$ )



Both the spectrum and perturbation based approach successfully recover the imprinted phase shift by free-streaming neutrinos

# Phase-shift constraints validation of phase shift extraction

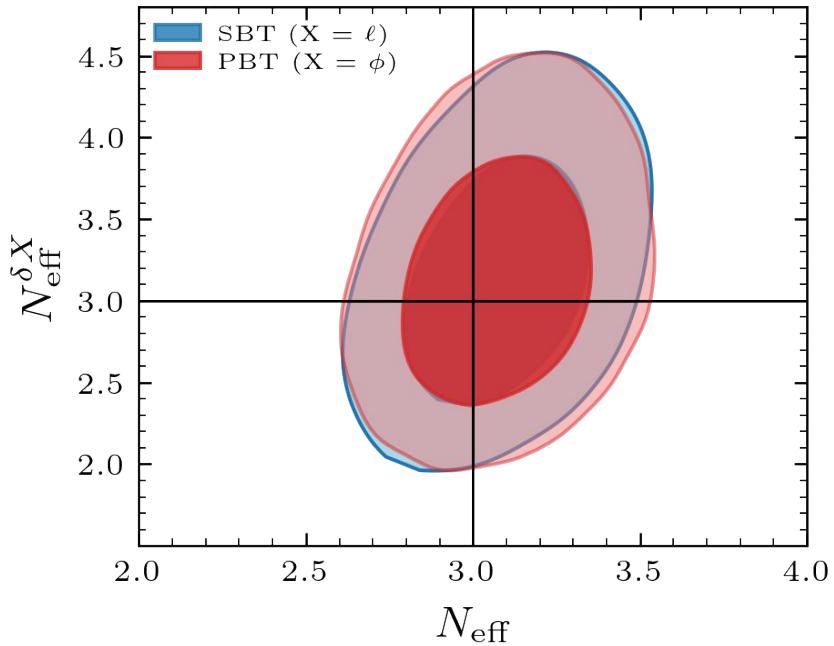
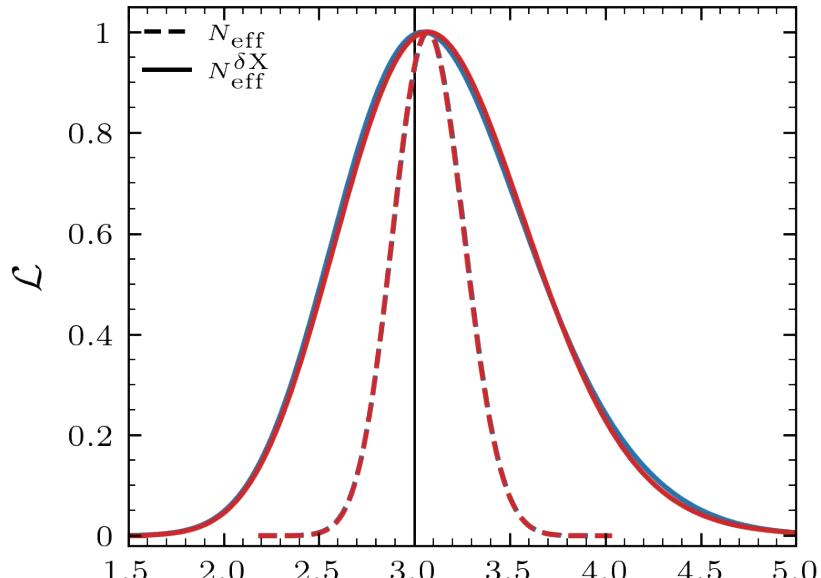
Planck 2018 Forecast:  $\Lambda\text{CDM} + N_{\text{eff}} = 2 + N_{\text{fluid}} = 1$  ( $M_\nu = 0$ )



Both the spectrum and perturbation based approach successfully recover the imprinted phase shift by free-streaming neutrinos

# Phase-shift constraints validation of phase shift extraction

Planck 2018 Forecast:  $\Lambda\text{CDM} + N_{\text{eff}} = 3.044$  ( $M_\nu = 0.06 \text{ eV}$ )



Neutrino masses have negligible impact on the phase shift extraction