

MARKING SCHEME
BSJE JOINT EXAMINATION
-2024 -

Kenya Certificate of Secondary Education

121/1 Mathematics Alt. A Paper 1

July, 2024 TIME: 2½ Hrs

Name: Index No:

School: Signature:

121/1 - Mathematics
Friday, 12TH July, 2024
Morning
8.00am-10.30am

Instructions to candidates.

- (a) Write your name and index number in the spaces provided above.
- (b) Sign and write the date of the examination in spaces provided above.
- (c) This paper consists of two sections: Section I and II.
- (d) Answer *all* the questions in section I and *only five* questions from section II.
- (e) Show *all* the steps in your calculations, giving your answer at each stage in the space provided.
- (f) Marks may be given for correct working even if the answer is wrong.
- (g) Non-programmable silent electronic calculators and KNEC mathematical tables may be used, except where stated otherwise.
- (h) *Candidates should check the question paper to ascertain that no questions are missing.*
- (i) *Candidates should answer the questions in English.*

For examiner's use only

SECTION I

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	TOTAL

SECTION II

17	18	19	20	21	22	23	24	TOTAL	GRAND TOTAL	TOTAL

SECTION I (50MARKS): Answer all the questions in this section in the spaces provided.

1. Evaluate without using tables or calculators (3marks)

$$\frac{\frac{6}{7} \text{ of } \frac{14}{3} \div 80 \times -20}{-2 \times 5 \div (14 \div 7) \times 3}$$

Num: $\frac{6}{7} \times \frac{14}{3} = 4$

$4 \div 80 = \frac{4}{80}$

$\frac{4}{80} \times -20 = \frac{4}{80} \times -\frac{20}{3} = -\frac{1}{3}$

Deno: $-2 \times \frac{5}{2} \times 3$
 $= -15$

$\frac{N}{D} = \frac{-\frac{1}{3}}{-15} = -\frac{1}{3} \times \frac{1}{-15}$
 $\Rightarrow \frac{1}{45}$

M ₁	Numerator
M ₁	Denominator
A ₁	
03	

2. Solve the following inequalities and represent the solution on a number line.

$$4 - 3 \leq 6x - 1 < 3x + 8$$

$$4x - 3 \leq 6x - 1$$

$$-2x \leq 2$$

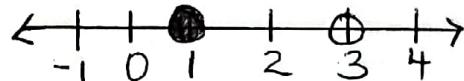
$$x \geq -1$$

$$6x - 1 < 3x + 8$$

$$3x < 9$$

$$x < 3$$

$$-1 \leq x < 3$$



(3marks)

M ₁	Both solutions
B ₁	Compound statement
B ₁	Correct number line
03	

3. Use tables of squares, cubes roots and reciprocals to evaluate;

(4marks)

$$23.5^3 - \sqrt[3]{(4411)} + \frac{1}{0.0071}$$

$$(2.35 \times 10)^3 - \sqrt[3]{4.411 \times 10^3} + \frac{1}{7.1 \times 10^{-3}}$$

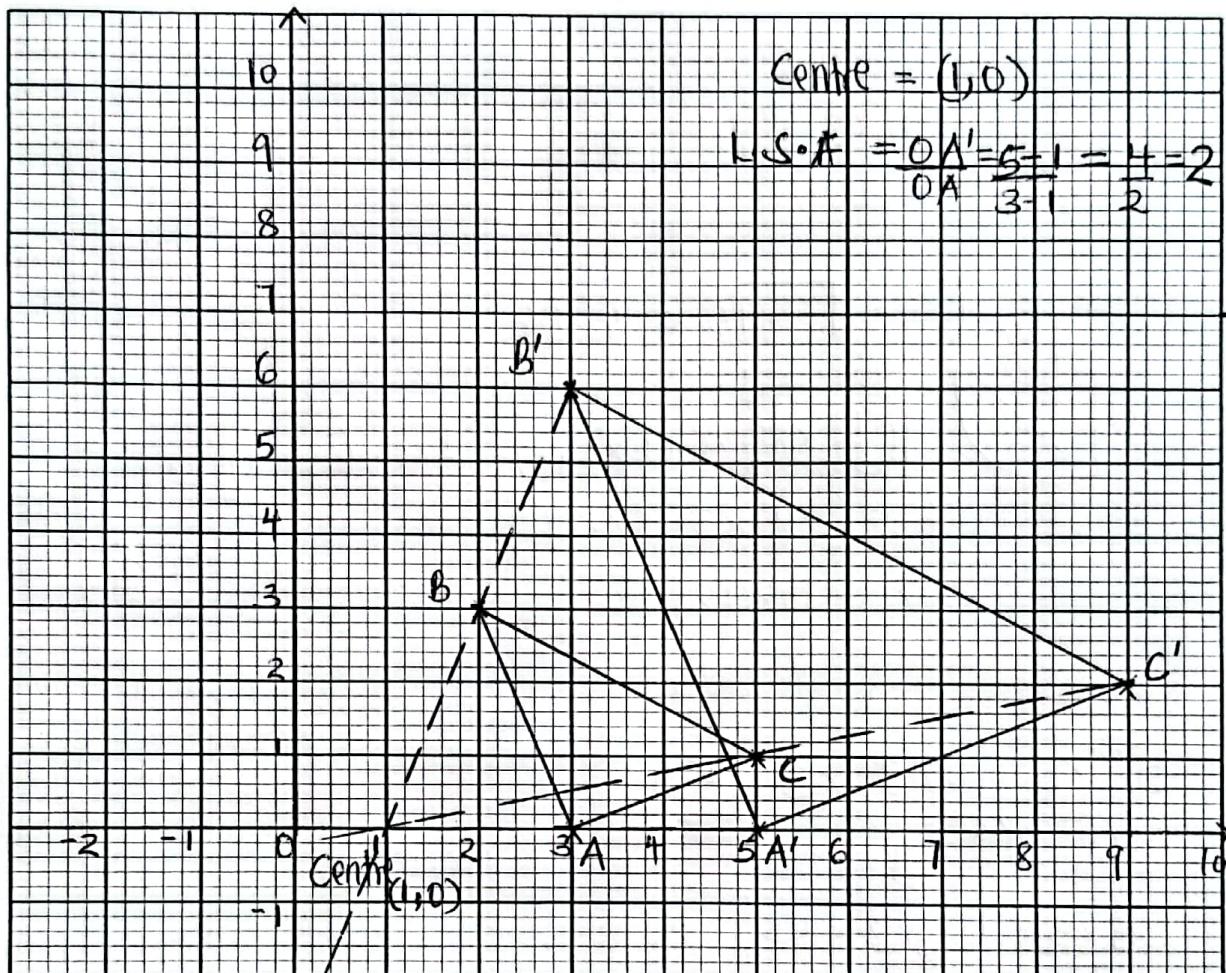
$$12.978 \times 10^3 - 1.64 \times 10 + 0.1408 \times 10^3$$

$$12978 - 16.4 + 140.8$$

$$\Rightarrow 13,102.4$$

M ₁	All logs correct
M ₁	Addition / Subtraction
M ₁	Multiplication
A ₁	
04	

4. Triangle ABC has its vertices at A(3, 0), B(2,3) and C(5,1) if A'(5, 0), B'(3,6) and C'(9,2) is the image of ABC under enlargement. On the same axes and grid provided below, determine the Centre of enlargement and linear scale factor. (3marks)



B₁ - Both diagrams

B₁ - Centre of enlargement

B₁ - L.S.F

5. Phenny is a saleslady. She is paid Ksh 15,375 per month. She is also paid a commission of 4 1/2 % on the amount of money she makes from her sales. In a certain month, she earned a total of Ksh. 28,875. Calculate the value of her sales that month. (3marks)

$$\text{Commission earned} = 28875 - 15375 = \text{ksh. } 13,500$$

$$4.5\% \rightarrow 13,500$$

$$100\% \rightarrow ??$$

$$\frac{100 \times 13,500}{4.5}$$

$$\Rightarrow \text{kshs. } 300,000$$

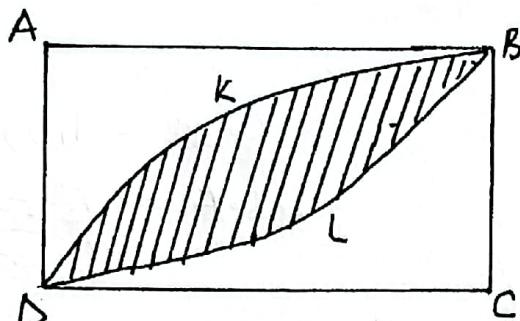
M₁ - Commission earned.

M₁ - Equation

A₁ - Sales

03

6. The figure drawn below is a square ABCD of sides 36.75cm. The shaded area is formed out of two segments. DCB and DKB. Find the area of the shaded region. (3marks)



$$\text{Length of square} = \sqrt{36.75} \approx 6.06$$

Area shaded ;

$$2\left[\left(\frac{90}{360} \times \frac{22}{7} \times 6.06 \times 6.06\right) - \left(\frac{1}{2} \times 6.06^2 \sin 90^\circ\right)\right]$$

$$\Rightarrow 2(28.85 - 18.36)$$

$$\Rightarrow 20.98 \text{ cm}^2$$

7. Solve for x in the equation: $3^{2x+1} + 4 \times 3^{2x} \times 3^1 = 45$

(3 marks)

$$3^{2x} \times 3^1 + 4 \times 3^{2x} \times 3^1 = 45$$

$$\text{Let } 3^{2x} = y$$

$$y \times 3 + 4 \times y \times 3 = 45$$

$$3y + 12y = 45$$

$$15y = 45$$

$$\frac{y}{15} = 3$$

$$3^{2x} = 3^1$$

$$2x = 1$$

$$x = \frac{1}{2}$$

8. Simplify the expression to its simplest form $\frac{24x^2 + 2ax - 12a^2}{18x^2 - 8a^2}$

(3marks)

$$\begin{aligned} N &= 24x^2 + 18ax - 16ax - 12a^2 \\ &= 6x(4x+3a) - 4a(4x+3a) \\ &\approx (6x-4a)(4x+3a) \\ &\frac{2(3x-2a)(4x+3a)}{2(3x-2a)(3x+2a)} \\ &= \frac{4x+3a}{3x+2a} \end{aligned}$$

Alternatively ;

$$\frac{2(12x^2 + 9ax - 6a^2)}{2(9x^2 - 4a^2)}$$

$$\begin{aligned} N &= 12x^2 + 9ax - 8ax - 6a^2 \\ &= 3x(4x+3a) - 2a(4x+3a) \\ &\quad (3x-2a)(4x+3a) \end{aligned}$$

$$D = (3x-2a)(3x+2a)$$

$$\frac{N}{D} = \frac{(3x-2a)(4x+3a)}{(3x-2a)(3x+2a)}$$

$$\Rightarrow \frac{4x+3a}{3x+2a}$$

Length of the square

M1

Expression / Equation

A1

Area shaded

O3

M1

Expanding the equation

M1

Finding the unknown

A1

Value of x

O3

M1

N

M1

D

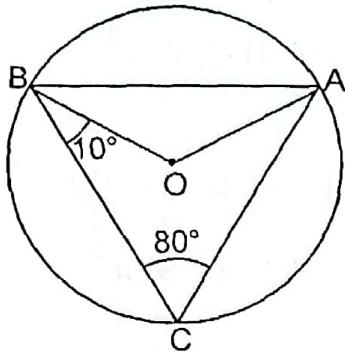
A1

An.s.

simplified

Fraction

9. In the figure below, O is the centre of circle. Angle $BCA = 80^\circ$ and angle $CBO = 10^\circ$. Determine the size of angle CAB. (3marks)



$$\begin{aligned}\angle AOB &= 160^\circ \\ \angle ABC &= 10^\circ \\ \therefore \angle CBA &= 10^\circ + 10^\circ \\ &\Rightarrow 20^\circ\end{aligned}$$

M1	For $\angle ADB = 160^\circ$
M1	For $\angle ABC = 10^\circ$
A1	$\angle CBA = 20^\circ$
O3	

10. A foreign exchange bureau in Mombasa buys and sells selected foreign currencies at the rates shown in the table below.

Currency	Buying (Ksh)	Selling (Ksh)
1 South African Rand	7.48	7.95
1 Chinese Yuan	20.03	20.20

A tourist arrived in Kenya from South Africa with 7,435,000 South African Rands. She converted the whole amount to Kenya shillings through an agent at a commission of 2%. While in Kenya, she spent 25% of this money and converted the balance to Chinese Yuan. Calculate the amount of Chinese Yuan that she received. (3 marks)

$$\begin{aligned}7.48 \times 7435000 &= \text{Ksh. } 54865800 \\ \text{Money Received} &\Rightarrow \frac{98}{100} \times 54865800 \\ &= \text{Ksh. } 53768484 \\ \text{Remaining Money} &= \frac{75}{100} \times (53768484) \\ &= \text{Ksh. } 40326363\end{aligned}$$

Balance in Tuan ; $\frac{40326363 \times 1}{20.20} \Rightarrow 1996354.60$ Chinese Tuan

M1	Money Received
M1	75% of Total Money
A1	Balance Tuan
O3	

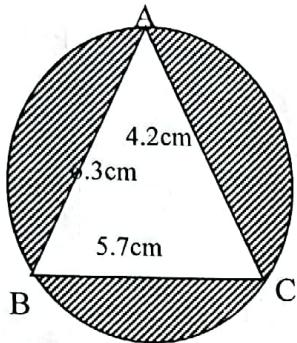
11. Two matrices A and B are such that $A = \begin{pmatrix} k & 4 \\ 3 & 2 \end{pmatrix}$ and $B = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$, given that the determinant of $AB = 4$, find the value of K. (3mks)

$$AB = \begin{pmatrix} k & 4 \\ 3 & 2 \end{pmatrix} \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \begin{pmatrix} k+12 & 2k+16 \\ 9 & 14 \end{pmatrix}$$

$$\begin{aligned}\text{Determinant} &= 14k + 168 - 18k - 144 = 4 \\ -4k &= 4 - 24 \\ k &= 5\end{aligned}$$

M1	For AB
M1	Expression / Equation of
A1	Det Value of K
O3	5

12. The circle below whose area is 18.05cm^2 circumscribes triangle ABC where AB = 6.3cm, BC = 5.7cm and AC = 4.2cm. Find the area of the shaded part. (4Marks)



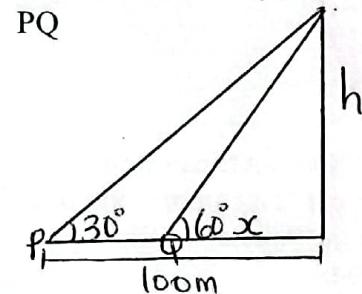
$$S = \frac{1}{2}[5.7 + 4.2 + 6.3] \\ = 8.1$$

$$\text{Area of triangle} = \sqrt{8.1(8.1 - 5.7)(8.1 - 4.2)(8.1 - 6.3)} \\ \Rightarrow 11.68\text{cm}^2$$

$$\text{Area shaded} \Rightarrow 18.05 - 11.68 \\ = 6.368\text{cm}^2$$

B1	for \triangle
M1	Expression of area
M1	FOR 11.682 or 11.68
A1	Shaded Area
O4	

13. A boat is at point P, a distance of 100km from the bottom of a hill. The angle of elevation of the top of the hill is 30° from P. The boat sails straight towards the hill to a point Q from where the angle of elevation to the top of the hill is now 60° . Calculate the distance PQ



$$\tan 30 = \frac{h}{100} \\ h \Rightarrow 100 \tan 30^\circ = 57.735 \\ \tan 60 = \frac{57.735}{x}$$

$$x = \frac{57.735}{\tan 60} \\ \Rightarrow 33.33\text{km}$$

$$PQ = 100 - 33.33 \\ \Rightarrow 66.67\text{km}$$

M1	For h the height of the hill
M1	For the equation/EPPR
A1	Distance PQ
O3	

14. The interior angle of a regular polygon is 108° larger than the exterior angle. Determine the number of sides of the polygon. (3 Marks)

$$\text{Interior} + \text{Exterior} = 180^\circ$$

$$x + x - 108 = 180^\circ$$

$$2x = 288$$

$$x = 144$$

$$\text{Exterior} = 36^\circ$$

$$\text{No. of sides} = \frac{360^\circ}{36} \Rightarrow 10 \text{ sides}$$

M1	For equation
M1	Exterior angle
A1	No. of sides
O3	

15. A piece of wire 18 cm long is to be bent to form a rectangle. If its length is x cm, obtain an expression for its area. Hence calculate the dimensions of the rectangle with maximum area from the expression

$$\frac{18-2x}{2} \quad p=18 \quad \frac{18-2x}{2}$$

$$\text{Width} = \frac{18-2x}{2} = 9-x$$

$$\begin{aligned}\text{Area} &= L \times W \\ &= x(9-x) \\ &= 9x - x^2\end{aligned}$$

For maximum area;

$$\frac{dA}{dx} = 9-2x=0$$

$$2x=9$$

$$x = 4.5$$

$$\therefore \text{Length} = 4.5 \text{ cm}$$

$$\text{Width} = 4.5 \text{ cm}$$

(3marks)

M1 - For expression of the width

B1 - Expression for the area

A1 - Dimensions

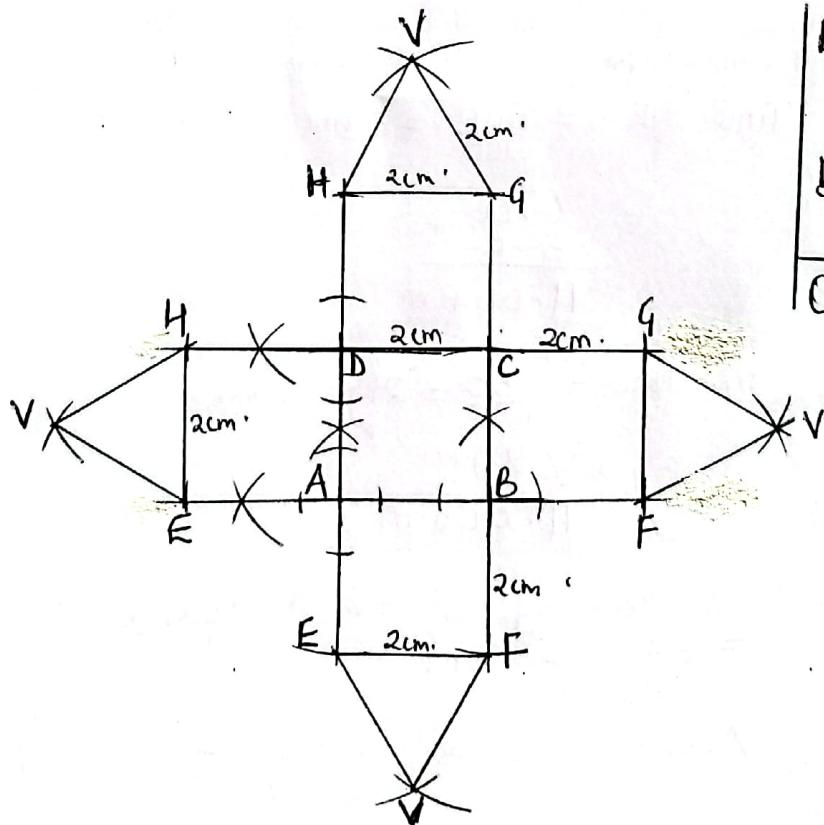
O3

16. A solid comprises of a cube ABCDEFGH of each side 2cm and a square based pyramid EFGHV. The slant edges of the pyramid $EV=FV=GV=HV=2\text{cm}$. Draw the net of the solid.

B1B1 - well drawn diagram

B1 - well labelled

O3



SECTION II(50 Marks)

Answer only five questions from this section in the spaces provided

17. A bus left Kisumu at 6.00a.m and travelled towards Usenge Boys at an average speed of 100km/hr. At 6.30 am, a van left Usenge Boys and travelled towards Kisumu to receive the bus with a number of students moving at an average speed of 125km/h. Given that the distance between Kisumu and Usenge Boys is 500km Calculate:

- a. The time the two vehicles met.

(4marks)

Distance covered by Bus;

$$\frac{1}{2} \times 100 = 50\text{km}$$

Time taken to meet

$$\frac{x}{100} = \frac{450-x}{125}$$

$$125x = 45000 - 100x$$

$$225x = 45000$$

$$x = 200\text{km.}$$

$$\text{Time taken} = \frac{200}{100} = 2\text{hrs.}$$

Alternatively;

Distance travelled by Bus;

$$\frac{1}{2} \times 100 = 50\text{km}$$

$$R.D = 500\text{km} - 50\text{km} = 450\text{km}$$

$$R.S = 125\text{km/h} + 100\text{km/h} = 225\text{km/h.}$$

$$R.T = \frac{450\text{km}}{225\text{km/h}} = 2\text{hrs}$$

$$\text{Time they met} \Rightarrow \frac{6.30}{2.00} +$$

$$= 8.30\text{a.m.}$$

M1

Distance covered by bus

M1

Equation for time taken (R,T)

M1

Equation at Addition.

A1

Meeting time

O4

- b. On meeting, the bus proceeded with its journey but the van had a break of 30 minutes before proceeding for Usenge Boys. Calculate:

- i. The time the bus arrived at Usenge Boys.

(3marks)

$$\text{Time taken} = \frac{500}{100} = 5\text{hrs}$$

$$\begin{array}{r} 6.00 \\ 5.00 \\ \hline 11.00\text{a.m} \end{array}$$

OR

$$\text{Time taken} = \frac{250}{100} = 2\text{hrs } 30\text{min}$$

$$+ \frac{8.30\text{a.m.}}{2.30}$$

$$\hline 11.00\text{a.m.}$$

M1

total time taken

M1

Addition

A1

Arrival time

O3

- ii. The time the van arrived at Usenge Boys

(3marks)

Time taken by the Van to Usenge

$$= \frac{250}{125} = 2\text{hrs}$$

$$\text{Arrival time} \Rightarrow + 8.30\text{a.m}$$

$$\begin{array}{r} 2.00 \\ 30 \\ \hline 11.00\text{a.m.} \end{array}$$

M1

Time taken

M1

Addition

A1

Arrival time

O3

18. Complete the table below for the function $y = x^2 - 3x + 6$ in the range $-2 \leq x \leq 8$. (2mks)

X	-2	-1	0	1	2	3	4	5	6	7	8
Y	16	10	6	4	4	6	10	16	24	34	46

B₂

O₂

- a. Use the trapezium rule with 10 strips to estimate the area bounded by the curve, $y = x^2 - 3x + 6$, the lines $x = -2$, $x = 8$ and the x-axis. (3mks)

$$\text{Height} = \frac{8 - -2}{10} = 1$$

$$\begin{aligned} \text{Area} &= \frac{1}{2} \times 1 \left[(16+46) + 2(10+6+4+4+6+10+16+24+34) \right] \\ &= 0.5 [62 + 228] \end{aligned}$$

$$\Rightarrow 145 \text{ square units.}$$

M₁ - Height

M₁ - Expression

A₁ Area

O₃

- b. Use the mid-ordinate rule with 5 strips to estimate the area bounded by the curve, $y = x^2 - 3x + 6$, the lines $x = -2$, $x = 8$ and the x-axis. (2mks)

$$\text{Height} = \frac{8 - -2}{5} = 2$$

$$A = 2(10 + 4 + 6 + 16 + 34)$$

$$\Rightarrow 140 \text{ square units.}$$

M₁ - Expression

A₁ Area

O₂

- c. By integration, determine the actual area bounded by the curve $y = x^2 - 3x + 6$, the lines $x = -2$, $x = 8$, and the x-axis. (3mks)

$$\int_{-2}^{M_1} (x^2 - 3x + 6) dx$$

$$\left[\frac{x^3}{3} - \frac{3x^2}{2} + 6x \right]_{-2}^8$$

$$\left[\frac{8^3}{3} - \frac{3(8)^2}{2} + 6(8) \right] - \left[\frac{(-2)^3}{3} - \frac{3(-2)^2}{2} + 6(-2) \right]$$

$$= (170\frac{2}{3} - 96 + 48) - (4 - 6 - 12)$$

$$= 122\frac{2}{3} - 22$$

$$\Rightarrow 144\frac{2}{3}$$

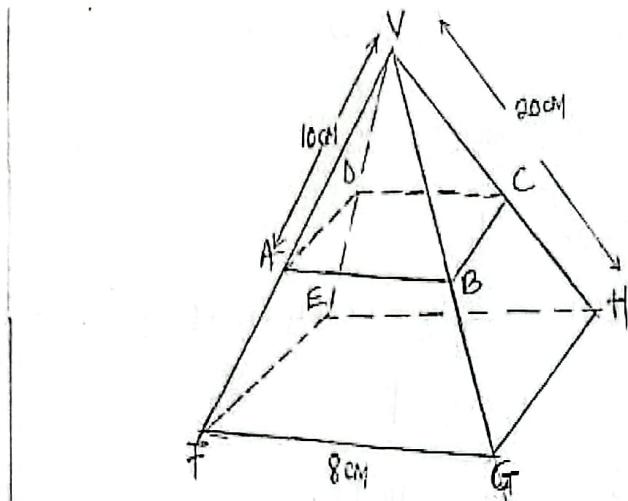
M₁ - Integrand

M₁ - Substitute

A₁ Area

O₃

19. The figure below is a right pyramid VEFGH with a square base of 8cm and a slant edge of 20cm. points A,B,C and D lie and plane ABCD is parallel to the base EFGH.



- a. Find the length of AB.

$$\frac{20}{10} = \frac{8}{x}$$

$$20x = 80$$

$$x = 4 \text{ cm}$$

- b. Calculate to 2 decimal places.

- i. The length of AC.

$$AC = \sqrt{4^2 + 4^2} = \sqrt{32}$$

$$\Rightarrow 5.66 \text{ cm}$$

- ii. The perpendicular height of the pyramid VABCD.

$$h = \sqrt{10^2 - 2.83}$$

$$= 9.59 \text{ cm}$$

- c. The pyramid VABCD was cut off. Find the volume of the frustum

ABCDEFGH correct to 2 decimal places.

(4marks)

$$\frac{4}{2} = \frac{x+9.59}{9.59}$$

$$2x + 19.18 = 38.36$$

$$2x = 19.18$$

$$x = 9.59$$

$$H = 9.59 + 9.59 \\ = 18.18 \text{ cm}$$

$$\text{Volume of Frustum } ABCDEFGH \\ = \frac{1}{3} (8 \times 8 \times 18.18) - \left(\frac{1}{3} \times 4 \times 4 \times 9.59 \right)$$

$$= 387.84 - 51.15$$

$$\Rightarrow 336.69 \text{ cm}^3$$

M1 Height of Pyramid

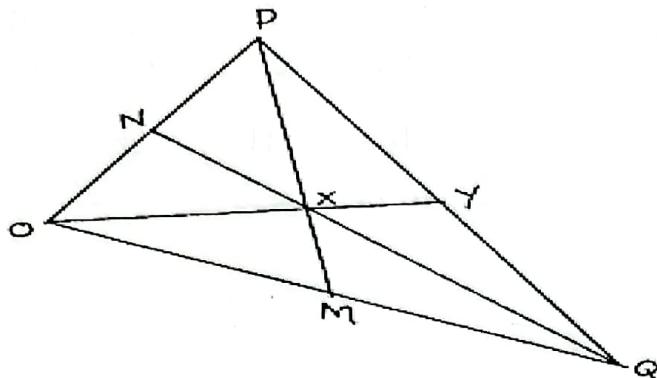
M1 Volume of pyramid

M1 Subtraction

A1 Volume of Frustum

10
04

20. The figure below is triangle OPQ in which $\mathbf{OP} = \mathbf{p}$ and $\mathbf{OQ} = \mathbf{q}$. M and N are points on \mathbf{OQ} and \mathbf{OP} respectively such that $\mathbf{ON} = \mathbf{NP} = 1:2$ and $\mathbf{OM}: \mathbf{MQ} = 3:2$.



(a) Express the following vectors in terms of \mathbf{p} and \mathbf{q} .

(i) \mathbf{PM} .

$$\begin{aligned}\mathbf{PM} &= \mathbf{PO} + \mathbf{OM} \\ &= -\mathbf{p} + \frac{3}{5}\mathbf{q} \\ &= \frac{2}{5}\mathbf{q} - \mathbf{p}\end{aligned}$$

(2 marks)

$\boxed{\mathbf{B}_1}$

(ii) \mathbf{QN} .

$$\begin{aligned}\mathbf{QN} &= \mathbf{QO} + \mathbf{ON} \\ &= -\mathbf{q} + \frac{1}{3}\mathbf{p} \quad \text{or} \\ &= \frac{1}{3}\mathbf{p} - \mathbf{q}\end{aligned}$$

(1 marks)

$\boxed{\mathbf{B}_1}$

(iii) \mathbf{PQ} .

$$\begin{aligned}\mathbf{PQ} &= \mathbf{PO} + \mathbf{OQ} \\ &= -\mathbf{p} + \mathbf{q} \quad \text{or} \\ &= \mathbf{q} - \mathbf{p}\end{aligned}$$

(1 marks)

$\boxed{\mathbf{B}_1}$

(b) Lines PN and QN intersect at X such that $\mathbf{PX} = r\mathbf{PM}$ and $\mathbf{QX} = t\mathbf{QN}$. Express \mathbf{OX} in two different ways and find the value of r and t .

(4 marks)

$$\mathbf{PX} = \frac{3}{5}r\mathbf{q} - r\mathbf{p}$$

$$(1-r)\mathbf{p} + \frac{3}{5}r\mathbf{q} = (1-t)\mathbf{q} + \frac{t}{3}\mathbf{p}$$

$\boxed{\mathbf{B}_1}$

$$\mathbf{OX} = \mathbf{OP} + \mathbf{PX}$$

$$t = 3 - 3r \quad | \quad 3r = 5 - 5t$$

$\boxed{\mathbf{B}_1}$

$$= \mathbf{p} + \frac{3}{5}r\mathbf{q} - r\mathbf{p}$$

$$3r = 5 - 5(3 - 3r) \quad | \quad t = 3 - 3\left(\frac{5}{6}\right)$$

$\boxed{\mathbf{B}_1}$

$$(1-r)\mathbf{p} + \frac{3}{5}r\mathbf{q} \quad \dots \text{(i)}$$

$$3r = 5 - 15 + 15r \quad | \quad t = \frac{1}{2}$$

$\boxed{\mathbf{M}_1}$

$$\mathbf{OX} = \mathbf{OQ} + \mathbf{QX}$$

$$-12r = -10 \quad | \quad r = \frac{5}{6}$$

$\boxed{\mathbf{M}_1}$

$$= \mathbf{q} + \frac{t}{3}\mathbf{p} - t\mathbf{q}$$

$$r = \frac{5}{6} \quad | \quad \therefore t = \frac{1}{2}$$

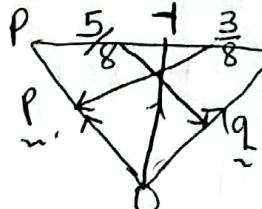
$\boxed{\mathbf{A}_1}$

$$(1-t)\mathbf{q} + \frac{1}{3}t\mathbf{p} \quad \dots \text{(ii)}$$

$$r = \frac{5}{6}$$

$\boxed{\mathbf{A}_1}$

(c) \mathbf{OX} produced meets \mathbf{PQ} at Y such that $\mathbf{PY}: \mathbf{YQ} = 5:3$. Using the ratio theorem or otherwise, find \mathbf{OY} in terms of \mathbf{p} and \mathbf{q} .



$$\mathbf{OY} = \frac{3}{8}\mathbf{p} + \frac{5}{8}\mathbf{q}$$

(2 mark)

$\boxed{\mathbf{B}_1}$

Alternatively.

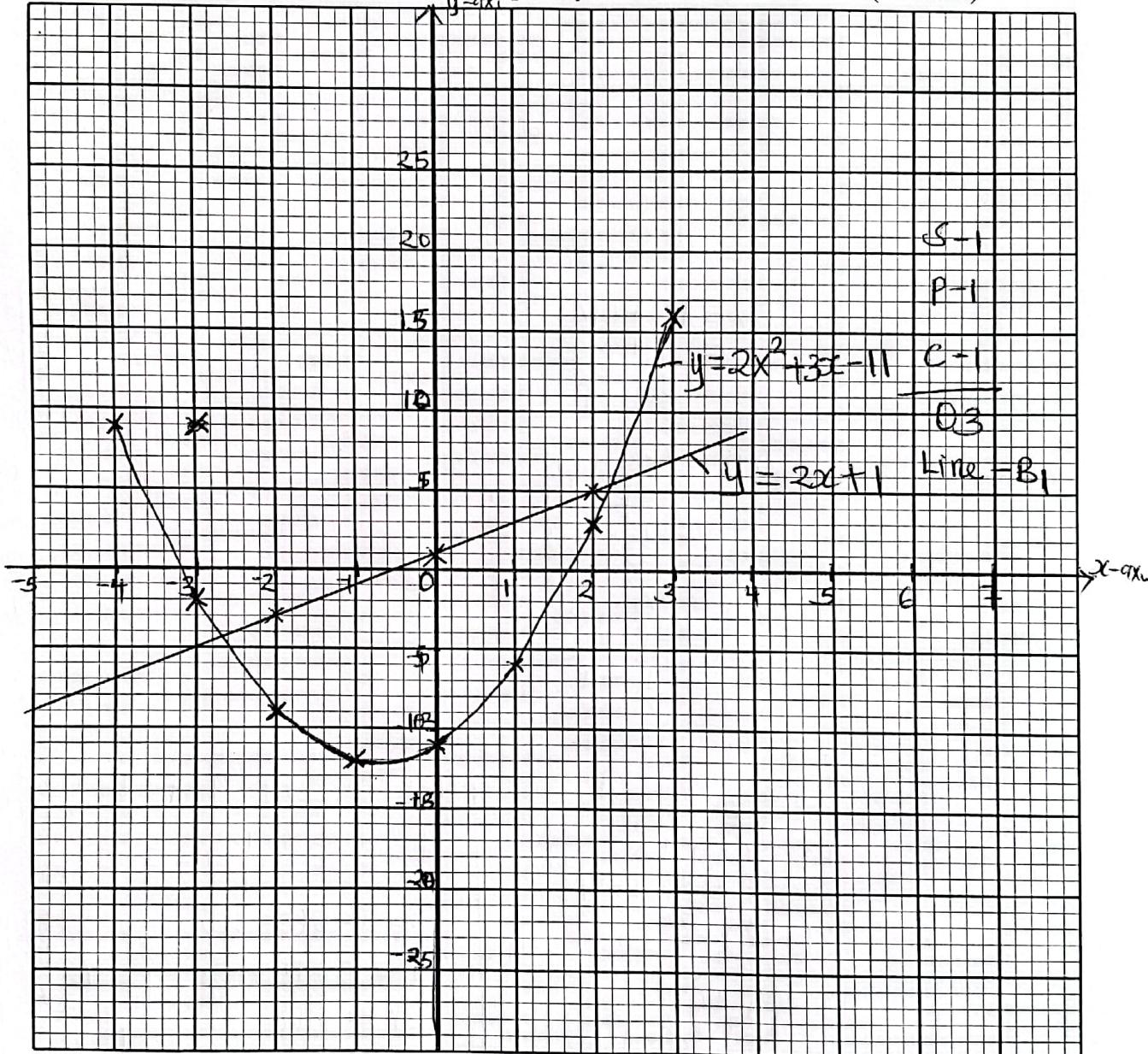
$$\begin{aligned}\mathbf{OY} &= \mathbf{OP} + \mathbf{PY} \\ &= \mathbf{p} + \frac{5}{8}(1-\mathbf{p}) = \frac{3}{8}\mathbf{p} + \frac{5}{8}\mathbf{q}\end{aligned}$$

21. Complete the table below for the equation $y = 2x^2 + 3x - 11$

(2 Marks)

x	-4	-3	-2	-1	0	1	2	3
$2x^2$	32	18	8	2	0	2	8	18
$3x$	-12	-9	-6	-3	0	3	6	9
-11	-11	-11	-11	-11	-11	-11	-11	-11
y	9	-2	-9	-12	-11	-6	3	16

(a) On the grid paper provided draw the graph of $y = 2x^2 + 3x - 11$ (3 Marks)



(b) On the same axes draw the graph of

$$y = 2x + 1 \quad (2 \text{ Marks})$$

x 0 2 -2	B1
y 1 5 -3	

(c) Use your graph to solve the quadratic

$$(i) 2x^2 + 3x - 11 = 0 \quad | \quad y = 0 \quad (1 \text{ Mark})$$

$$(ii) 2x^2 + x - 12 = 0 \quad | \quad x = -3 \cdot 2 \pm 0 \cdot 1 \text{ or } 1 \cdot 7 \pm 0 \cdot 1 \quad (2 \text{ Marks})$$

$$\begin{array}{l|l} y = 2x^2 + 3x - 11 & x = -2 \cdot 6 \pm 0 \cdot 1 \\ 0 = 2x^2 + x - 12 & \text{or} \\ \hline y = 2x + 1 & 2 \cdot 3 \pm 0 \cdot 1 \end{array}$$

22. A straight line L1 passes through the points (8, -2) and (4, -4).

(a) Write its equation in the form $ax + by + c = 0$, where a, b and c are integers. (3 Marks)

$$m = \frac{-4 - (-2)}{4 - 8} = \frac{-2}{-4} = \frac{1}{2}$$

$$\frac{y + 2}{x - 8} = \frac{1}{2}$$

$$2y + 4 = x - 8$$

$$-x + 2y + 12 = 0$$

or

$$x - 2y - 12 = 0$$

M1	Gradient.
M1	Expression equated to gradient
A1	Correct form
03	

(b) If the line L1 above cuts the x-axis at point P, determine the coordinates of P.

(2 Marks)

$$\text{at } x = \text{when } y = 0$$

$$-x + 12 = 0$$

$$x = 12$$

Coordinates of P (12, 0)

M1	Expression
A1	Coordinates
02	

(c) Another line L2, which is a perpendicular bisector to the line in (a) above cuts the y axis at the point Q. Determine the coordinates of point Q. (3 Marks)

$$m \text{ of } L_2 = -2$$

$$\text{Coordinates of point of intersection} = x = \frac{8+4}{2}, y = \frac{-4+(-2)}{2} = (6, -3)$$

$$\text{Equation of } L_2 = \frac{y+3}{x-6} = -2$$

$$y = -2x + 9$$

$$\text{at } y\text{-intercept; } x=0 \therefore y = 9, Q = (0, 9)$$

(d) Find the length of QP

$$\text{Length } QP \Rightarrow \sqrt{(12)^2 - (0)^2} = \sqrt{12^2}$$

$$\sqrt{(12)^2 + (-9)^2}$$

$$\Rightarrow 15 \text{ units.}$$

B1	Coordinate of intersection
M1	Expression equal to gradient.
A1	Q (coordinates)
03	

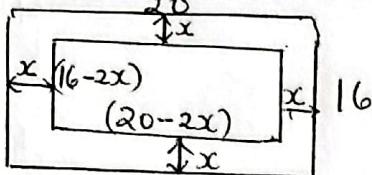
(2 Marks)

$$M1 \rightarrow \sqrt{12^2 + (-9)^2}$$

$$A1 \rightarrow C.A.O$$

23. A rectangular field measures 20 metres by 16 metres. A path of uniform width x - metres is made all round it. This makes the area of the field to reduce in the ratio 7 : 16.

- a) Find an expression in x for the new length and the width



$$\text{New length} = 20 - 2x$$

$$\text{New width} = 16 - 2x$$

(1mark)

B1 - For Both.

(1mark)

B1 Expression.

(4 marks)

- b) Find the expression in x for the new area.

$$\text{New area expression; } (20-2x)(16-2x)$$

$$= 4x^2 - 72x + 320$$

$$\Rightarrow 320 - 72x + 4x^2$$

- c) Find the possible value of x

$$\frac{20 \times 16}{4x^2 - 72x + 320} = \frac{16}{7}$$

$$16(4x^2 - 72x + 320) = 20 \times 16 \times 7$$

$$4x^2 - 18x + 80 = 20 \times 7$$

$$x^2 - 18x + 80 = 35$$

$$x^2 - 18x + 45 = 0$$

$$x^2 - 3x - 15x + 45 = 0$$

$$x(x-3) - 15(x-3) = 0$$

$$(x-15)(x-3) = 0$$

$$x = 15 \text{ or } 3$$

$$\text{Ignoring } 15 \therefore x = 3 \text{ m}$$

M1 Original expression involving ratios

M1 Simplified expression
 $x^2 - 18x + 45 = 0$

M1 Factorized expression

A1 C,A,D (3m)

04

- d) The remaining area of the field is divided among three siblings Abdi, Bor and Celine such that the ratio of Abdi to Bor's is 3 : 4 while that of Bor's to Celine's is 6 : 5. Find the difference between the area of Celine's share and Abdi's share.

$$\text{Remaining area} = (20-6)(16-6) = 160 \text{ m}^2$$

(4marks)

$$\begin{aligned} A:B &= (3:4)6 &\Rightarrow 18:24 \\ B:C &= (6:5)4 &\Rightarrow 24:20 \end{aligned}$$

M1 For expression leading to 160m²

$$A:B:C$$

$$18:24:20$$

$$9:12:10$$

$$\text{Celine's} \Rightarrow \left(\frac{10}{31} \times 160\right) = 51.62 \text{ m}^2$$

M1 Ratio A:B:C

$$\text{Abdi's} \Rightarrow \left(\frac{9}{31} \times 160\right) = 46.45 \text{ m}^2$$

M1 subtraction

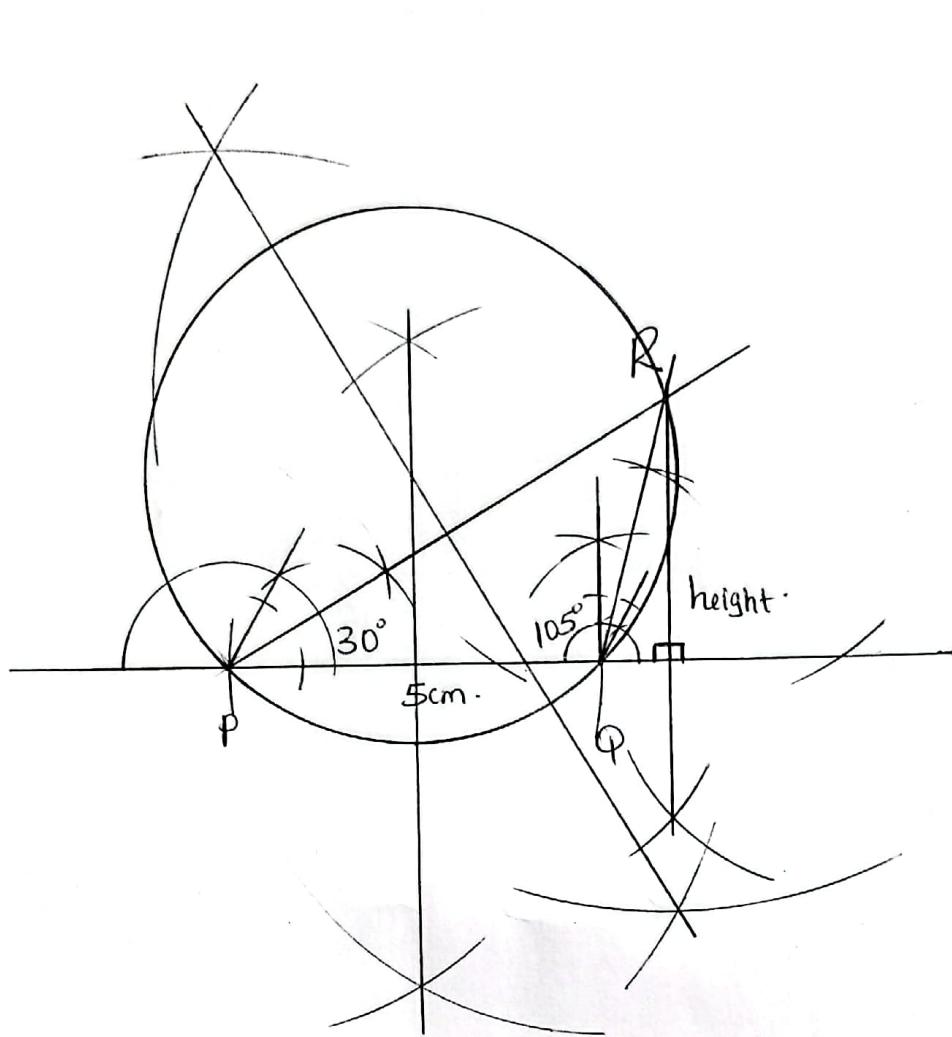
$$\text{Difference} = 51.62 - 46.45 \Rightarrow 5.17 \text{ m}^2$$

A1 Difference in area

24. Using a pair of compass and ruler only construct.

(a) Triangle PQR in which $PQ = 5\text{cm}$, $\angle QPR = 30^\circ$ and $\angle PQR = 105^\circ$.

(3marks)



B_1	Construction of 30°
B_1	105° constructed
B_1	Complete triangle PQR
03	
B_1	Bisector of line
B_1	Complete circle
B_1	Radius measure
03	
B_1	Dropping h
B_1	Height of triangle
02	

(b) A circle that passes through the vertices of the triangle PQR. Measure its radius.

$$\text{Radius} = 3.5 \pm 0.1 \text{ cm.}$$

(3marks)

(c) The height of triangles PQR with PQ as the base. Measure the height.

$$\text{Height} = 3.4 \pm 0.1 \text{ cm.}$$

(2marks)

(d) Determine the area of the circle that lies outside the triangle correct to 2 decimal places

Area of the circle outside the $\triangle PQR$

$$\left(\frac{22}{7} \times 3.5 \times 3.5\right) - \left(\frac{1}{2} \times 3.4 \times 5\right)$$

$$= 38.5 - 8.5$$

$$= 30 \text{ cm}^2$$

(2marks)

M_1	Equation of the two areas
A_1	Area outside the triangle