



**SCHOOL OF COMPUTING**  
**SRM INSTITUTE OF SCIENCE AND TECHNOLOGY**  
**KATTANKULATHUR – 603 203**

**Course Code: 18CSC204J**

**Course Name: Design And Analysis Of Algorithm**

<b>Title of the Experiment</b>	Finding defective chessboard by using divide and conquer.
<b>Name of the candidate</b>	GAJULAPALLI NAGA VYSHNAVI
<b>Team members</b>	Shruthi Kannan (RA2011003010037) Aryan Sinha (RA2011003010066)
<b>Register Number</b>	RA2011003010049
<b>Date of the experiment</b>	27-06-2022

**Staff Signature with date**



**SRM**  
INSTITUTE OF SCIENCE & TECHNOLOGY  
Deemed to be University u/s 3 of UGC Act, 1956

***SRM INSTITUTE OF SCIENCE AND TECHNOLOGY***

**S.R.M NAGAR, KATTANKULATHUR – 603 203**

**BONAFIDECERTIFICATE**

**REGISTER NO. \_\_\_\_\_**

***Certified to be bonafide record of the work done by \_\_\_\_\_ of \_\_\_\_\_***

***B.tech degree course in the practical***

***18CSC204J- Design and Analysis of Algorithms in SRM Institute of Science and Technology, Kattankulathur during the academic year 2021-22.***

**Date:**

**Lab Incharge:**

**Submitted for university examination held in**

**SRM Institute of Science and Technology, Kattankulathur.**

## **TABLE OF CONTENTS**

### **SECTION 1:**

1. Problem statement
2. Description

### **SECTION 2:**

1. Methodology

### **SECTION 3:**

1. Algorithm
2. Code

### **SECTION 4:**

1. Time Complexity
2. Output
3. Conclusion
4. References

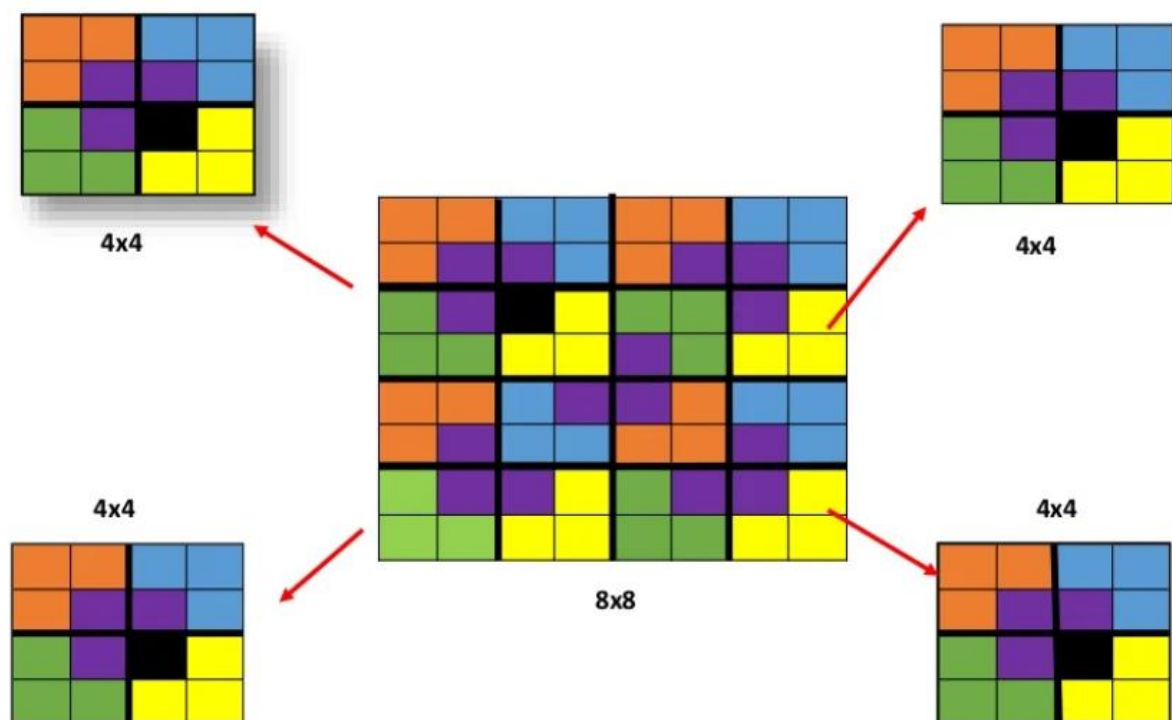
### Abstract:

The defective chessboard problem is solved with the help of divide and conquer approach. So in this defective chessboard problem of size  $n \times n$  the board has one missing cell of size  $1 \times 1$ . Task is to fill the board using L-shaped tiles. L-shaped tile is a  $2 \times 2$  square which has one of the cells of its dimension of  $1 \times 1$  missing. Task is to fill the board using L-shaped tiles such that it covers the entire chessboard except the missing cell.

### SECTION 1:

#### PROBLEM STATEMENT:

Finding defective chessboard by using divide and conquer.



## DESCRIPTION:

### Selection of Algorithm Design Strategy

#### DIVIDE AND CONQUER

Divide and conquer is an algorithm design paradigm. A divide-and-conquer algorithm recursively breaks down a problem into two or more sub-problems of the same or related type, until these become simple enough to be solved directly.

This technique can be divided into the following three parts:

1. **Divide:** This involves dividing the problem into smaller sub-problems.
2. **Conquer:** Solve sub-problems by calling recursively until solved.
3. **Combine:** Combine the sub-problems to get the final solution of the whole problem.

## SECTION 2:

### METHODOLOGY:

#### Steps to find the defective chessboard:

1. We have a chessboard of size  $n \times n$ , where  $n = 2k$ . Exactly one square is defective in the chessboard. The tiles are in L-shape i.e. 3 squares.  
Objective Cover all the chessboard with L-shape tiles, except the defective square.
2. It is possible to cover all non-defective squares. Let's see how. As the size of the chessboard is  $n \times n$  and  $n = 2k$ . Therefore, Total no. of squares  $= 2k \times 2k = 4k^2$ . No. of non-defective squares  $= 4k^2 - 1$ . Now, for the value of  $k$ ,  $4k^2 - 1$  is divisible by 3.
3. Defective chessboards.  $1 \times 1$   $2 \times 2$   $2 \times 2$   $2 \times 2$   $2 \times 2$  As the Size of these chessboards displayed here,  $1 \times 1$  and  $2 \times 2$  we don't have to place any L-shape tile in the first and rest can be filled by just using 1 L-shaped tile. For  $4 \times 4$  chessboard.
4. For  $8 \times 8$  DEFECTIVE CHESS BOARD.
  - One of the cell is defective.

- We divide the chess board into equal sub half's. Creation of defective box.
- Trick to cover the chess board with tiles.
- Again creation of defective boxes as we divide the chess board division of problems into sub-problems.
- As we have finally divided the problem into  $2 \times 2$  board we will put the tiles.
- The procedure will continue until all the sub board are covered with the tiles.
- The final chess board covered with all the tiles and only left with the defectives which we created.
- Here we will cover the defectives which we have created as in the last, there should be only one defective left. Combining of all sub problems.
- $8 \times 8$   $4 \times 4$   $4 \times 4$   $4 \times 4$   $4 \times 4$
- $2 \times 2$   $2 \times 2$   $2 \times 2$   $4 \times 4$   $2 \times 2$
- $1 \times 1$   $2 \times 2$   $4 \times 4$   $8 \times 8$

### **SECTION 3:**

#### **ALGORITHM:**

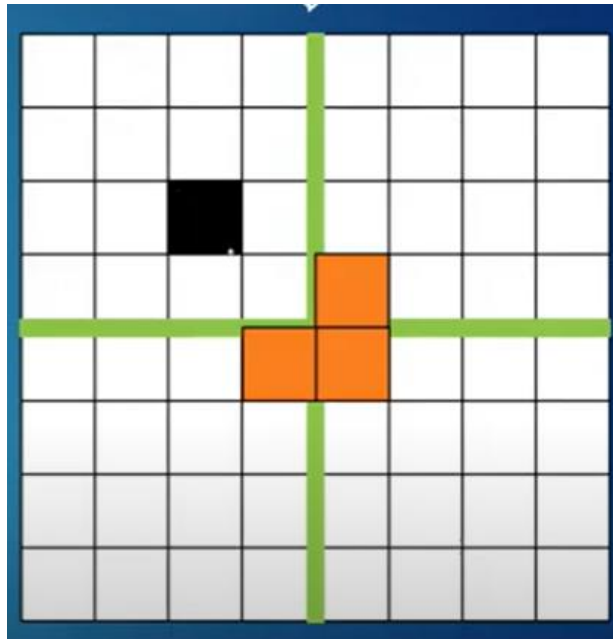
Step-1:

Apply Divide and conquer and divide the cell as  $4 \times 4$  cells

Step-2:

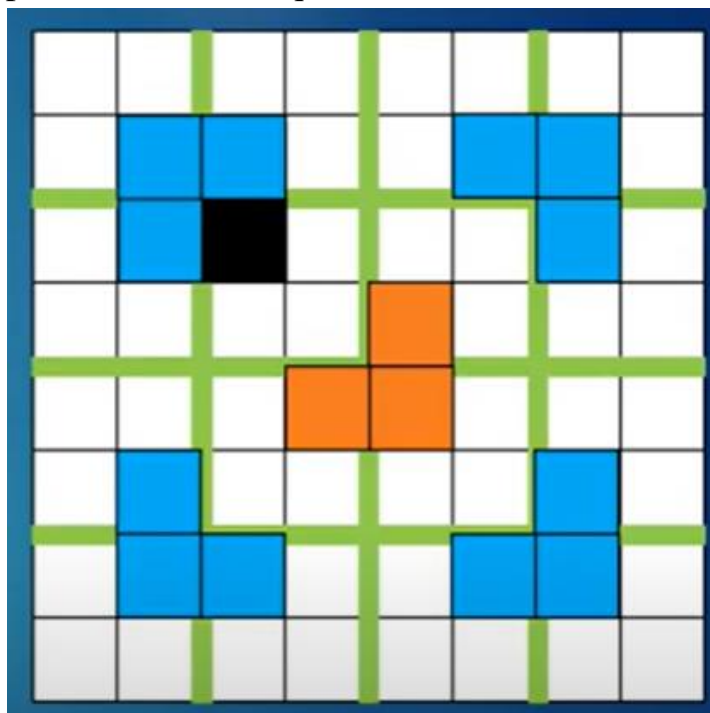
Place a L shaped tile at the centre such that it does not cover the  $n/2 \times n/2$  sub square that has a missing square.

Now all four sub-squares of size  $n/2 \times n/2$  have a missing cell



### Step-3:

Now the 4x4 sub square is divided into further 2x2 squares (ie) solve the problem recursively until the base case is reached. To make every sub-problem a smaller version of our original problem add defects at the center, with one square in each of the four quadrants of our board, except for the one with our original defect would allow use to make four proper sub-problems, at the same time ensuring that we can solve the complete problem by adding a last trionimo to cover up the pseudo-defective squares we added.



#### Step-4:

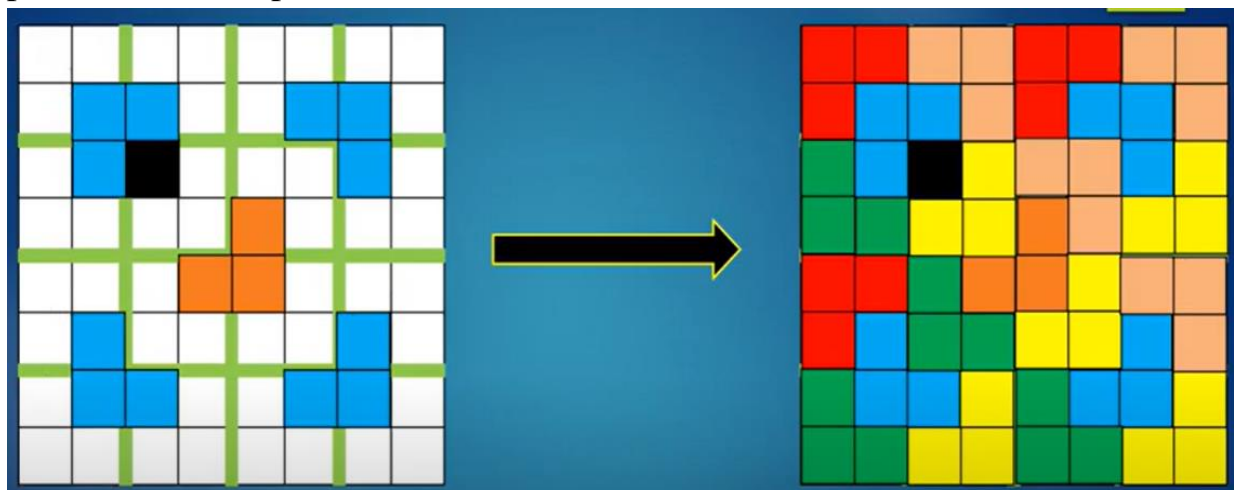
Once the base case is reached then fill the L shaped tiles.

After solving each of the four sub-problems and putting them together to form a complete board, we have 4 defects in our board: the original one will lie in one of the quadrants, while the other three were those we had intentionally added to solved the problem using DAC. All we have to do is add a final trionimo to cover up those defects.

Every recursive algorithm must have a base case, to ensure that it terminates. So we have 2x2 block with a single defect as a base case.

#### Step-5:

Now the chess board except the missing tile part has been successfully been placed with L shape tiles





**Code:**

```
//MINI PROJECT-FINDING DEFECTIVE CHESSBOARD
```

```
//RA201103010049
```

```
//RA201103010037
```

```
//RA201103010066
```

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
int size_of_grid, b, a, cnt = 0;
```

```
int arr[128][128];
```

```
// Placing tile at the given coordinates
```

```
void place(int x1, int y1, int x2,
```

```
           int y2, int x3, int y3)
```

```
{
```

```
    cnt++;
```

```
    arr[x1][y1] = cnt;
```

```
    arr[x2][y2] = cnt;
```

```
    arr[x3][y3] = cnt;
```

```
}
```

```
int tile(int n, int x, int y)
```

```
{
```

```
    int r, c;
```

```
    if (n == 2) {
```

```
        cnt++;
```

```
        for (int i = 0; i < n; i++) {
```

```
            for (int j = 0; j < n; j++) {
```

```
                if (arr[x + i][y + j] == 0) {
```

```
                    arr[x + i][y + j] = cnt;
```

```

    }
}
}
return 0;
}
// finding vaccant location
for (int i = x; i < x + n; i++) {
    for (int j = y; j < y + n; j++) {
        if (arr[i][j] != 0)
            r = i, c = j;
    }
}
// If missing tile is 1st quadrant
if (r < x + n / 2 && c < y + n / 2)
    place(x + n / 2, y + (n / 2) - 1, x + n / 2,
          y + n / 2, x + n / 2 - 1, y + n / 2);
// If missing Tile is in 3rd quadrant
else if (r >= x + n / 2 && c < y + n / 2)
    place(x + (n / 2) - 1, y + (n / 2), x + (n / 2),
          y + n / 2, x + (n / 2) - 1, y + (n / 2) - 1);
// If missing Tile is in 2nd quadrant
else if (r < x + n / 2 && c >= y + n / 2)
    place(x + n / 2, y + (n / 2) - 1, x + n / 2,
          y + n / 2, x + n / 2 - 1, y + n / 2 - 1);
// If missing Tile is in 4th quadrant
else if (r >= x + n / 2 && c >= y + n / 2)
    place(x + (n / 2) - 1, y + (n / 2), x + (n / 2),
          y + (n / 2) - 1, x + (n / 2) - 1,

```

```

        y + (n / 2) - 1);

// dividing it again in 4 quadrants
tile(n / 2, x, y + n / 2);
tile(n / 2, x, y);
tile(n / 2, x + n / 2, y);
tile(n / 2, x + n / 2, y + n / 2);
return 0;
}
int main()
{
    size_of_grid = 8;
    memset(arr, 0, sizeof(arr));
    a = 0, b = 0;
    arr[a][b] = -1;
    tile(size_of_grid, 0, 0);
    for (int i = 0; i < size_of_grid; i++) {
        for (int j = 0; j < size_of_grid; j++)
            cout << arr[i][j] << " \t";
        cout << "\n";
    }
}

```

## SECTION 4:

### Time Complexity:

$$T(n) = 4T(n/2) + C$$

The problem is divided into 4 subproblem (ie) 8x8 problem divides into 4 subproblems of 4x4 which further divides into base case 4 2x2 subproblems there by forming 16 subproblems

By Using Master Theorem,  $T(n) = a T(n/b) + f(n)$

$F(n) = \Theta(n^0 \log^0 n)$

$a=4$   $b=2$

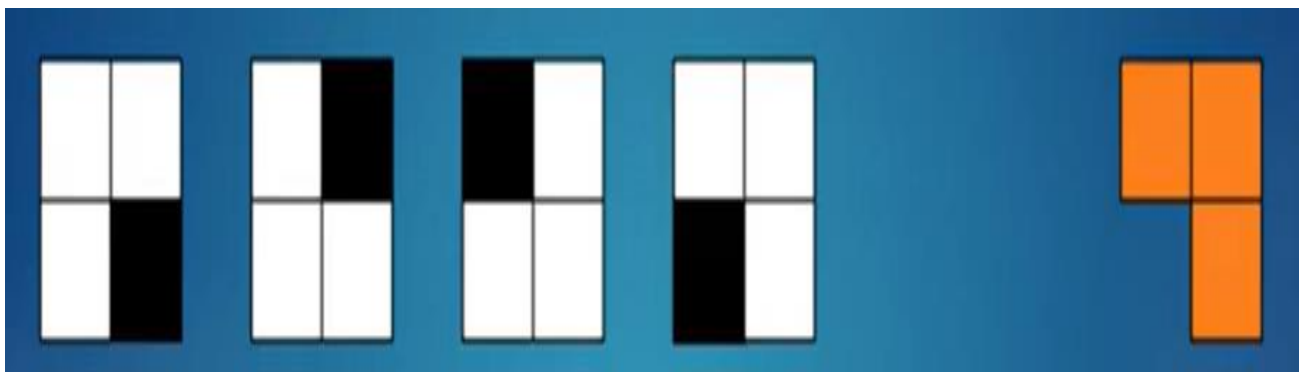
$\log_2 4 = 2 > 0$

There for time complexity  $= \Theta(n^2)$

Best case :

If the given chessboard is  $2 \times 2$  with one tile missing and just 1 single tile covers the chessboard.

Best case time complexity:  $O(1)$



## OUTPUT:

	input						
-1	9	8	8	4	4	3	3
9	9	7	8	4	2	2	3
10	7	7	11	5	5	2	6
10	10	11	11	1	5	6	6
14	14	13	1	1	19	18	18
14	12	13	13	19	19	17	18
15	12	12	16	20	17	17	21
15	15	16	16	20	20	21	21

## Conclusion:

Defective chessboard concept is implemented successfully and it's complexity is analysed.

## References:

<https://www.geeksforgeeks.org/tiling-problem-using-divide-and-conquer-algorithm/>