

ESFERAS E SUAS PARTES

① a) pois a esfera pode ser formada pela rotação de 360° de um semicírculo em volta do seu diâmetro.

② $V = \frac{4\pi R^3}{3}$ $V_1 = \frac{4\pi \cdot 1^3}{3} = \frac{4\pi}{3}$ → Volume da esfera de raio 1

$V_2 = \frac{4\pi R^3}{3} \rightarrow \frac{4\pi R^3}{3} = 1.000.000 \cdot \frac{4\pi}{3}$

$R^3 = 10^6$

$R = \sqrt[3]{10^6}$

$R = 10^2 = 100$

③

Volume esfera:

$V_E = \frac{4\pi R^3}{3}$

Volume cilindro

raio = $2r$

$h = 4r$

$V_C = \pi r^2 h$

$V_C = \pi \cdot 4r^2 \cdot 4r$

$V_C = 16\pi r^3$

Proporção:

$x = \frac{V_E}{V_C} = \frac{\left(\frac{4\pi r^3}{3}\right)}{16\pi r^3} = \frac{4}{3} = \frac{4:16}{3} = \frac{4 \cdot 1}{3 \cdot 16} = \frac{4}{3 \cdot 4 \cdot 12} = \frac{1}{3 \cdot 4 \cdot 12} = \frac{1}{12}$ (E)

④ Volume dos dois esferas = Volume cilindro

$V = \left(\frac{4\pi \cdot 1^3}{3}\right) + \left(\frac{4\pi \cdot 2^3}{3}\right)$

$V = \frac{4\pi \cdot 1}{3} + \frac{4\pi \cdot 8}{3} = \frac{4\pi}{3} + \frac{32\pi}{3} = 12\pi$

$12\pi = \pi r^2 \cdot 3$

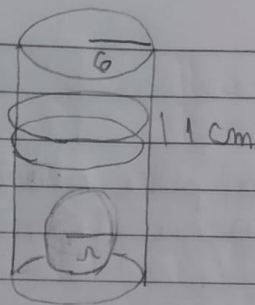
$r^2 = \frac{12\pi}{3\pi}$

$r^2 = 4$ B)

$r = \sqrt{4} = 2$

$r = \sqrt{4} = 2$ (tilibra)

⑤



$$V_{\text{cilindro}} = \pi \cdot 6^2 \cdot 11 = 396\pi$$

$$V_{\text{esfera}} = \frac{4}{3} \pi \cdot r^3$$

$$\frac{4}{3} \pi \cdot r^3 = 396\pi$$

$$\cancel{4\pi} \cdot r^3 = 108\cancel{\pi}$$

$$r^3 = 27$$

$$r = 3 \text{ cm} \quad c)$$

⑥ $V_E = 288\pi$

$$\frac{4\pi}{3} r^3 = 288\pi$$

$$r^3 = 864$$

$$r = \sqrt[3]{864}$$

$$r = 6$$

$$2R = 12$$

$$R = 6 \quad E)$$

⑦ Cilindro

$$V_c = \pi \cdot r^2 \cdot h$$

$$V_c = \pi \cdot 10^2 \cdot 16$$

$$V_c = 1600\pi \text{ cm}^3$$

Volume de um doce em formato de
cilindro

$$V_D = \frac{4\pi \cdot r^3}{3}$$

$$V_D = \frac{4\pi \cdot 2^3}{3}$$

$$V_D = \frac{32\pi}{3}$$

número de doces

$$N = \frac{V_c}{V_D}$$

$$N = \frac{1600\pi}{\left(\frac{32\pi}{3}\right)}$$

$$N = \frac{4800}{32} = 150$$

$$\textcircled{8} V = \frac{1}{2} \cdot \frac{4}{3} \cdot \pi R^3 = \pi R^2 \cdot H = \frac{1}{3} \cdot \pi R^2 \cdot h$$

$$\frac{2}{3} \pi R^3 = \pi R^2 \cdot H$$

$$\frac{2}{3} \pi R^3 = \pi R^2 \cdot H$$

$$2R = 3H$$

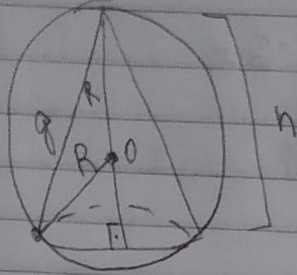
$$\pi R^2 \cdot H = \frac{1}{3} \cdot \pi R^2 \cdot h$$

$$h = 3H$$

$$2R = h = 3H$$

INSCRIÇÃO E CIRCUNSCRIÇÃO DE SÓLIDOS

①



$$SE = 100\pi$$

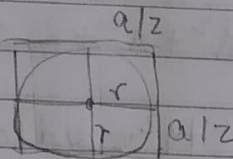
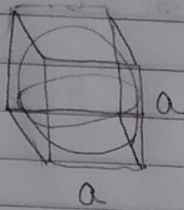
$$4\pi R^2 = 100\pi$$

$$R^2 = \frac{100}{4}$$

$$R = \sqrt{25} = 5$$

(não consegui chegar a 3m)

②



Área da superfície do cubo:

$$Sc = 6 \cdot a^2$$

medida do raio da esfera
↳ metade da aresta do cubo

$$r = \frac{a}{2}$$

Área da superfície da esfera

$$SE = 4\pi \cdot r^2$$

$$SE = 4\pi \cdot \left(\frac{a}{2}\right)^2$$

$$SE = 4\pi \cdot \frac{a^2}{4}$$

$$SE = \pi \cdot a^2$$

Razão:

$$\frac{SE}{Sc} = \frac{\pi \cdot a^2}{6 \cdot a^2} = \frac{\pi}{6}$$

$$\frac{SE}{Sc} = \frac{\pi}{6} \quad \boxed{6} \quad A)$$

③ $VE = \frac{4\pi R^3}{3}$

$$Vc = a^3$$

$$Vc = \left(\frac{2\sqrt{3}R}{3}\right)^3$$

$$Vc = \frac{8 \cdot 3\sqrt{3} \cdot R^3}{27}$$

$$Vc = \frac{24\sqrt{3}R^3}{27}$$

$$Vc = \frac{8\sqrt{3}R^3}{9}$$

$$Vc = \frac{8\sqrt{3}R^3}{9}$$

$$Vc = \frac{8\sqrt{3}R^3}{9}$$

$$d_o = 2R$$

$$a\sqrt{3} = 2R$$

$$a = \frac{2R \cdot \sqrt{3}}{\sqrt{3}}$$

$$a = \frac{2\sqrt{3}R}{3}$$

$$a = \frac{2\sqrt{3}R}{3}$$

$$a = \frac{2\sqrt{3}R}{3}$$

$$\frac{VE}{Vc} = \frac{\frac{4\pi R^3}{3}}{\frac{8\sqrt{3}R^3}{9}} = \frac{4\pi R^3}{3} \cdot \frac{9}{8\sqrt{3}R^3} = \frac{3\pi}{2\sqrt{3}} = \frac{\sqrt{3}\pi}{2} \quad \boxed{2} \quad B)$$

$$\textcircled{4} \quad RB = 3 \quad H_{co} = h_{ci} \rightarrow 12 = H - x$$

$$H = 12$$

$$D_{co} = h_{ci}$$

$$6 \quad x$$

$$12x = 6 \cdot 12 - 6x$$

$$18x = 72$$

$$x = 4 = 2R$$

$$n = 2$$

$$V_{ci} = 2\pi n^3$$

$$V_{ci} = 2\pi 2^3$$

$$V_{ci} = 16\pi \text{ cm}^3$$

$$\textcircled{5} \quad V_{sol} = V_{tro} = \frac{\pi h}{3} (R^2 + r^2 + R \cdot r)$$

$$R = 2$$

$$r = 1$$

$$= \frac{\pi \cdot 1}{3} (2^2 + 1^2 + 2 \cdot 1)$$

$$= \frac{\pi \cdot 1}{3} (2^2 + 1^2 + 2 \cdot 1)$$

$$= \frac{\pi \cdot 1}{3} (4 + 1 + 2) = \frac{\pi \cdot 1}{3} (7) = \frac{8\pi}{3} \text{ cm}^3$$