



AGUDA is an imperative programming language composed of expressions alone.

A program in AGUDA is a sequence of declarations, each announced with keyword **let**. Value declarations introduce an identifier and a type. For example:

```
let maxSpeed : Int = 120
```

Declarations may also introduce functions, as in

```
let succ (n) : Int -> Int = n + 1
```

Functions can be recursive:

```
let add (n, m) : (Int, Int) -> Int =  
  if n == 0 then m else succ(add (n - 1, m))
```

or even mutually recursive:

```
let even (x) : Int -> Bool =  
  x == 0 || odd(x - 1)
```

```
let odd (x) : Int -> Bool =  
  x != 0 && even(x - 1)
```

Imperative means state changing. How do we change state? By means of (imperative) variables and assignment. Here's addition in imperative style:

```
let AddI (n, m) : (Int, Int) -> Int =  
  let sum : Int = m;  
  while n > 0 do (  
    set sum = sum + 1;  
    set n = n - 1  
  );  
  sum
```

A few points to notice:

- The body of the function is composed of three *expressions*, separated by a semicolon;
- The value of the function is given by the last expression in the semicolon separated sequence, namely, `sum`;

- The body of the **while** expression is a sequence of two expressions; we enclose them in parenthesis.
- Assignments are announced by the **set** keyword

Each expression has a value, including the **while** loop. The value of **while** is **unit**, the only value of type **Unit**. This means that we can “store” a while loop in a variable, as in

```
let x : Unit = while i > 0 do set i = i - 1
```

or “return” a while loop from a function, as in

```
let f (n) : Int -> Unit = while n > 0 do set n = n - 1
```

An assignment stores a value in a variable and returns the value. Given the below declaration, a call to `f (unit)` yields value 3.

```
let f (x) : Unit -> Int = let x : Int = let y : Int = 3
```

Equipped with the **unit** value, an if-then expression **if** `exp1` **then** `exp2` is an abbreviation for an if-then-else **if** `exp1` **then** `exp2` **else** **unit**.

Let us now look at the support provided for arrays. We start with an example: creating an $n \times n$ matrix, where all entries are 0, except for the diagonal which is filled with 1.

```
let diagonal (n) : Int -> Int[][] =
  let a : Int[][] = new Int[] [n | new Int [n | 0]] ;
  let i : Int = 0 ;
  while i < length(a) do (
    set a[i][i] = 1 ;
    set i = i + 1
  ) ;
  a
```

Expression `new Int [n | 0]` creates an integer array of size `n`, each cell initialised to 0. Likewise, `new Int[] [n | new Int [n | 0]]` creates a $n \times n$ matrix of zero values. Expression `set a[i][i] = 1` writes 1 in the *i*-th position of the *i*-th array of matrix `a`, that is, in line *i*, column *i* of `a`.

Below is a function that prints a matrix, line by line, each value terminated with a space. It includes two *primitive* functions: **length** returns the number of elements in an array; **print** sends to the prints `stdout` the textual representation of a given value. Both functions are overloaded: **length** works on any array; **print** accepts any value. More primitive functions shall be announced later.

```
let printMatrix (a) : Int[][] -> Unit =
  let i : Int = 0 ;
  while i < length(a) do (
```

```
while j < length(a[0]) do (  
  print(a[i][j]) ; print(" ") ;  
  set j = j + 1  
);  
print("\n") ;  
set i = i + 1  
)
```

A “little” main function exercises the two array-related functions.

```
let main : Unit =  
  printMatrix(diagonal(10))
```

Expressions

- Variable: `id`
- Literals: `...`, `-1`, `0`, `1`, `...`, `true`, `false`, `null`, in addition to quote-enclosed string literals
- Binary operators: `;` `+` `-` `*` `/` `%` `^` `==` `!=` `<` `<=` `>` `>=` `!` `||` `&&`
- Unary operators: `-` `!`
- Function call: `id(exp1, ..., expn)` with $n \geq 1$
- Assignment: `set LHS = exp`
- Variable declarations: `let id : type = exp`
- Conditionals: `if exp1 then exp2 else exp3` and `if exp1 then exp2`
- While loop: `while exp1 do exp2`
- Array creation: `new type [exp1 | exp2]`
- Array access: `exp1[exp2]`
- Parenthetical expression: `(exp)`

The left-hand-side (LHS) of an assignment, that is, the part at the left of `=`, can be:

- A variable
- An array location: `LHS[exp]`

Operator precedence and associativity

- For `+`, `-`, `*`, `/`, `%`, `==`, `!=`, `<`, `<=`, `>`, `>=`, `!`, `||`, `&&` take the precedence and associativity of the Java programming language
- The unary minus binds tighter than any other arithmetic operator
- The power operator, `^`, is right associative and binds tighter than any other arithmetic operator (different from unary minus). For example, `2 ^ - 3 ^ 4 * 5` is to be understood as `(2 ^ ((-3) ^ 4)) * 5`
- The sequencing operator, `;`, associates to the right and binds loser than all other operators. For example, `1 ; 2 || 3 ; 4` is to be understood as `1 ; ((2 || 3) ; 4)`
- The precedence of **while** loops and conditionals (both **if-then-else** and **if-then**) seats between that of `;` and `||`. For example, **while** `b` **do** `false || true` should be understood as **while** `b` **do** `(false || true)`, but **while** `b` **do** `false ; true` should be understood as `(while b do false) ; true`. Similarly for conditionals
- Keywords **then** and **else** associate to the right, so that **if** `a` **then** **if** `b` **then** `c` **else** `d` is to be understood as **if** `a` **then** `(if b then c else d)`
- The arrow type operator, `->`, associates to the right

Top-level declarations

- Variables: as in expressions
- Functions: **let** `id` (`id1`, ..., `idn`) : `type` = `exp` with $n \geq 1$

Programs A non-empty sequence of declarations.

Types

- Basic: **Int**, **Bool**, **Unit**, **String**
- Array: `type[]`
- Function: `type -> type` or `(type1, ..., typen) -> type` with $n \geq 1$. There are no zero-ary functions. If needed, use `f (_) : Unit -> type = exp` and call as `f (unit)`.

Lexing

- Identifiers (variable or function names) start with a letter and are followed by zero or more letters, digits, underscore symbols (`_`) and single quotes (`'`)
- Integer values start with an optional sign, followed by a non-zero digit and then followed by zero or more digits
- Strings are sequences of characters (not including new line), enclosed in quotes (`"`)
- Comments: Line comments only, starting with `--`.