Assignment 10

CS21BTECH11020 (Harsh Goyal)

June 27, 2022



Outline

Problem Statement

Papoulis Ch-9 Ex-9.37

The process x(t) is normal with zero mean and $R_x(\tau) = Ie^{-\alpha|\tau|}cos(\beta\tau)$. Show that if $y(t) = x^2(t)$. then $C_y(\tau) = I^2e^{-2\alpha|\tau|}(1+cos(2\beta\tau))$. Find $S_v(\omega)$.

Solution

We Know,

$$E\{x^{2}(t+\tau)x^{2}(t)\} = E\{x^{2}(t+\tau)\}E\{x^{2}(t)\} + 2E^{2}\{x^{2}(t+\tau)x^{2}(t)\}$$
(1)

Hence,

$$R_y(\tau) = R_x^2(0) + 2R_x^2(\tau) = I^2(1 + e^{-2\alpha|\tau|} + e^{-2\alpha|\tau|}\cos(2\beta\tau))$$
 (2)

$$S_{y}(\omega) = \left[2\pi\delta(\omega) + \frac{4\alpha}{4\alpha^{2} + \omega^{2}} + \frac{2\alpha}{4\alpha^{2} + (\omega - 2\beta)^{2}} + \frac{2\alpha}{4\alpha^{2} + (\omega + 2\beta)^{2}}\right]$$
(3)

Futhermore,

$$n_y = Ex^2(t) = R_x(0)$$
 (4)

$$C_{y}(\tau) = 2R_{x}^{2}(\tau) \tag{5}$$