

LISTA - FATORIAL DE NÚMEROS NATURAIS

EXERCÍCIOS:

1) a) $4! = 4 \cdot 3 \cdot 2 \cdot 1 = 24$

b) $5! - 6!$ $6! = 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 720$
 $120 - 720$ $5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 120$
 $- 600$

c) $\frac{9!}{6!} = \frac{9 \cdot 8 \cdot 7 \cdot 6!}{6!} = 504$

d) $\frac{98}{100} = \frac{98}{100 \cdot 99 \cdot 98} = \frac{1}{9900}$

2) $\frac{1-n}{n! \cdot (n+1)!} = \frac{1}{(n+1)!}$
 $\frac{1-n}{n! \cdot (n+1) \cdot n!} = \frac{n+1-n}{(n+1) \cdot n!} = \frac{1}{(n+1)!}$

3) $\frac{(n!)^2 - (n-1)! \cdot n!}{(n-1)! \cdot n!} = \frac{(n!) \cdot (n!) - (n-1)! \cdot n!}{(n-1)! \cdot n!} = \frac{n! - (n-1)!}{(n-1)!} =$
 $\frac{n(n-1)! - (n-1)!}{(n-1)!} = \frac{n-1 \cdot (n-1)!}{(n-1)!} = n-1$

$$(n+1)! (n-1)!$$

$$(n+1) \quad (n-1), (n-2)!$$

$(n-1)$

$$n+2 = 4n-4$$

$$3n = 6$$

6

$$(n+1)! \quad n+1$$

$$(n+1) \cdot \cancel{n!} \quad n+1$$

(b) $n \in \mathbb{N}, n \geq 1$
 $(n-1)![(n+1)! - n!] = (n-1)![(n+1)! - n!] = (n-1)! \cdot n! \cdot (n+1) = n! \cdot (n+1) = (n+1)!$

$$(n-1)!(n!n) = [n(n-1)!][n!] = (n!) \cdot (n!) = (n!)^2$$

7) $n! + (n-1)! = 6$

$$(n+1) \cdot n(n-1)! - n(n-1) \cdot (n+1) \cdot n - n$$

$$n(n+1)-1$$

$$25 \cdot (n+1) = 6 \cdot n^2$$

$$25n + 25 - 6n^2 = 0 \quad (-1)$$

$$6n^2 - 25n - 25 = 0$$

$$\Delta = -(-25)^2 - 4 \cdot 6 \cdot (-25)$$

$$\Delta = 625 + 600$$

$$\Delta = 1225$$

$$\Delta = 35$$

$$x = \frac{-(-25) \pm 35}{12} = \frac{60}{12} = 5 \quad (1+n)$$

$$x = \frac{25 - 35}{12} = \frac{-10}{12} = -\frac{5}{6}$$

$$8) \quad 21! - 22!$$

$$21 = 510909421709440000$$

$$22 = 112400072777607680000$$

1 2 3 4 5 6 7 8 9 10



7