

Entailment:

Knowledge Base:

1. Alice is the mother of Bob
2. Bob is the father of Charlie
3. A father is a parent
4. A mother is a parent
5. All parents have children
6. If someone is a parent, their children are siblings
7. Alice is married to David.

$M(Alice, Bob)$

$F(Bob, Charlie)$

$\forall x (Father(x, y) \rightarrow Parent(x, y))$

$\forall x (Mother(x, y) \rightarrow Parent(x, y))$

$\forall x (Parent(x, y) \rightarrow Child(y, x))$

$\forall x (Parent(x, y) \wedge Parent(x, z) \wedge y \neq z \rightarrow Siblings(y, z))$

$M(Alice, David)$

1, 4
2, 3
6
1, 2

Step by step solution

1. Hypothesis: "Charlie is a sibling of Bob"

2. Entailment Process:

- Considering statements 1 & 4, we can conclude that Alice is a parent of Bob $\Rightarrow Parent(Alice, Bob)$
- Considering statements 2 & 3, we can conclude that Bob is a parent of Charlie $\Rightarrow Parent(Bob, Charlie)$
- Considering statement 6, we say that if children are siblings then they must have a common parent.
- Considering statement 1 & 2, (Alice is a parent of Bob & Bob is a parent of Charlie), we can say that Bob and Charlie don't have a same parent.
- Therefore, Charlie & Bob are not siblings.

3. Conclusion

The hypothesis "Charlie is a sibling of Bob" is not entailed by the knowledge base.

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