

Motivation
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DP
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HP
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DHP
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PDP
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PDHP
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Houston
oooooooooooo

Conclusion
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Dirichlet-Point processes

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November 2021



Introduction

- Every minute:

 400h of video
 350 000 tweets

 500 000 comments
 4 200 000 searches

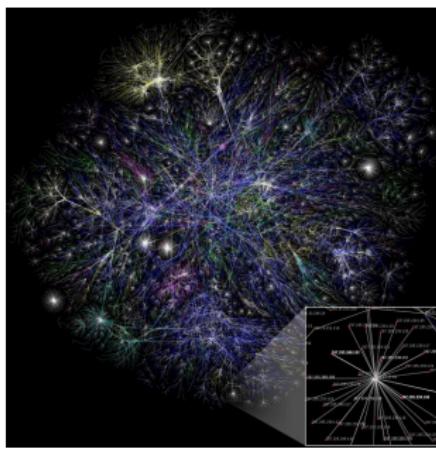


Figure 1: Snapshot of the internet (Wikipedia)

Motivation

- Every minute:



400h of video



350 000 tweets



500 000 comments



4 200 000 searches

- How to make sense out of *that*?

- 1 News - Peering into the future? Facebook's 2 days ago
- 1 News - More Antarctic penguin research identifies travel's 3,000km to New Zealand's 2 days ago
- 1 News - 200 million Americans... 3 weeks ago
- 1 News - Protecting athletes... 3 years ago
- 1 News - The NYPD is using machine learning to spot crime patterns | StateScreener.com 3 years ago
- 1 News - 75 updates 37 comments 4 weeks ago
- 1 News - Protecting athletes 23 days ago
- 1 News - Climate change: Major US oil companies face grilling by Congress 23 days ago
- 1 News - 75 updates 37 comments 3 weeks ago
- 1 News - Protecting athletes 3 years ago
- 1 News - Efficient algorithms outperform deep-learning machines at video 79 updates 32 comments 4 weeks ago

- 1 Chees** - Posted by [@chees](#) (only 2 years ago)
- Powerful antibiotic discoscovered using machine learning for first time**
11K upvotes, 1K comments - 10 days ago
- 1 Chees** - Posted by [@chees](#) (only 13 days ago)
- New extratives predict climate change is coming for crops sooner than we thought**
2.1K upvotes, 2K comments - 8 days ago
- 1 Chees** - Posted by [@chees](#) (only 3 days ago)
- U.S. holds historic oil and gas lease sale in Gulf of Mexico days after summit**
1.7K upvotes, 17K comments - 6 days ago
- 1 Chees** - Posted by [@chees](#) (only 10 days ago)
- Doug the ugly New Zealand potato could be world's biggest**
www.vice.com

-  **Cheyne** - Posted by [Cheyne](#) 4 days ago
New Zealand's Covid-19 cases touch all-time high, govt pushes for vaccination
1,080 replies · 10 comments · 3 hours ago
-  **Cheyne** - Posted by [Cheyne](#) 5h ago
\$150m+ - Thousands protest in New Zealand against COVID-19 rules.
116 replies · 10 comments · 5h ago
-  **Cheyne** - Posted by [Cheyne](#) 3 months ago
Only Humans, Not AI Machines, Can Get a U.S. Patent, Judge Rules
8,816 replies · 10 comments · 3 months ago
-  **Cheyne** - Posted by [Cheyne](#) 2 years ago
Earth gets hotter, deadlier during decades of climate talk
1,258 replies · 10 comments · 2 years ago

Figure 2: A typical stream from r/news

Motivation

- Every minute:



400h of video



350 000 tweets



500 000 comments



4 200 000 searches

- How to make sense out of *that*?
→ Hidden semantic links

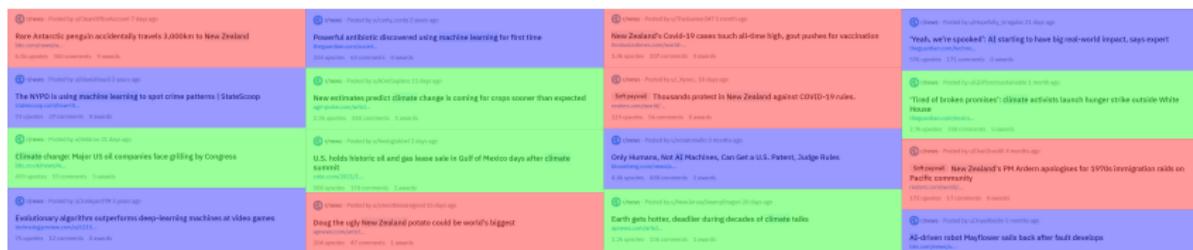


Figure 2: A typical stream from r/news – with topics

Available information

- Main clues:
 - Textual information

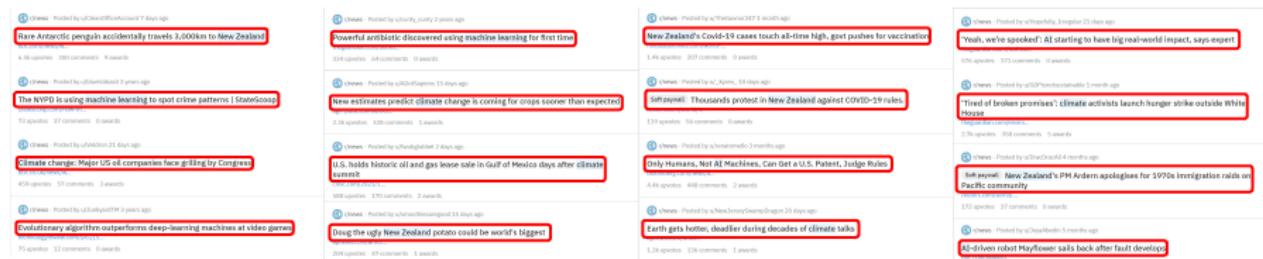


Figure 3: We can use textual information

Available information

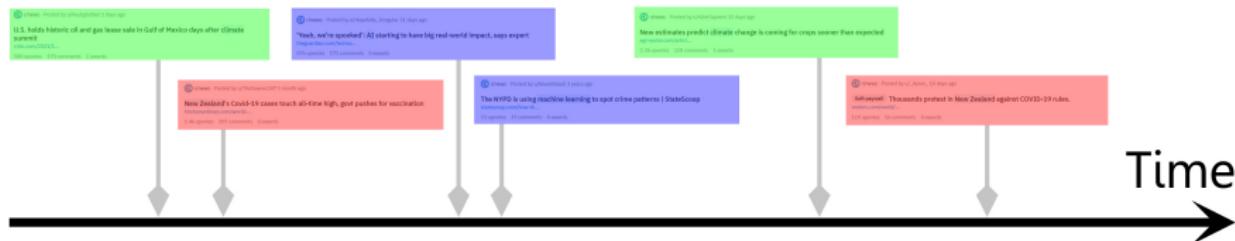
- Main clues:
 - Textual information
 - Temporal information



Figure 3: We can use textual information and temporal information

Documents stream

- The data is therefore a documents stream



Dirichlet process

- Dirichlet processes fit to consider streams as inputs
- Dirichlet distribution: $\vec{X} \sim Dir(\alpha)$ s.t. $\sum_k X_k = 1$
- Often used as a prior distribution in Bayesian clustering
 - ◊ Typically X_k is the probability to belong to cluster k
- Can be represented in several ways:
 - ◊ Stick-breaking process
 - ◊ Polya-Urn process
 - ◊ Chinese restaurant process

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Chinese restaurant process

$$CRP(C_i = c | C_1, C_2, \dots, C_{i-1}, \alpha) = \begin{cases} \frac{N_c}{\alpha + N} & \text{if } c = 1, \dots, K \\ \frac{\alpha}{\alpha + N} & \text{if } c = K+1 \end{cases}$$



Handling a stream of documents

$$CRP(C_i = c | C_1, C_2, \dots, C_{i-1}, \alpha) = \begin{cases} \frac{N_c}{\alpha + N} & \text{if } c = 1, \dots, K \\ \frac{\alpha}{\alpha + N} & \text{if } c = K+1 \end{cases}$$

- Useful for sequential modeling (explicit prior at each step, allows Gibbs sampling)

$$\underbrace{P(n^{th} obs = c | D, history)}_{Posterior} \propto \underbrace{P(D | n^{th} obs = c)}_{Likelihood} \times \underbrace{P(n^{th} obs = c | history)}_{CRP \ prior}$$

- “rich-get-richer” hypothesis

Variants

- Variants of DP exist:
 - ◊ Uniform process [Wallach et al., 2010]
 - ◊ Pitman-Yor process [Pitman and Yor, 1997]
 - ◊ Hierarchical Dirichlet process [Teh et al., 2006]
 - ◊ Nested Dirichlet process [Rodríguez et al., 2008]

- All consider counts
- Most exhibit “rich-get-richer” property
- No temporal dimension

Modeling time as a continuous variable

- Time often “modeled” by sampling observations (DTM [Blei and Lafferty, 2006], TOT [Wang and McCallum, 2006], RCRP [Ahmed and Xing, 2008], DDCRP [Blei and Frazier, 2010], etc.)
 - ◊ Problems: how to slice data, which sampling function use, how to weight observations, etc.
- Whole literature modeling time explicitly: point processes

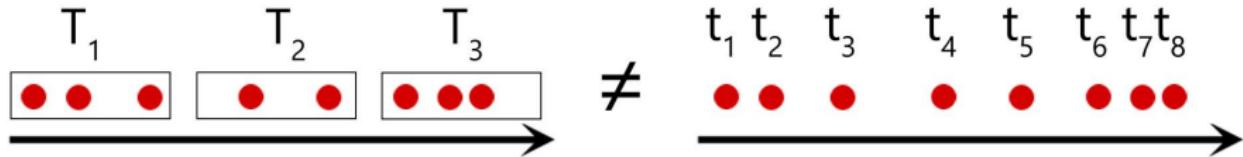


Figure 4: Data sampling/slicing is an approximation

Poisson process

- Poisson processes are characterized by an **intensity** λ .
 - ◊ $P(\mathbb{N}(t) = n) = \frac{(\lambda t)^n}{n!} e^{-\lambda t}$ = probability for n events to happen within a time t
- Instantaneous PDF of **one** event (or inter-arrival time PDF):

$$f(t) = \frac{P(\mathbb{N}(t) = 1)}{t} = \lambda e^{-\lambda t}$$

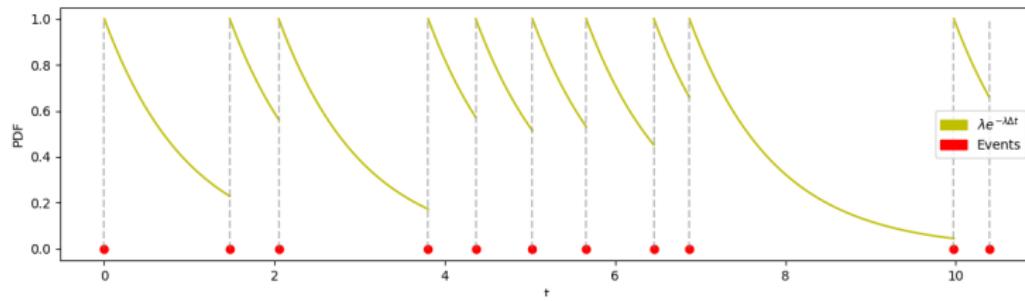


Figure 5: Could model radioactive decay events of atoms whose half-life is 1

Non-homogeneous Poisson process

- $\lambda(t)$ is a function
 - $\lambda(t) = \lim_{\Delta t \rightarrow 0} \frac{P(\mathbb{N}(t+\Delta t) - \mathbb{N}(t) = 1)}{\Delta t}$

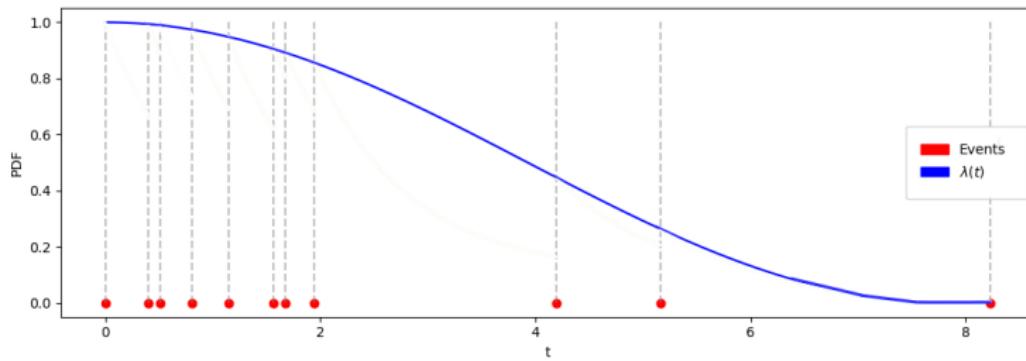


Figure 6: Could model cars arrival at gas station throughout a day

Hawkes process

- Hawkes processes: $\lambda(t)$ depends on past events $\mathcal{H}_t = \{t_i | t_i < t\}$
→ “Self-exciting process”
- Typically: $\lambda(t) = \lambda_0 + \sum_{t_i \in \mathcal{H}_t} \phi(t - t_i)$

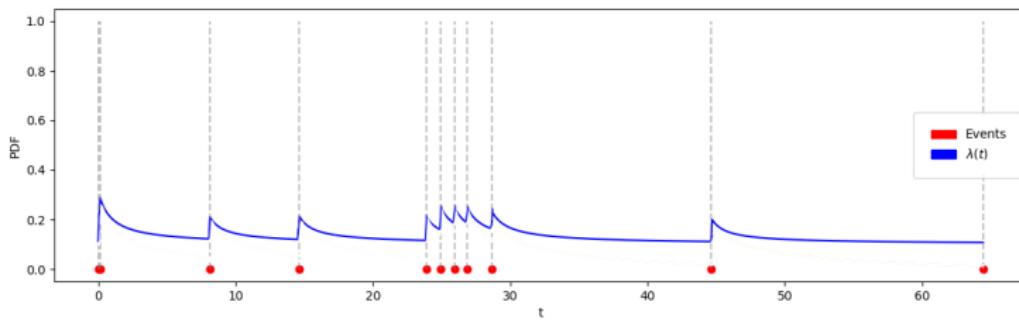


Figure 7: Could model online posting dynamics

Inference

- Log-likelihood $\mathcal{L}(\lambda)$ fit for data streams:

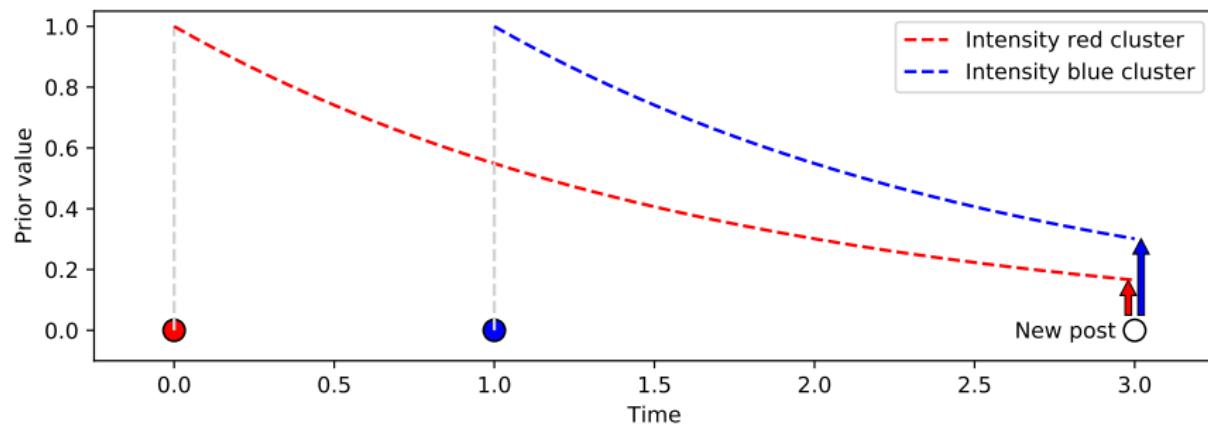
$$\begin{aligned} - \int_{t_0}^{t_N} \lambda(t) dt + \sum_{t_i < t_N} \log \lambda(t_i) &= \log \lambda(t_1) - \int_{t_0}^{t_1} \lambda(t) dt \\ &\quad + \log \lambda(t_2) - \int_{t_1}^{t_2} \lambda(t) dt \\ &\quad + \dots \\ &\quad + \log \lambda(t_N) - \int_{t_{N-1}}^{t_N} \lambda(t) dt \end{aligned}$$

- Convex for certain shapes of $\lambda(t)$ (exp, ray, PL, Gaussian, ...).

Dirichlet-Hawkes process

- [Du et al., 2015]: Dirichlet-Hawkes prior (Bayesian inference)
- Merges Dirichlet priors and Hawkes processes

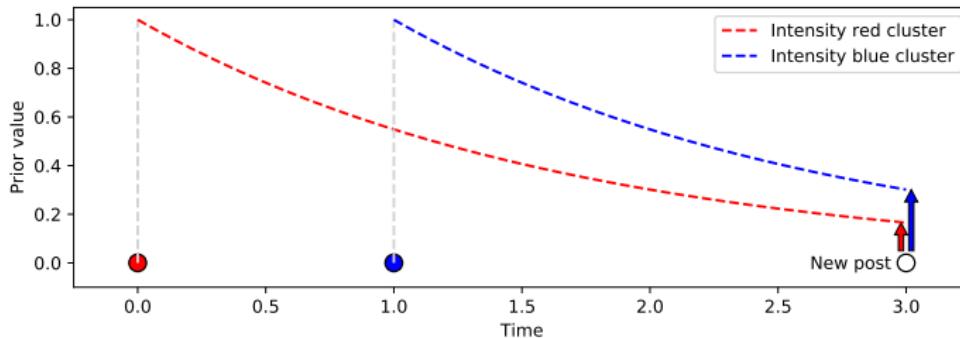
$$P(\text{cluster}|\text{text}, \text{time}, H) \propto \underbrace{P(\text{text}|\text{cluster})}_{\text{Textual likelihood} \\ (\text{Dirichlet-Multinomial})} \times \underbrace{P(\text{cluster}|\text{time}, H)}_{\text{Temporal prior} \\ (\text{Dirichlet-Hawkes})}$$



Dirichlet-Hawkes process – Explicit

- $P(c|t, \mathcal{H})$: prior probability of cluster c at time t given history \mathcal{H}
- $\lambda_c(t)$: intensity of cluster c at time t
- Dirichlet process with counts N_c replaced by $\lambda_c(t)$

$$\underbrace{P(c|t, \mathcal{H})}_{\substack{\text{Temporal prior} \\ (\text{Dirichlet-Hawkes})}} = \begin{cases} \frac{\lambda_c(t)}{\alpha_0 + \sum_k \lambda_k(t)} & \text{if } c = 1, \dots, K \\ \frac{\alpha_0}{\alpha_0 + \sum_k \lambda_k(t)} & \text{if } c = K+1 \end{cases}$$



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PDHP

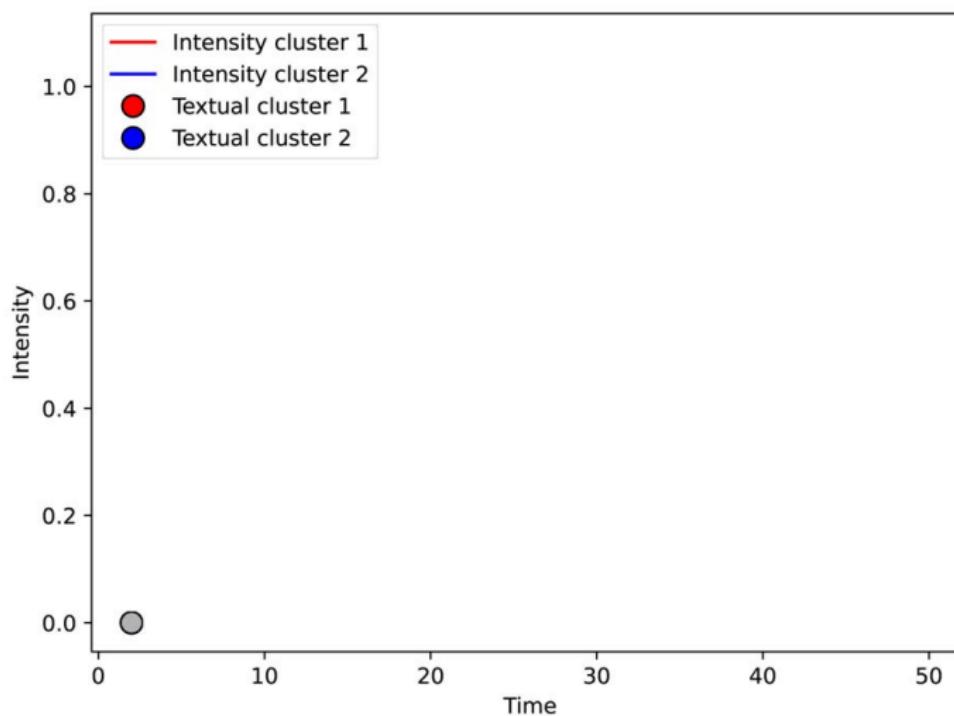
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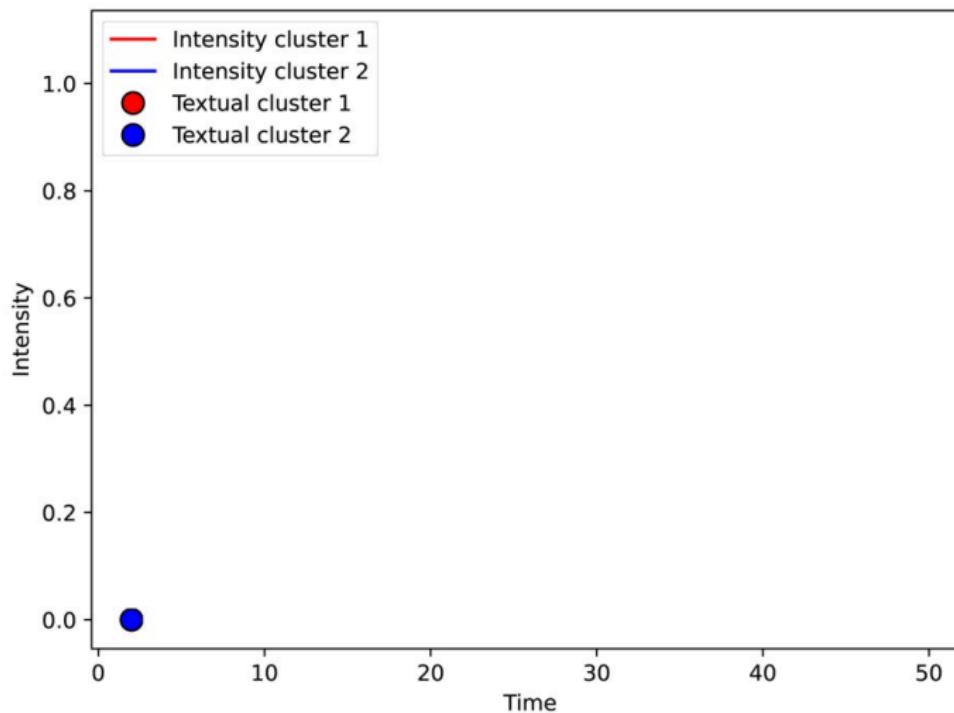
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Conclusion

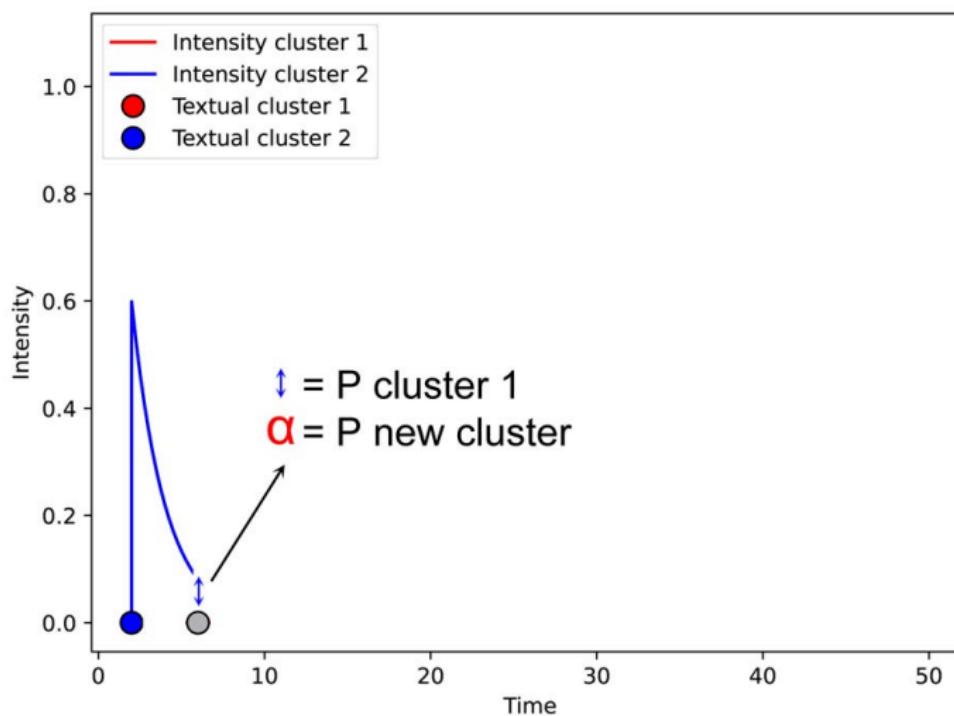
Inference (1 particle)



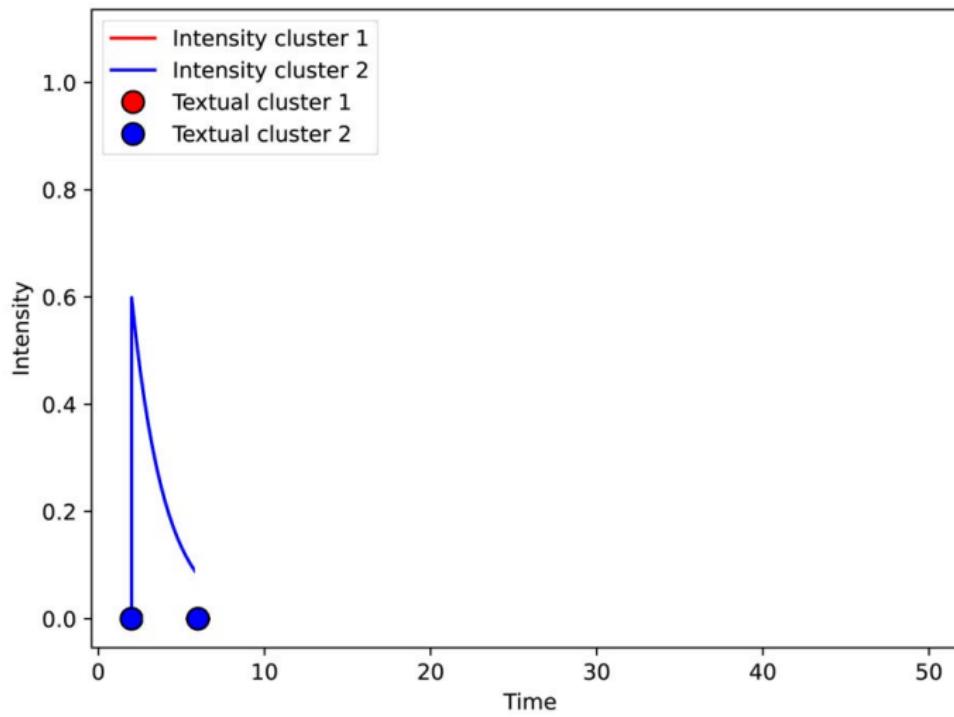
Inference (1 particle)



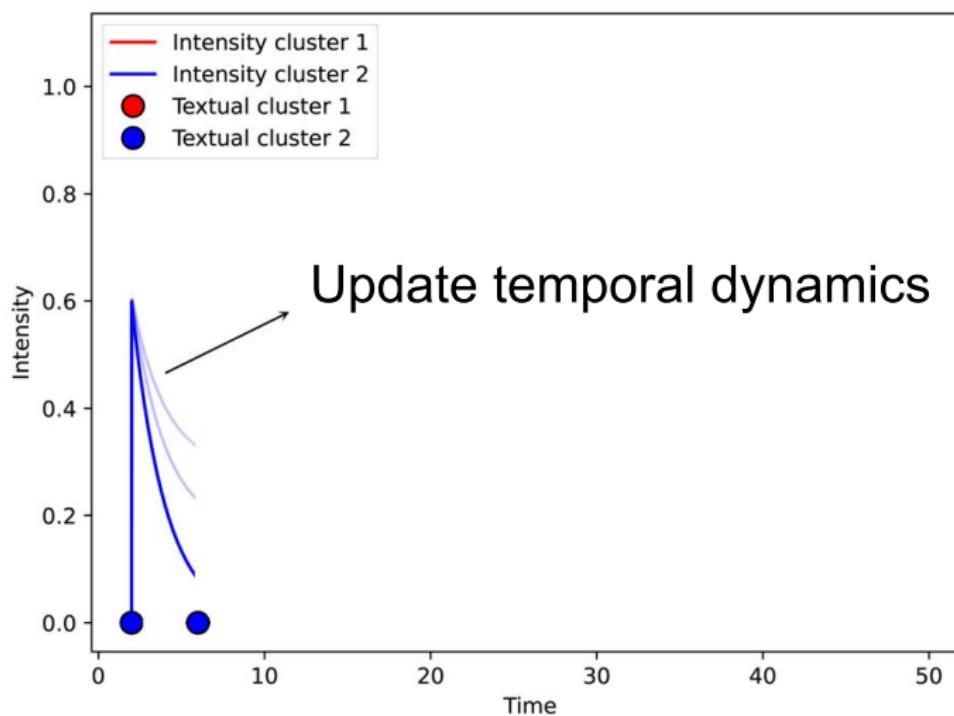
Inference (1 particle)



Inference (1 particle)

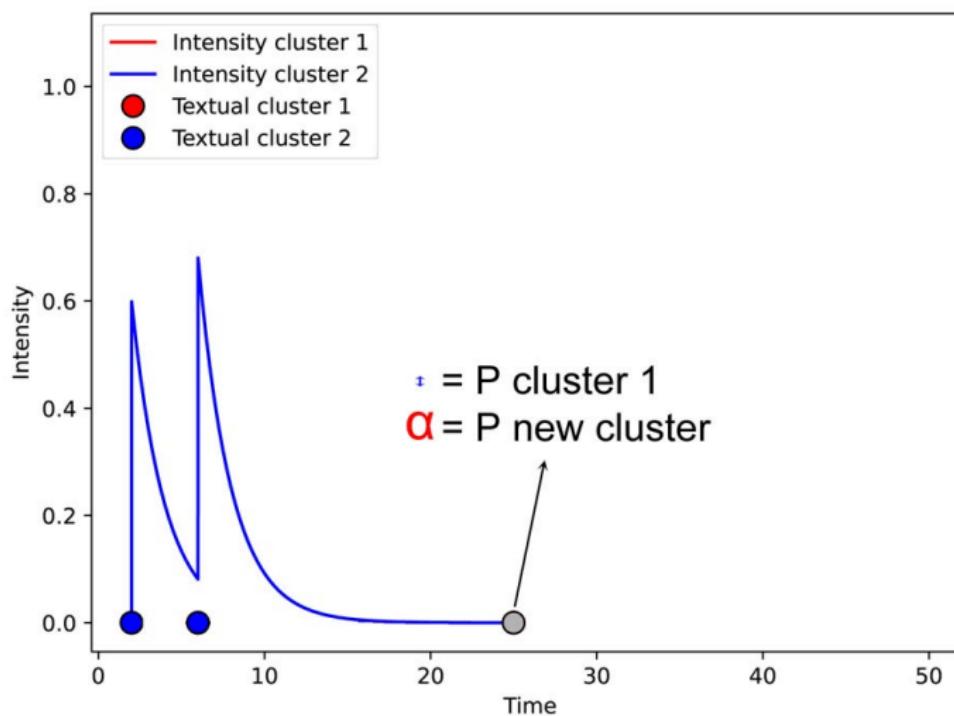


Inference (1 particle)

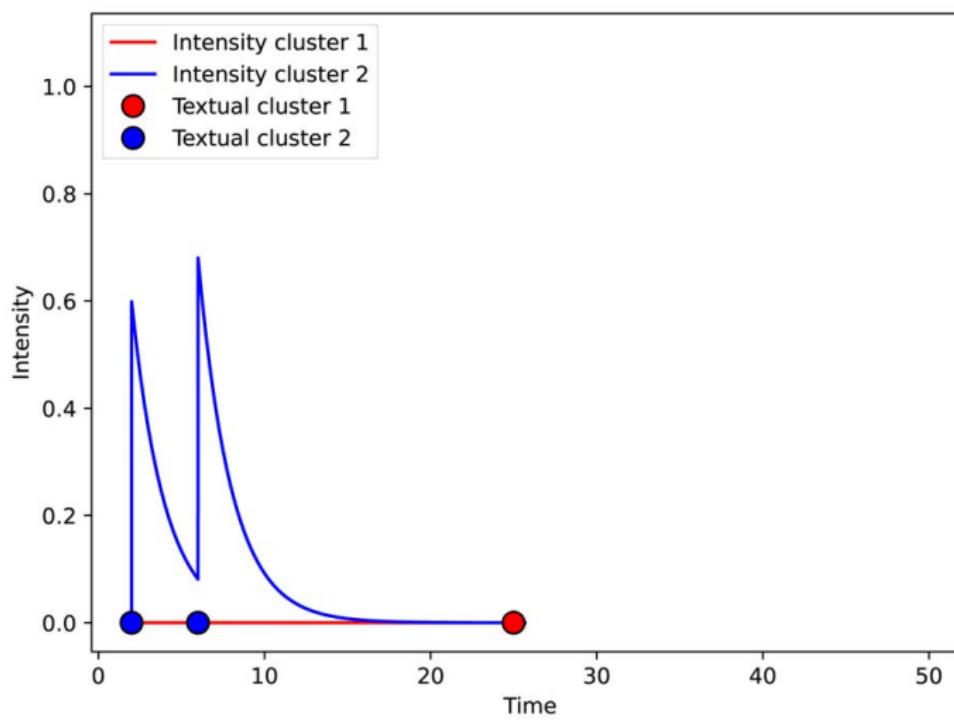


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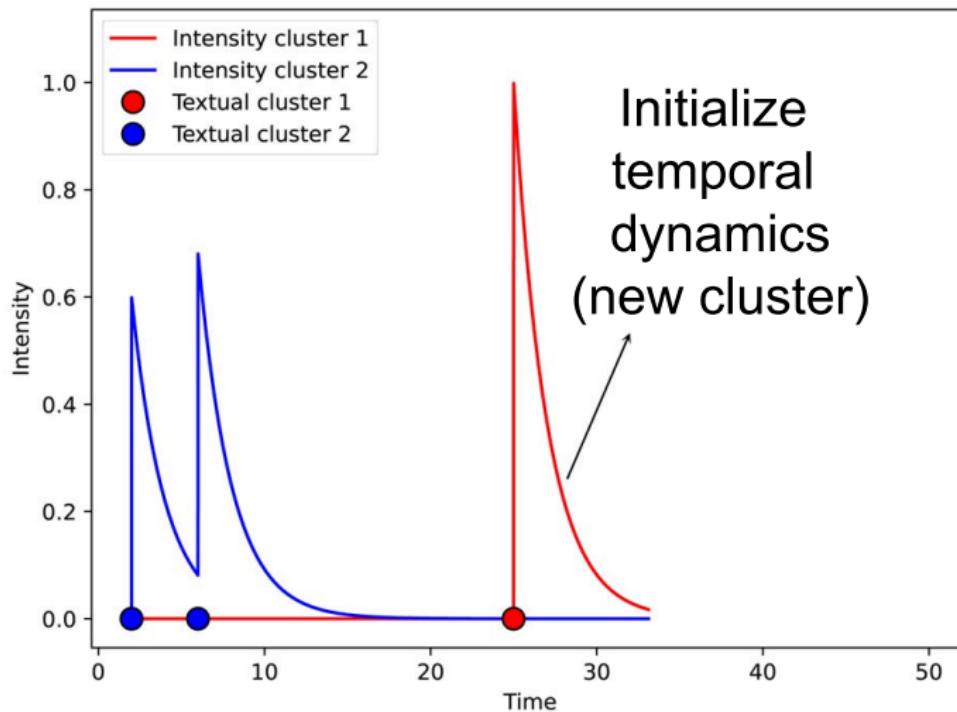
Inference (1 particle)



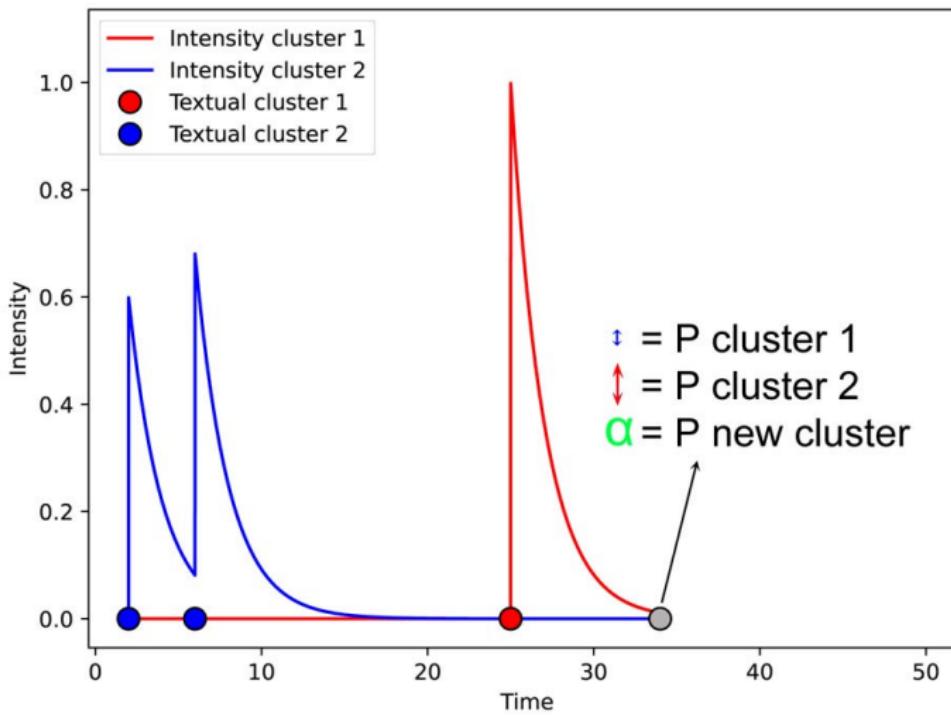
Inference (1 particle)



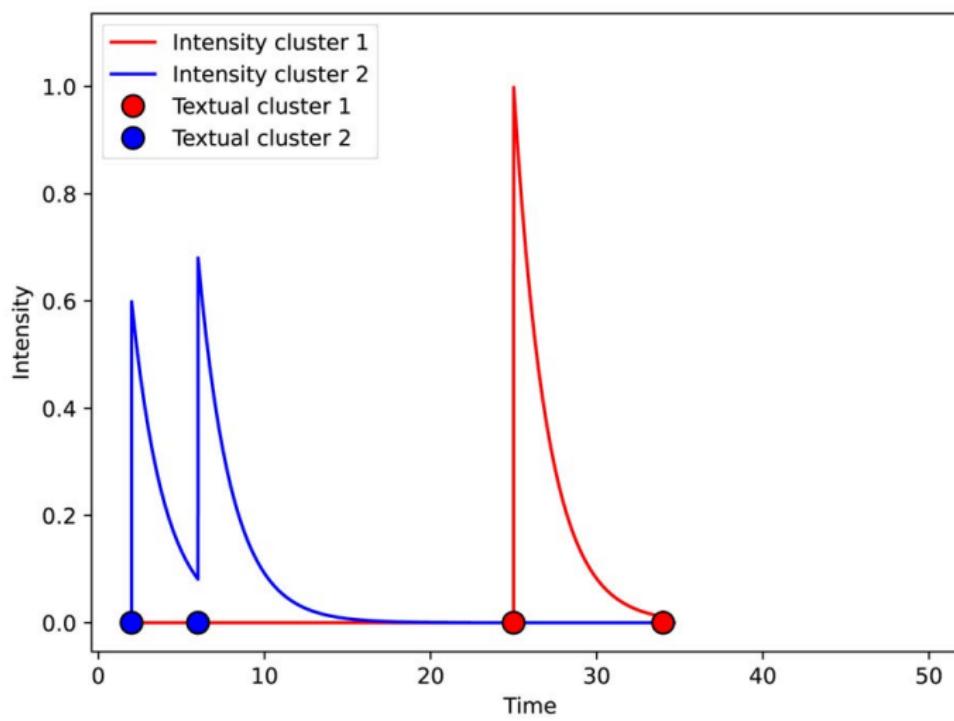
Inference (1 particle)



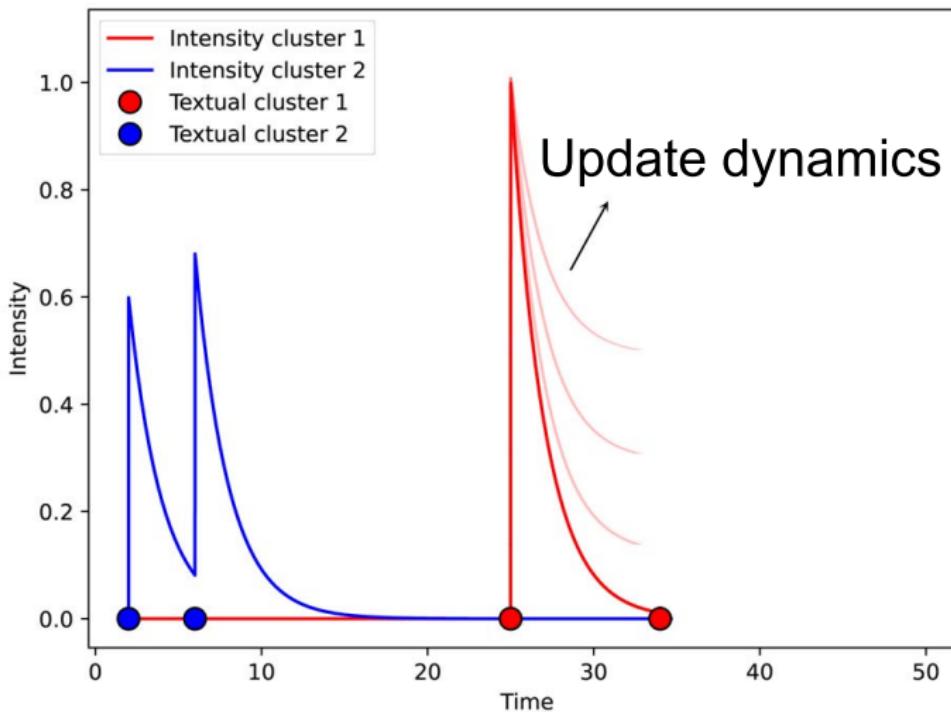
Inference (1 particle)



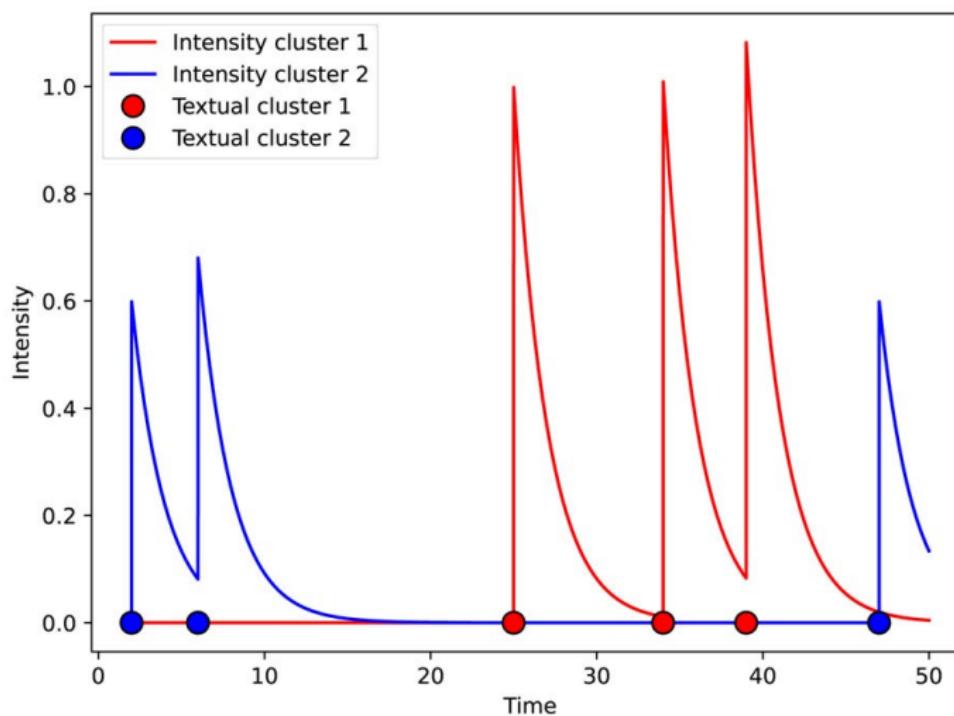
Inference (1 particle)



Inference (1 particle)

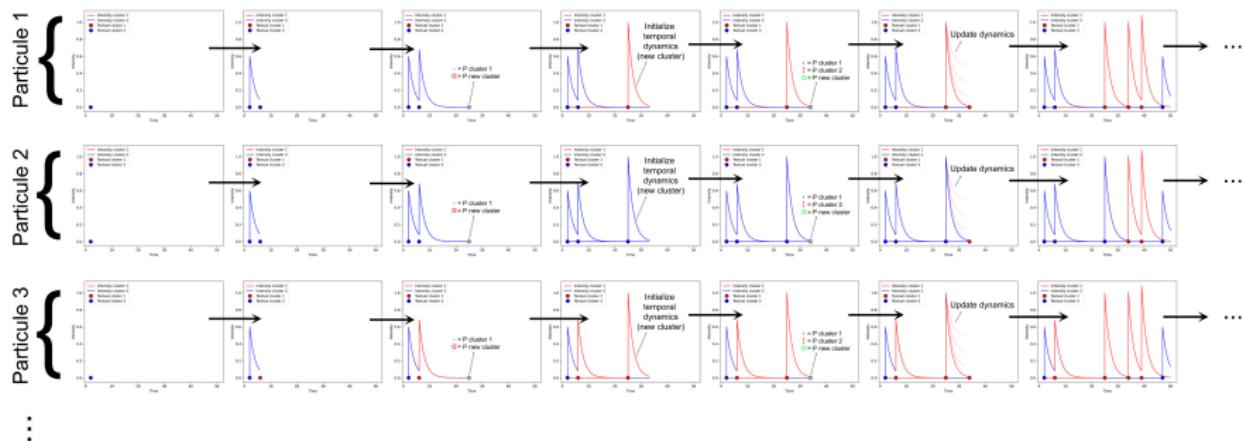


Inference (1 particle)



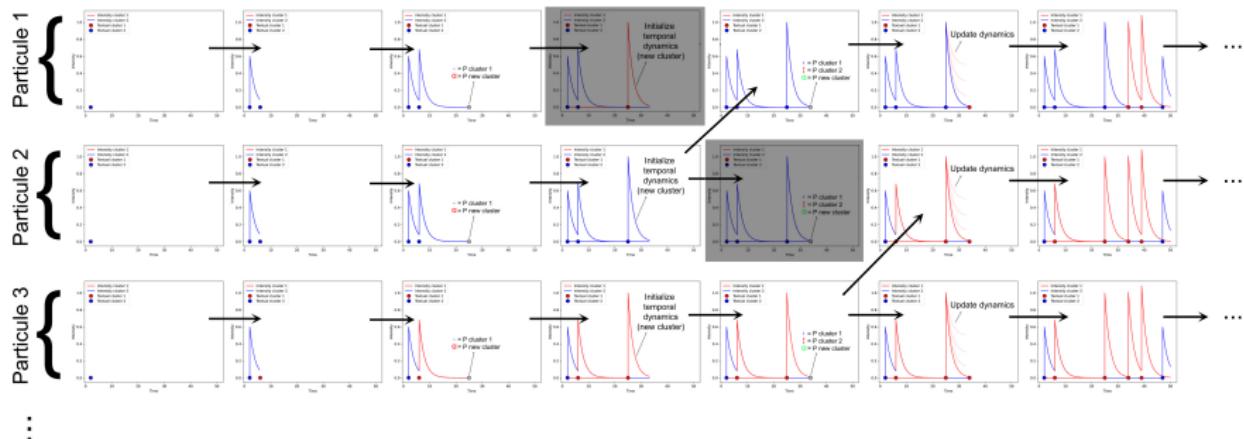
Inference (all particles)

- Run simultaneously on several *particles*



Inference (all particles)

- Discard unlikely particles and replace them by more likely ones

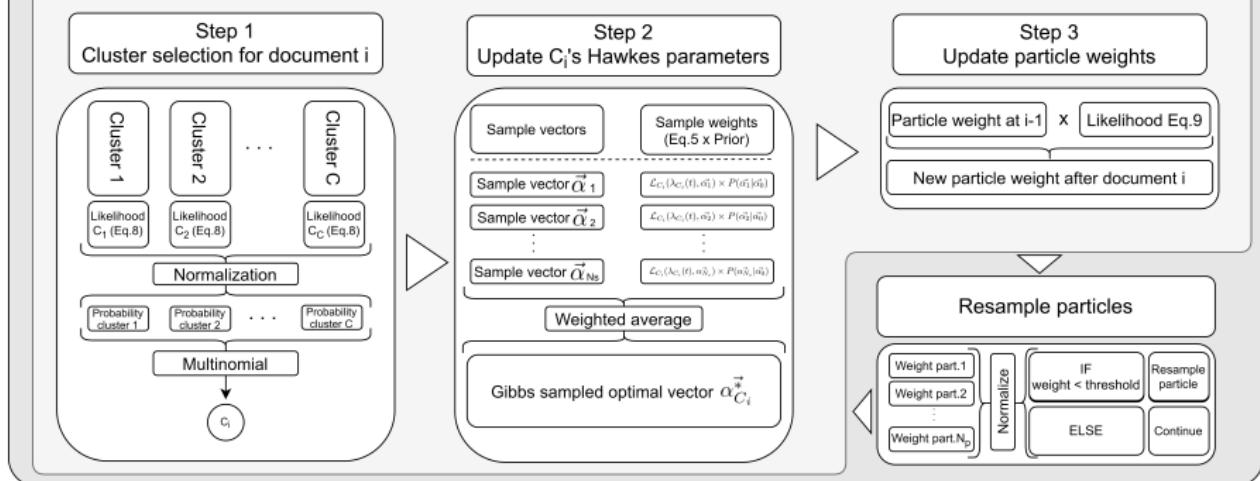


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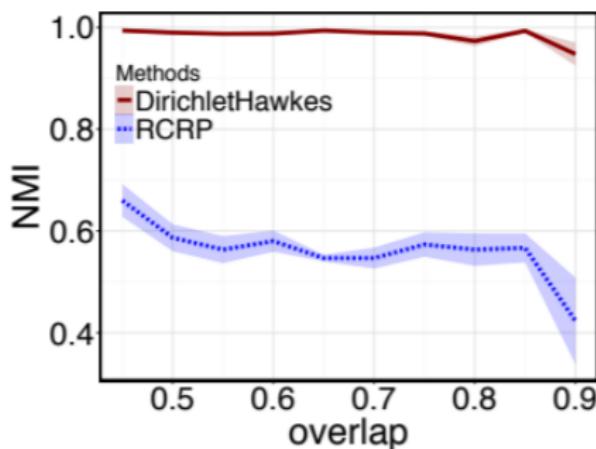
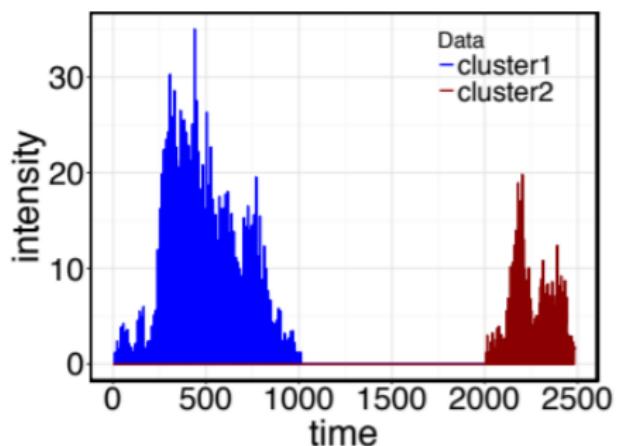
Inference (summarized)

For each new document

For each particle



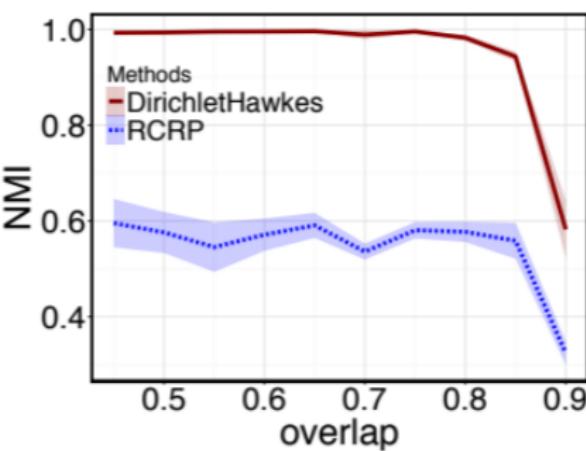
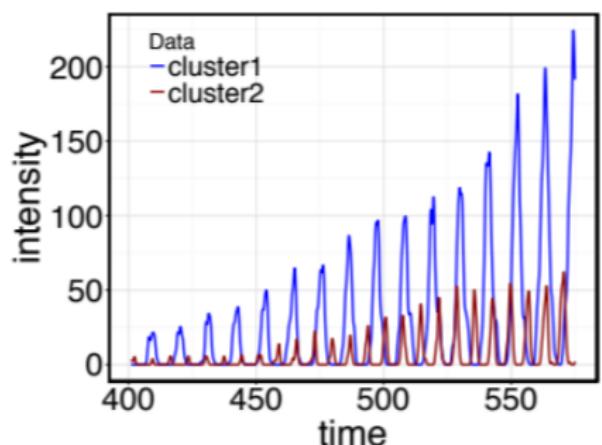
Performances (well-separated)



(a) Temporally well-separated clusters.

Figure 10: [Du et al., 2015]

Performances (“not” well-separated)



(b) Temporally interleaved clusters.

Figure 11: [Du et al., 2015]

Output

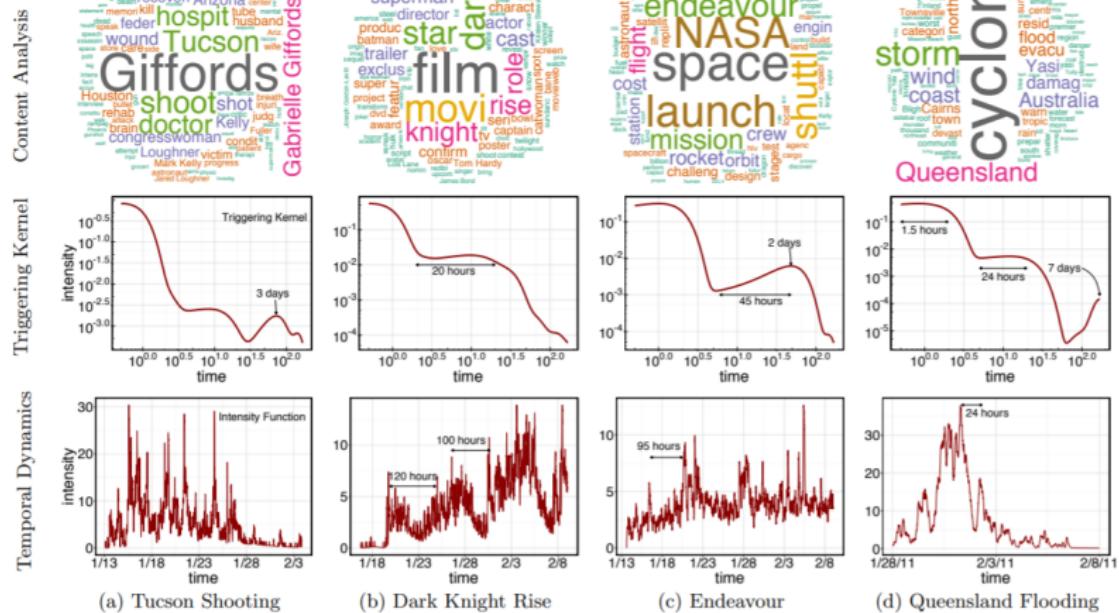


Figure 12: [Du et al., 2015]

Variants

- Numerous variants based on Dirichlet-Hawkes process
 - Hierarchical (CRF) and Nested (nCRP) extensions of DHP
 - Multivariate DHP [Zheng et al., 2021]
 - Not-vanishing DHP prior [Kapoor et al., 2018]

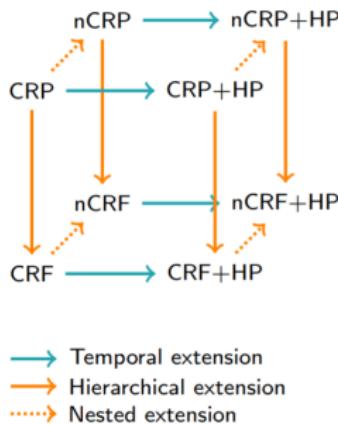


Figure 13: [Kapoor et al., 2018]

Dirichlet prior is a choice

- Dirichlet-based priors are an arbitrary choice
 - ◊ Other priors are as fit [Welling, 2006]
 - ◊ The choice of the prior matters [Wallach et al., 2009]
 - ◊ Few variations proposed [Wallach et al., 2010, Pitman and Yor, 1997]
- DP exhibits “rich-get-richer” property
 - ◊ Why linear dependence?
 - ◊ Why this assumption at all? [Wallach et al., 2010]

Powered Dirichlet process

- Powered Chinese Restaurant Process:

$$PCRP(C_i = c | C_1, \dots, C_{i-1}, \alpha, r) = \begin{cases} \frac{N_c^r}{\alpha + \sum_k N_k^r} & \text{if } c = 1, \dots, K \\ \frac{\alpha}{\alpha + \sum_k N_k^r} & \text{if } c = K+1 \end{cases}$$

- ◊ $r < 0$: “rich-get-poorer”
- ◊ $r = 0$: “rich-get-no-richer” (Uniform Process)
- ◊ $0 < r < 1$: “rich-get-less-richer”
- ◊ $r = 1$: “rich-get-richer” (Dirichlet Process)
- ◊ $r > 1$: “rich-more-richer”

PDP impact

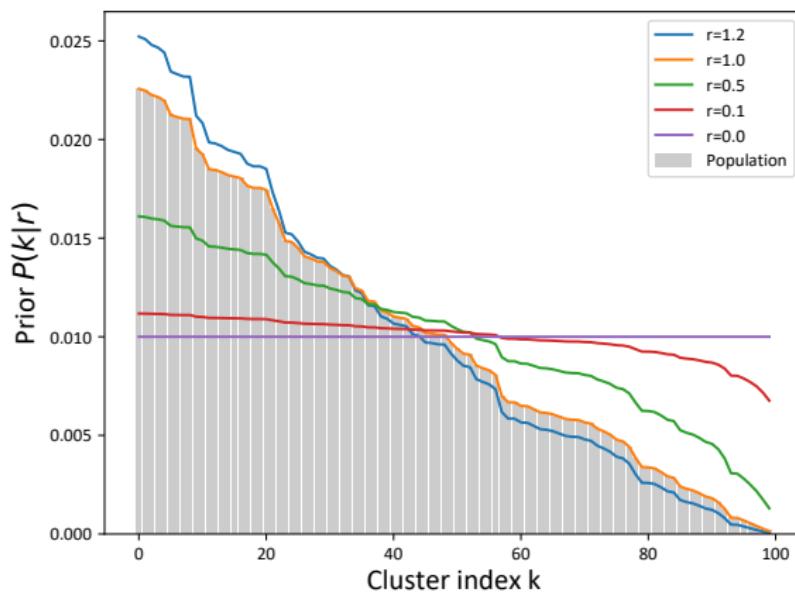
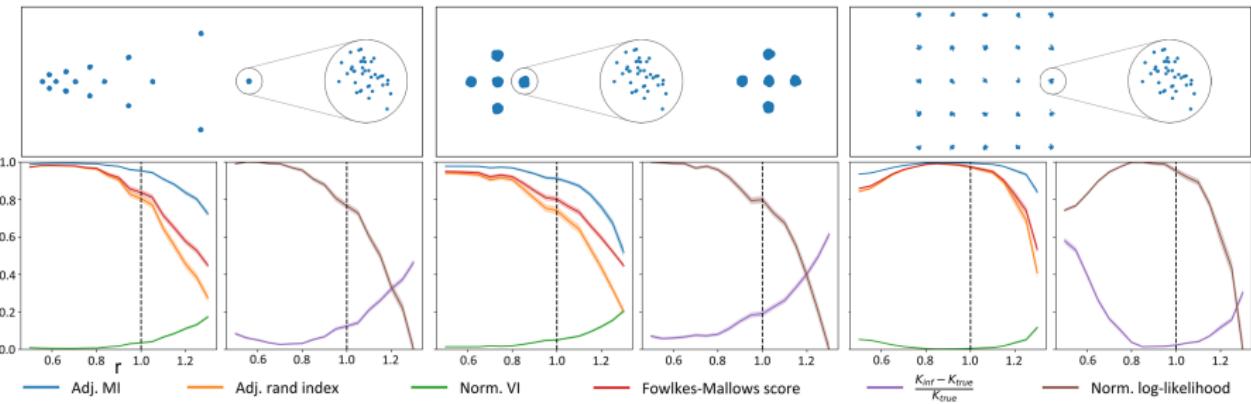


Figure 14: Prior probability for each of 100 clusters whose population is known (grey bars) w.r.t. r

Results

- Use as prior for IGMM
- DP not always the best prior



PDP into DHP

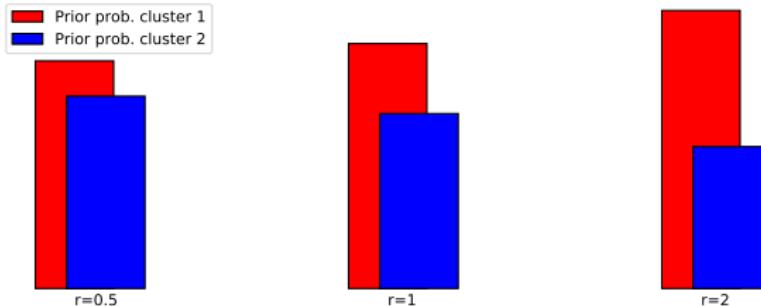
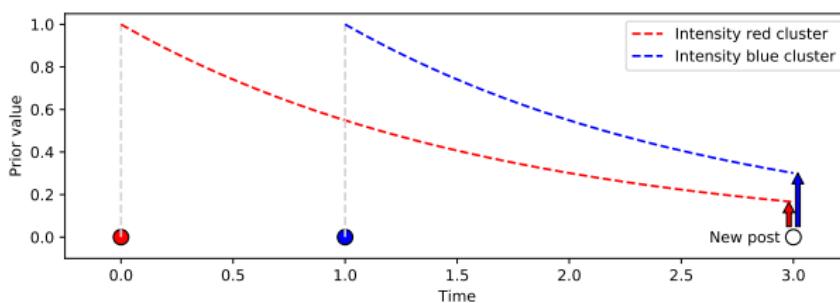
- Powered priors: controlling the informativeness of the prior
 - ◊ PDP: strength of the “rich-get-richer” hypothesis
 - ◊ PDHP: strength of the temporal dependence hypothesis
- PDHP [Poux-Médard et al., 2021]:

$$\underbrace{P(c|t, \mathcal{H}, \textcolor{red}{r})}_{\text{PDHP prior}} = \begin{cases} \frac{\lambda_c(t)^{\textcolor{red}{r}}}{\alpha_0 + \sum_k \lambda_k(t)^{\textcolor{red}{r}}} & \text{if } c = 1, \dots, K \\ \frac{\alpha_0}{\alpha_0 + \sum_k \lambda_k(t)^{\textcolor{red}{r}}} & \text{if } c = K+1 \end{cases}$$

- Generalization:
 - ◊ Uniform process: $r = 0$ (only textual information)
 - ◊ Dirichlet-Hawkes process: $r = 1$ (temporal and textual information)
 - ◊ Deterministic Hawkes process: $r \rightarrow \infty$ (only temporal information)

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Effect of r



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Changes induced by PDHP

$$P(\text{cluster}|\text{text}, \text{time}) \propto \underbrace{P(\text{text}|\text{cluster})}_{\text{Textual likelihood}} \times \underbrace{P(\text{cluster}|\text{time}, r, \text{history})}_{\text{PDHP temporal prior}}$$

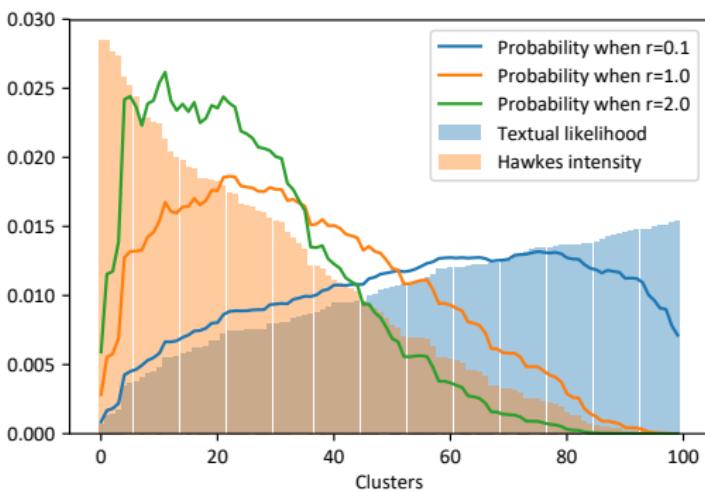


Figure 15: [Poux-Médard et al., 2021]

Why is it relevant - Overlaps

- In general, when a piece of information is more informative than the other:
 - ◊ Twitter: short texts (few information) but informative cascade dynamics
- Happens often because of overlaps:

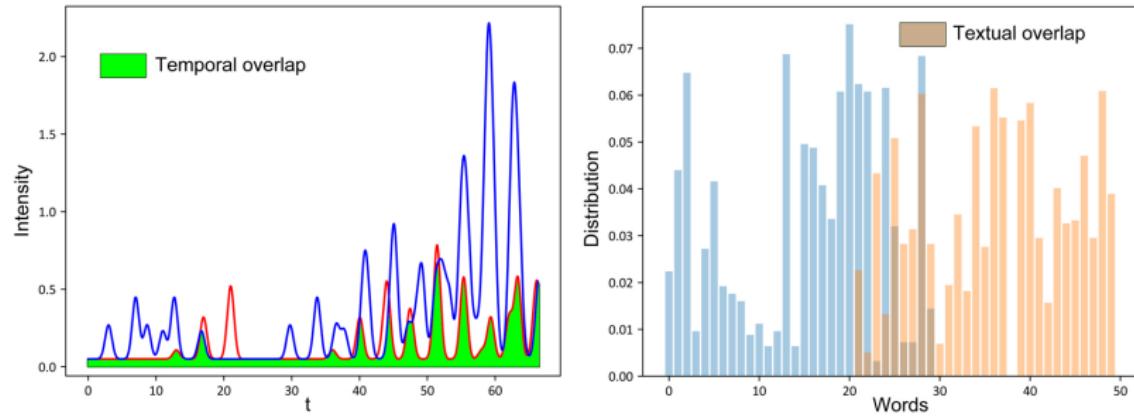
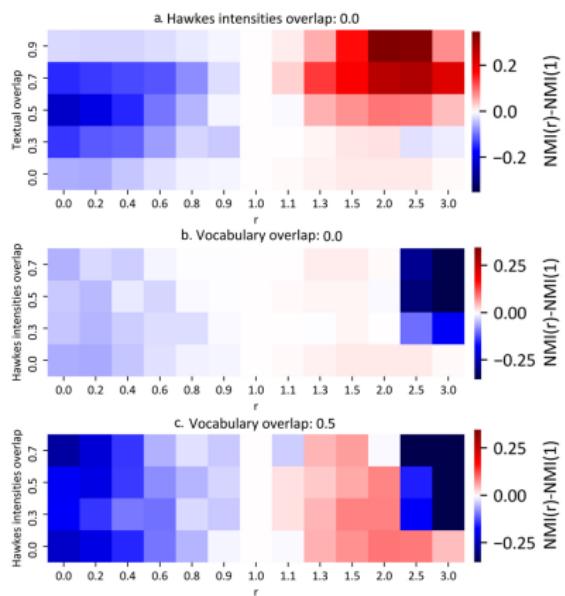


Figure 16: [Poux-Médard et al., 2021]

Results for various overlaps



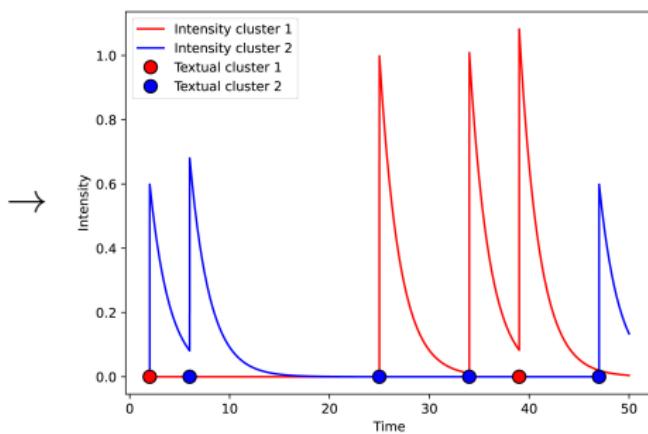
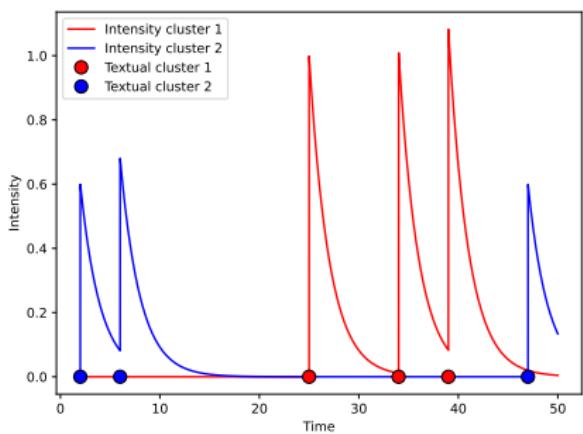
- PDHP adapts to various situations better than DHP:
 - ◊ Large textual overlap
 - ◊ Large temporal overlap
 - ◊ No overlap
- Up to +0.3 NMI in our case

Figure 17: [Poux-Médard et al., 2021]

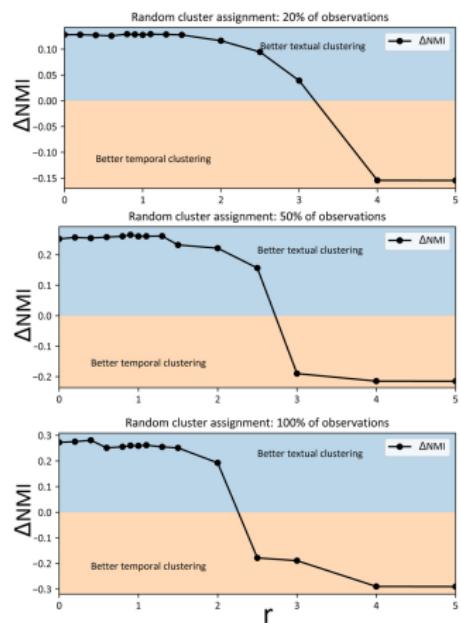
Why is it relevant - Decorrelations

- Decorrelations:

- ◊ Ex: influent journal publishing on a topic does not have same dynamics as less influent one on the same topic



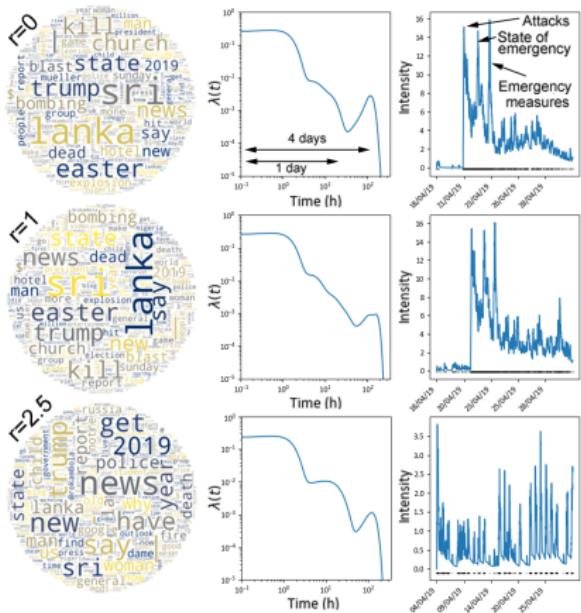
Results for various decorrelations



- PDHP retrieves either temporal or textual clusters
 - ◊ Small r : good textual clusters
 - ◊ Large r : good temporal clusters

Figure 18: [Poux-Médard et al., 2021]

Reddit r/news - Typical output



- Real world data: r/news
- Different clusters and dynamics for different r
 - ◊ Small r : similar vocabulary
 - ◊ Large r : specific dynamics

Figure 19: [Poux-Médard et al., 2021]

Reddit r/news, r/TodayILearned, r/AskScience - Some metrics

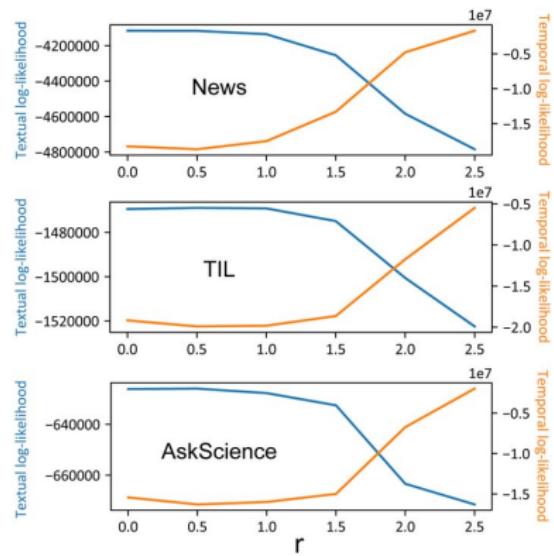


Figure 20: Textual and temporal likelihood vs r
[Poux-Médard et al., 2021]

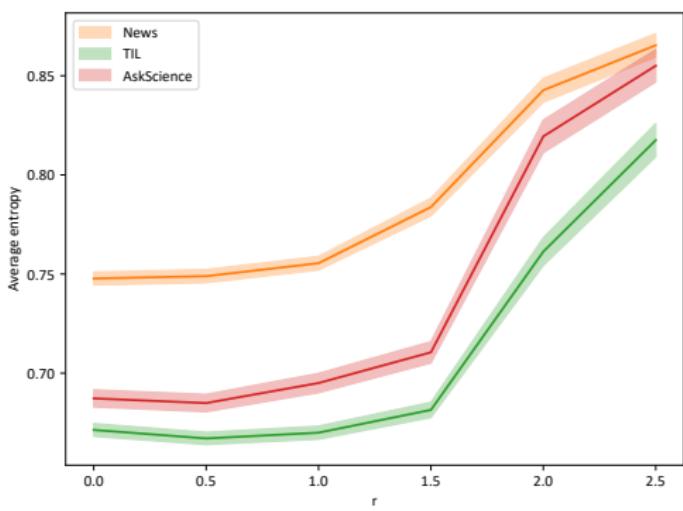


Figure 21: Entropy of textual clusters:
sharper textual clusters for low r
[Poux-Médard et al., 2021]

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Conclusion
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Structure matters!

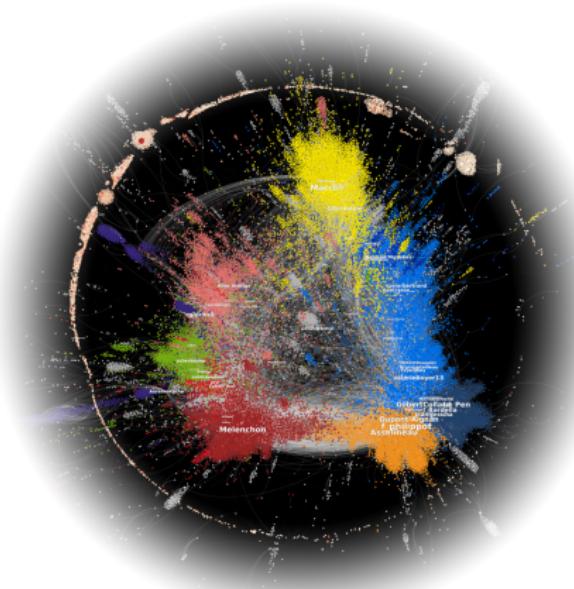


Figure 22: A sample from the Twitter structure (Politoscope [Gaumont et al., 2018])

Why (P)DHP is incomplete

- DHP prior accounts for time but not structure
 - ◊ Infers aggregated dynamics
 - ◊ Misses the structural aspect: discussions are not the same among different groups

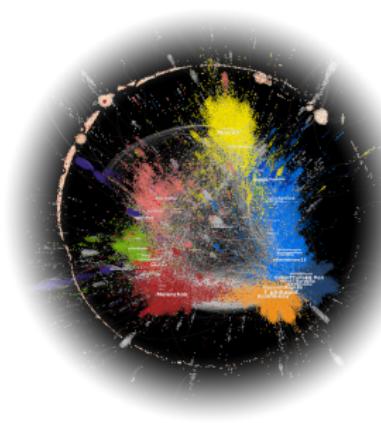
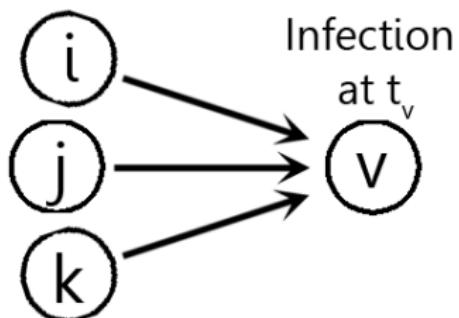


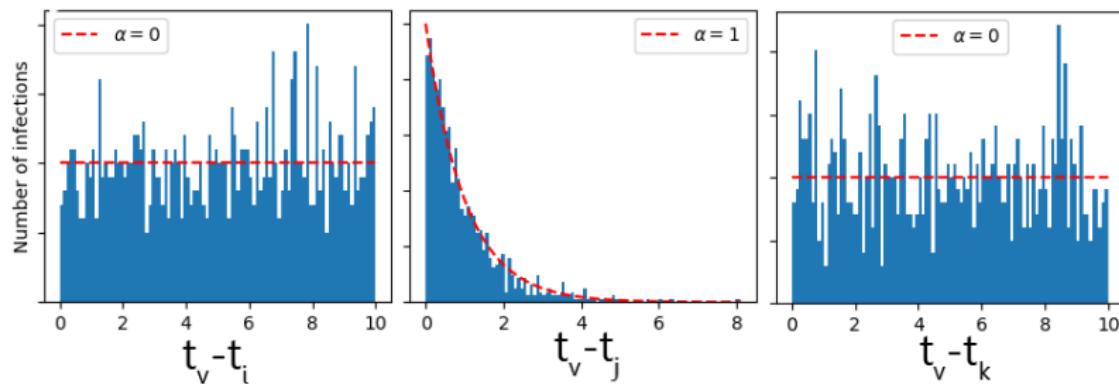
Figure 23: A sample from the Twitter structure (Politoscope [Gaumont et al., 2018])

Motivation
ooooDP
ooooHP
ooooooDHP
ooooooooPDP
ooooPDHP
ooooooooHouston
ooo●ooooConclusion
oo

Network inference



Exponential model $P(t) = a \cdot e^{-\alpha t}$



Network inference – Literature

- Several works on network inference using survival analysis:
 - ◊ NetRate/InfoPath [Gomez-Rodriguez et al., 2011, Gomez-Rodriguez et al., 2013a]
 - ◊ KernelCascade [Du et al., 2012]
 - ◊ MoNet [Wang et al., 2012]
 - ◊ TopicCascade [Du et al., 2013]
- They are all special cases of [Gomez-Rodriguez et al., 2013b]
 - ◊ Bridges the gap between survival analysis and point processes
 - ◊ Formulates each of previous models as a counting point process

Point process

- Network inference literature naturally embeds into point processes one
 - We can derive a temporal *and* structural Bayesian prior

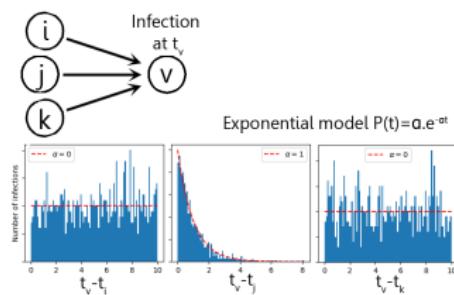


Figure 24: Survival process

Both are
point
processes
 $\langle \approx \rangle$

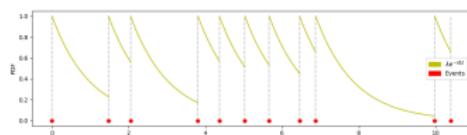


Figure 25: Hawkes process

Temporal and structural prior

- Houston: Heterogeneous Online User-Topic Network inference
- Prior on cluster membership C_i of observation i observed on node u at time t given history \mathcal{H} and cluster-dependent networks A :

$$P(C_i = k | u, t, \mathcal{H}, A)$$

$$= \begin{cases} \frac{\lambda_0^{(k)} + \sum_{\mathcal{H}_{i,c}^{(k)}} H(t_i^c | t_j^c, \alpha_{u_j^c, u_i^c}^{(k)})}{\lambda_0^{(K+1)} + \sum_k \lambda_0^{(k)} + \sum_{\mathcal{H}_{i,c}^{(k)}} H(t_i^c | t_j^c, \alpha_{u_j^c, u_i^c}^{(k)})} & \text{if } k = 1, \dots, K \\ \frac{\lambda_0^{(K+1)}}{\lambda_0^{(K+1)} + \sum_k \lambda_0^{(k)} + \sum_{\mathcal{H}_{i,c}^{(k)}} H(t_i^c | t_j^c, \alpha_{u_j^c, u_i^c}^{(k)})} & \text{if } k = K+1 \end{cases}$$

$$= \begin{cases} \frac{\text{Strength of incoming edges of cluster/subnetwork } k \text{ at time } t}{\text{Normalizing term}} & \text{if } k = 1, \dots, K \\ \frac{\text{Probability of a new cluster/subnetwork } k+1 \text{ at time } t}{\text{Normalizing term}} & \text{if } k = K+1 \end{cases}$$

Motivation
oooo

DP
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HP
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DHP
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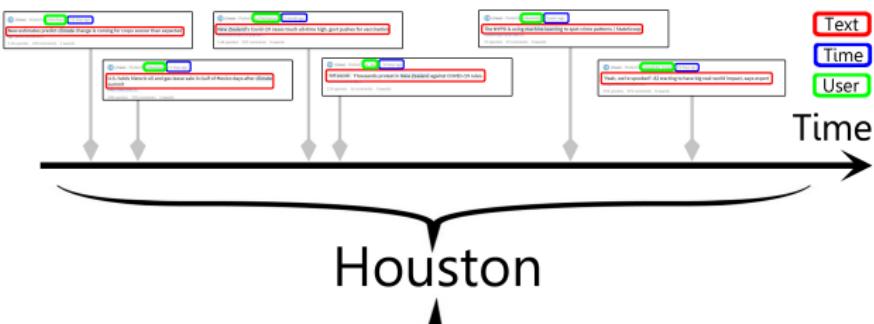
PDP
ooo

PDHP
oooooooo

Houston
oooooo•ooo

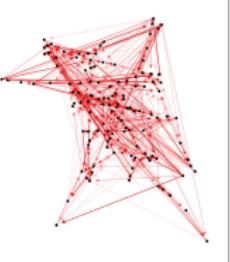
Conclusion
oo

Task



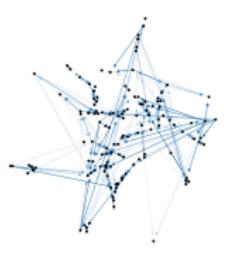
Cluster 1

• New COVID-19 cases change &
New COVID-19 cases change &
New COVID-19 cases change &



Cluster 2

• The WHO's using mobile app to map urban and rural | The World
The WHO's using mobile app to map urban and rural | The World



Cluster 3

• U.S. adds millions of gas lease rate to Gulf of Mexico days after climate
U.S. Energy Information Agency



Motivation
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DP
oooo

HP
oooooo

DHP
oooooooo

PDP
oooo

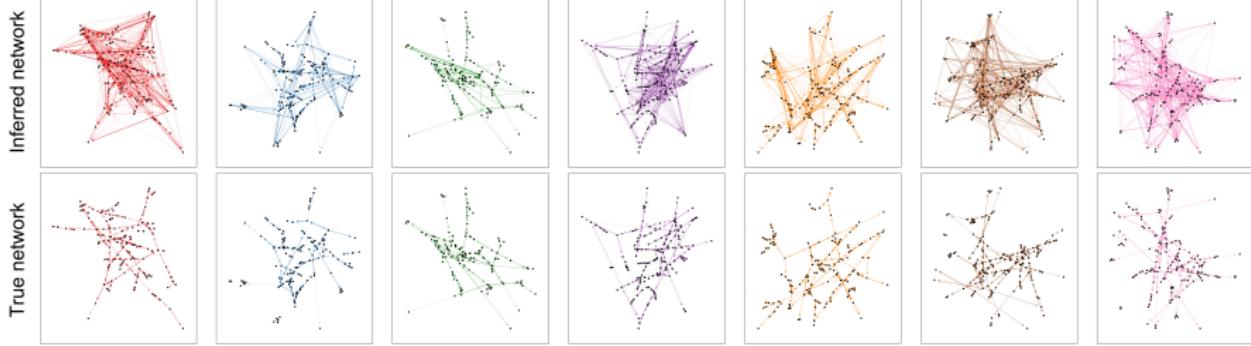
PDHP
oooooooo

Houston
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Conclusion
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Results – Synthetic

- We simulate the spread of documents drawn from 5 topics, each with its own vocabulary and subnetwork



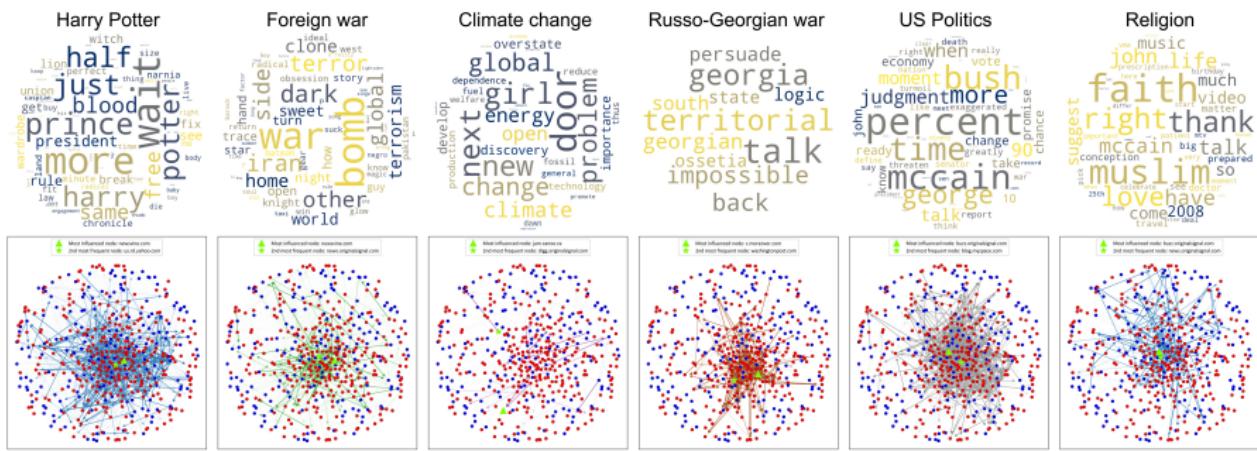
Motivation
ooooDP
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ooooooDHP
ooooooooPDP
ooooPDHP
ooooooooHouston
ooooooooooooConclusion
oo

Numerical results

		Houston	TC	DHP	NetRate
PL	NMI	0.809	0.669	0.449	-
	ARI	0.688	0.330	0.063	-
	AUC	0.807	0.719	-	0.731
	MAE	0.267	0.338	-	0.460
ER	NMI	0.787	0.711	0.638	-
	ARI	0.631	0.488	0.411	-
	AUC	0.849	0.800	-	0.659
	MAE	0.229	0.278	-	0.481
Blogs	NMI	0.750	0.668	0.372	-
	ARI	0.609	0.365	0.023	-
	AUC	0.701	0.613	-	0.710
	MAE	0.374	0.444	-	0.499

Results – Real world

- Memetracker data (2009)



Conclusion

- Dirichlet and Hawkes process have an old and separate history
 - ◊ Only recently (2015) they have been brought together
 - ◊ Their reunion launched a new branch of inductive machine learning
- The number of extensions based on Dirichlet-Point-Processes might be enormous, because we touched core concepts of machine learning
 - ◊ Dirichlet processes (PDP): could be used to redefine hierarchical DP, nested DP, or any models built on them (LDA, SBMs, among others)
 - ◊ Point processes (Poisson, Hawkes, Survival/Counting, etc.): the new possibility to merge them with DP could lead to a potentially infinite number of different Dirichlet-Point-Process priors.
- We presented 2 of such extensions:
 - ◊ PDP+HP → PDHP (flexible temporal prior)
 - ◊ DP+Survival → Houston (temporal+structural prior)

Thanks for your attention!

(DP, HDP, nHDP, **PDP**, IBP, PIBP, PnHDP, PPY, PnPY, PHPY, ...)

×

(Hawkes, Survival, Cox, Poisson, Determinantal, Geometric, ...)

=

(DHP, HDHP, IBHP, **PDHP**, **Houston**, ...?)



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