

Digital Image Processing

Image Enhancement (Histogram Processing)

Over the next few lectures we will look at image enhancement techniques working in the spatial domain:

- What is image enhancement?
- Different kinds of image enhancement
- Histogram processing
- Point processing
- Neighbourhood operations

A Note About Grey Levels

So far when we have spoken about image grey level values we have said they are in the range $[0, 255]$

- Where 0 is black and 255 is white

There is no reason why we have to use this range

- The range $[0, 255]$ stems from display technologies

For many of the image processing operations in this lecture grey levels are assumed to be given in the range $[0.0, 1.0]$

What Is Image Enhancement?

Image enhancement is the process of making images more useful

The reasons for doing this include:

- Highlighting interesting detail in images
- Removing noise from images
- Making images more visually appealing

Image Enhancement Examples



Image Enhancement Examples (cont...)

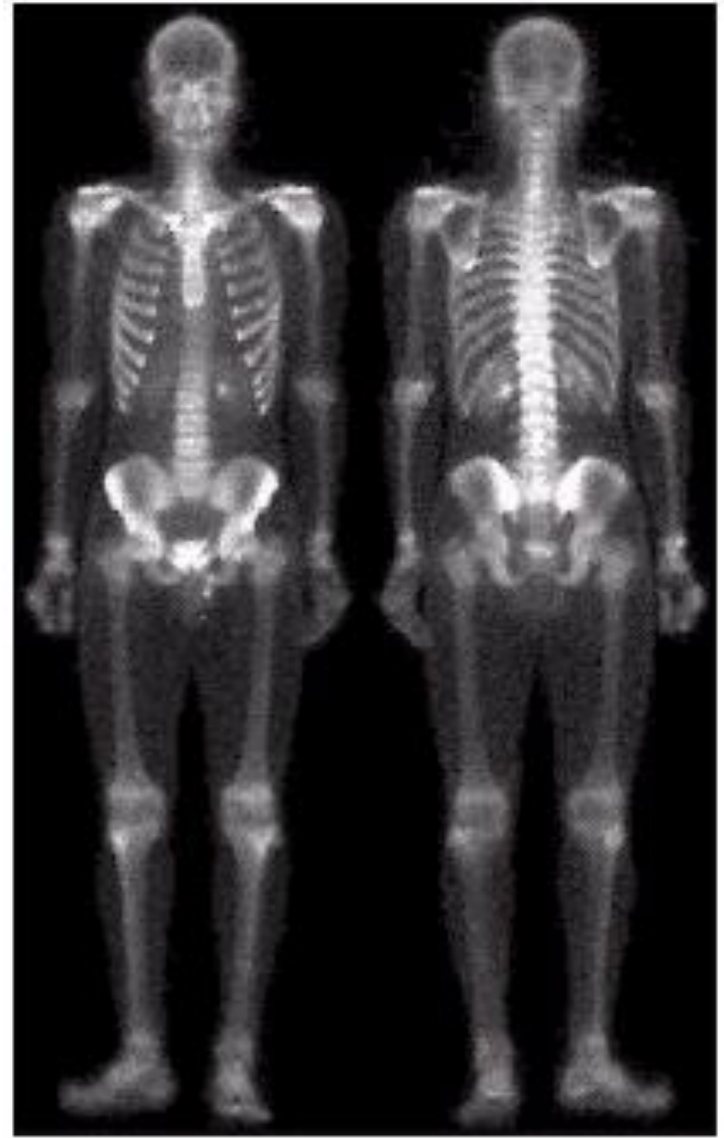
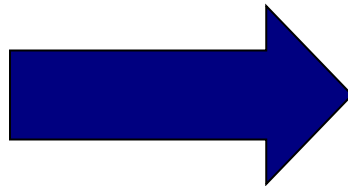
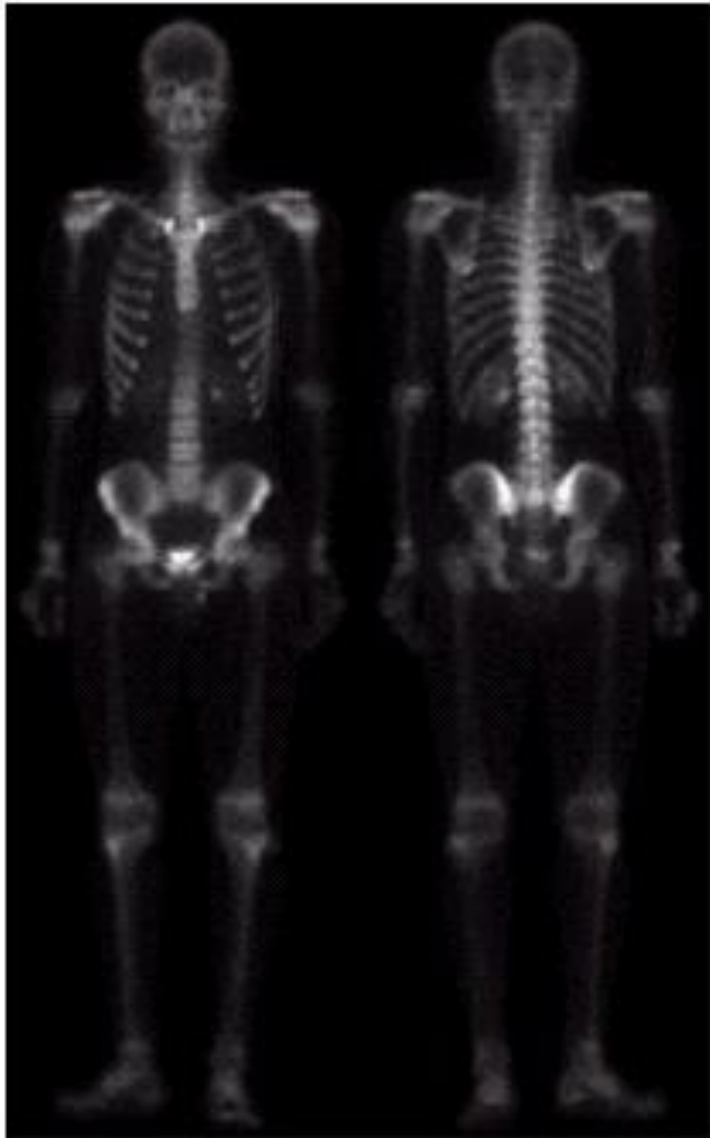


Image Enhancement Examples (cont...)

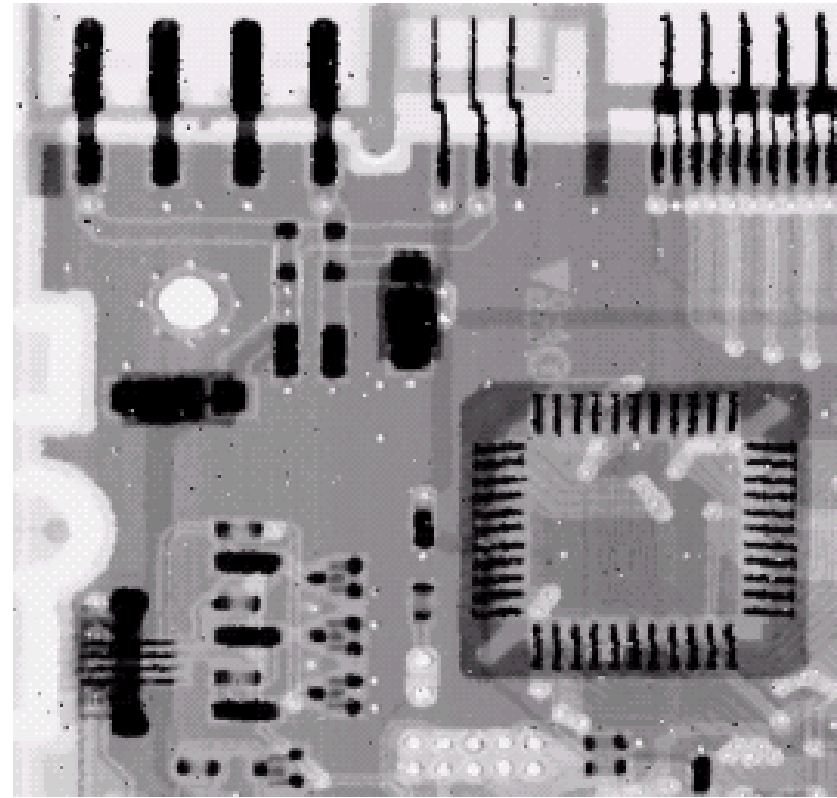
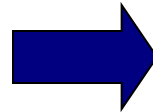
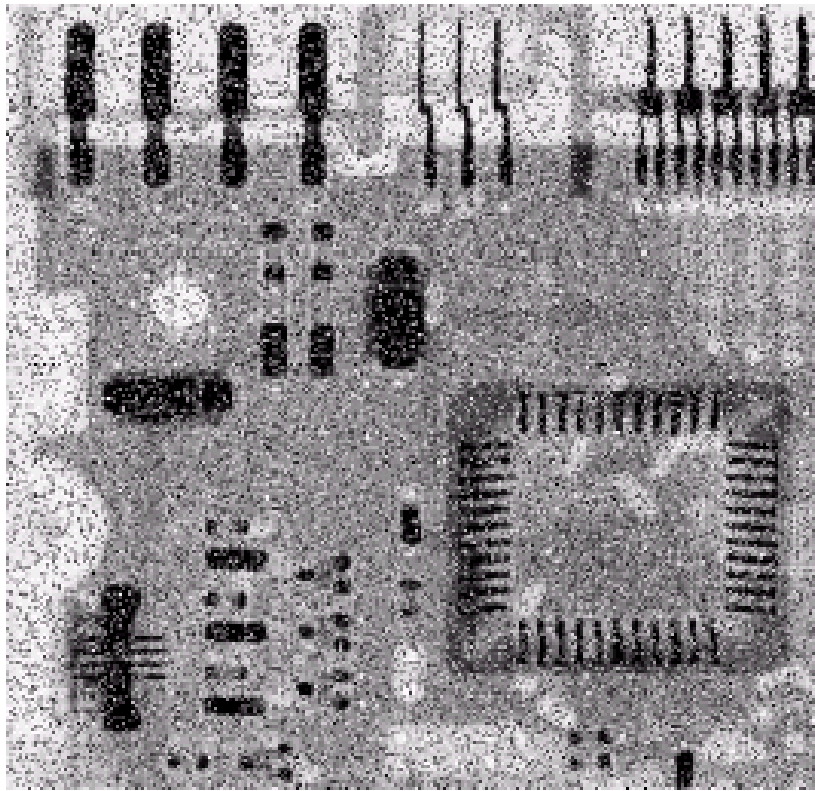


Image Enhancement Examples (cont...)



Spatial & Frequency Domains

There are two broad categories of image enhancement techniques

- Spatial domain techniques
 - Direct manipulation of image pixels
- Frequency domain techniques
 - Manipulation of Fourier transform or wavelet transform of an image

For the moment we will concentrate on techniques that operate in the spatial domain

Histogram: the distribution of gray intensity over all pixels in the images

r presents the gray level of a pixel

n presents the number of pixels with intensity r

L presents the highest gray level

Normalized histogram: Divide its value to total number of pixels

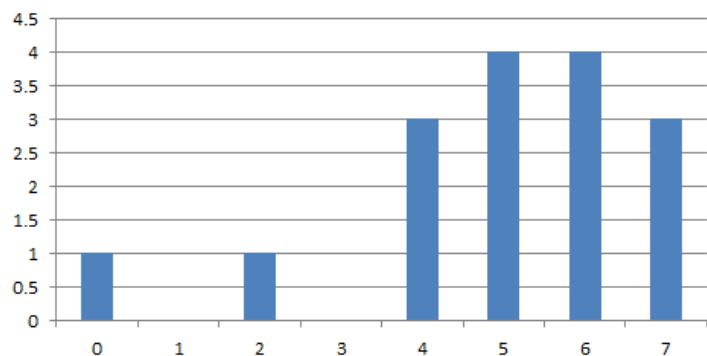
N presents total number of pixels in the image

Histogram Example

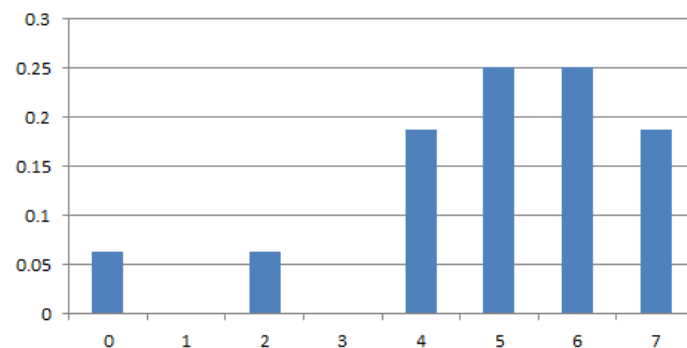
2	5	7	6
4	5	4	7
6	5	6	4
0	7	5	6

Intensity	0	1	2	3	4	5	6	7
Histogram	1	0	1	0	3	4	4	3
N.Histogram	0.0625	0	0.0625	0	0.1875	0.25	0.25	0.1875

Histogram



N.Histogram

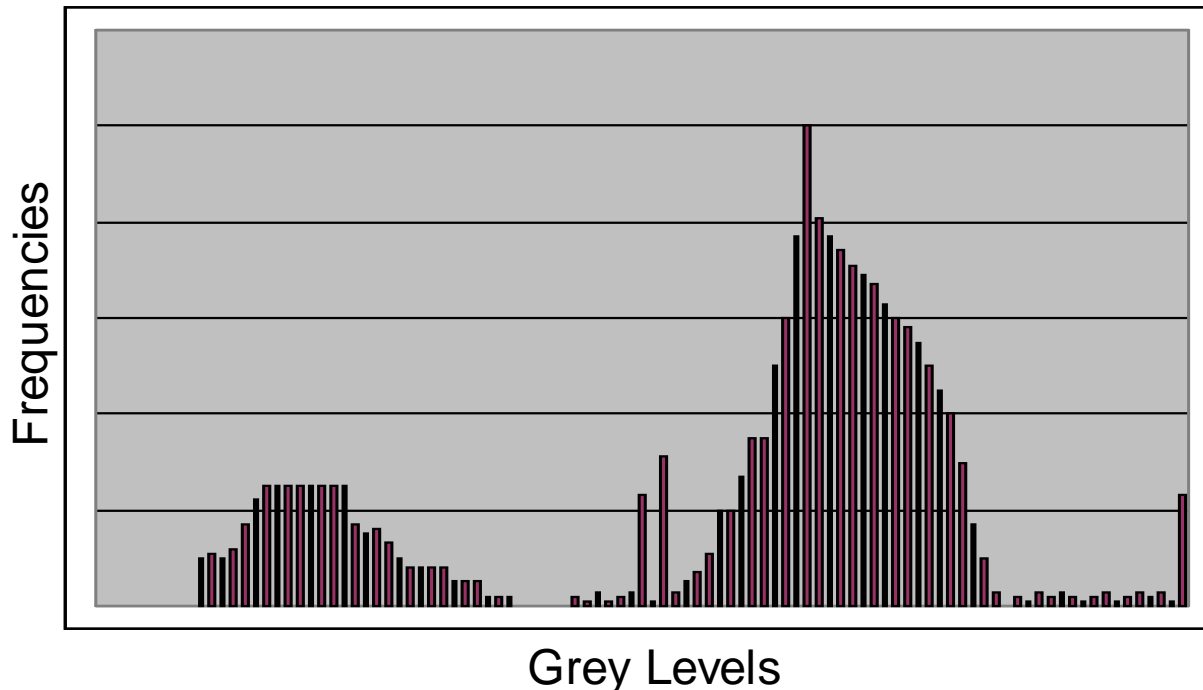


0	2	1	7
3	2	5	2
1	1	7	6
5	0	0	3

3	3	2
1	1	0
2	2	2

The histogram of an image shows us the distribution of grey levels in the image

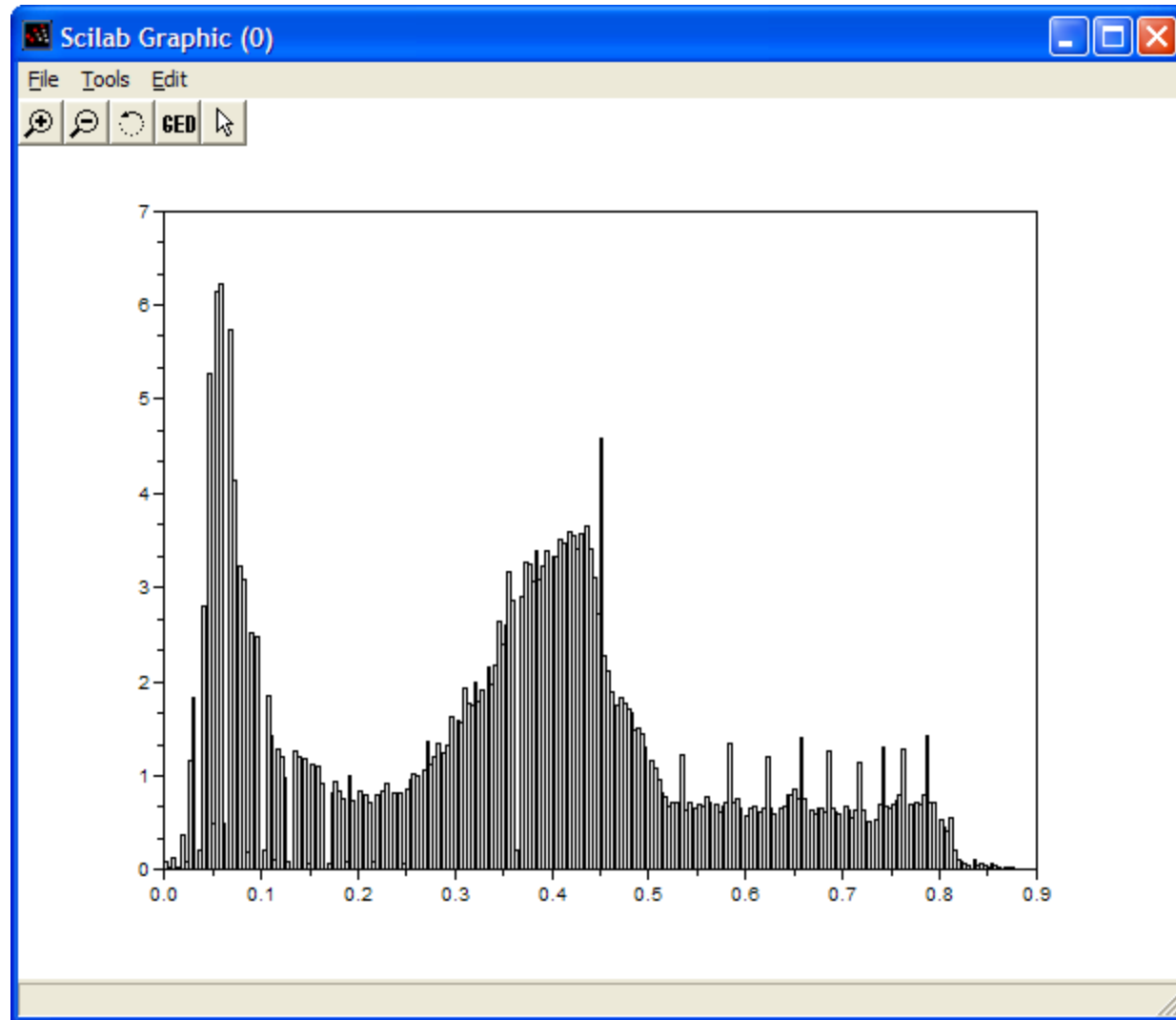
Massively useful in image processing, especially in segmentation



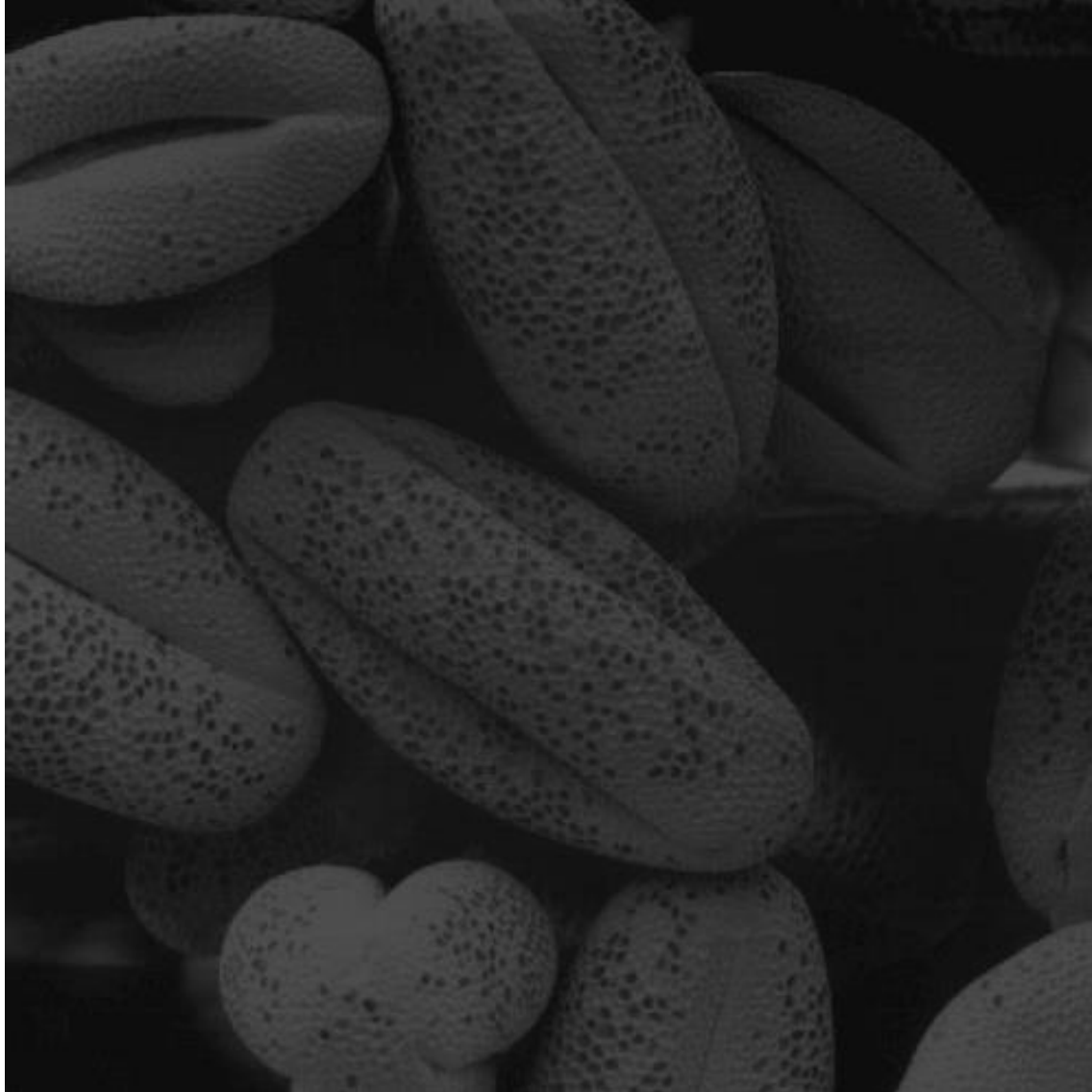
Histogram Examples



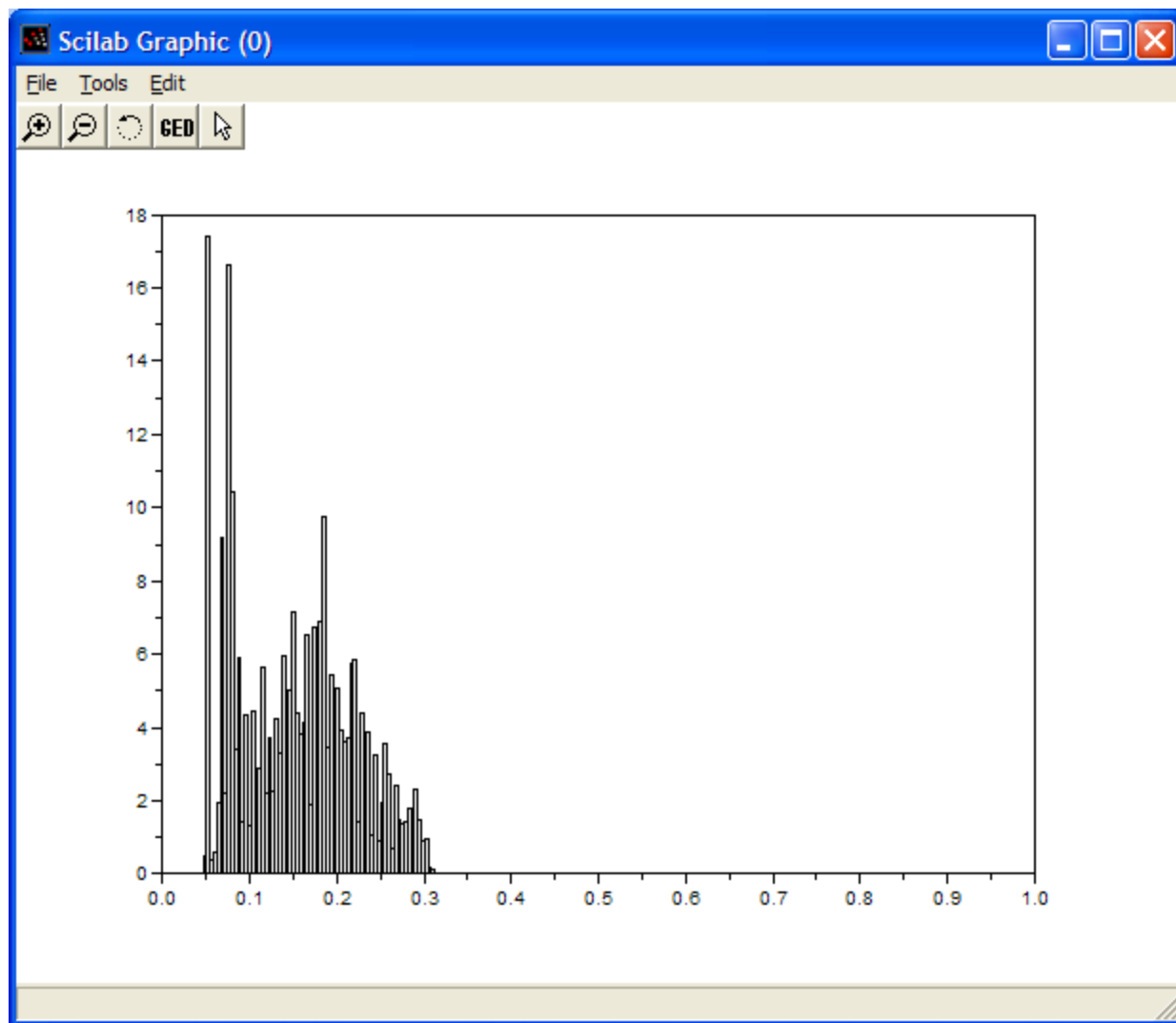
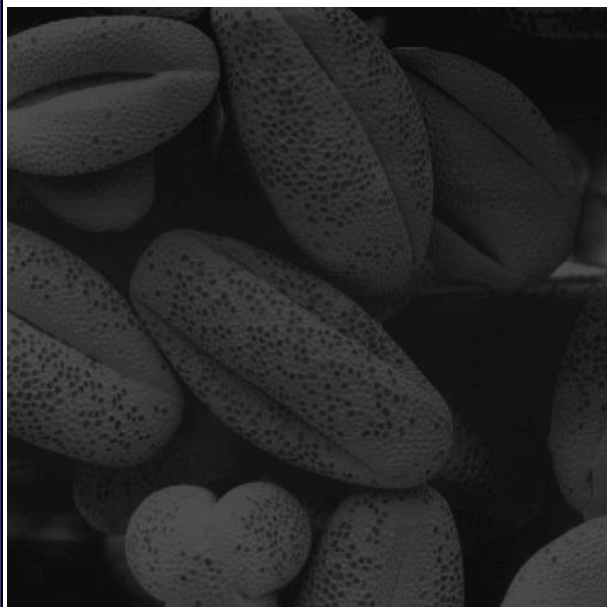
Histogram Examples (cont...)



Histogram Examples (cont...)



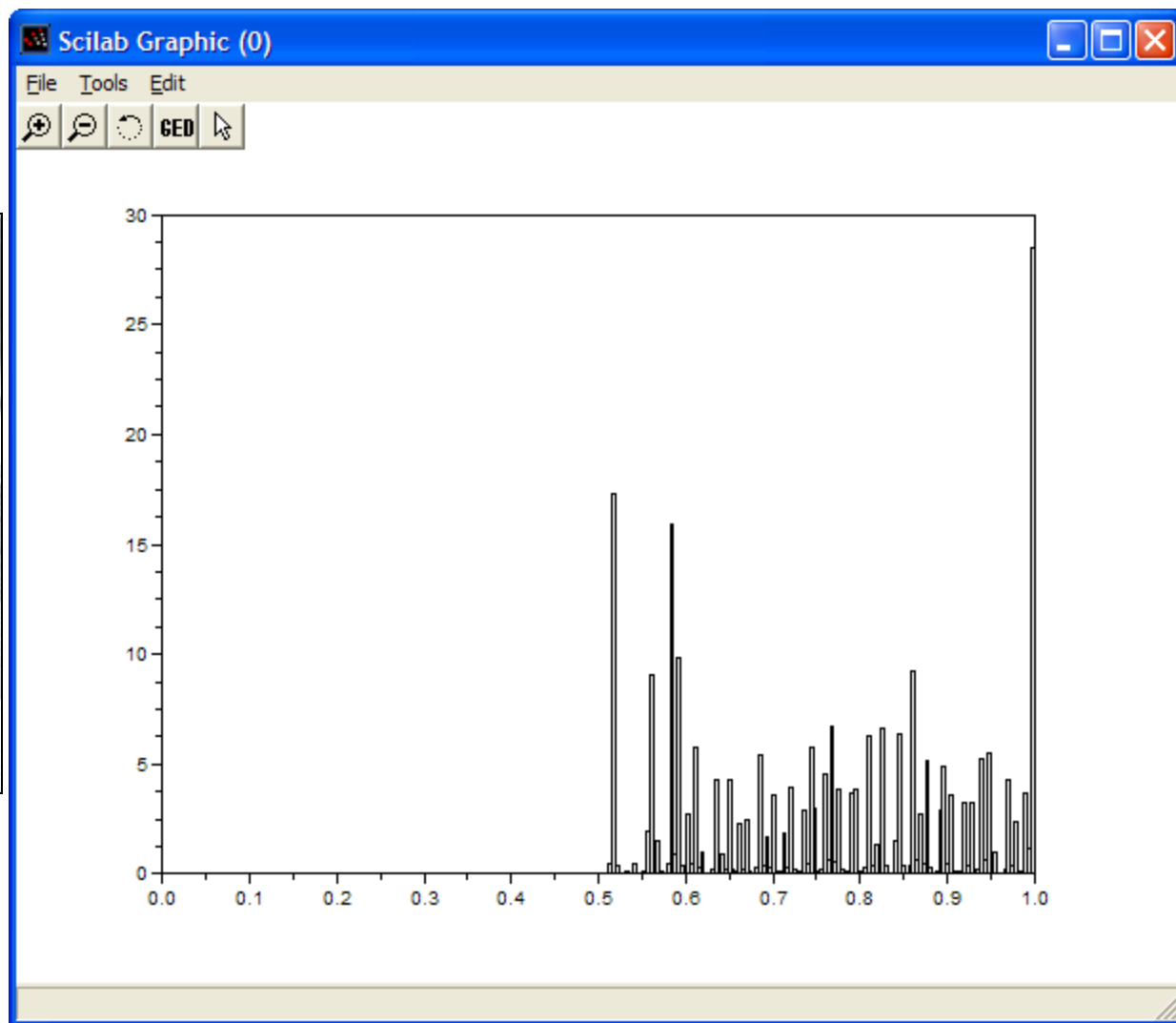
Histogram Examples (cont...)



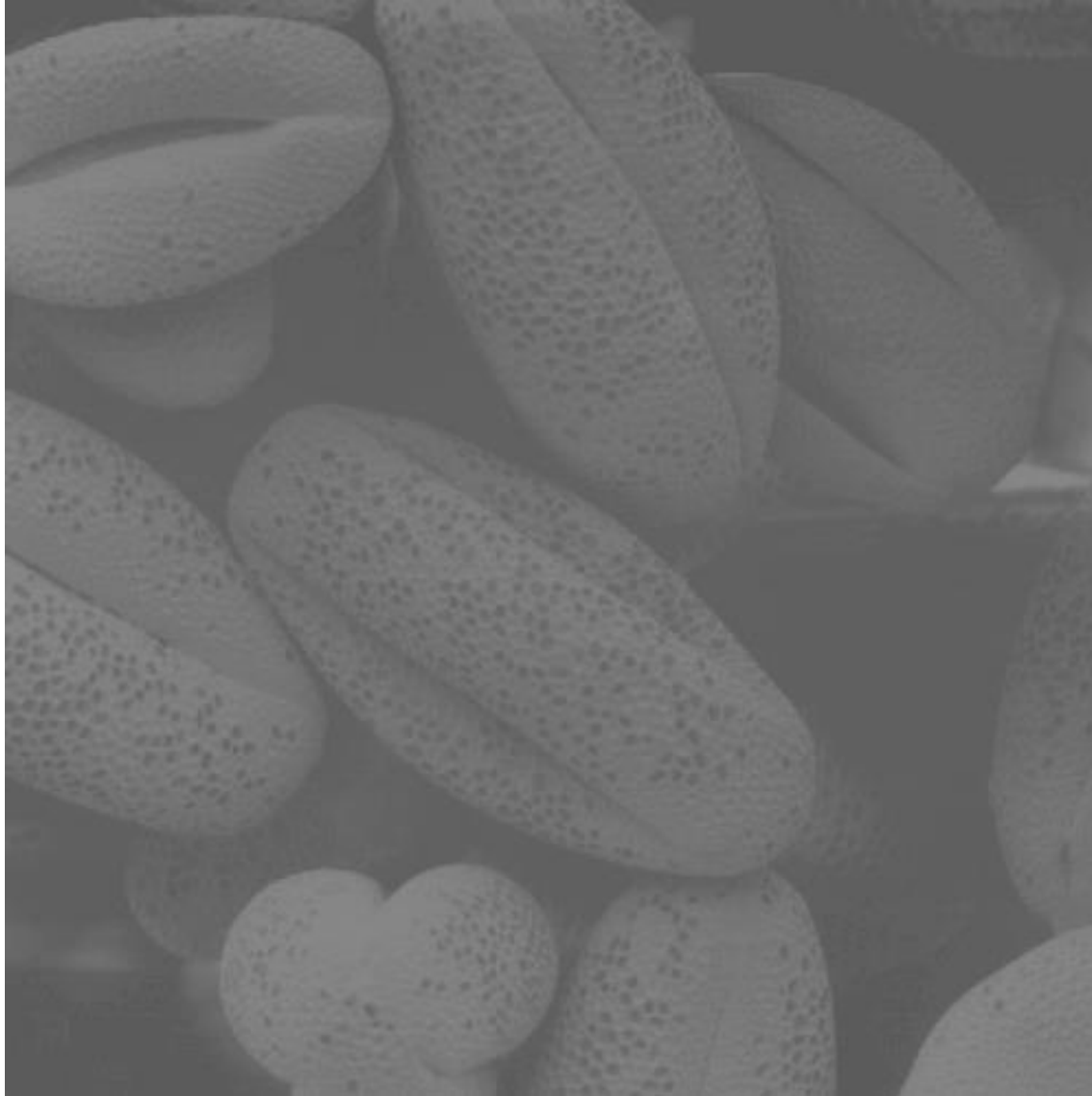
Histogram Examples (cont...)



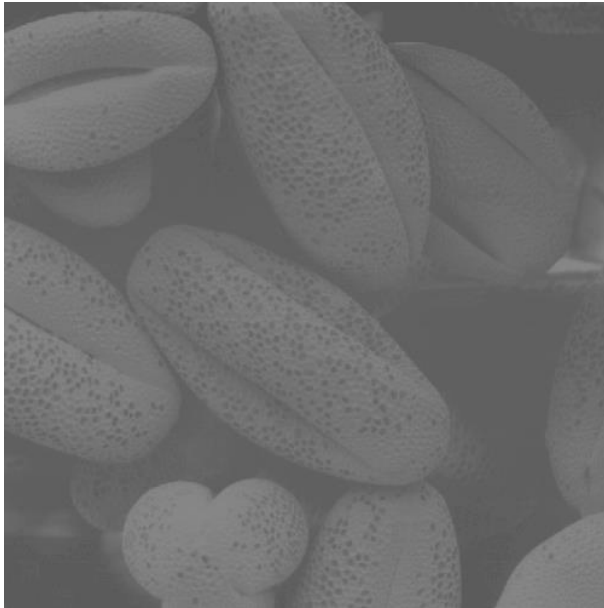
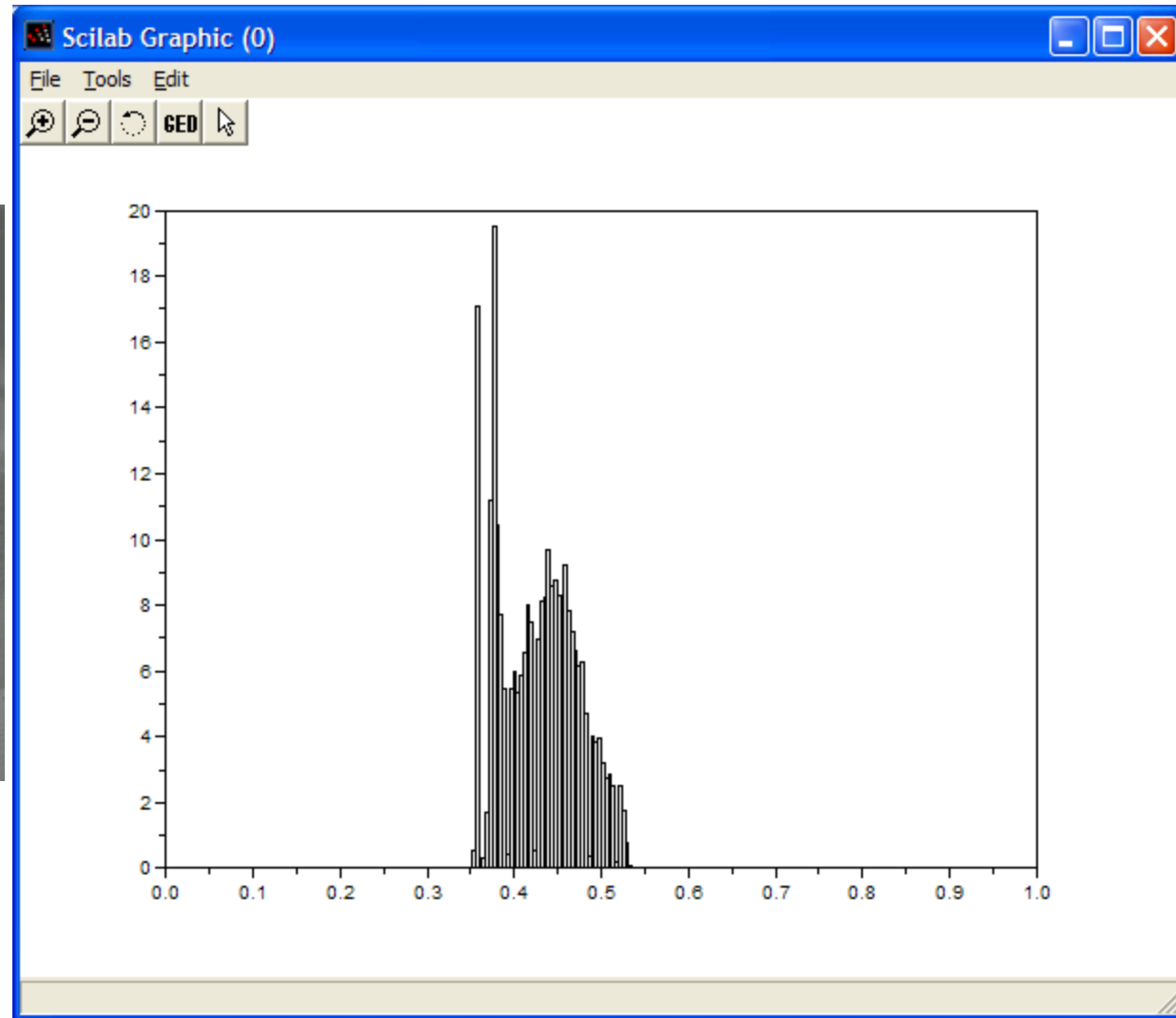
Histogram Examples (cont...)



Histogram Examples (cont...)



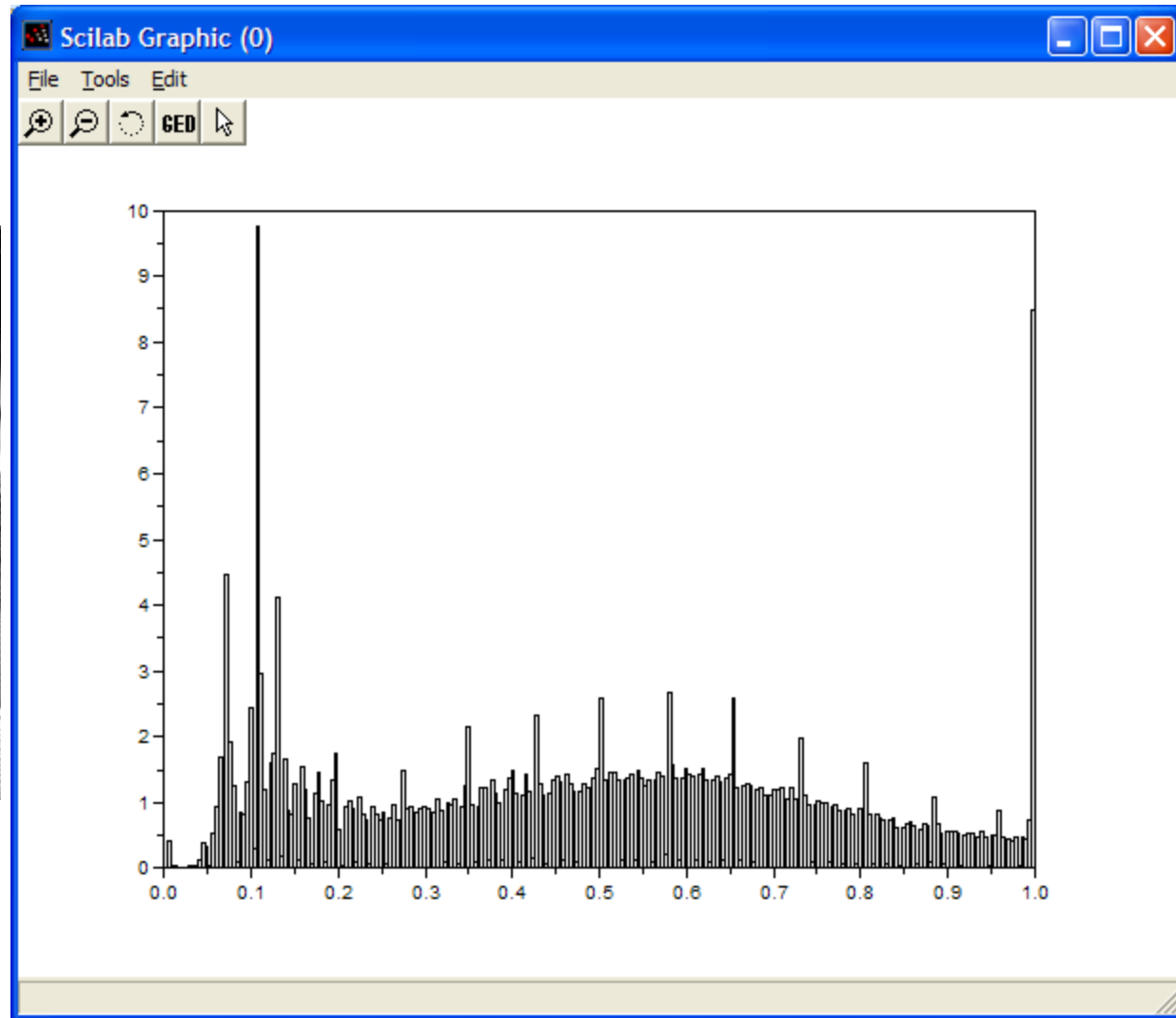
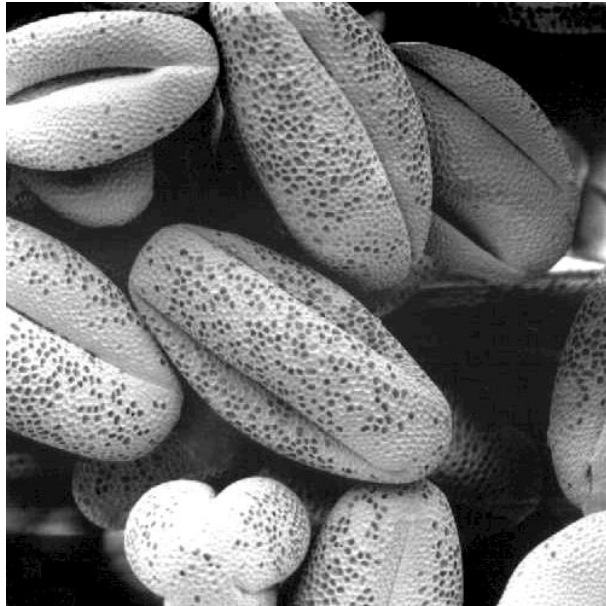
Histogram Examples (cont...)



Histogram Examples (cont...)



Histogram Examples (cont...)

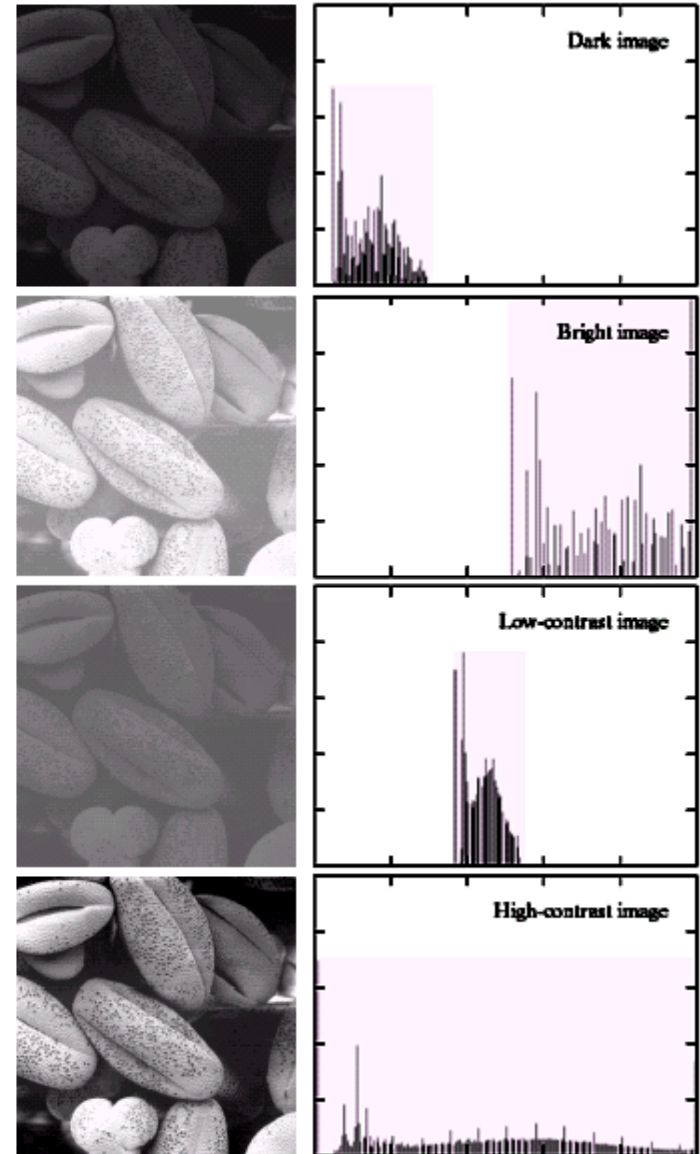


Histogram Examples (cont...)

A selection of images and their histograms

Notice the relationships between the images and their histograms

Note that the high contrast image has the most evenly spaced histogram



Contrast Stretching

We can fix images that have poor contrast by applying a pretty simple contrast specification

The interesting part is how do we decide on this transformation function?



Histogram Equalisation

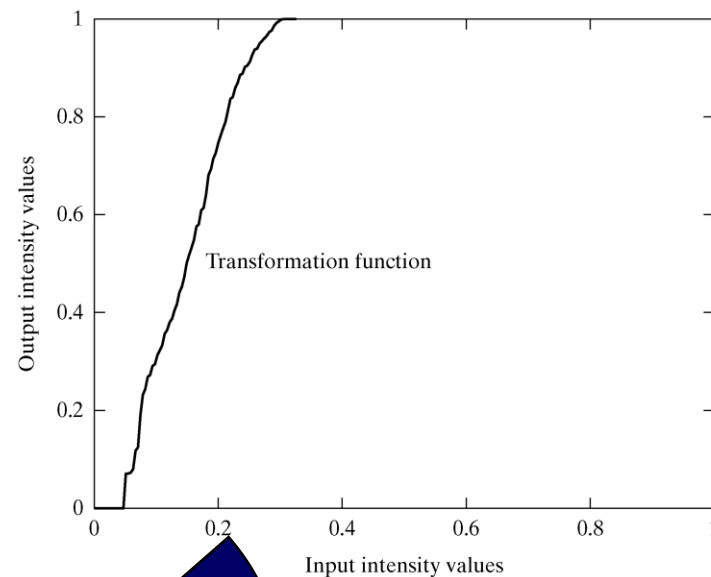
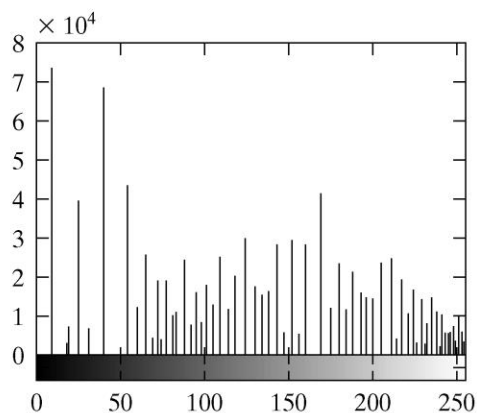
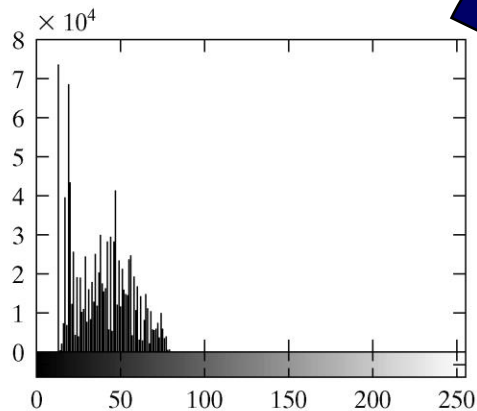
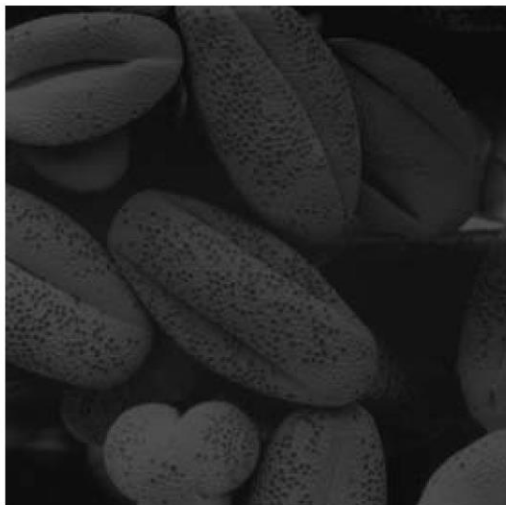
Spreading out the frequencies in an image (or equalising the image) is a simple way to improve dark or washed out images

The formula for histogram equalisation is given where

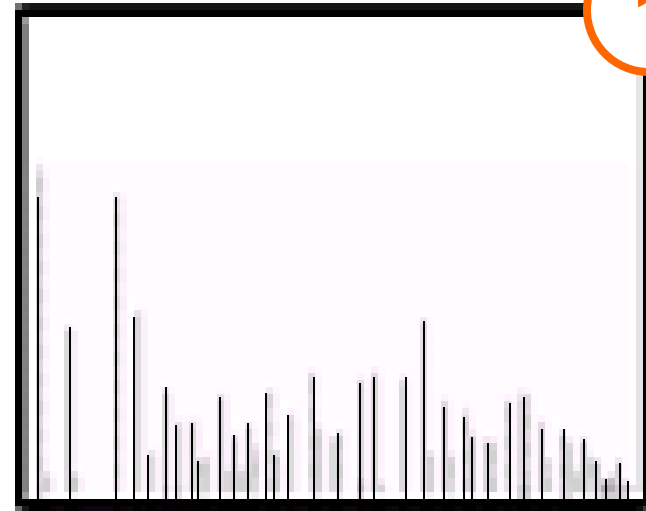
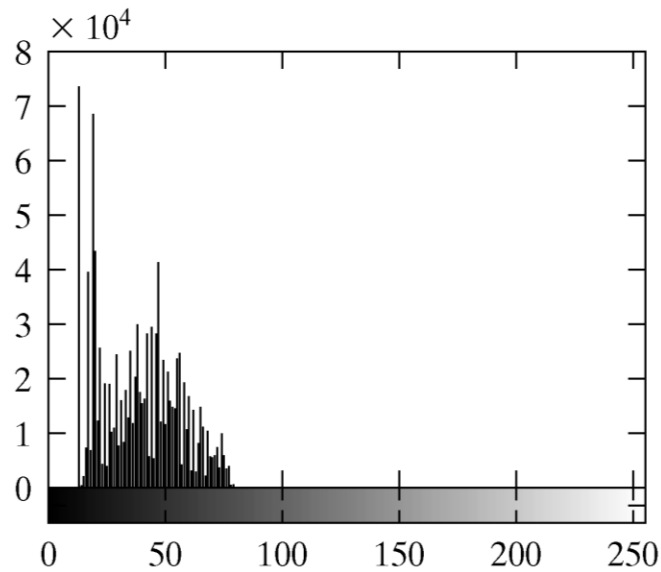
- r_k : input intensity
- s_k : processed intensity
- k : the intensity range (e.g 0.0 – 1.0)
- n_j : the frequency of intensity j
- n : the sum of all frequencies

$$\begin{aligned} s_k &= T(r_k) \\ &= \sum_{j=1}^k p_r(r_j) \\ &= \sum_{j=1}^k \frac{n_j}{n} \end{aligned}$$

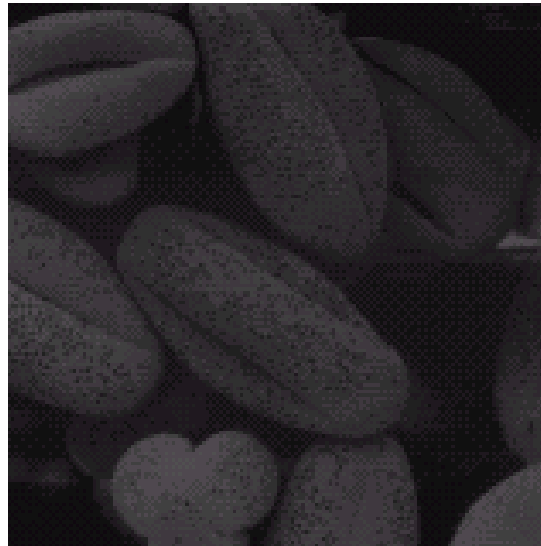
Equalisation Transformation Function



Equalisation Examples

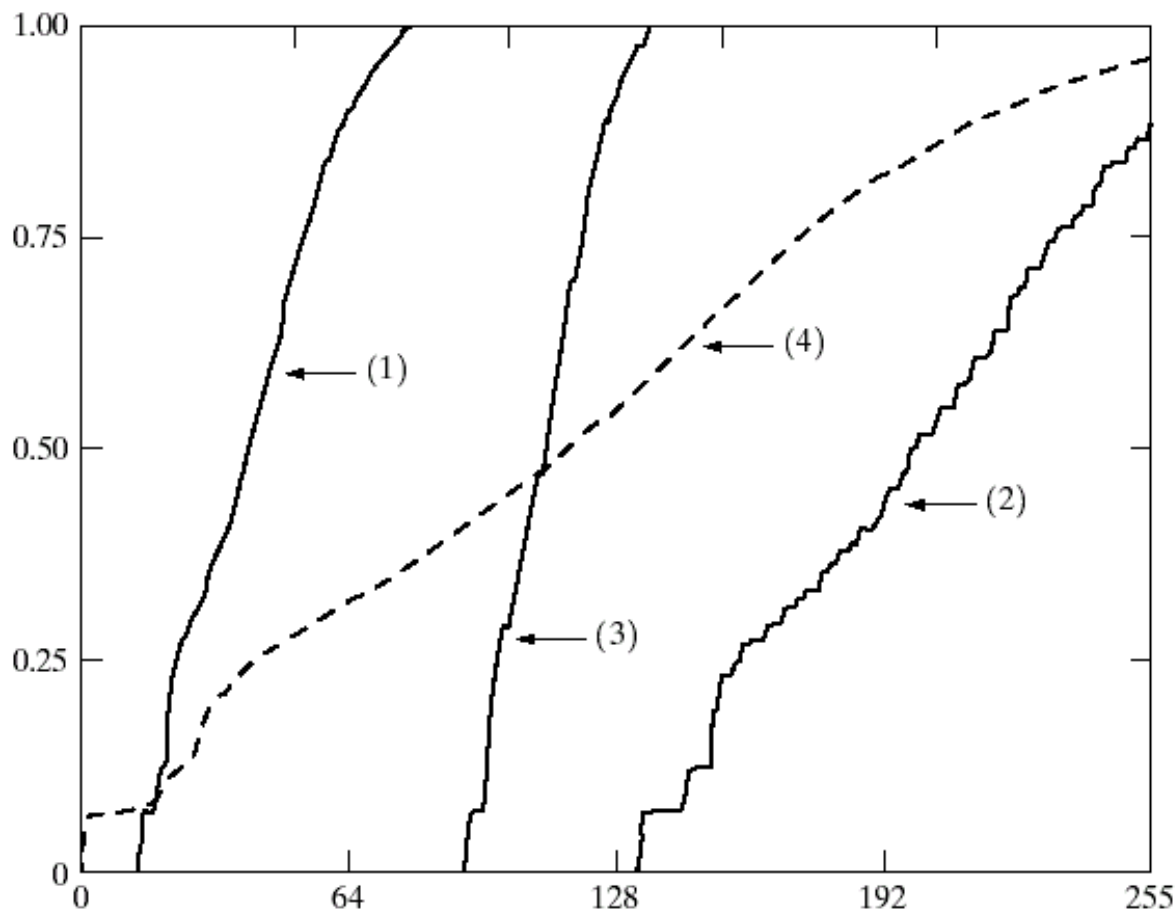


1

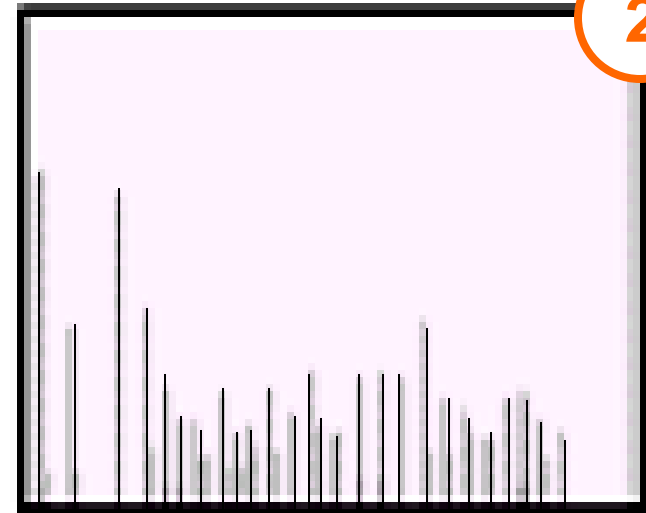
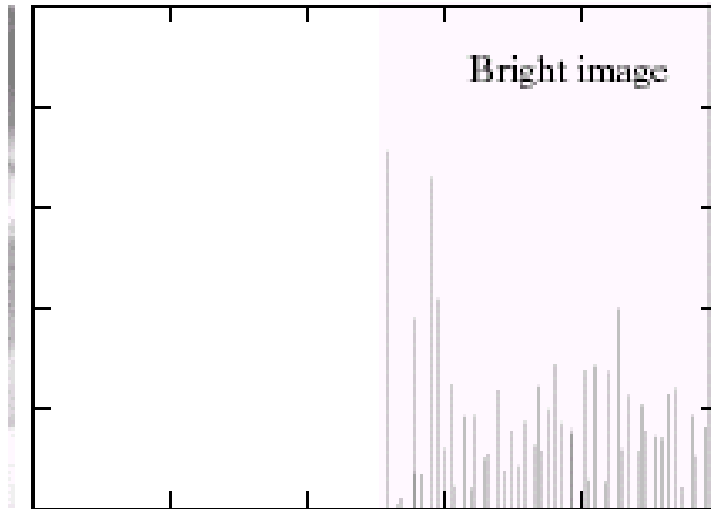


Equalisation Transformation Functions

The functions used to equalise the images in the previous example

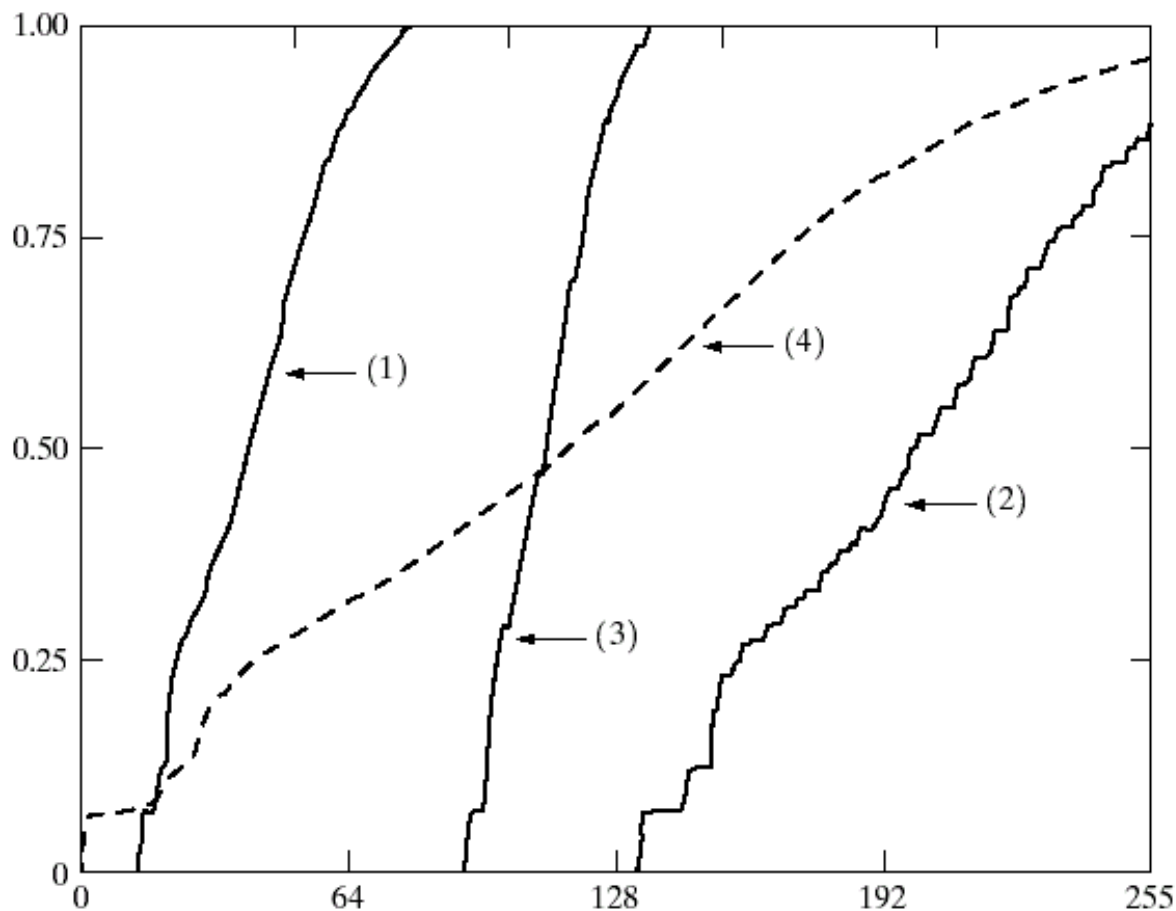


Equalisation Examples

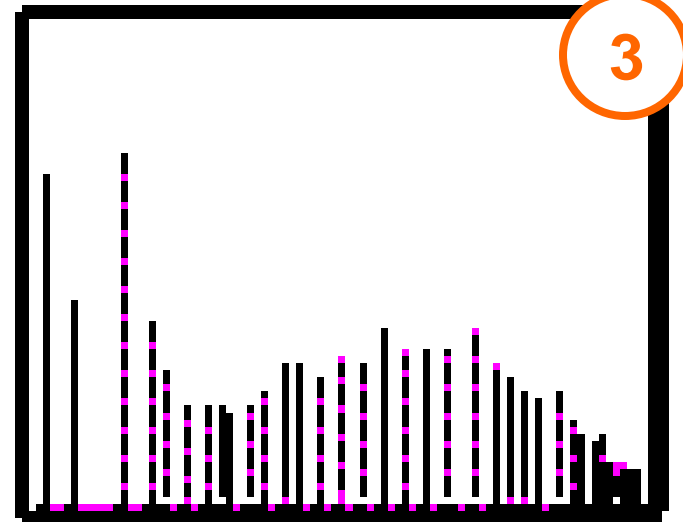
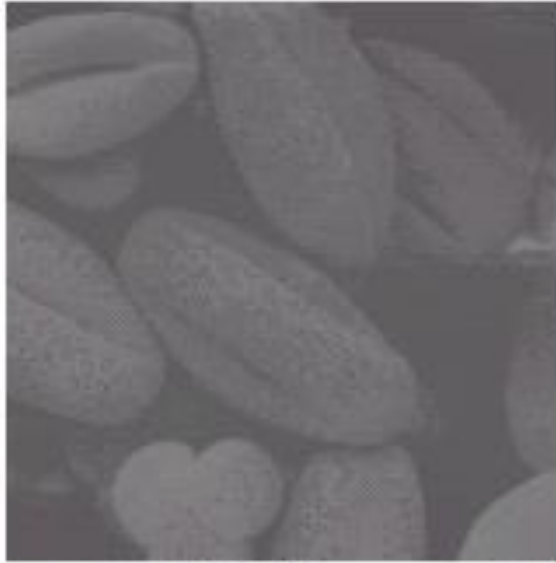


Equalisation Transformation Functions

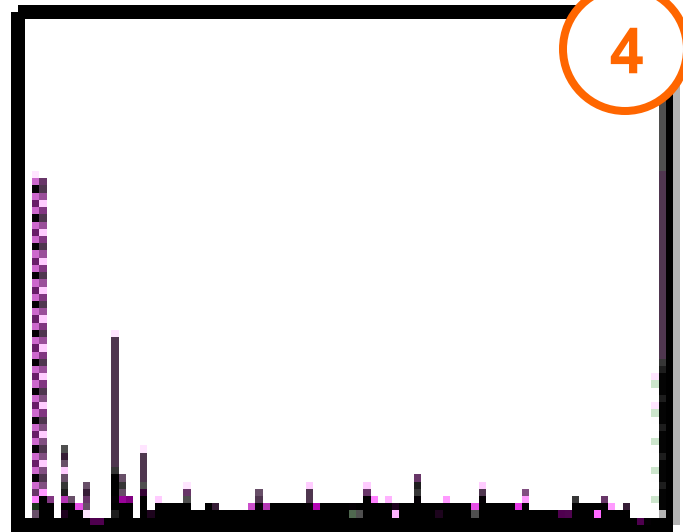
The functions used to equalise the images in the previous example



Equalisation Examples (cont...)

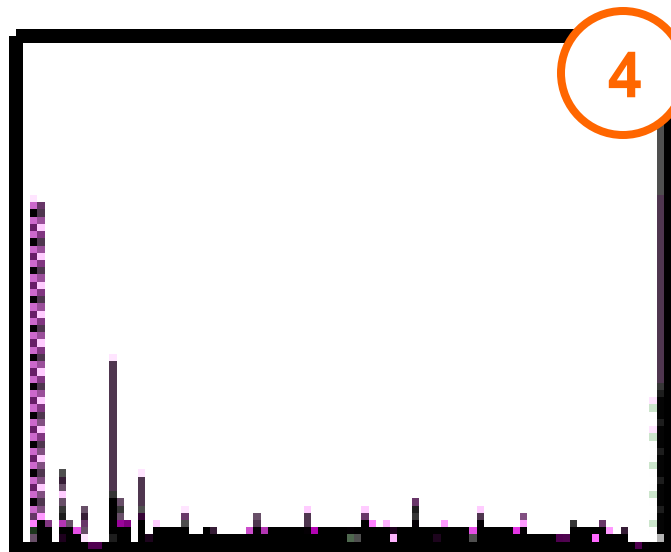
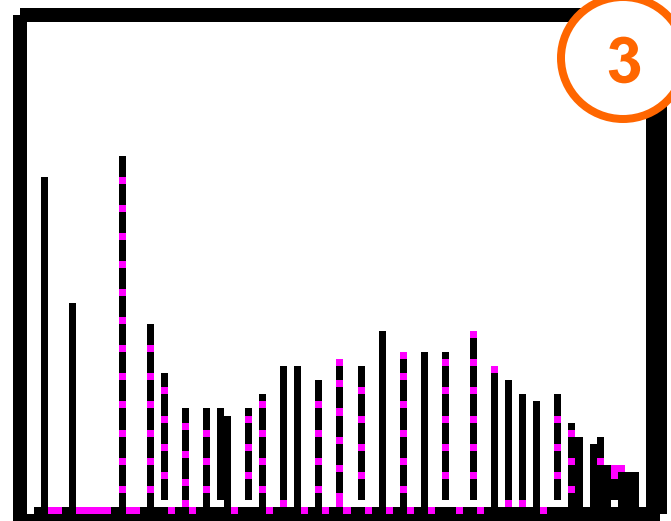
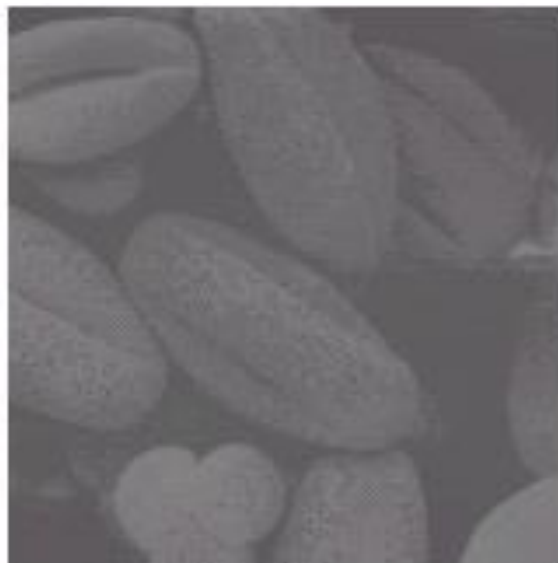


3



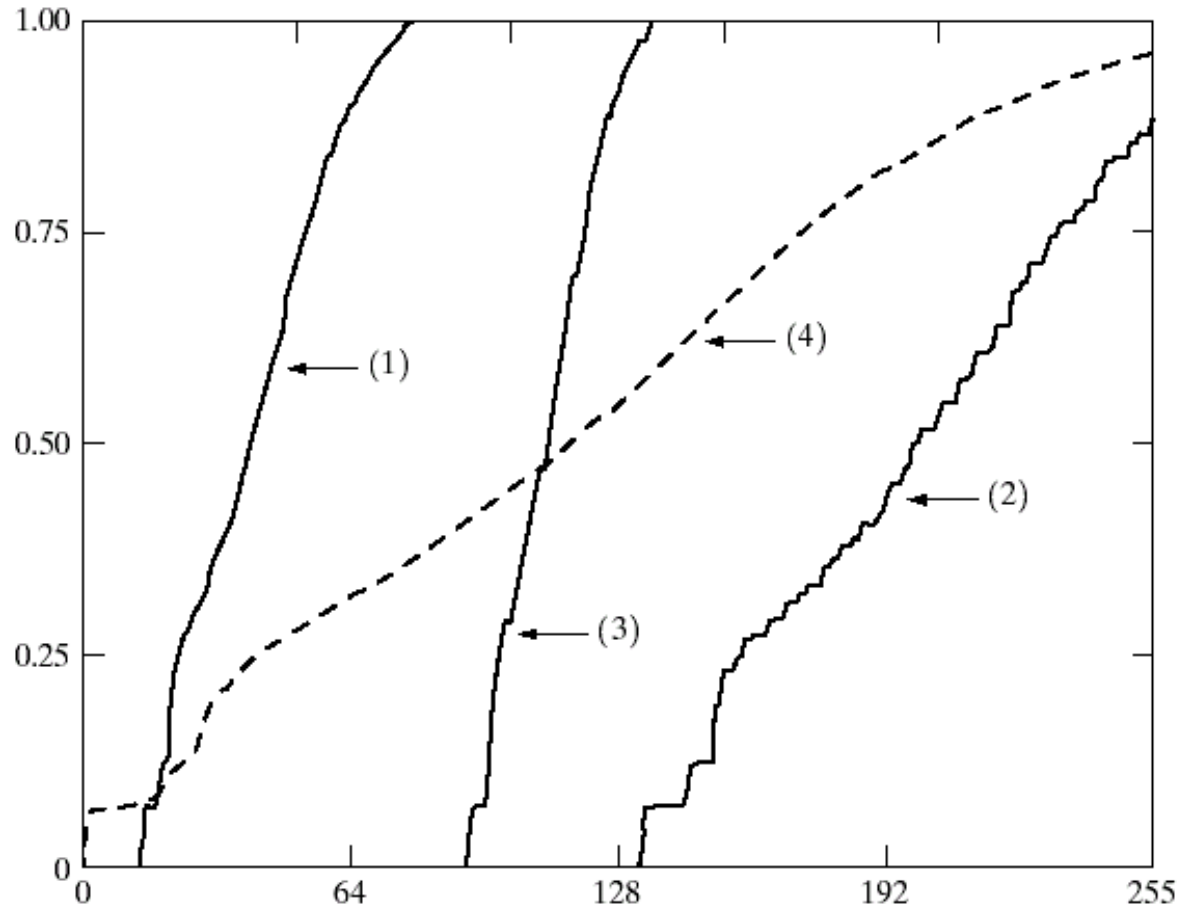
4

Equalisation Examples (cont...)

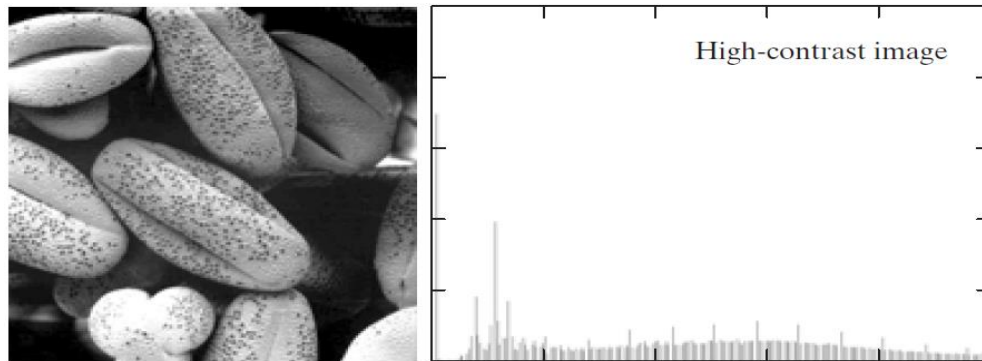
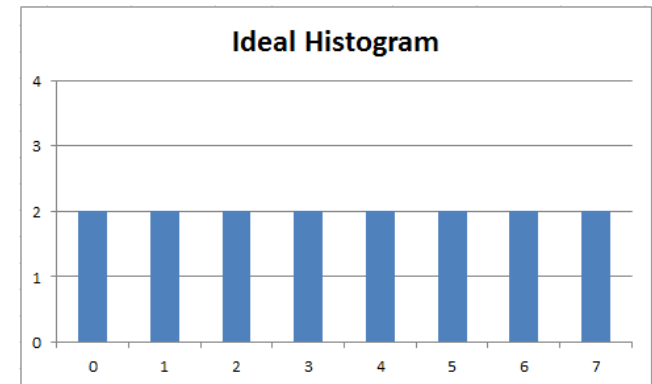
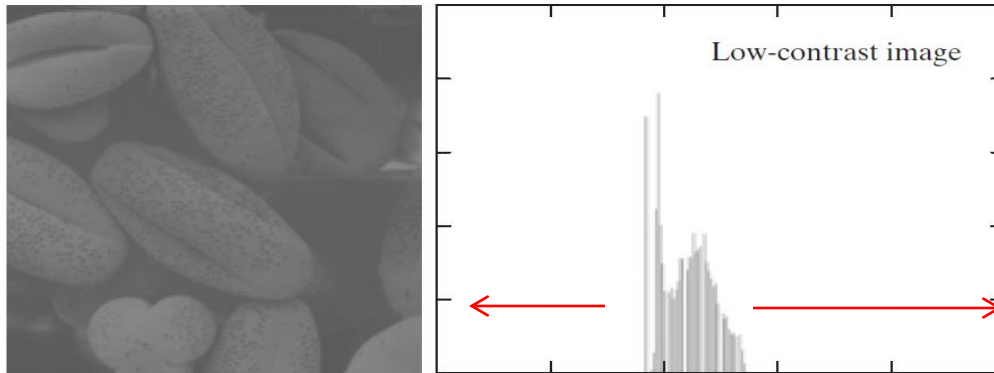


Equalisation Transformation Functions

The functions used to equalise the images in the previous examples



Histogram equalization



- Cumulative Distribution Function: $cdf(r)$ the total number of pixels with intensity up to r

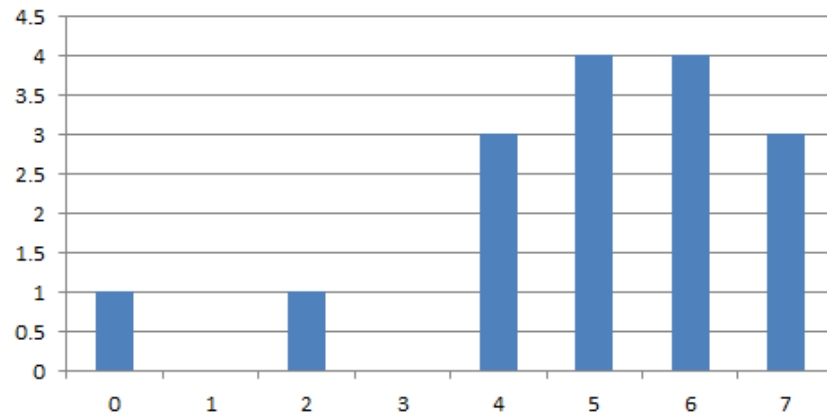
$$cdf(r) = \sum_{i=0}^r h(i)$$

- Histogram $h(r)$ the number of pixels with intensity r

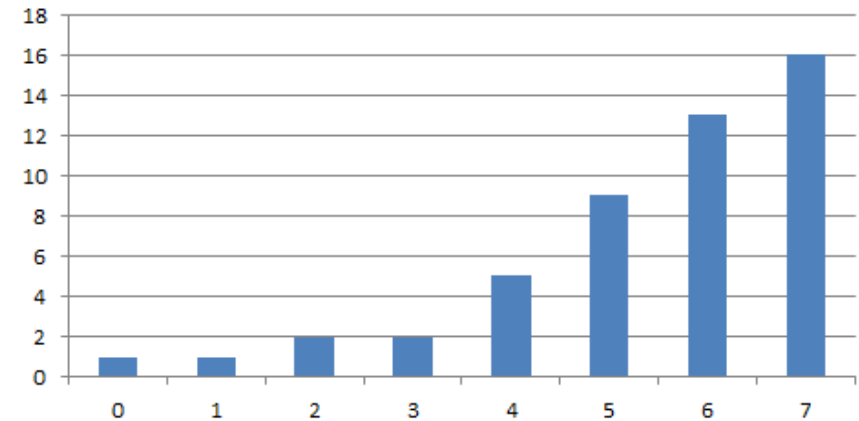
Intensity	0	1	2	3	4	5	6	7
Histogram	1	0	1	0	3	4	4	3
N.Histogram	0.0625	0	0.0625	0	0.1875	0.25	0.1875	0.25
cdf	1	1	2	2	5	9	13	16

Histogram and cumulative distribution function

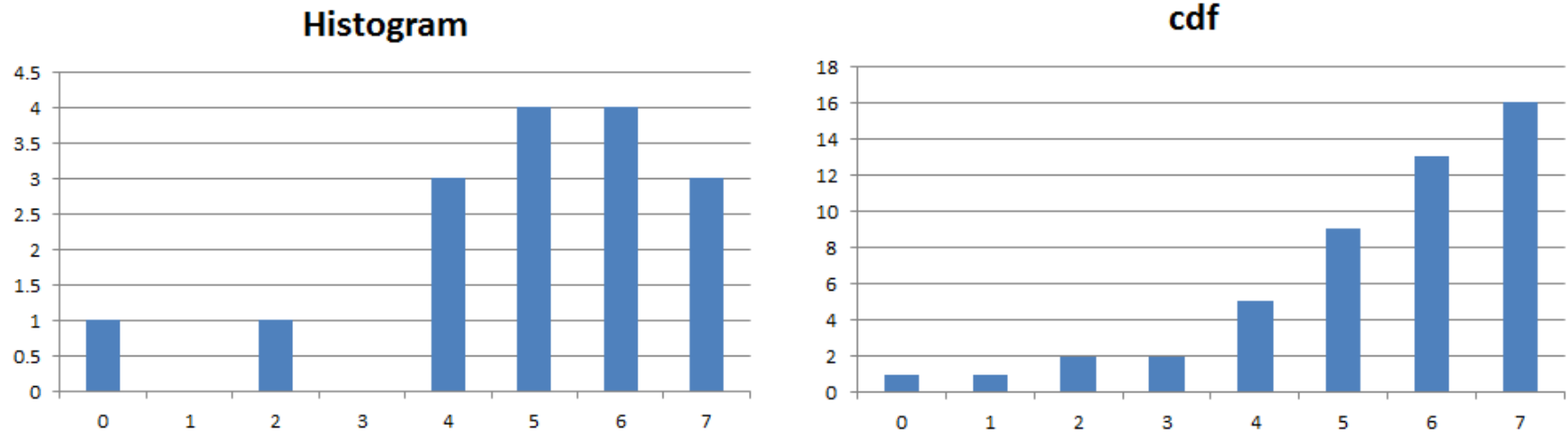
Histogram



cdf

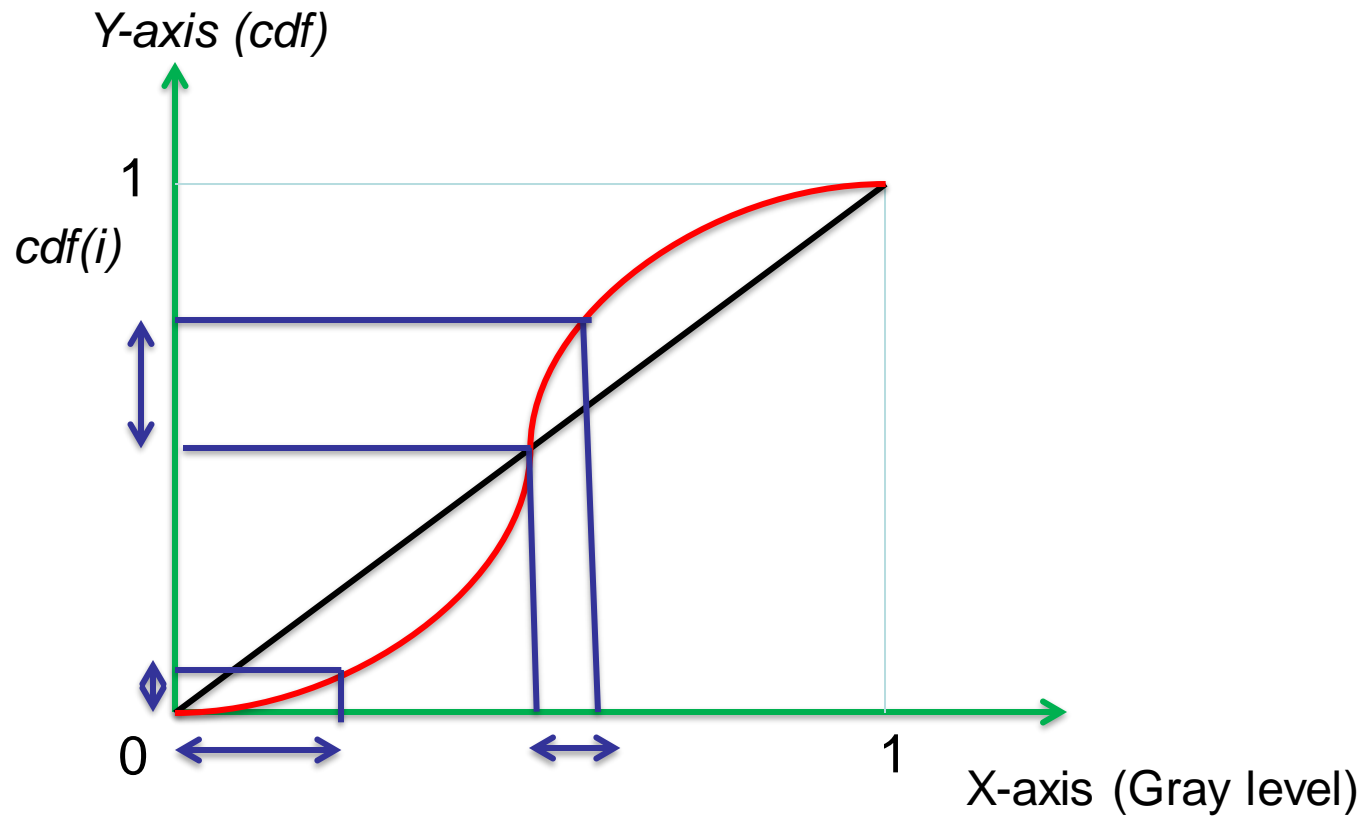


Histogram and CDF are identical



Ideal histogram \Leftrightarrow Ideal CDF

Histogram Equalization Technique



Histogram Equalization Technique

2	5	7	6
4	5	4	7
6	5	6	4
0	7	5	6

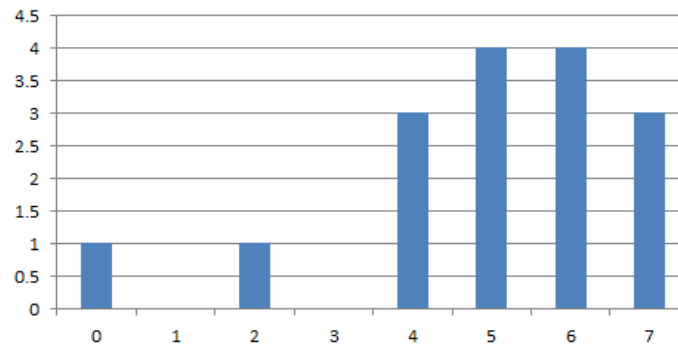
Intensity	0	1	2	3	4	5	6	7
Histogram	1	0	1	0	3	4	4	3
N.Histogram	0.0625	0	0.0625	0	0.1875	0.25	0.1875	0.25
cdf	1	1	2	2	5	9	13	16
N.cdf	0.0625	0.0625	0.125	0.125	0.3125	0.5625	0.8125	1
N.cdf*L	0.4375	0.4375	0.875	0.875	2.1875	3.9375	5.6875	7
New Intensity	0	0	1	1	2	4	6	7

Histogram Equalization Technique

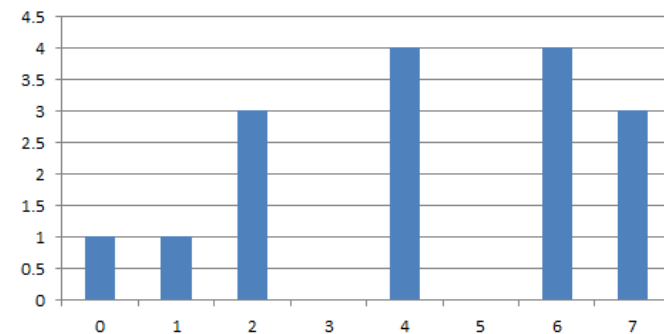
2	5	7	6
4	5	4	7
6	5	6	4
0	7	5	6

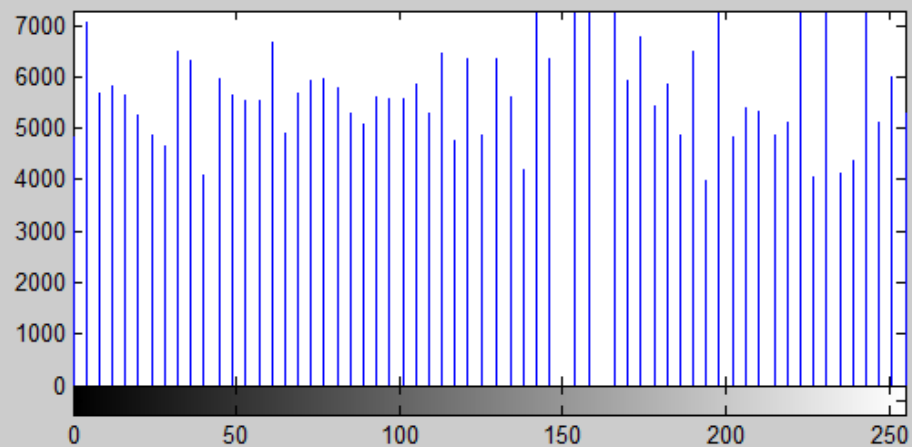
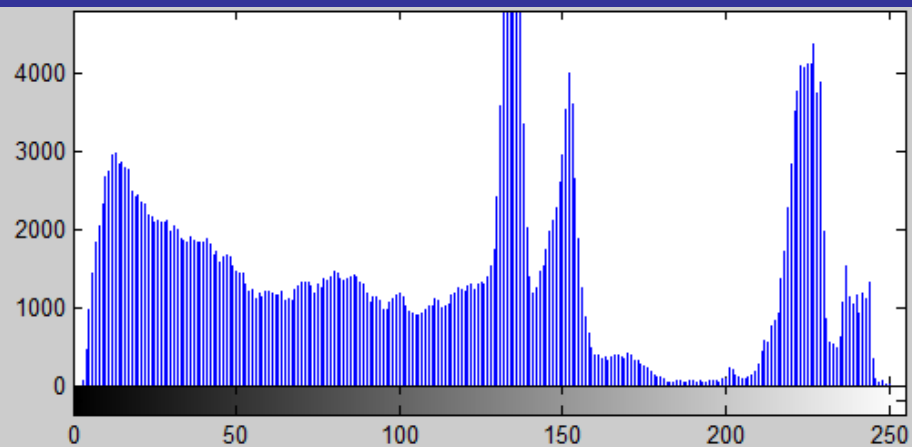
1	4	7	6
2	4	2	7
6	4	6	2
0	7	4	6

Histogram



Equalized Histogram





Thank you for your attention !