

the art* of ct

*** the algebraic reconstruction technique for computed tomography**

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agenda



- CT basics
- overview of the current ct systems
[the ct zoo]
- algebraic reconstruction technique
[ART]

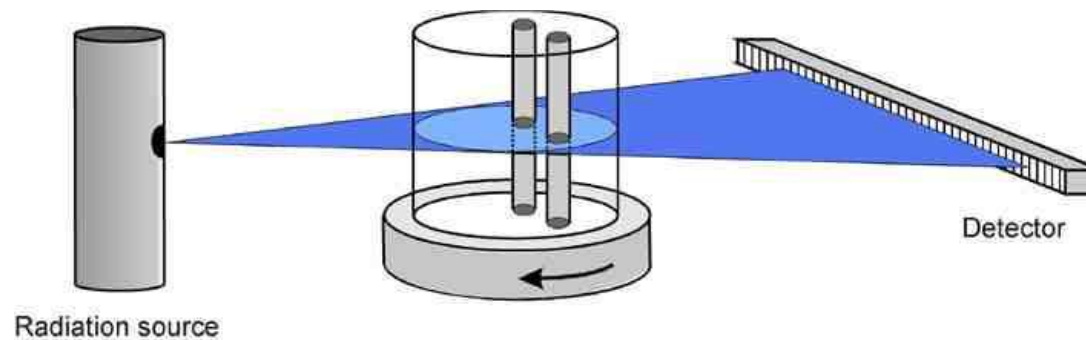
ct basics

computed tomography basics

- what is ct?
- how does ct function?
- what is measured?
- how is it measured?
- what happens with the measured data?
- how do the results look like?



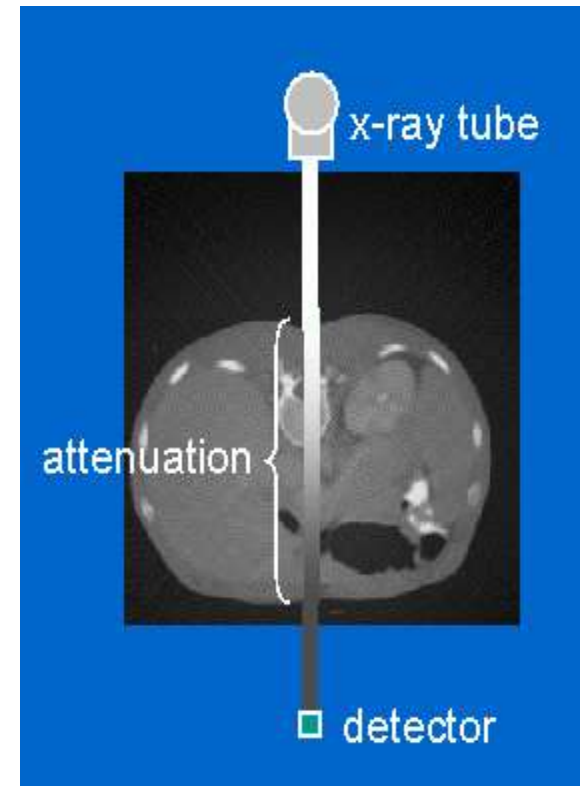
computed tomography scan process



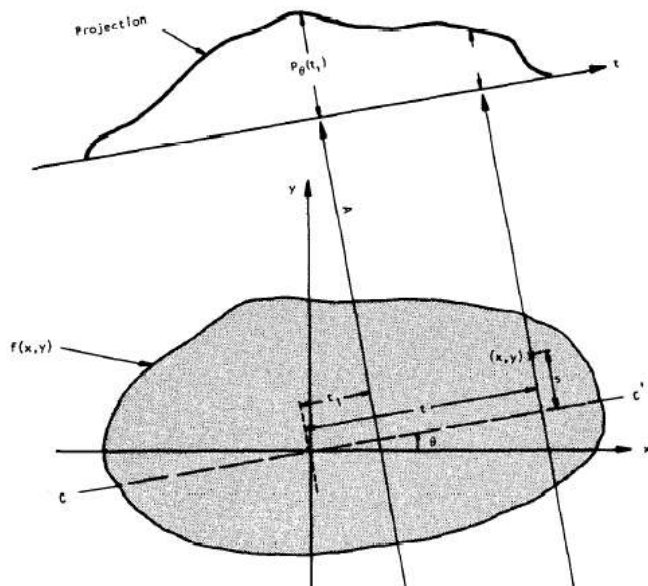
- scanning the object with x-rays => projections
- reconstructing the object: making an image out of projections

what is actually measured?

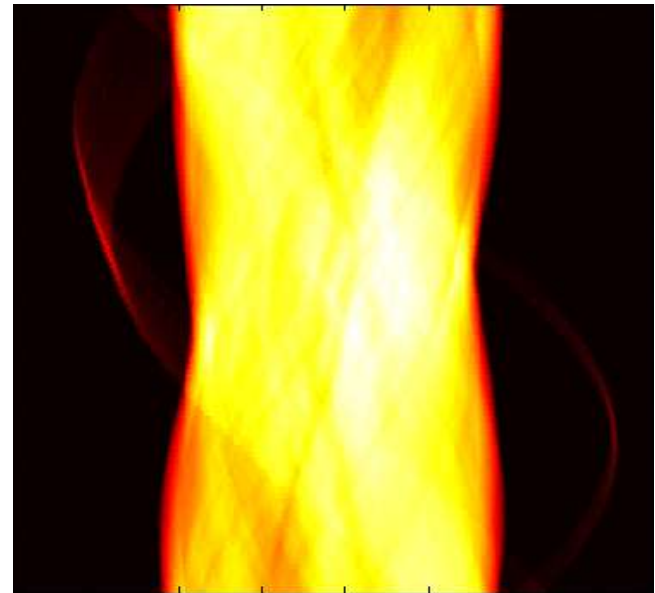
- attenuation: describing how much x-ray intensity is reduced by the material
- only morphological properties [anatomy] can be measured
=> no functional imaging



reconstruction: from projections...

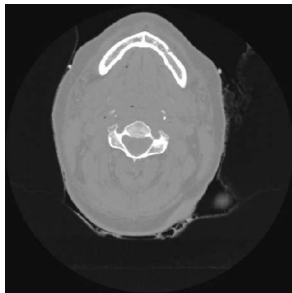


one projection

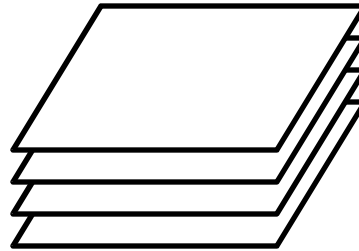


many projections
=
sinogram

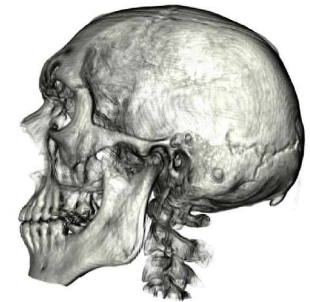
... to images



individual slice



stack of slices

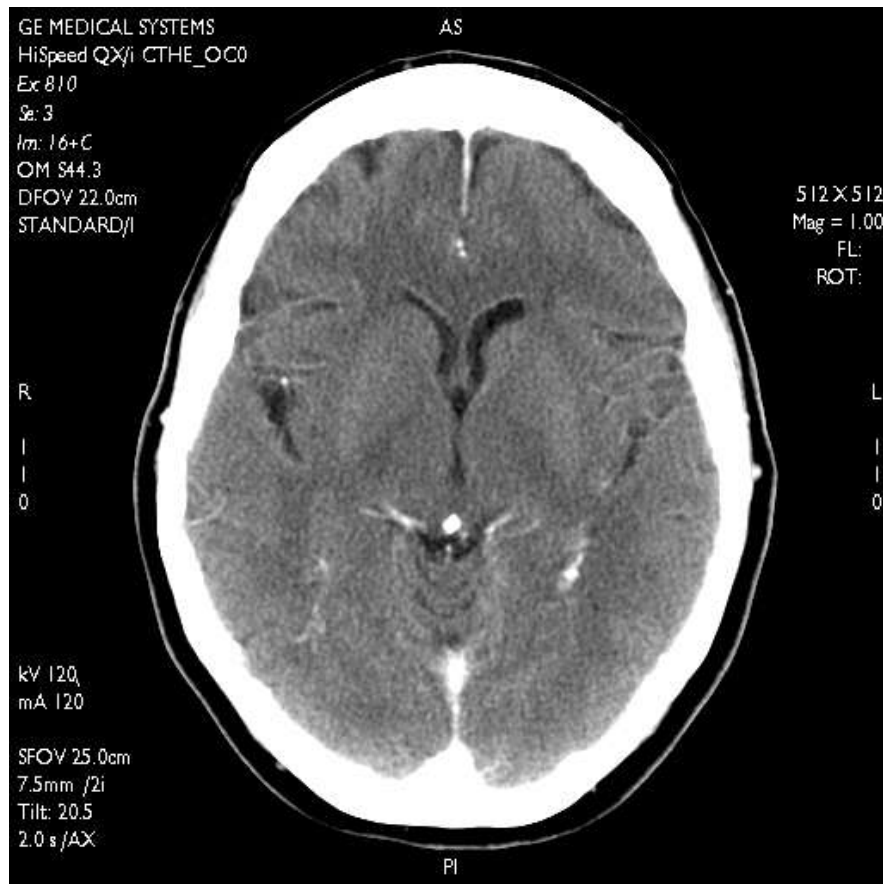


3D volume

reconstruction methods

- direct methods:
 - fourier reconstruction
 - filtered back-projection [FBP]
- iterative methods:
 - algebraic reconstruction technique [ART]

how do reconstructed images look like?



objectives

- small dose
 - as few projections as possible
 - low intensity
- fast data acquirement
 - scans of moving body parts: heart, lungs, angiography ...
 - 4D tomography
- fast image reconstruction
 - intra-operative use

overview of current ct systems

modern ct systems



history

- 1971 Dr. Godfrey Newbold Hounsfield
- EMI Laboratories, England
- 1979 Nobel Prize in Medicine with Allan McLeod Cormack
- British Knighthood



history

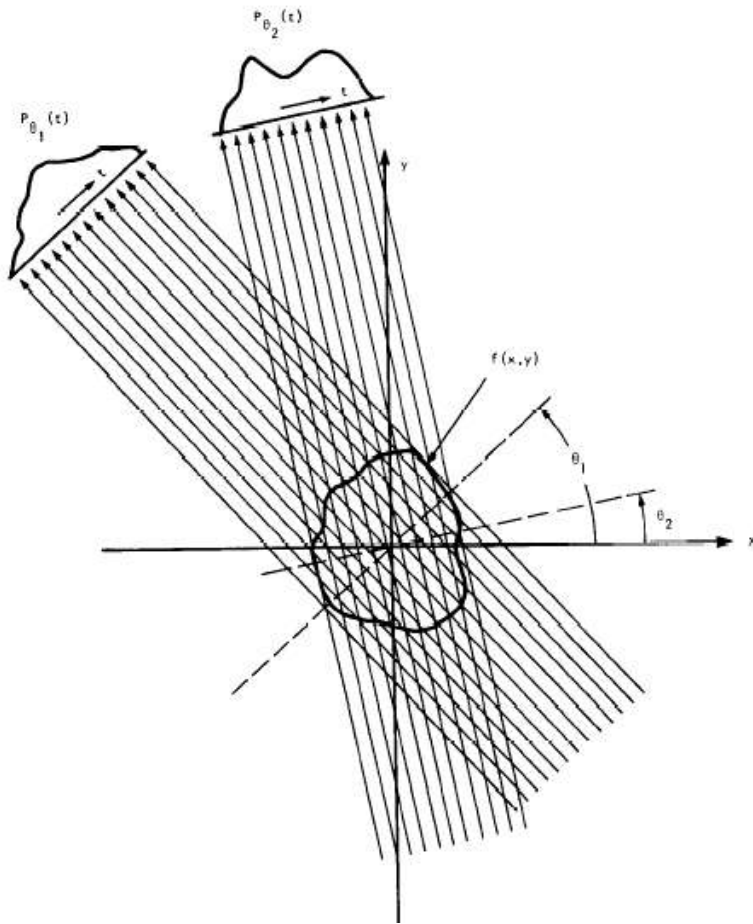
- 1967:
 - first prototypes
 - data acquisition: several hours
 - reconstruction: several days
- 1971
 - brain images only
 - data acquisition: 5 min.
 - reconstruction: 20 min.
- 1974/1975
 - first clinical installations
- 1976
 - whole body scanners



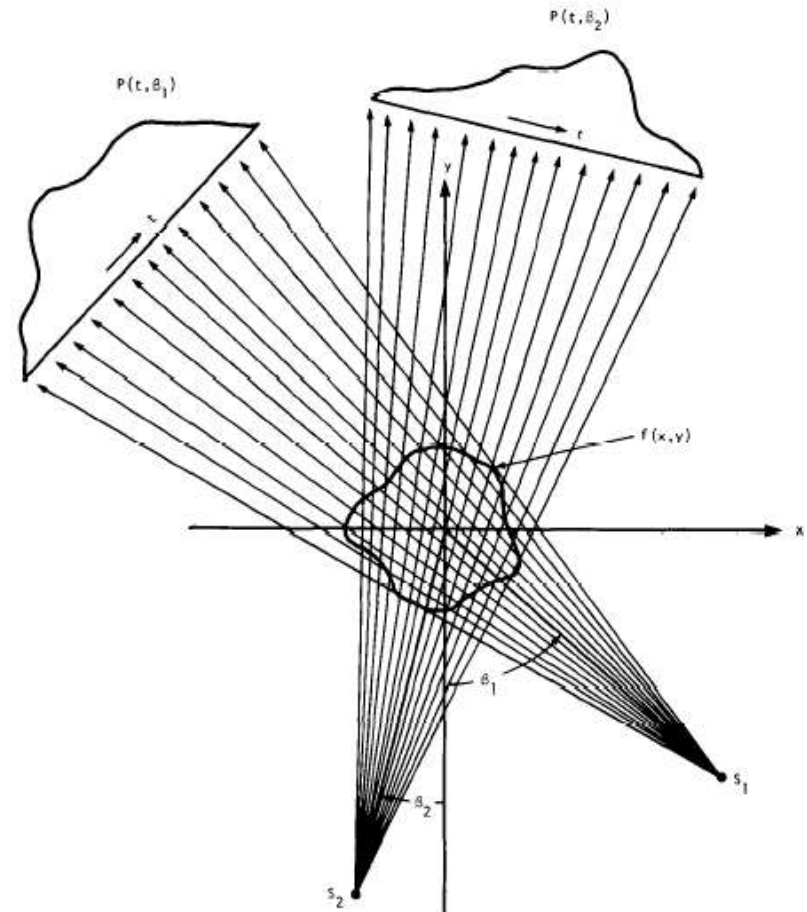
clinical head scanner 1974

image source: <http://imagingis.com/faq/history.asp>

data acquisition :: one slice per projection

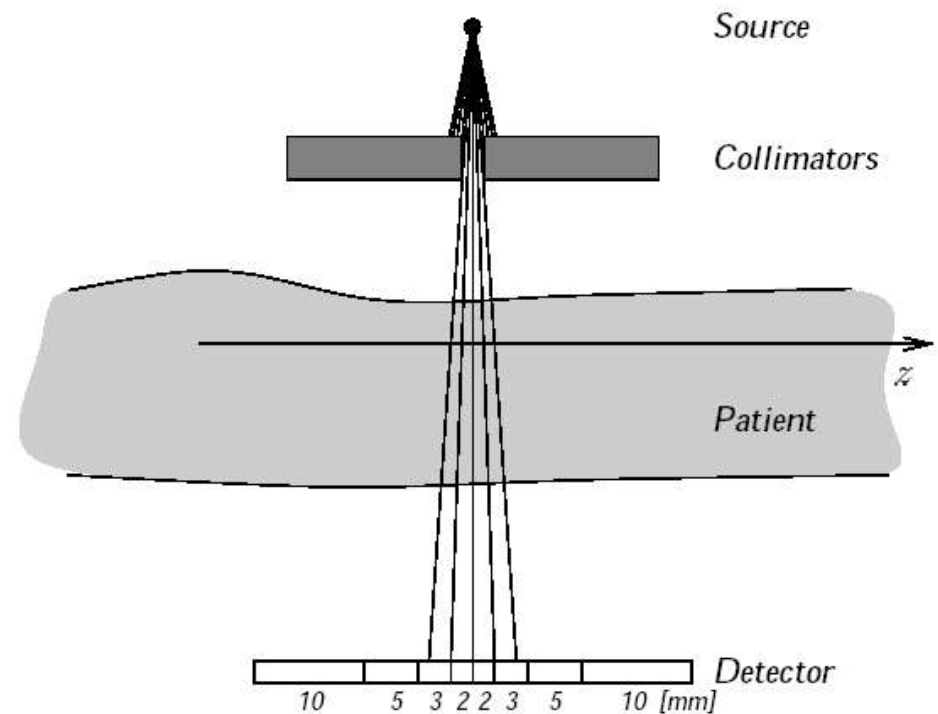
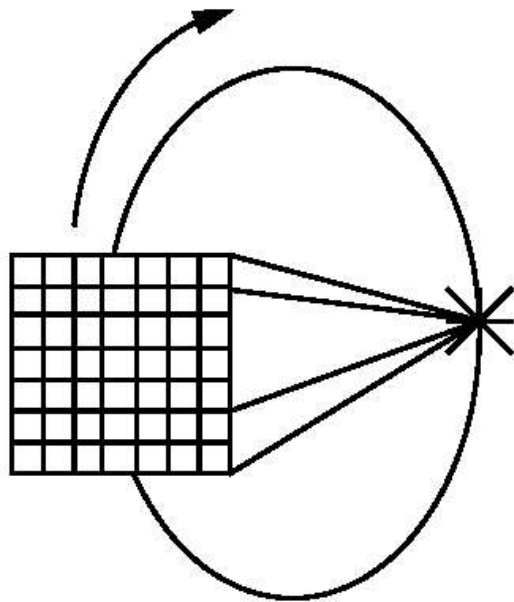


parallel beam



fan beam

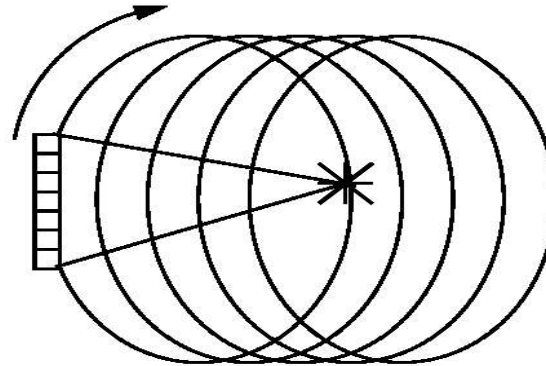
data acquisition :: several slices per projection



cone beam

scan methods

- slice based ct



- helical ct [1989]

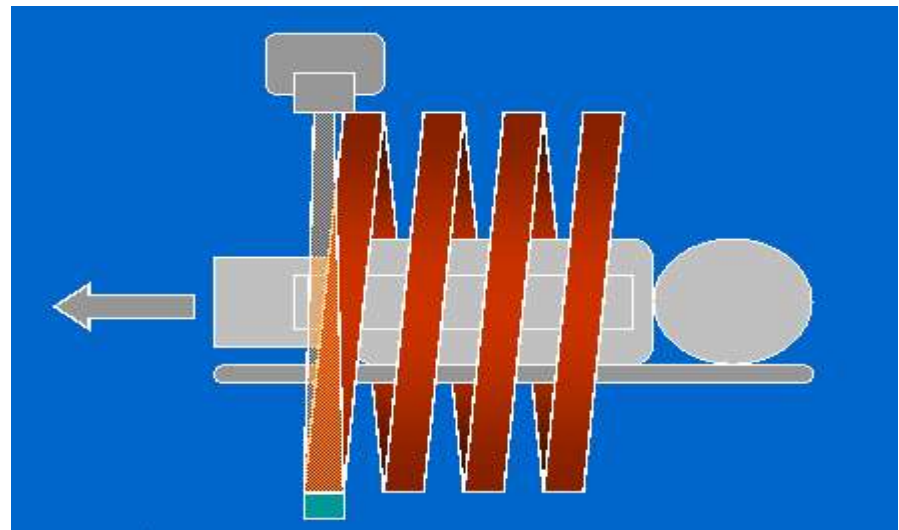
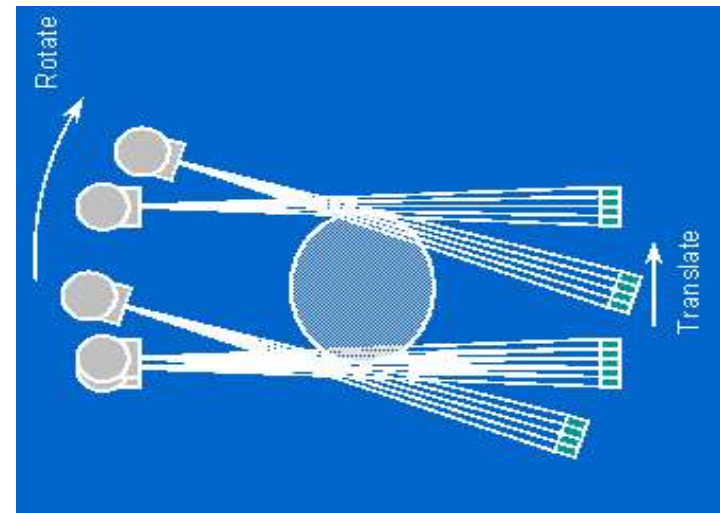
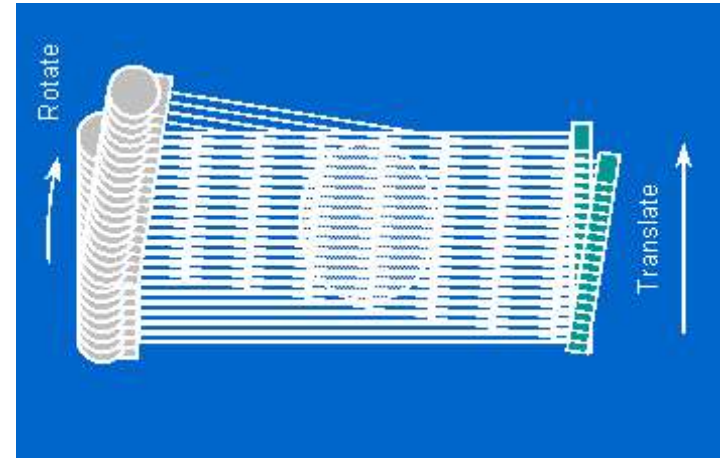


image source: Mueller

ct systems :: past

- 1th generation:
 - parallel-beam geometry
 - single highly collimated x-ray pencil beam and detector
 - scan time: 5 min.

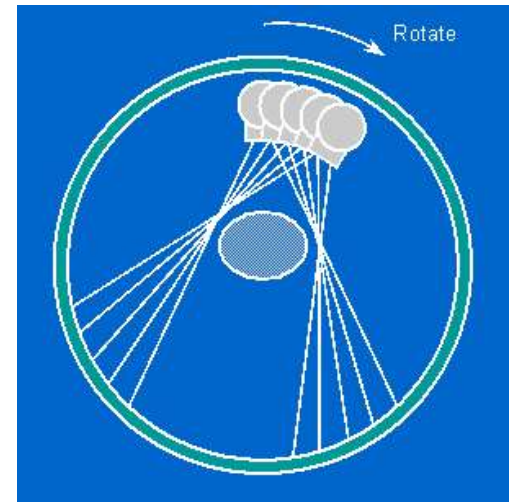
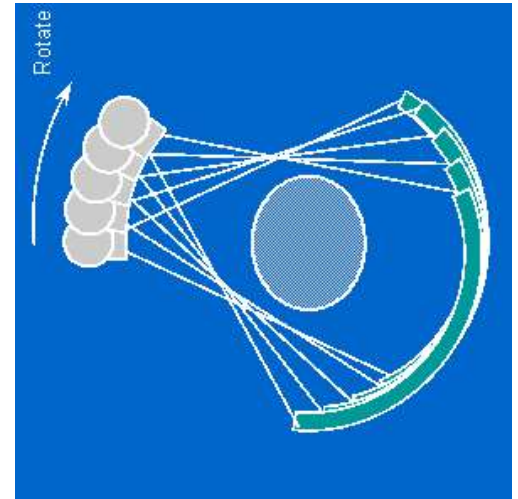
- 2nd generation:
 - narrow fan beam
 - linear detector array
 - scan time: 30 sec.



ct systems :: today

- 3rd generation:
 - since 1976
 - rotating fan/cone beam
 - rotating detectors
 - scan time: 1 sec.

- 4th generation:
 - rotating fan/cone beam
 - fixed detector
 - scan time: 1 sec.



ct systems :: today

- cine CT [5th generation]
 - stationary X-ray source and detector
 - no mechanical scanning motion
 - X-ray source: large semicircular anode
 - scan time: 50 ms

- slip ring technology [1985]
 - replacing cables for power and data transfer

ct systems :: today

- mobile C-arm / C-arc:
 - operating room, emergency dept., ...
 - scan time: 60° per second
 - drawbacks:
 - smaller field of view [30 cm]
 - focus on iso-center
 - less stability

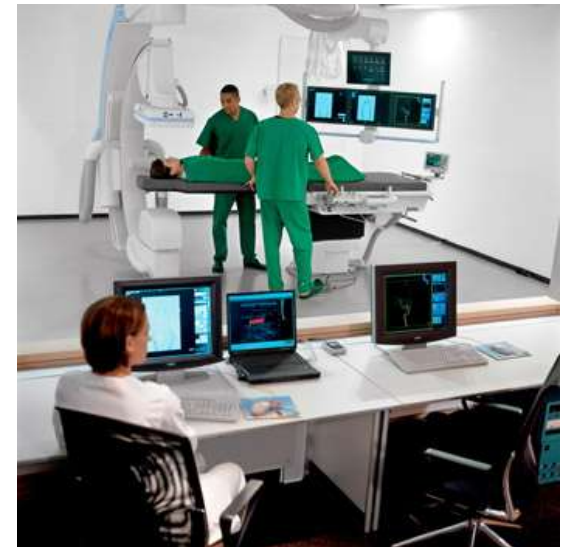
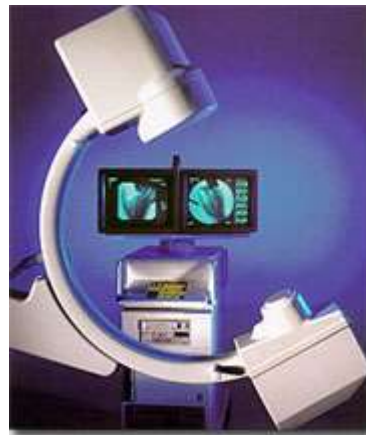


image source: Siemens Press, GE Medical Systems

current systems

- example: SOMATOM Sensation 64, SIEMENS
- 4th generation cone beam scanner
- gentry rotation: 0.37 sec
- 64 slices per rotation
- down to 0.3mm slice distance
- resolution: 0.4 mm
- field of view: 82 cm
- reconstruction time: ~ 5 frames per second*
*valid for another comparable system

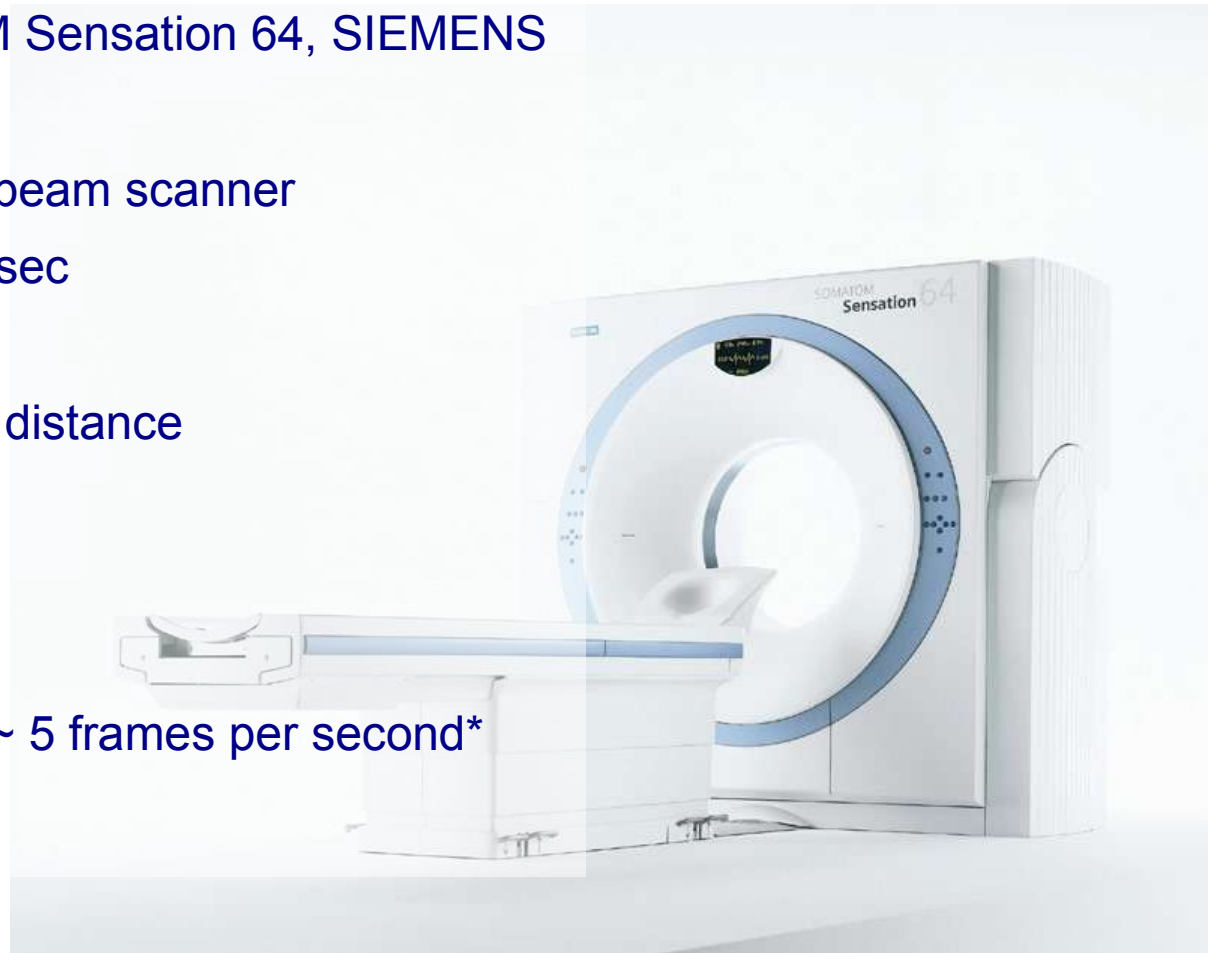
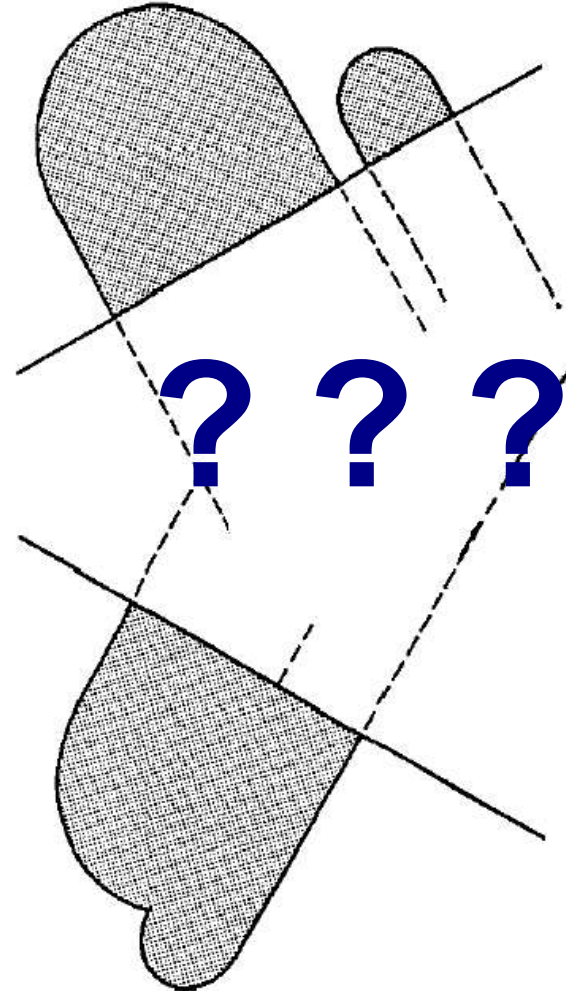


image source: Siemens press picture

algebraic reconstruction technique

art :: the problem

- given:
set of projections of the image
- goal:
reconstruct the original image



art :: the idea

- make initial guess
- check how well it corresponds to the measured data
[back-projection]
- calculate the difference between the result and real measurement
- correct the values
- repeat until results satisfying

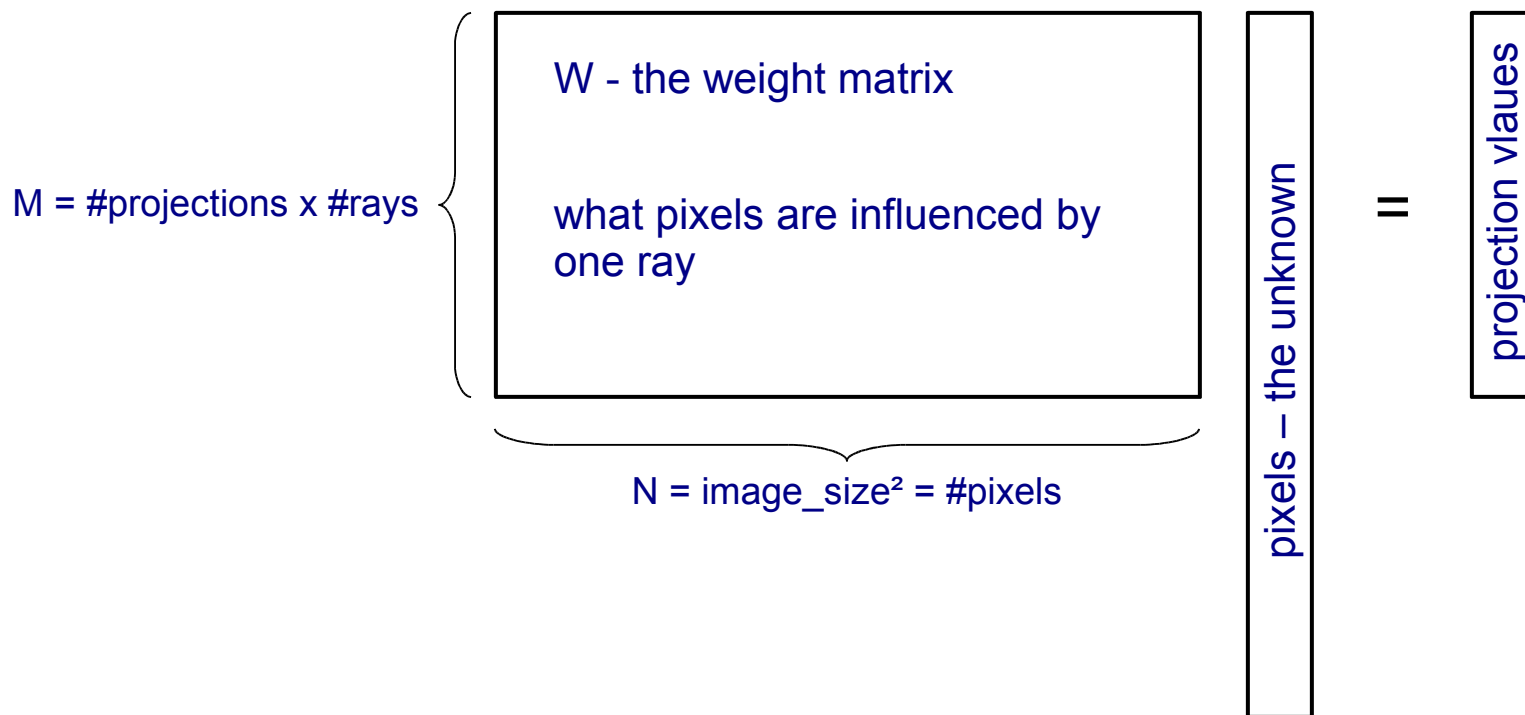
art :: simple example

3	12	3
3	12	3
3	12	12

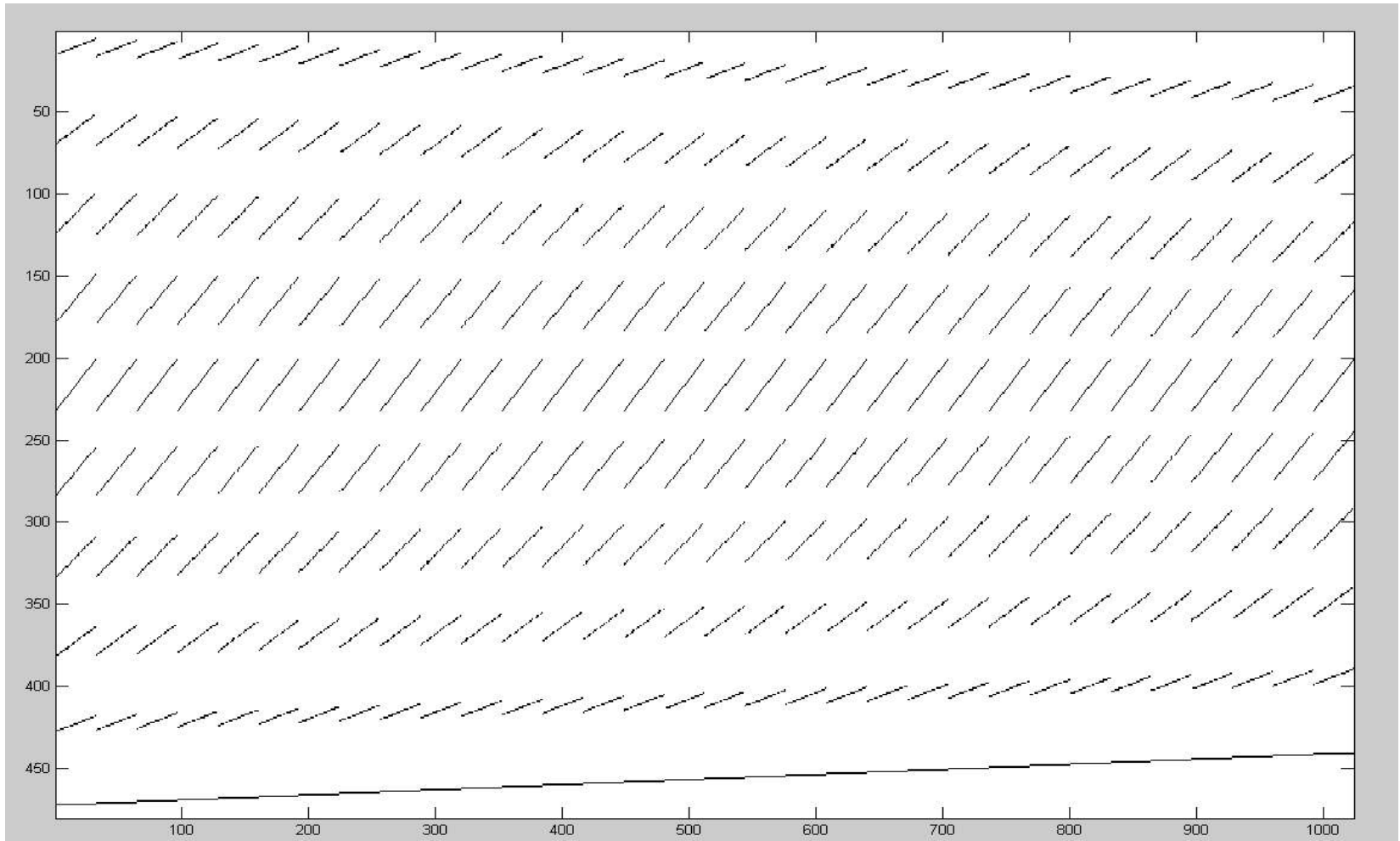
- make initial guess
- while convergence not reached // iterations
 - for each projection
 - for each ray
 - compute back-projection
 - compute difference to measured projection
 - distribute difference
 - end for
 - end for
- end while

the equation system

$$W \cdot f = p$$



details :: weight matrix structure



one iteration step :: the kaczmarz method

- update for one single ray projection k:
 - for a pixel $j=1:N$ do:

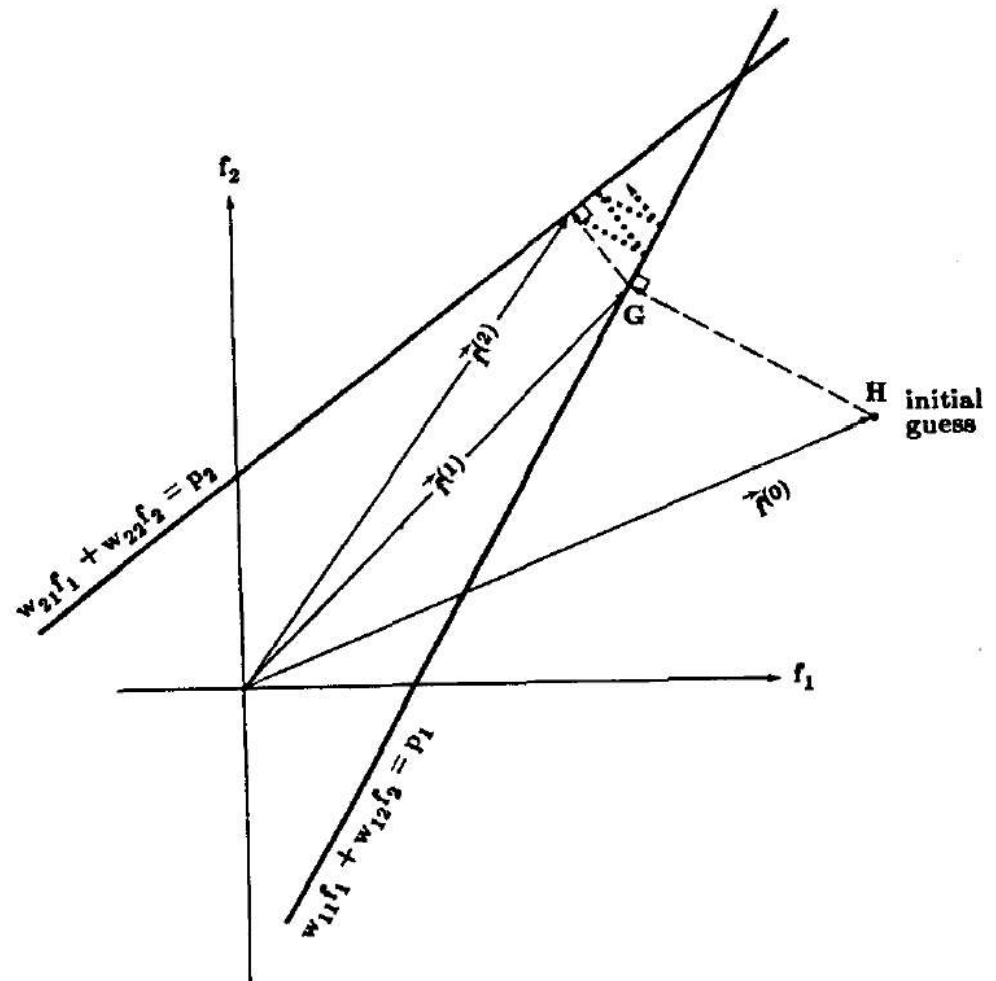
$$f_j^{(i)} = f_j^{(i-1)} + \lambda \cdot \frac{p_k - \vec{w}_k \vec{f}^{i-1}}{\sum_{l=1}^N W_{kl}^2} \cdot W_{kj}$$

Diagram illustrating the Kaczmarz method update step for a single ray projection k and pixel j :

- $f_j^{(i)}$: new pixel value
- $f_j^{(i-1)}$: old pixel value
- λ : relaxation parameter
- $p_k - \vec{w}_k \vec{f}^{i-1}$: the difference (between the current projection and the projection of the current estimate)
- $\sum_{l=1}^N W_{kl}^2$: normalizing the difference
- W_{kj} : weighting the correction

a different view at the method

- one iterative step can be seen as a projection of the current solution on a corresponding hyperplane



solution :: existence and uniqueness

- the equation system can be :
 - underdetermined [$M < N$]
 - overdetermined [$M > N$]
 - inconsistent through noise

- it can be shown that:
 - if unique solution given,
the kaczmarz method converges towards it
 - if solution not unique,
the kaczmarz method yields the result colsest to the initial
guess

tuning options

- reducing noise:
 - relaxation parameter [λ]
 - simultaneous steps
 - heuristics [hamming window]
- improving convergence:
 - order of equations: orthogonality
 - heuristics - using a priori information
[hamming window, initial guess, using borders for values]

alternatives

- SIRT
 - no ray-by-ray iterations, simultaneous steps instead
 - result: better quality & slower convergence

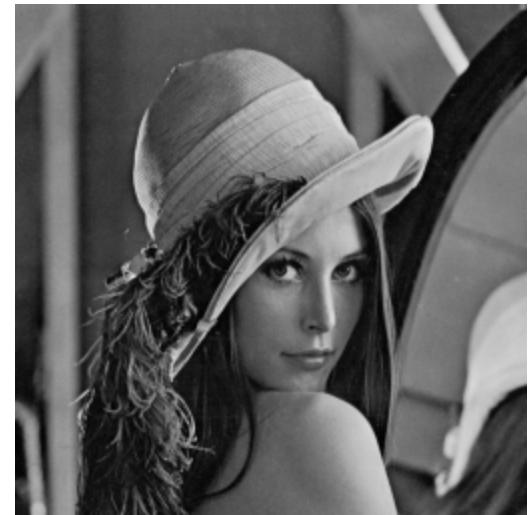
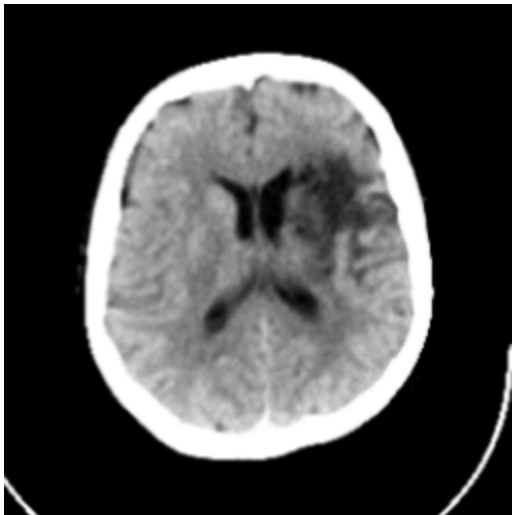
- SART
 - reducing errors in ray integral approximation by replacing pixels by bilinear elements
 - simultaneous iteration steps [as in SIRT]
 - heuristic use: Hamming window
 - result: better quality & faster convergence
 - gives reasonable images in one iteration

a little demo

- parallel beam scan
- almost perfect weight matrix [sart-like results for art]
=> nalmost no errors in back-projections
=> this art-version corresponds to real sart
- art and sirt simulation
- tests for source size [truncation], number of projections, number of iterations, lambda variation, run times
- tests for use of hamming window, initial guess, a priori information
- comparison with matlab in-build FBP reconstruction

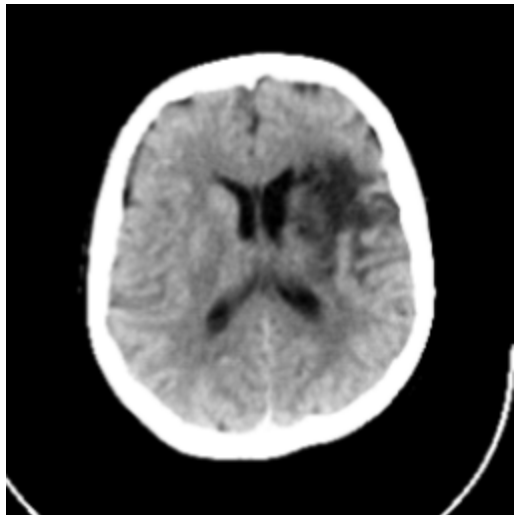
the experiment

- test images [resolution: 128^2 , greyscale 8bit [0:255]]



some experimental results

- brain 256x256

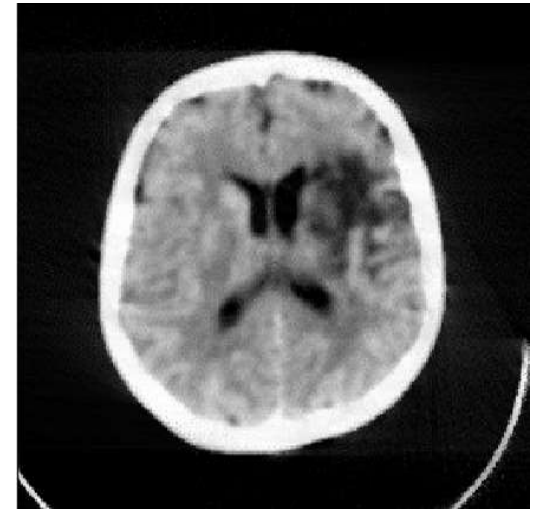


original image



art without “smart”
initial guess

1 iteration, 100 projections,
256*1.5 rays per projection

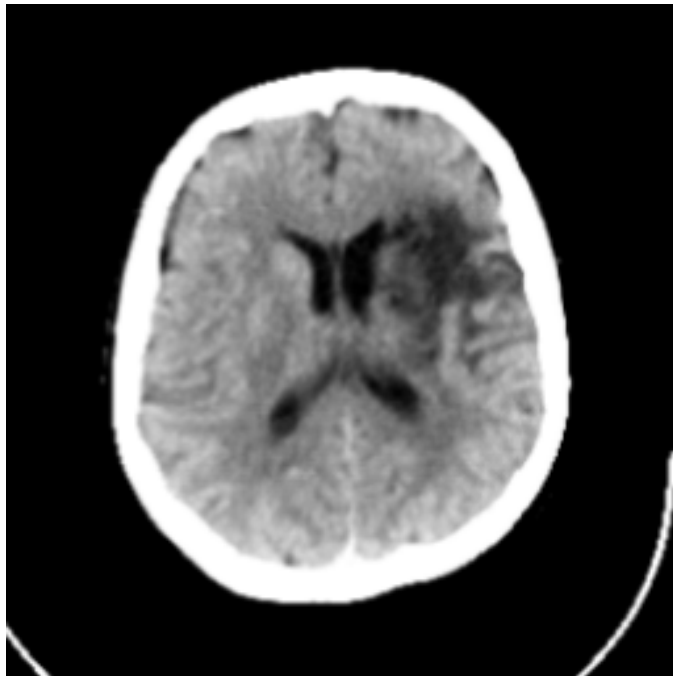


art with “smart” initial
guess

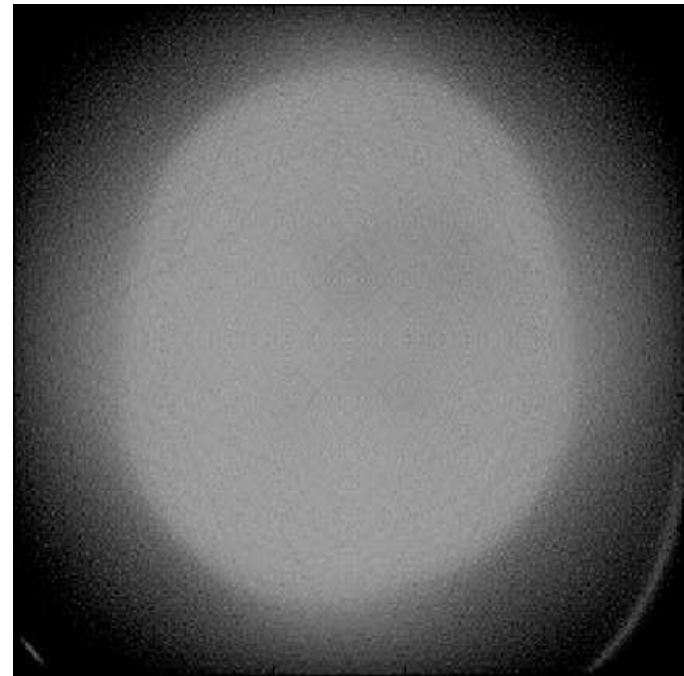
1 iteration, 100 projections,
256*1.5 rays per projection

some experimental results

- brain 256x256



original image



sirt

3 iterations, 100 projections,
256*1.5 rays per projection

some experimental results

- lena 256x256



original image



art

3 iterations, 100 projections,
256*1.5 rays per projection



fbp

matlab in-built fbp [iradon],
90 projections

comparison of ART and FBP

ART

- + better noise tolerance
- + needs less projections
- + better handling of non-uniformly distributed projection datasets

- aliasing effects for large fan-beam angles [$>20^\circ$]

FBP [filtered back projection]

+ more
computationally
efficient

readings

- Kak, Slaney “Principles of Computerized Tomographic Imaging”
- Albert Macovski “Medical Imaging Systems”
- Klaus Mueller “Fast and Accurate Three-Dimensional Reconstruction from Cone-Beam Projection Data Using Algebraic Methods”
- G. T. Herman “Topics in Applied Physics”
- Henrik Turbell “Cone-Beam Reconstruction Using Filtered Backprojection”
- online resources:
 - Hiroki Yoshikawa, “X-Ray Computed Tomography”, <http://ctlab.bk.tsukuba.ac.jp/~hiroki/blind/x-rayCT.html>
 - Siemens Medical Solutions Website: <http://www.medical.siemens.com>
 - General Electric Medical Systems Website: <http://www.gemedicalsystemseurope.com>
 - <http://www.amershamhealth.com/medcyclopaedia>
 - <http://en.wikipedia.org>
 - <http://www.impactscan.org>
 - <http://imagingis.com/>