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> INT := proc(f::algebraic, x::name) local c, u, v, n, i;
  if diff(f,x) = 0 then
    return f*x;
  elif type(f, name) then
    if f=x then
      return (1/2)*x^2;
    else
      return f*x;
    fi;
  elif op(0, f) = `*` then
    c := 1;
    for i from 1 to nops(f) do
      if diff(op(i,f), x) <> 0 then
        u := op(i, f);
        v := subsop(i=1, f);
        break;
      fi
    od;

    for i from 1 to nops(v) do
      if type(op(i,v), numeric) then
        c:= op(i, v);
        v := subsop(i=1, v);
        break;
      fi
    od;

    if u = x and v = exp(x) then
      return c*(u*v - v)
    elif op(0, u) = `^` and v = exp(x) then
      n := op(2, u);
      v := op(2,f);
      return c*(u*v - n * INT(x^(n-1)*v, x));
    elif op(0, u) = `^` and op(0, v) = ln then
      return c*(INT(u, x)*v - INT(INT(u, x)*diff(v, x), x)
);
    else
      return c* v * INT(u, x);
    fi;

  elif op(0, f) = `+` then
    return INT(op(1,f), x) + INT(f-op(1,f), x);

  elif op(0, f) = `^` and op(1, f) = x and diff(op(2,f), x) = 0
then
    c := op(2,f);
    if c = -1 then
      return ln(op(1,f));
    else
      return 1/(c+1)*x^(c+1);
    fi;

  elif op(0, f) = exp then
    u := op(1,f);
    if u = x then
      return exp(x);

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    elif type(op(1,u), numeric) then
        return exp(x)*(1/op(1, u));
    fi;

    elif op(0, f) = ln and diff(op(1,f), x) <> 0 then
        u := op(1,f);
        c := lcoeff(u);
        return (1/c)*op(1,f)*(ln(op(1,f)) - 1);
    else return 'INT'(f, x);
    fi;
end:

```

```
> INT( x^2 + 2*x + 1, x );
```

$$\frac{1}{3}x^3 + x^2 + x \quad (1)$$

```
> INT( x^(-1) + 2*x^(-2) + 3*x^(-1/2), x );
```

$$\frac{1}{x^2}, 1$$

$$\frac{1}{\sqrt{x}}, 1$$

$$\ln(x) - \frac{2}{x} + 6\sqrt{x} \quad (2)$$

```
> INT( exp(x) + ln(x) + sin(x), x );
```

$$e^x + x(\ln(x) - 1) + \text{INT}(\sin(x), x) \quad (3)$$

```
> INT( 2*f(x) + 3*y*x/2 + 3*ln(2), x );
```

$$2 \text{INT}(f(x), x) + \frac{3yx^2}{4} + 3x \ln(2) \quad (4)$$

```
> INT( x^2*exp(x) + 2*x*exp(x), x );
```

$$x^2 e^x \quad (5)$$

```
> INT( 2*exp(-x) + ln(2*x+1), x );
```

$$-2e^x + \frac{(2x+1)(\ln(2x+1) - 1)}{2} \quad (6)$$

```
> INT( 4*x^3*ln(x) + 3*x^2*ln(x), x );
```

$$x^4 \ln(x) - \frac{x^4}{4} + x^3 \ln(x) - \frac{x^3}{3} \quad (7)$$