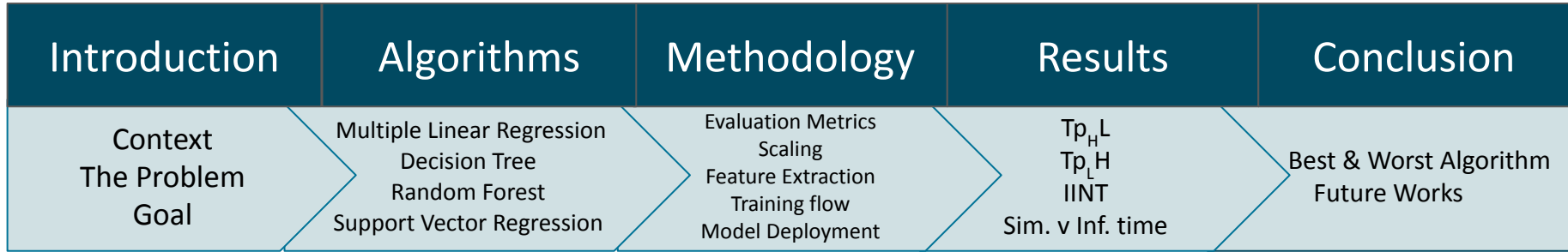




# Exploring Machine Learning for Electrical Behavior Prediction: **The CMOS Inverter Case Study**

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Universidade Federal de Santa Catarina

# Structure



# Context



## IBM Creates First 2nm Chip

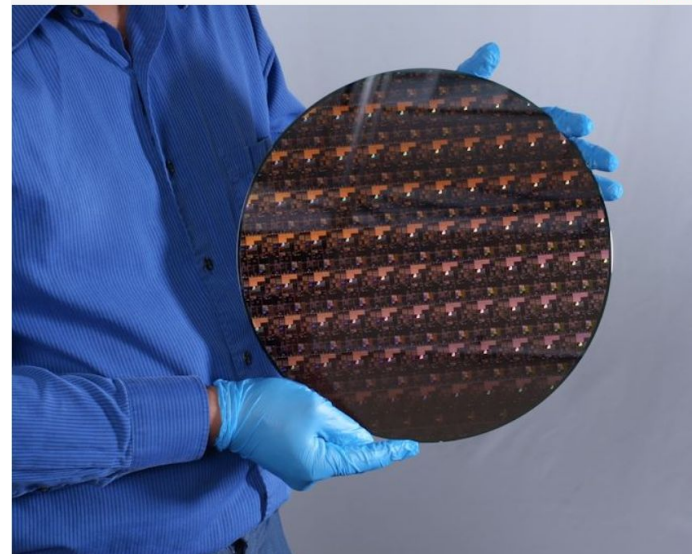
by [Dr. Ian Cutress](#) on May 6, 2021 6:00 AM EST

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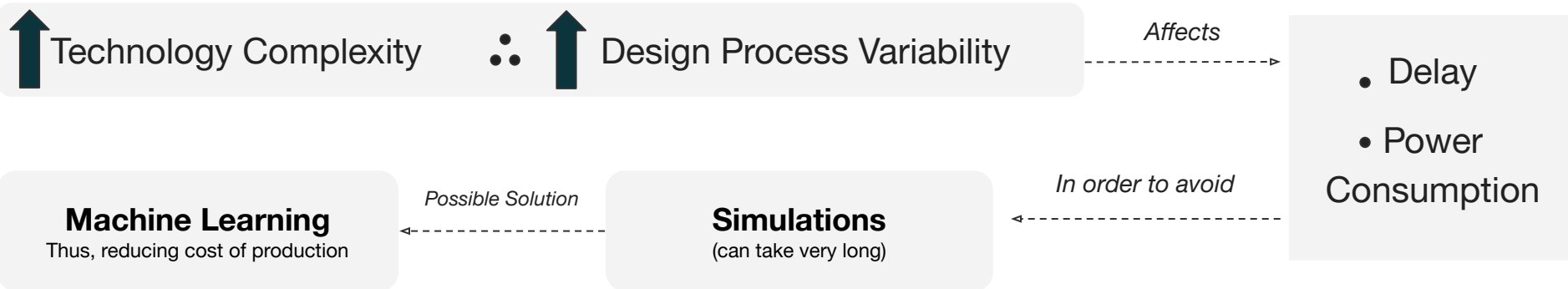
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Comments

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# The Problem

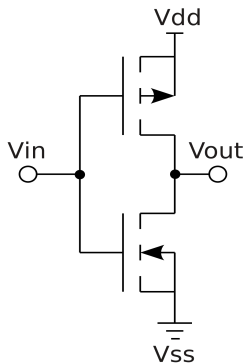


- More corner cases must be considered during the electrical characterization
- Machine learning can assist digital design in many levels

# Goal

## Regression Task!

### CMOS INVERTER CIRCUIT



SIMULATION DATA

(temperature, voltage,  
process variability...)

### SUPERVISED ALGORITHMS

#### MACHINE LEARNING MODELS

Multiple Linear Regression  
Support Vector Regression  
Decision Trees  
Random Forest

PREDICTION

### TARGETS

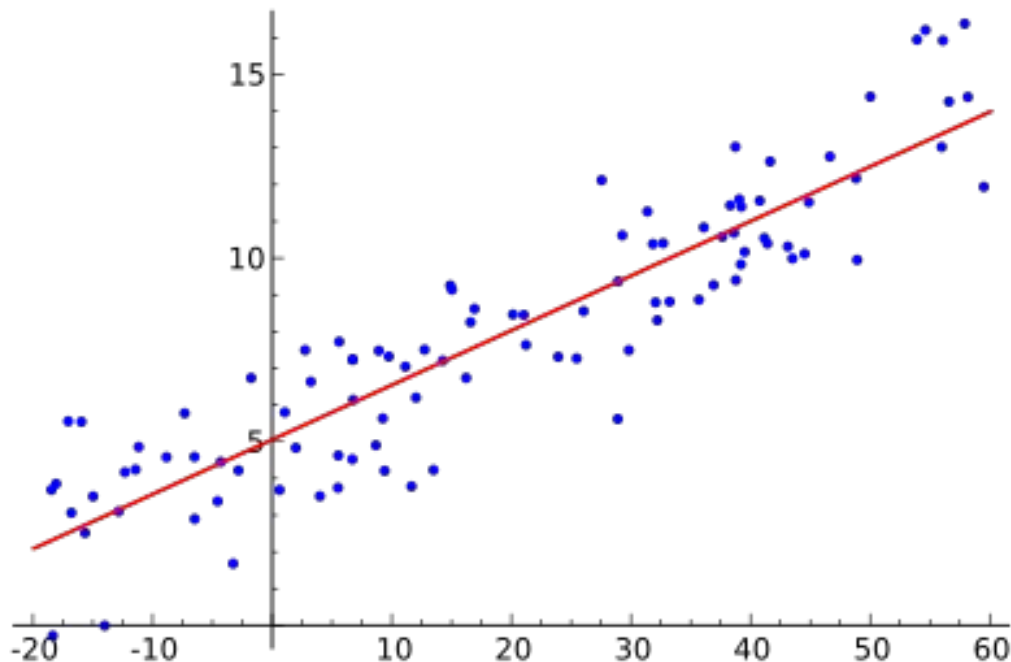
$T_{pLH}$

$T_{pHL}$

Energy

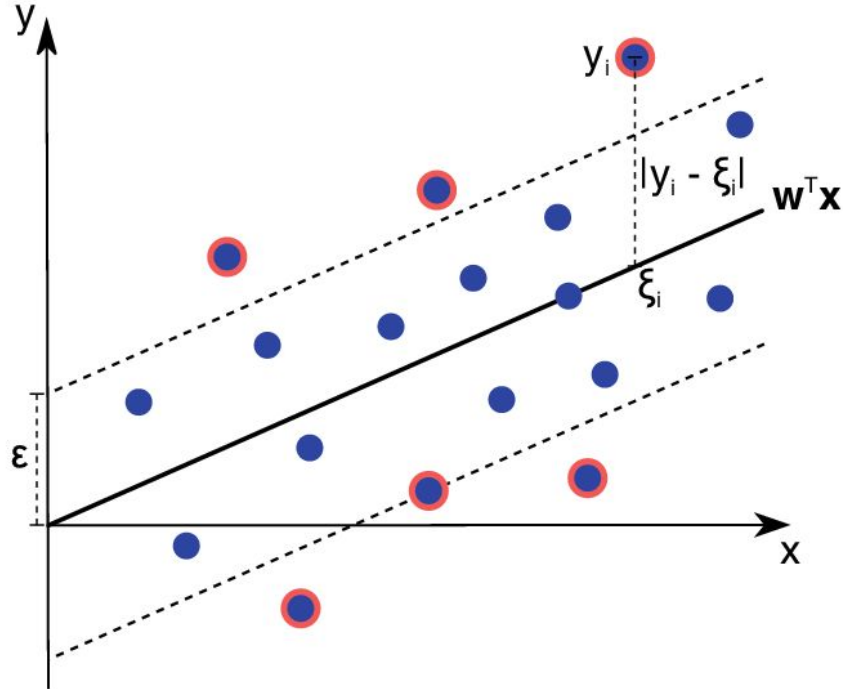
<https://pt.wikipedia.org/wiki/CMOS>

# Multiple Linear Regression (MLR)



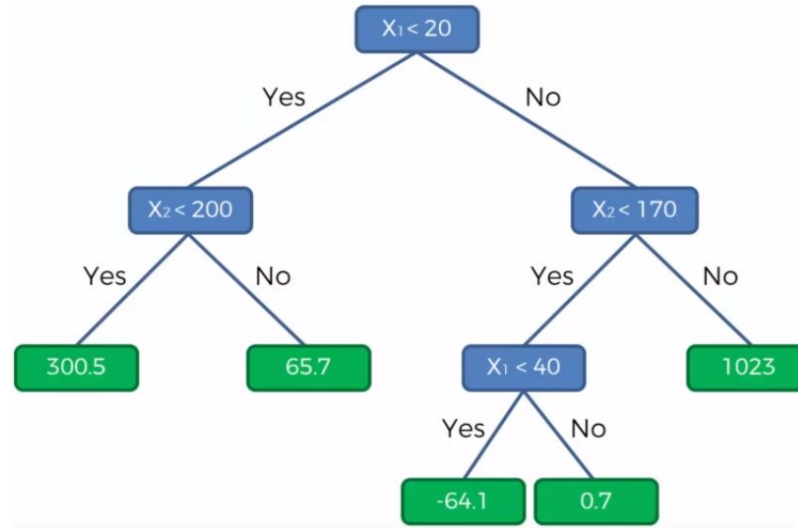
$$\hat{y} = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

# Support Vector Regression



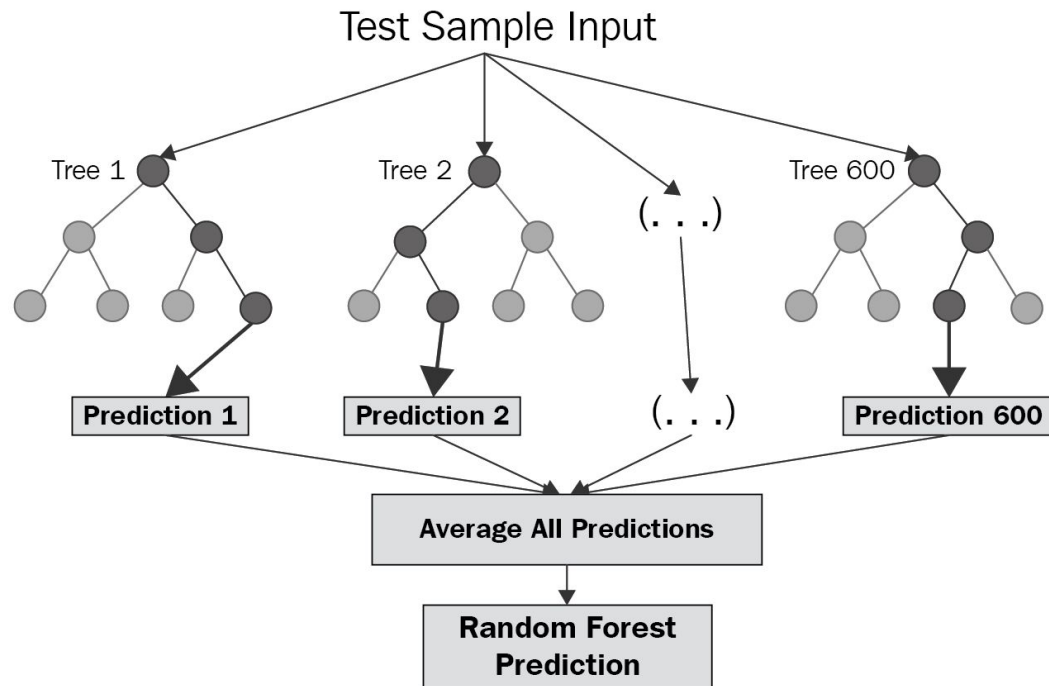
$$\hat{y} = w^T x + b$$

# Decision Tree



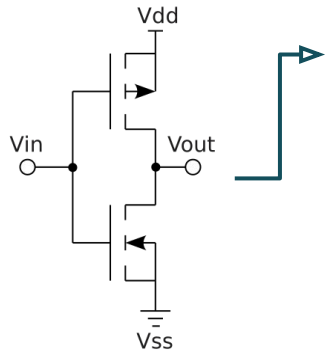


# Random Forest



# Training Flow - Overview

## I. Simulation



## II. Feature Extraction

## III. Data Processing

## IV. Algorithms

## V. Evaluation

## VI. Results

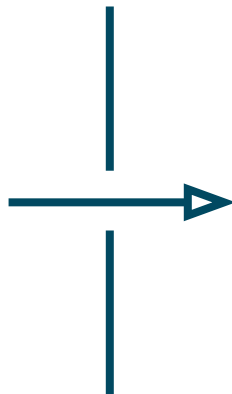
## VII. Model Deployment

# Feature Extraction

1000 Monte Carlo transient simulations of 20ns with step of 0.1ns in HSPICE

## Features

NMOS Vth0  
PMOS Vth0 (threshold voltage)  
Temperature (-25, 0, 50, 75, 100°C)  
Voltage (0.6, 0.7, 0.8, 0.9V)  
Width PMOS (70, 140, 280, 350, 420nm)  
Width NMOS (70, 140nm)  
Length (20, 32, 40nm)



## Targets

High-Low Propagation ( $T_{p_{HL}}$ )  
Low-High Propagation ( $T_{p_{LH}}$ )  
Energy

## Data processing (Scaling)

$$x' = \frac{x - \min(x)}{\max(x) - \min(x)}$$

**MIN-MAX Scaler**

# Algorithms (Cross Validation)

## Values & Best Hyperparameters

- DT - **Max Depth**: 1, 5, 10, 25, 50
- RF - **Max Depth**: 1, 5, 10, 25, 50
- RF - **N Estimators**: 5, 25, 50, 100, 150

	DT - Max Depth	RF - Max Depth	RF - N Estimators
Tp <sub>H</sub> L	5	5	25
Tp <sub>L</sub> H	10	10	150
Energy	10	10	150

50%  
Training Set

25%  
Validation Set

25%  
Test Set

## Evaluation Metrics

$$\sqrt{\frac{1}{m} \sum_{i=1}^m (h(x^{(i)}) - y^{(i)})^2}$$

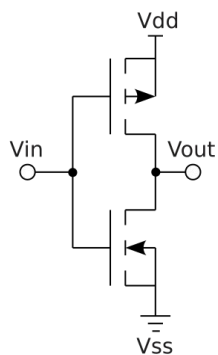
**Root Mean Square Error (RMSE)**

$$R^2 = 1 - \frac{\sum_i (y_i - \hat{y}_i)^2}{\sum_i (y_i - \bar{y}_i)^2}$$

**Coefficient of Determination ( $R^2$ )**

# Training Flow

## I. Simulation



## II. Targets

Energy  
TPHL  
TPLH

## II. Features

Voltage  
Temperature  
Width PMOS  
Width NMOS  
Length  
Nmos Vth0  
Pmos Vth0

## III. Data Processing

Min-Max Scaler

$$x' = \frac{x - \min(x)}{\max(x) - \min(x)}$$

50%

Training Set

25%

Validation Set

25%

Test Set

## IV. Algorithms

Multiple Linear Regression  
Support Vector Machine  
Decision Trees  
Random Forest

## V. Evaluation

$$\sqrt{\frac{\sum_{t=1}^T (\hat{y}_t - y_t)^2}{T}}$$

## VI. Results

## VII. Model Deployment

# Model Deployment

**Electrical Characterization Prediction**

This app predicts the electrical behaviour of a circuit given some features and some random variability. Currently only a CMOS inverter is available

**User Input features**

Awaiting CSV file to be uploaded. Currently using example input parameters (shown below).

	voltage	width_pmos	width_nmos	length	temper	nmos@var	pmos@varp
0	0.6000	140.0000	70.0000	32.0000	-25	0.5166	-0.4341

**Energy Prediction**

0 0.4864

0 0.1122

**High-Low Propagation Prediction**

0 0.1137

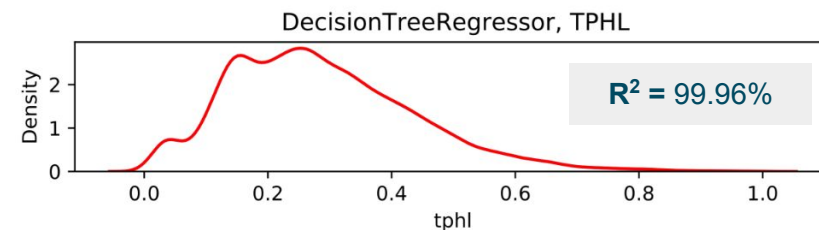
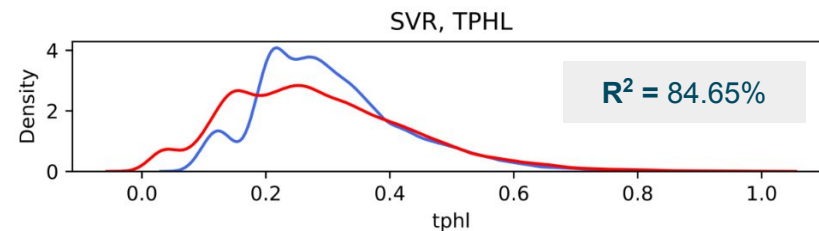
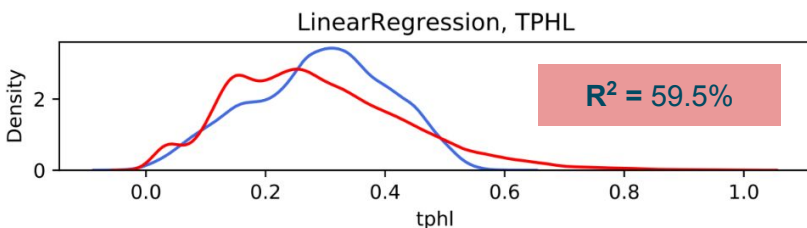
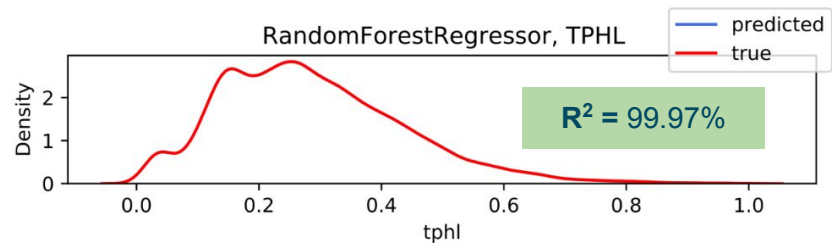
0 2.7740

**Low-High Propagation Prediction**



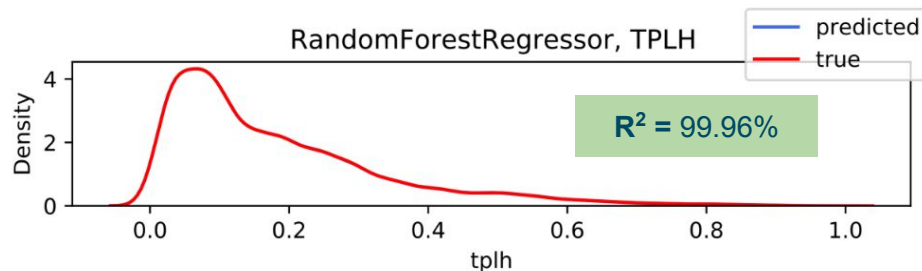


# $T_{p_H}L$ Prediction

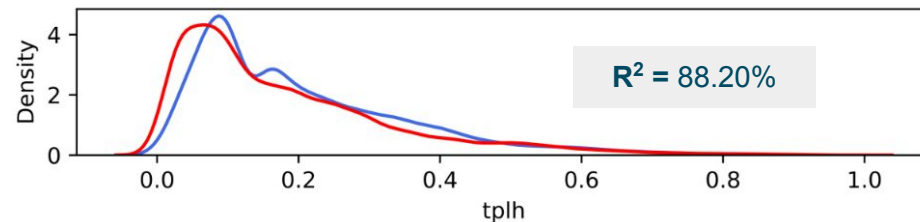


# Tp<sub>L</sub>H Prediction

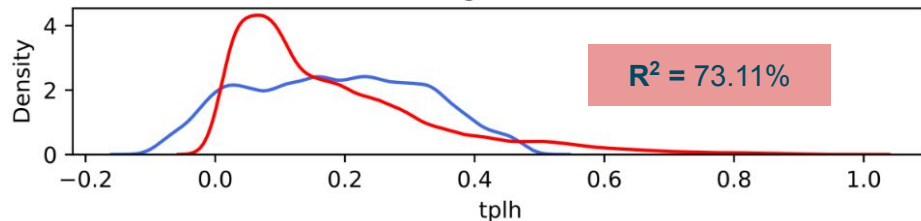
RandomForestRegressor, TPLH



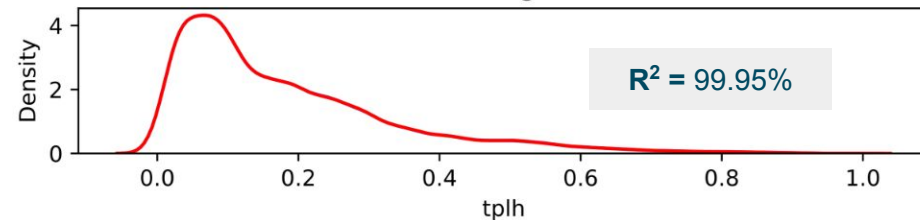
SVR, TPLH



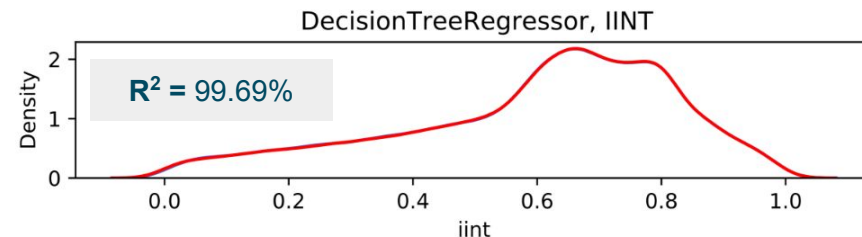
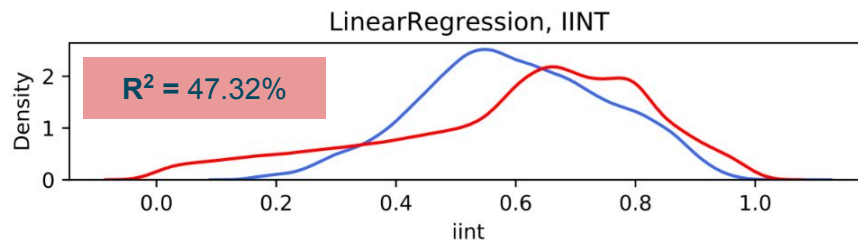
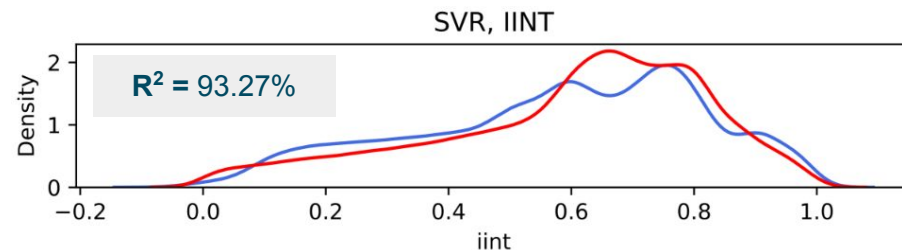
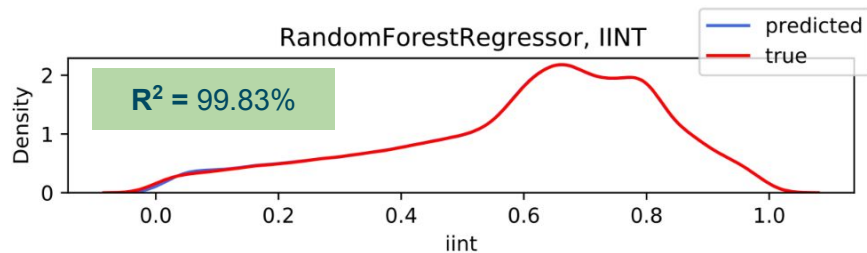
LinearRegression, TPLH



DecisionTreeRegressor, TPLH



# Energy Prediction



## Simulation vs Inference Time

Single Hspice electrical simulation = 0.069 s

DT = 0.0006 s (115×)

RF = 0.0432 s (1.59×)

Best Algorithm

**Random Forest**

Worst Algorithm

**Multiple Linear Regression**

## Possible Applications

Foundries can adopt ML to cell characterization and make available the machine learning model trained, protecting the private data of the device models.

## Future Works

Basic gates from a standard cell library

Investigate Neural Networks architectures

Evaluate the dependencies between the ML models and the technology node, considering FinFET devices

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# Appendix

## Pearson Correlation Coefficients

