

ECE 046211 - Technion - Deep Learning

HW3 - Sequential Tasks and Training Methods



Keyboard Shortcuts

- Run current cell: Ctrl + Enter
- Run current cell and move to the next: Shift + Enter
- Show lines in a code cell: Esc + L
- View function documentation: **Shift + Tab** inside the parenthesis or help(name_of_module)
- New cell below: Esc + B
- Delete cell: Esc + D, D (two D's)



Students Information

• Fill in

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Submission Guidelines

- Maximal garde: 100.
- Submission only in pairs.
 - Please make sure you have registered your group in Moodle (there is a group creation component on the Moodle where you need to create your group and assign members).
- **No handwritten submissions.** You can choose whether to answer in a Markdown cell in this notebook or attach a PDF with your answers.
- SAVE THE NOTEBOOKS WITH THE OUTPUT, CODE CELLS THAT WERE NOT RUN WILL NOT GET ANY POINTS!
- What you have to submit:
 - If you have answered the questions in the notebook, you should submit this file only, with the name: ece@46211_hw3_id1_id2.ipynb .
 - If you answered the questionss in a different file you should submit a .zip file with the name ece046211_hw3_id1_id2.zip with content:
 - ece046211_hw3_id1_id2.ipynb the code tasks
 - o ece046211_hw3_id1_id2.pdf answers to questions.
 - No other file-types (.py , .docx ...) will be accepted.
- Submission on the course website (Moodle).
- Latex in Colab in some cases, Latex equations may no be rendered. To avoid this, make sure to not use *bullets* in your answers ("* some text here with Latex equations" -> "some text here with Latex equations").



Working Online and Locally

• You can choose your working environment:

- 1. Jupyter Notebook , locally with Anaconda or online on Google Colab
 - Colab also supports running code on GPU, so if you don't have one, Colab is the way to go. To enable GPU on Colab, in the menu: Runtime → Change Runtime Type → GPU.
- 2. Python IDE such as PyCharm or Visual Studio Code.
 - Both allow editing and running Jupyter Notebooks.
- Please refer to Setting Up the Working Environment.pdf on the Moodle or our GitHub (https://github.com/taldatech/ee046211-deep-learning) to help you get everything installed.
- If you need any technical assistance, please go to our Piazza forum (hw3 folder) and describe your problem (preferably with images).



Agenda

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- Part 2 Code Assignments Sequence-to-Sequence with Transformers
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 - Task 2 Preparing the Data Separating to Inputs and Targets
 - Task 3 Define Hyperparameters and Initialize the Model
 - Task 4 Train and Evaluate the Language Model
 - Task 5 Generate Sentences
- Credits



Part 1 - Theory

- You can choose whether to answser these straight in the notebook (Markdown + Latex) or use another editor (Word, LyX, Latex, Overleaf...) and submit an additional PDF file, **but no handwritten submissions**.
- You can attach additional figures (drawings, graphs,...) in a separate PDF file, just make sure to refer to them in your answers.
- \bullet $\mathit{LAT}_{E}X$ Cheat-Sheet (to write equations)
 - Another Cheat-Sheet



Question 1 - Transformers Efficeincy

For a series of T values, each with d features $X \in \mathbb{R}^{T \times d}$, a Self-Attention (SA) layer with parameters

$$W_O \in \mathbb{R}^{d \times D}, W_K \in \mathbb{R}^{d \times D}, W_V \in \mathbb{R}^{d \times M}$$

is defined as:

(1)
$$Q = XW_{Q}, K = XW_{K}, V = XW_{V}.$$

(2)
$$SA(X) = V' = \operatorname{softmax}\left(\frac{QK^T}{\sqrt{D}}\right)V$$
.

We will now look at an Encoder-Decoder Transformer.

- 1. Give an example usage for this kind of architecture.
- 2. Shortly explain each of the following component: Positional Encoding, AddNorm, Feed Forward.
- 3. Exaplain the difference between the Encoder and Decoder components.

- 4. One of the issues in computing SA is the computation speed and the memory required for this computation. How many multiplications are required for calculation of a single SA layer, as defined in Equation 2 (without the computation needed for Equation 1).
- 5. We will now see how to make this computation more efficient. We define a similarity function between the vectors $q \in \mathbb{R}^{1 \times D}$ and $k \in \mathbb{R}^{1 \times D}$ as follows:

$$\mathrm{sim}(q,k) = \mathrm{exp}\Bigg(rac{qk^T}{\sqrt{D}}\Bigg).$$

Show that the expression for the i^{th} value in the series (1 $\leq i \leq$ T):

(3) $V_i' = \frac{\sum_{j=1}^T \sin(Q_i, K_j) V_j}{\sum_{r=1}^T \sin(Q_i, K_r)}$ is equivalent to Equation 2 above, where a matrix with index i denotes the i^{th} row in the matrix. For example, Q_i denotes the vector of the i^{th} row of the matrix Q.



Question 2 - Preventing Variance Explosion

This question relates to lectures 8-9 (from slide 7):

Find an initializtion scheme such that

$$\forall l, i, : (1) \mathbb{E}[F_l(u_l)|u_l] = 0, (2) Var(u_l[i]) = 1,$$

assuming skip connections: $u_{l+1} = u_l + F_l(u_l)$ with a single skip $F_l(u_l) = W_l\phi(u_l) + b_l$ and the activation is ReLU: $\phi(x) = \text{ReLU}(x) = \max(0, x)$.



Question 3 - Recurrent Neural Networks

You are given a recurrent/feedback neural network with LReLU activations $\phi(u) = \max[pu, u]$, with input x_t and a representation $v_t \in \mathbb{R}^d$ that is updated as follows:

$$\forall \tau = 1, 2, \dots t : v_{\tau} = \phi(u_{\tau}), u_{\tau} = Wv_{\tau-1} + Bx_{\tau},$$

from initialization v_0 , and outputs $\hat{y}_t = Cv_t$. The network is trained with GD on a single long series $\{x_\tau, y_\tau\}_{\tau=1}^t$ with a cost function $\ell(y_t, \hat{y}_t)$ over the last term in the series.

- 1. Calculate the exact gradient $\frac{\partial \ell}{\partial W[i,j]}$ using Backpropagation through time (BPTT).
- 2. Recall that calculating the gradient using the method in the previous section there are two issues for $t \to \infty$: (1) the required computational resources grow indefinitely, and (2) the gradients explode or vanish. For each problem: explain it, provide an example for a method to alleviate it and describe any limitations of this method.



Part 2 - Code Assignments

- You must write your code in this notebook and save it with the output of all of the code cells.
- Additional text can be added in Markdown cells.
- You can use any other IDE you like (PyCharm, VSCode...) to write/debug your code, but for the submission you must copy it to this notebook, run the code and save the notebook with the output.

```
In [ ]: # imports for the practice (you can add more if you need)
        import numpy as np
        import matplotlib.pyplot as plt
        import time
        import os
        import math
        from typing import Tuple
        # pytorch
        import torch
        from torch import nn, Tensor
        import torch.nn.functional as F
        from torch.nn import TransformerEncoder, TransformerEncoderLayer
        from torch.utils.data import dataset
        # torchtext
        import torchtext
        from torchtext.datasets import WikiText2
        from torchtext.data.utils import get_tokenizer
        from torchtext.vocab import build_vocab_from_iterator
        seed = 211
        np.random.seed(seed)
        torch.manual_seed(seed)
```

```
In [ ]: print(f'pytorch: {torch.__version__}, torchtext: {torchtext.__version__}')
```



Sequence-to-Sequence with Transformers

- In this exercise, you are going to build a language model using PyTroch's Transformer module.
- We will work with the **Wikitext-2** dataset: the WikiText language modeling dataset is a collection of over 100 million tokens extracted from the set of verified Good and Featured articles on Wikipedia.
- After training, you will be able to generate senetences!



Task 1 - Loading and Observing the Data

- 1. Run the following cells that define the functions batchify and data_process and initialize the tokenizer, vocabulary and the WikiText2 train dataset.
- 2. Create the train, valid and test data using the provided $\,$ batchify $\,$ function.
- 3. Print the shape of train_data, write in a comment the meaning of each dimension (e.g. # [meaning of dim1, meaning of dim2]).
- 4. Print the first 20 words of one training sample from train_data. Use the vocabulary you built to transfer between tokens to words: itos = vocab.vocab.get_itos() will give a "int to string" list.

```
In [ ]: def batchify(data, bsz):
    """Divides the data into bsz separate sequences, removing extra elements
    that wouldn't cleanly fit.

Args:
    data: Tensor, shape [N]
    bsz: int, batch size

Returns:
    Tensor of shape [N // bsz, bsz]
    """

seq_len = data.size(0) // bsz
data = data[:seq_len * bsz]
data = data.view(bsz, seq_len).t().contiguous()
    return data.to(device)
In [ ]: def data_process(raw_text_iter: dataset.IterableDataset) -> Tensor:
```

```
In []: def data_process(raw_text_iter: dataset.IterableDataset) -> Tensor:
    """Converts raw text into a flat Tensor."""
    data = [torch.tensor(vocab(tokenizer(item)), dtype=torch.long) for item in raw_text_iter]
    return torch.cat(tuple(filter(lambda t: t.numel() > 0, data)))
```

```
In [ ]: train_iter = WikiText2(root="./data", split='train')
        tokenizer = get_tokenizer('basic_english')
        vocab = build_vocab_from_iterator(map(tokenizer, train_iter), specials=['<unk>'])
        vocab.set_default_index(vocab['<unk>'])
In [ ]: # train_iter was "consumed" by the process of building the vocab,
        # so we have to create it again
        train_iter, val_iter, test_iter = WikiText2()
        train_data = data_process(train_iter)
        val_data = data_process(val_iter)
        test_data = data_process(test_iter)
        device = torch.device('cuda:0' if torch.cuda.is_available() else 'cpu')
In [ ]: batch_size = 20
        eval_batch_size = 10
In [ ]: """
        Your Code Here
        train_data = # complete
        val data = # complete
        test_data = # complete
```



Task 2 - Preparing the Data - Separating to Inputs and Targets

- For a language modeling task, the model needs the following words as Target .
 - For example, for the senetence "I have a nice dog", the model will be given "I have a nice" as input, and "have a nice dog" as the target.
- Implement (complete) the function <code>get_batch(source, i, bptt)</code> : it generates the input and target sequence for the transformer model. It subdivides the source data into chunks of length <code>bptt</code> .
 - For example, for bptt=2 and at i=0, the output of data, target = get_batch(train_data, i=0, bptt=2): data will be of shape (2, 20), where the batch size is 20 and target will be of length 40 (the target for each element is two words, but we flatten target).
 - Example: for bptt=2, and the ABCDEFG... characters as input, our batches will be in the form of: data=[a, b], target=[b, c]. For bptt=3: data=[a, b, c], target=[b, c, d] and so on. This one example is a batch.
 - Print a sample from data and target.



Task 3 - Define Hyperparameters and Initialize the Model

- Define the following hyperparameters ([a, b] means in the range between a and b):
 - Embedding size: choose from [200, 250]
 - Number of hidden units: choose from [200, 250]
 - Number of layers: choose from [2, 4]
 - Number of attention heads: choose from [2, 4]

- Dropout: choose from [0.0, 0.3]
- Loss criterion: nn.CrossEntropyLoss()
- Optimizer: choose from [SGD, Adam, RAdam]
- Learning rate: choose from [5e-3, 5.0]
- Learning Scheduler: torch.optim.lr_scheduler.StepLR(optimizer, 1.0, gamma=0.95) or any scheduler of your choosing.
- Transformer LayerNormalization: post (norm_first=False) or pre (norm_first=True).
- Intialize an instance of TransformerModel (given) and send it to device. Note that you need to give it the number of tokens to define the output of the decoder. You should use the number of tokens in the vocabulary. Print the number of tokens, print all the chosen hyper-parameters and print the model (print(model).

```
In [ ]: class PositionalEncoding(nn.Module):
            def __init__(self, d_model, dropout=0.1, max_len=5000):
                 super(PositionalEncoding, self).__init__()
                self.dropout = nn.Dropout(p=dropout)
                pe = torch.zeros(max_len, d_model)
                position = torch.arange(0, max_len, dtype=torch.float).unsqueeze(1)
                \label{eq:div_term} \mbox{div\_term = torch.exp(torch.arange(0, d\_model, 2).float() * (-math.log(10000.0) / d\_model))} \\
                pe[:, 0::2] = torch.sin(position * div_term)
                pe[:, 1::2] = torch.cos(position * div_term)
                pe = pe.unsqueeze(0).transpose(0, 1)
                self.register_buffer('pe', pe)
            def forward(self, x):
                x = x + self.pe[:x.size(0), :]
                return self.dropout(x)
        class TransformerModel(nn.Module):
            def __init__(self, ntoken, ninp, nhead, nhid, nlayers, dropout=0.5, norm_first=False):
                super(TransformerModel, self).__init__()
                self.pos_encoder = PositionalEncoding(ninp, dropout)
                encoder_layers = TransformerEncoderLayer(ninp, nhead, nhid, dropout, norm_first=norm_first)
                self.transformer_encoder = TransformerEncoder(encoder_layers, nlayers)
                self.encoder = nn.Embedding(ntoken, ninp)
                self.ninp = ninp
                self.decoder = nn.Linear(ninp, ntoken)
                self.init_weights()
            def generate_square_subsequent_mask(self, sz):
                mask = (torch.triu(torch.ones(sz, sz)) == 1).transpose(0, 1)
                mask = mask.float().masked_fill(mask == 0, float('-inf')).masked_fill(mask == 1, float(0.0))
                return mask
            def init_weights(self):
                initrange = 0.1
                self.encoder.weight.data.uniform_(-initrange, initrange)
                 self.decoder.bias.data.zero_()
                self.decoder.weight.data.uniform_(-initrange, initrange)
            def forward(self, src, src_mask):
                src = self.encoder(src) * math.sqrt(self.ninp)
                src = self.pos_encoder(src)
                output = self.transformer_encoder(src, src_mask)
                output = self.decoder(output)
                return output
```

```
In []: """
Your Code Here
"""
```



Task 4 - Train and Evaluate the Language Model

- Fill in the missing line in the training code and train the model.
- Use bptt=35.

- Use the provided function to evaluate it on the validatation set (after each epoch) and on test test (after training is done). **Print and plot** the results (loss and perplexity).
- If you see that the performance does not improve, go back to Task 3 and re-think you hyper-parameters.

```
In [ ]: def evaluate(model, eval_data):
            model.eval() # turn on evaluation mode
            total_loss = 0.
            src_mask = model.generate_square_subsequent_mask(bptt).to(device)
            with torch.no_grad():
                for i in range(0, eval_data.size(0) - 1, bptt):
                    data, targets = get_batch(eval_data, i, bptt)
                    seq_len = data.size(0)
                    if seq len != bptt:
                        src_mask = src_mask[:seq_len, :seq_len]
                    output = model(data, src_mask)
                    output_flat = output.view(-1, ntokens)
                    total_loss += seq_len * criterion(output_flat, targets).item()
            return total_loss / (len(eval_data) - 1)
In [ ]: """
        Your Code Here
        def train(model, bptt):
            model.train() # turn on train mode
            total loss = 0.
            log interval = 200
            start_time = time.time()
            src_mask = model.generate_square_subsequent_mask(bptt).to(device)
            num_batches = len(train_data) // bptt
            for batch, i in enumerate(range(0, train_data.size(0) - 1, bptt)):
                data, targets = get_batch(train_data, i, bptt)
                seq len = data.size(0)
                if seq_len != bptt: # only on last batch
                   src_mask = src_mask[:seq_len, :seq_len]
                output = # complete
                loss = # complete
                optimizer.zero_grad()
                loss.backward()
                torch.nn.utils.clip_grad_norm_(model.parameters(), 0.5)
                optimizer.step()
                total_loss += loss.item()
                if batch % log interval == 0 and batch > 0:
                    lr = scheduler.get_last_lr()[0]
                    ms_per_batch = (time.time() - start_time) * 1000 / log_interval
                    cur_loss = total_loss / log_interval
                    ppl = math.exp(cur_loss)
                    print(f'| epoch {epoch:3d} | {batch:5d}/{num_batches:5d} batches | '
                          f'lr {lr:02.2f} | ms/batch {ms_per_batch:5.2f} |
                          f'loss {cur_loss:5.2f} | ppl {ppl:8.2f}')
                    total loss = 0
                    start_time = time.time()
In [ ]: """
        Your Code Here
        best_val_loss = float("inf")
        epochs = # complete the number of epochs to run
        best_model = None
        bptt = 35
        for epoch in range(1, epochs + 1):
            epoch start time = time.time()
            # complete: call train() here with appropriate paramteters
            val loss = evaluate(model, val data)
            print('-' * 89)
            print('| end of epoch {:3d} | time: {:5.2f}s | valid loss {:5.2f} | '
                   'valid ppl {:8.2f}'.format(epoch, (time.time() - epoch_start_time),
                                             val_loss, math.exp(val_loss)))
            print('-' * 89)
            if val_loss < best_val_loss:</pre>
                best_val_loss = val_loss
                best model = model
```

scheduler.step()



Task 5 - Generate Sentences

Use the following function to generate 3 sentences of length 20, and print them. Do they make sense? (you can compare generated sentences over epochs, to see if some logic is gained during training).

```
In [ ]: def generate(model, vocab, nwords=100, temp=1.0):
            model.eval()
            ntokens = len(vocab)
            itos = vocab.vocab.get_itos()
            model_input = torch.randint(ntokens, (1, 1), dtype=torch.long).to(device)
            words = []
            with torch.no_grad():
                for i in range(nwords):
                    output = model(model_input, None)
                    word_weights = output[-1].squeeze().div(temp).exp().cpu()
                    word_idx = torch.multinomial(word_weights, 1)[0]
                    word_tensor = torch.Tensor([[word_idx]]).long().to(device)
                    model_input = torch.cat([model_input, word_tensor], 0)
                    word = itos[word_idx]
                    words.append(word)
            return words
In [ ]: """
        Yout code Here
```



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