Assignment 7

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Outline

Problem Statement

Solution

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Papoulis Ch-5 Ex 5.29

Using (5-86), find $E(x^3)$ if $\eta_x = 10$ and $\sigma_x = 2$

Equation: 5-86

$$E(g(x)) \approx g(\eta) + g''(\eta) \frac{\sigma^2}{2}$$
 (1)

where,

 $\eta = \mathsf{Mean} \ \mathsf{of} \ \mathsf{the} \ x$

 $\sigma = \mathsf{Standard} \; \mathsf{Deviation} \; \mathsf{in} \; \mathsf{x}$

Solution

Let g(x) be a function such that $g(x) = x^3$, we have

$$\eta_{\mathsf{x}} = 10 \tag{2}$$

$$\sigma_{\mathsf{x}} = 2 \tag{3}$$

$$g''(x) = 6x \tag{4}$$

Using Equation (1), we got

$$E(x^3) \approx \eta_x^3 + 6\eta_x \frac{\sigma_x^2}{2} = 10^3 + 6 \times 10 \times \frac{4}{2} = 1120$$
 (5)

