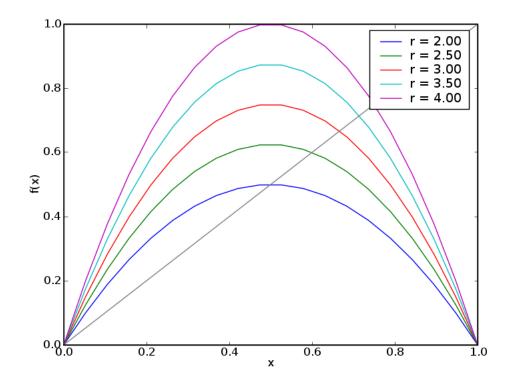
## Bifurcation diagram of a mapping

```
#!/usr/bin/env python
1
  from scipy import *
2
  from pylab import *
```

We are interested in the long term behavior of a sequence created by a the iteration of map.

## The logistic map

```
f = lambda x, r : r * x * (1 -x)
     The logistic map is parametrised by "r"
   x = linspace(0, 1, 20)
15
   rlist = linspace(2, 4, 5)
16
   hold (True)
17
                     plot(x, f(x,r), label = r = \%.2 f, % r)
   for r in rlist:
18
   legend()
19
   xlabel('x')
20
   ylabel('f(x)')
21
   plot(x,x,color=(0.5,0.5,0.5), label = ' ')
23
   show()
```



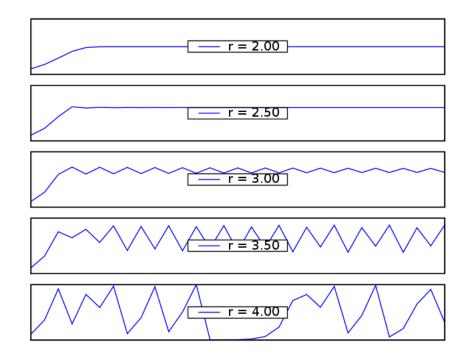
## Behavior of the sequence

The sequence is created by iteration of the map over an initial value:

```
X = [0.1, ]
27
   for i in arange(0,9):
                             X += [f(X[-1],2)]
28
   print array(X)
       0.1
                     0.18
                                  0.2952
                                               0.41611392
                                                            0.48592625
                                                                         0.49960386
       0.49999969
                    0.5
                                  0.5
                                               0.5
```

The sequence converges to a stable fixed point if it has one, but can also oscillated between different unstable fixed points, or have no stable long term behavior, exibiting chaos.

```
X = [0.1 * ones_like(rlist),]
   for i in arange (0,30): X += [f(X[-1], rlist)]
34
   X = vstack(X)
35
   figure()
36
37
   for i, r in enumerate(rlist):
       subplot( rlist.size , 1, i+1)
38
       plot( X[:, i], label = 'r = \%.2 f' % r)
39
       ylim (0, 1)
yticks('')
40
41
       xticks('')
42
       legend(loc = 10)
43
   show()
44
```



## Bifurcation diagram

To study the lont term behavior of the sequence we can plot the values it visit after many iterations, as a function of the parameter

```
rlist = linspace(2, 4, 800)
49
   X = [0.5 * ones_like(rlist),]
50
   for i in arange (0,10000): X \leftarrow [f(X[-1], rlist),]
51
   X = hsplit(vstack(X[-2000:]), rlist.size)
52
   from scipy import stats
53
   H = map(lambda Z : stats.histogram(Z, defaultlimits=(0,1), numbins=300)[0]
54
      ],X)
   H = map(lambda Z : 1-Z/Z.max(), H)
55
   H = vstack(H)
56
57
   figure()
   imshow(rot90(H), aspect = 'auto', extent = [2, 4, 0, 1])
58
59
   bone()
   xlabel('r')
60
   ylabel(r'$X_{n \rightarrow \infty}$')
61
   show()
62
```

