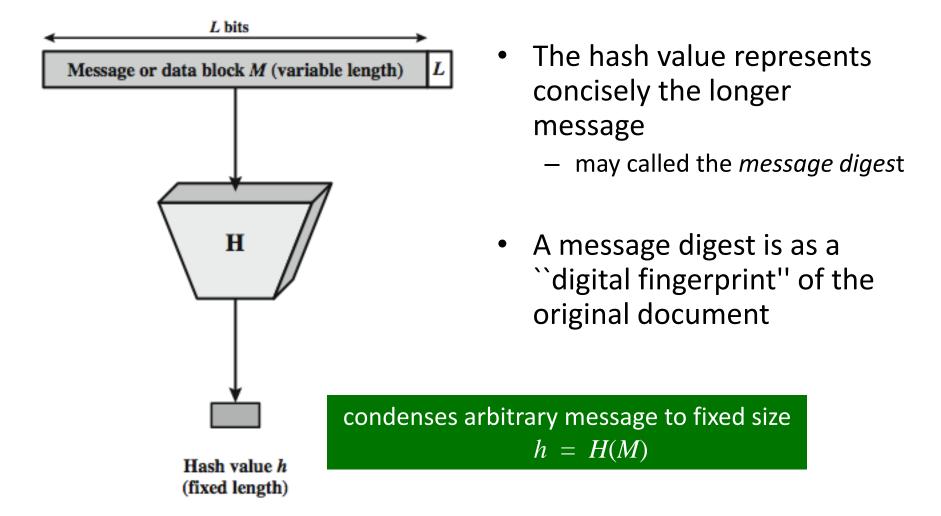


Hash Functions

BSCH4-NS
Jason Farina
Jason.farina@griffith.ie



Hash Function



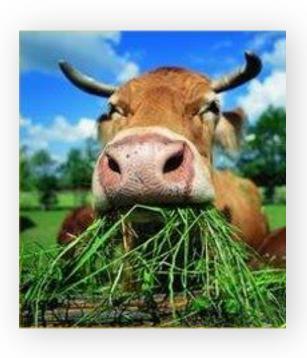


- A file hash is an algorithm that encodes a variable length message to a fixed length string.
- ABCDEFGHIJKLMNOPQRSTUVWXYZ => A
- INFOSEC IS FUN => B
- Wheeeeeee! => C
- Given the ciphertext (A, B or C) we have no way to know how long the original plaintext message was.



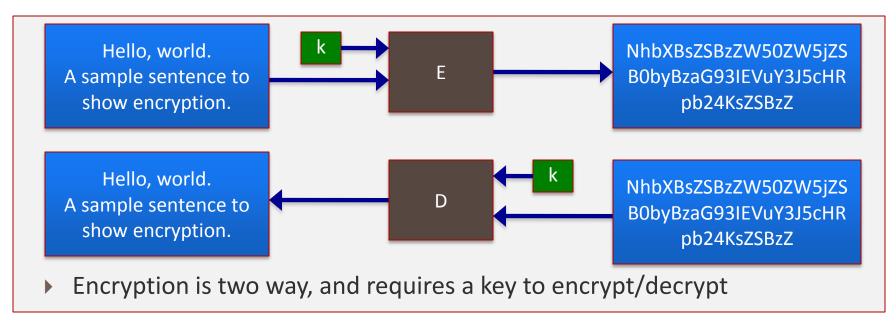
Chewing functions

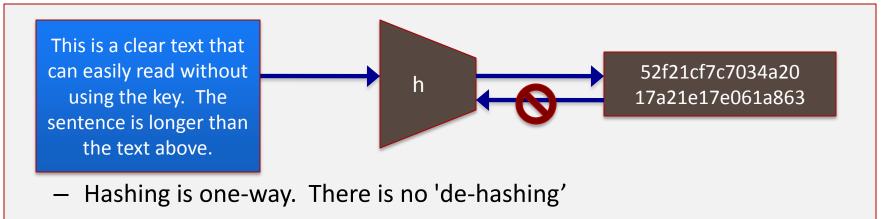
▶ Hashing function as "chewing" or "digest" function





GRIFFITH COLLEGE Hashing V.S. Encryption





Motivation for Hash Algorithms

Intuition

- Re-examine the non-cryptographic checksum
- Main Limitation
 - An attack is able to construct a message that matches the checksum

Goal

- Design a code where the original message can not be inferred based on its checksum
- such that an accidental or intentional change to the message will change the hash value

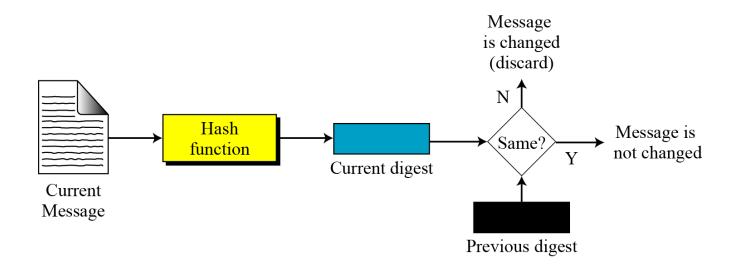


Hash Function Applications

- Used Alone
 - Fingerprint -- file integrity verification, public key fingerprint
 - Password storage (one-way encryption)
- Combined with encryption functions
 - Message Authentication Code (MAC)
 - protects both a message's integrity as well as its authenticity
 - Digital signature
 - Ensuring Non-repudiation
 - Encrypt hash with private (signing) key and verify with public (verification) key



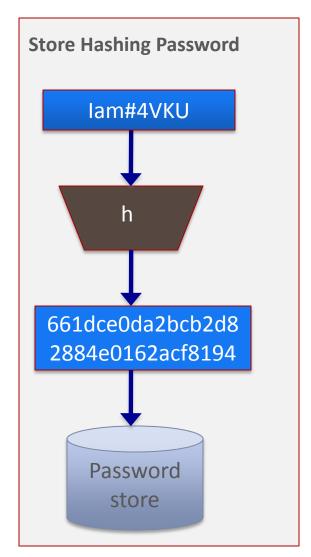
Integrity

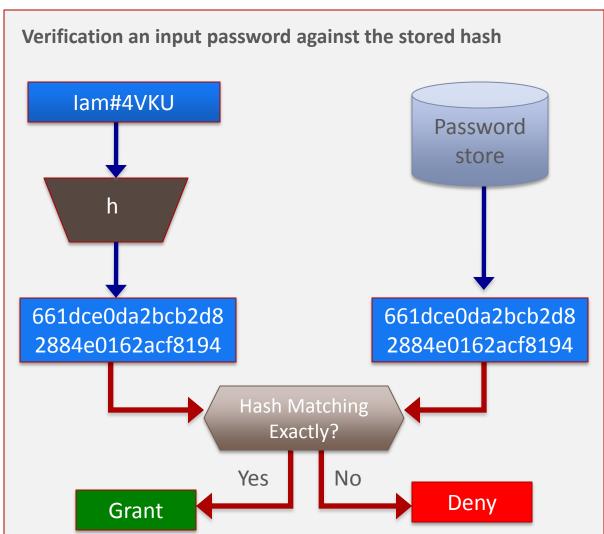


- to create a one-way password file
 - store hash of password not actual password
- for intrusion detection and virus detection
 - keep & check hash of files on system



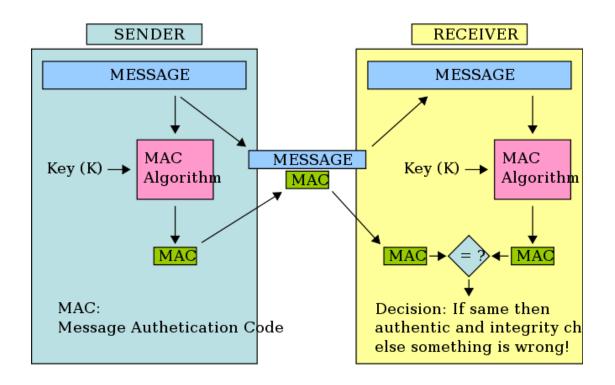
Password Verification







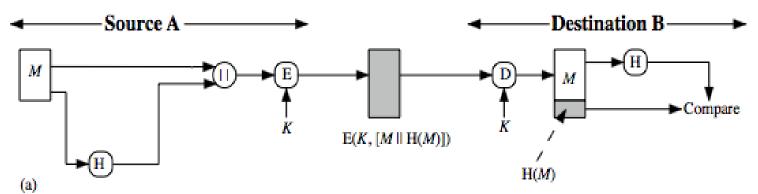
Authentication



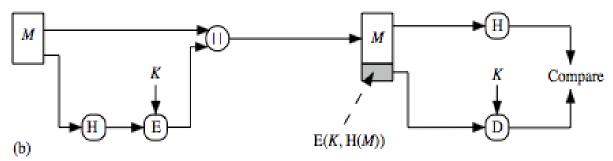
 protects both a message's integrity as well as its authenticity, by allowing verifiers (who also possess the secret key) to detect any changes to the message content



Hash Function Usages (I)



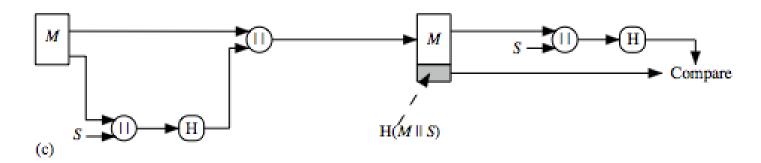
Message encrypted: Confidentiality and authentication



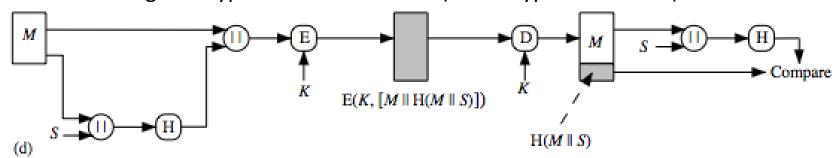
Message unencrypted: Authentication



Hash Function Usages (II)



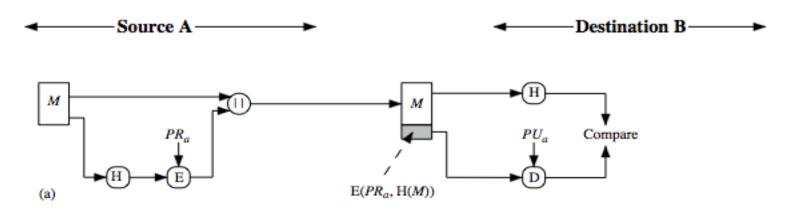
Message encrypted: Authentication (no encryption needed!)



Message unencrypted: Authentication, confidentiality



Hash Function Usages (III)



Authentication, digital signature

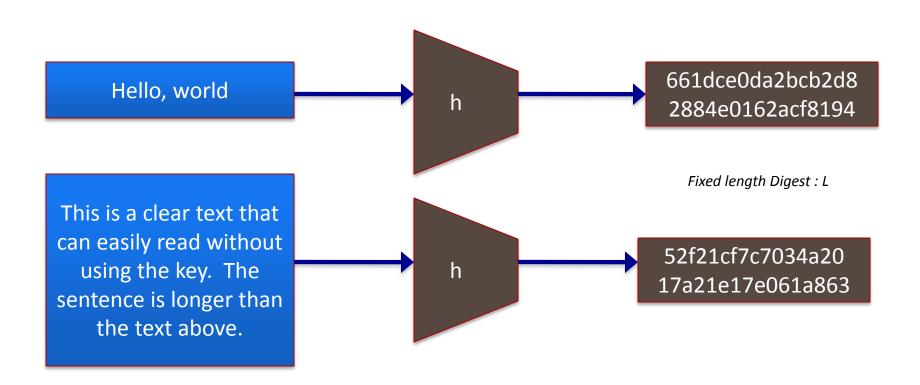


Authentication, digital signature, confidentiality



- Common properties
- Deterministic: the same input should produce the same output regardless of the system it is being run on.
- Collision resistant: for any given message (m) there should not exist m1 such that h(m) = h(m1)
- Given H(m) it should be realistically impossible to determine m
- Any change in m should change the value of h(m)

Properties: Fixed length



Arbitrary-length message to fixed-length digest



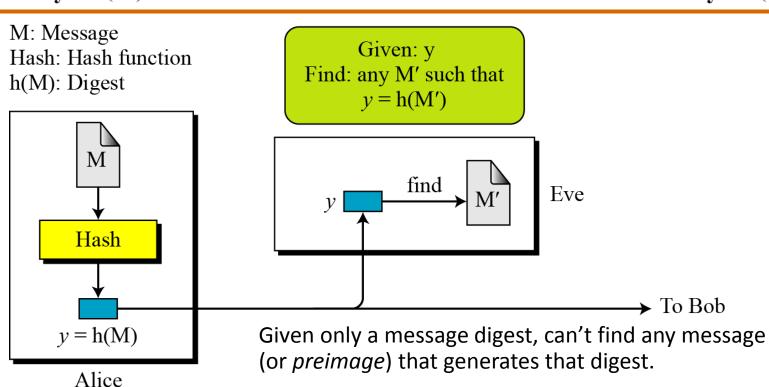
Preimage resistant

- This measures how difficult to devise a message which hashes to the known digest
- Roughly speaking, the hash function must be one-way.

Preimage Attack

Given: y = h(M)

Find: M' such that y = h(M')





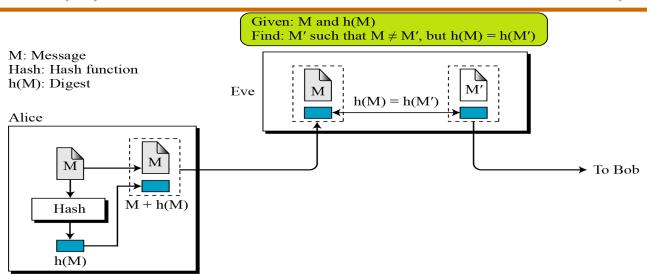
Second preimage resistant

This measures how difficult to devise a message which hashes to the known digest and its message

Second Preimage Attack

Given: M and h(M)

Find: $M' \neq M$ such that h(M) = h(M')



- Given one message, can't find another message that has the same message digest. An attack that finds a second message with the same message digest is a second pre-image attack.
 - It would be easy to forge new digital signatures from old signatures if the hash function used weren't second preimage resistant



Collision Resistant

Collision Attack

Given: none

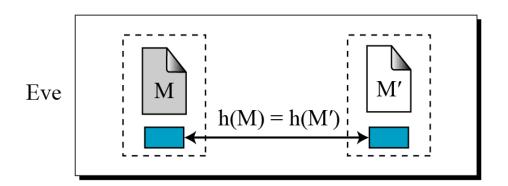
Find: $M' \neq M$ such that h(M) = h(M')

M: Message

Hash: Hash function

h(M): Digest

Find: M and M' such that $M \neq M'$, but h(M) = h(M')



- Can't find any two different messages with the same message digest
 - Collision resistance implies second preimage resistance
 - Collisions, if we could find them, would give signatories a way to repudiate their signatures

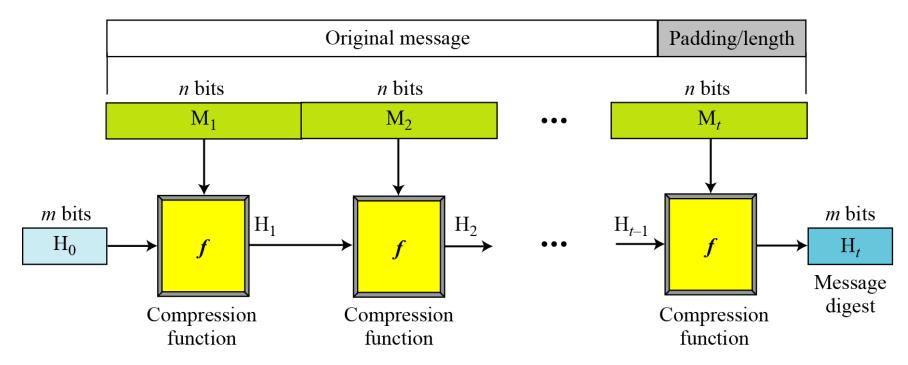


- MD5: Message digest5 takes an input of arbitrary length and produces a 128bit output (16 bytes usually represented by 32 Hex characters)
- DOG = b0e603b215aa2da0e6c605301d79efe4
- CAT = c01ae1a5f122f25ce5675f86028b536a
- dog = 06d80eb0c50b49a509b49f2424e8c805
- canis canem=02a35181a31072d1ac0436572ca77abe



- canis canem=02a35181a31072d1ac0436572ca77abe
- canis caneM = 0c89f84deee731b74615d536dd7dabd4
- A minor change in the plaintext results in a drastic change to the message digest.
- Online tools such as: http://www.md5.cz/
- Offline such as md5sum, command line utility for windows or *nix
- Note: the DATA section of a file is hashed, NOT the system metadata.

GRIFFITH COLLEGE Merkle-Damgard Scheme



- Well-known method to build cryptographic has function
- A message of arbitrary length is broken into blocks
 - length depends on the compression function f
 - padding the size of the message into a multiple of the block size.
 - sequentially process blocks, taking as input the result of the hash so far and the current message block, with the final fixed length output

GRIFFITH COLLEGE WO Group of Compression

- Functions
 The compression function is made from scratch
 - Message Digest

- A symmetric-key block cipher serves as a compression function
 - Whirlpool



Hash Functions Family

- MD (Message Digest)
 - Designed by Ron Rivest
 - Family: MD2, MD4, MD5
- SHA (Secure Hash Algorithm)
 - Designed by NIST
 - Family: SHA-0, SHA-1, and SHA-2
 - SHA-2: SHA-224, SHA-256, SHA-384, SHA-512
 - SHA-3: New standard in competition
- RIPEMD (Race Integrity Primitive Evaluation Message Digest)
 - Developed by Katholieke University Leuven Team
 - Family: RIPEMD-128, RIPEMD-160, RIPEMD-256, RIPEMD-320,

GRIFFITH COLLEGIMD5, SHA-1, and RIPEMD-160

Digest length
Basic unit of processing
Number of steps
Maximum message size
Primitive logical functions
Additive constants used
Endianness

MD5	SHA-1	RIPEMD-160		
128 bits	160 bits	160 bits		
512 bits	512 bits	512 bits 160 (5 paired rounds of 16)		
64 (4 rounds of 16)	80 (4 rounds of 20)			
00	2 ⁶⁴ - 1 bits	2 ⁶⁴ - 1 bits		
4	4	5		
64	4	9		
Little-endian	Big-endian	Little-endian		



MD2, MD4 and MD5

- Family of one-way hash functions by Ronald Rivest
 - All produces 128 bits hash value
- MD2: 1989
 - Optimized for 8 bit computer
 - Collision found in 1995
- MD4: 1990
 - Full round collision attack found in 1995
- MD5: 1992
 - Specified as Internet standard in RFC 1321
 - since 1997 it was theoretically not so hard to create a collision
 - Practical Collision MD5 has been broken since 2004
 - CA attack published in 2007



- MD5 is produced using 5 steps
- Step 1. Append Padding Bits

Pad the message so it becomes 448 mod 512 bits long. The pad consists of 1+0000000...000

Step 2. Append Length

The length is appended as (length of message) mod 64

Step 3. Initialize MD Buffer

Initialises to

var int a0 := 0x67452301 //A

var int b0 := 0xefcdab89 //B

var int c0 := 0x98badcfe //C

var int d0 := 0x10325476 //D

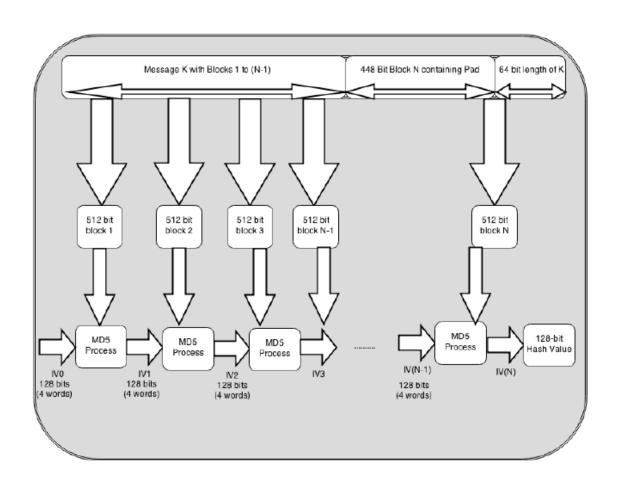
Step 4. Process Message in 16-Word Blocks

Each word is 32 bits giving each message block 512 bits long.

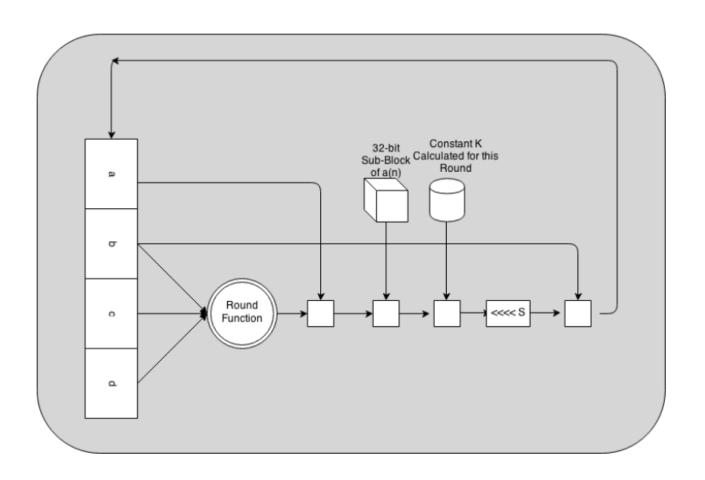
Step 5. Output

Outputs a single 128bit value that becomes the MD buffer for the next round



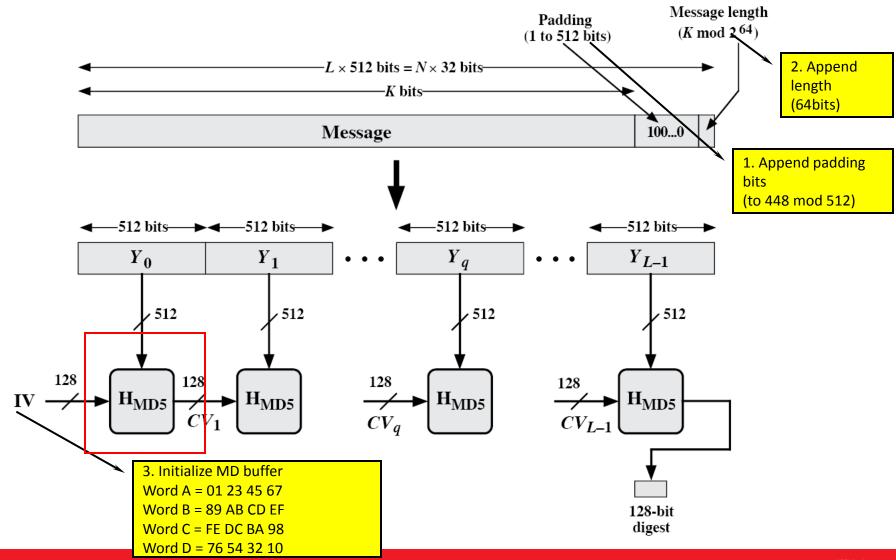


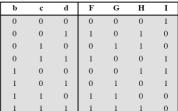




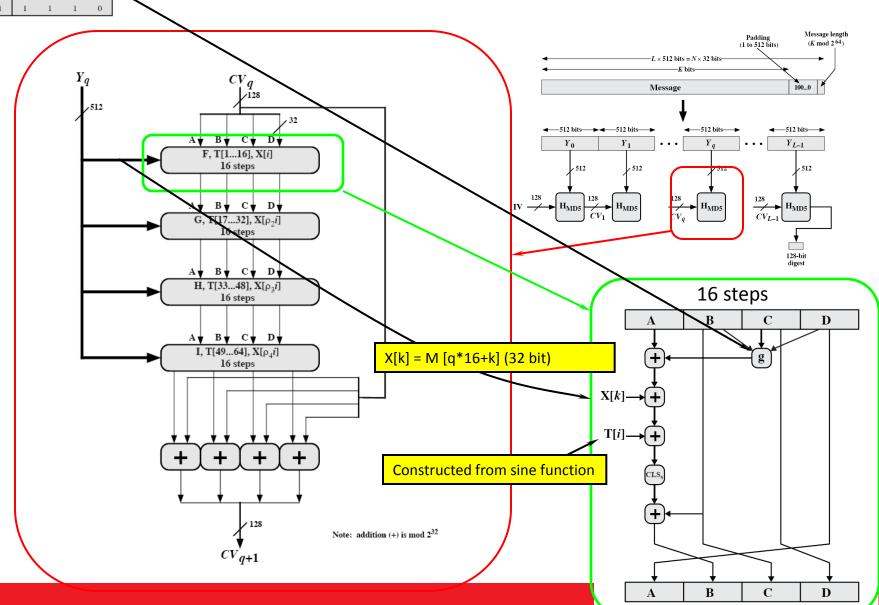


MD5 Overview





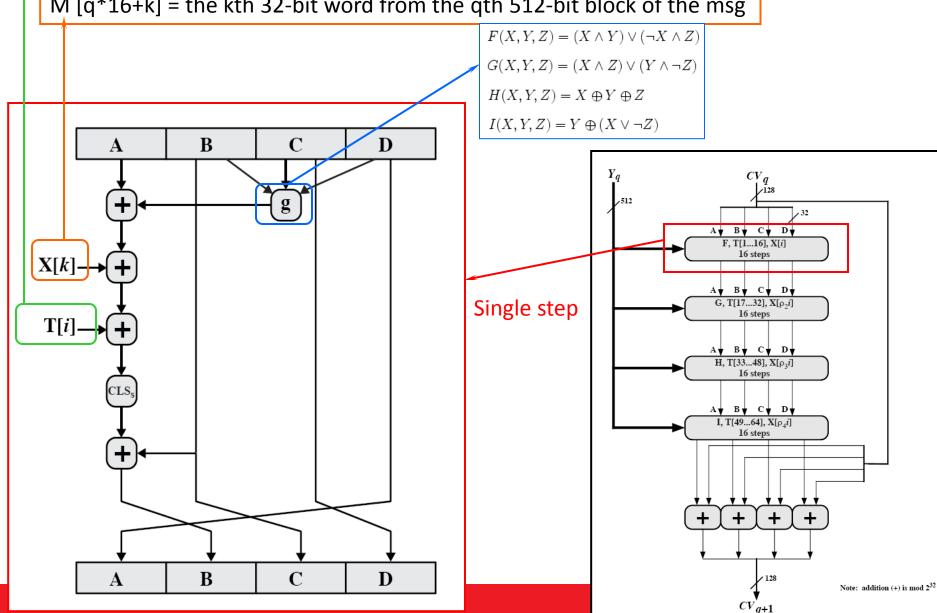
Hash Algorithm Design — MD5



he ith 32-bit word in matrix T, constructed from the sine function

GRIFFITH COLLEGE

M [q*16+k] = the kth 32-bit word from the qth 512-bit block of the msg





Advantages: fast to compute
 Still accepted as legal evidence in court.

Disadvantages:

Broken. Collisions can be generated.

Modern computing power enables brute force matching (theoretically)

```
C5 e6
                              40
   ad 34
           06 09 f4
                                     88
   51 25 e8 f7
                          9f
                                     bd
                                 1d
   82 3e 31 56
                  34
                          5b
                                 6d
                                     ac
                                     63
                 57
                      7e
                          e8
                                     b6
                              ce
                                 54
       21 bc b6 a8 83
                          93
                              96
                                 £9
Input vector 2:
                                     88
          e8 f7
                  cd
                      c9
                                 1d
                                     bd
      3e 31
              56
                  34
                          5b
                              ae
                                     ac
                                         d4
```

Identical MD5 value, verified with WinHex: 79054025255fb1a26e4bc422aef54eb4



Secure Hash Algorithm

- > SHA originally designed by NIST & NSA in 1993
- was revised in 1995 as SHA-1
- > US standard for use with DSA signature scheme
 - standard is FIPS 180-1 1995, also Internet RFC3174
- based on design of MD4 with key differences
- produces 160-bit hash values
- recent 2005 results on security of SHA-1 have raised concerns on its use in future applications



Revised SHA

- ➤ NIST issued revision FIPS 180-2 in 2002
- > adds 3 additional versions of SHA
 - •SHA-256, SHA-384, SHA-512
- designed for compatibility with increased security provided by the AES cipher
- > structure & detail is similar to SHA-1
- hence analysis should be similar
- > but security levels are rather higher



SHA Versions

	SHA-1	SHA-224	SHA-256	SHA-384	SHA-512
Digest size	160	224	256	384	512
Message size	< 2 ⁶⁴	< 2 ⁶⁴	< 2 ⁶⁴	< 2 ¹²⁸	< 2 ¹²⁸
Block size	512	512	512	1024	1024
Word size	32	32	32	64	64
# of steps	80	64	64	80	80



 Sha-1 is currently the least secure cryptographic hash function supported by NIST

_	orithm and variant	Output size (bits)	Internal state size (bits)	Block size (bits)	Max message size (bits)	Rounds	Operations	Security (bits)	Example Performance (MiB/s) ^[45]
MD5 (as reference)	128	128 (4×32)	512	2 ⁶⁴ – 1	64	add mod 232, and, or, xor, rot	<64 (collisions found)	335
	SHA-0	160	160 (5×32)	512	2 ⁶⁴ – 1	80	add mod 232, and, or, xor, rot	<80 (collisions found)	-
,	SHA-1	160	160 (5×32)	512	2 ⁶⁴ – 1	80	add mod 232, and, or, xor, rot	<80 (theoretical attack ^[46] in 2 ⁵¹)	192
SHA-2	SHA-224 SHA-256	224 256	256 (8×32)	512	2 ⁸⁴ – 1	64	add mod 232, and, or, xor, shr, rot	112 128	139
	SHA-384 SHA-512 SHA-512/224 SHA-512/256	384 512 224 256	512 (8x64)	1024	2 ¹²⁸ – 1	80	add mod 2°4, and, or, xor, shr, rot	192 256 112 128	154
SHA-3	SHA3-224 SHA3-256 SHA3-384 SHA3-512 SHAKE128 SHAKE256	224 256 384 512 d (arbitrary) d (arbitrary)	1600 (5×5×64)	1152 1088 832 576 1344 1088	ou.	24	and, xor, not, rot	112 128 192 256 min(d/2, 128) min(d/2, 256)	



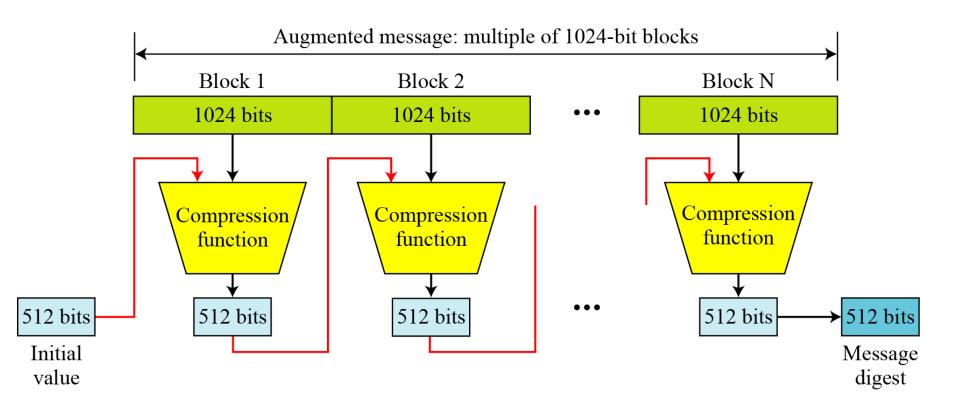
Sample Processing

Type	bits	data processed
md5	128	469.7MB/s
sha1	160	339.4MB/s
sha512	512	177.7MB/s

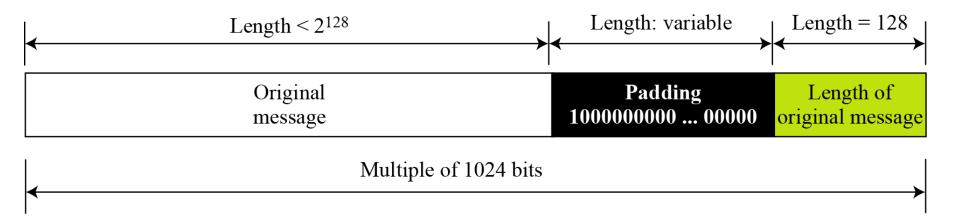
- Mac Intel 2.66 Ghz core i7
- 1024 bytes block of data



SHA-512 Overview



GRIFFITH ackning and length field in SHA-512



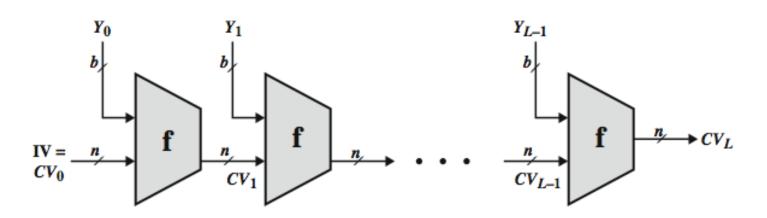
- What is the number of padding bits if the length of the original message is 2590 bits?
- We can calculate the number of padding bits as follows:

$$|P| = (-2590 - 128) \mod 1024 = -2718 \mod 1024 = 354$$

The padding consists of one 1 followed by 353 0's.

GRIFFITH COLLEGE ASh Function Cryptanalysis

- ryptanalytic attacks exploit some property of alg so faster than exhaustive search
- hash functions use iterative structure
 - process message in blocks (incl length)
- right attacks focus on collisions in function f





Attacks on Hash Functions

- ➤ have brute-force attacks and cryptanalysis
- > a preimage or second preimage attack
 - ullet find y s.t. H(y) equals a given hash value
- > collision resistance
 - find two messages x & y with same hash so H(x) = H(y)



Birthday Attack

- How many people do you need so that the probability of having two of them share the same birthday is > 50%?
- N distinct values, k randomly chosen ones
 - P(N,i) = prob(i randomly selected values from 1..N have at least one match)
 - P(N,2) = 1/N
 - P(N,i+1) = P(N,i)+(1-P(N,i))(i/N)
- For P(N,k)>0.5, need $k \approx N^{1/2}$
- For m bits hash code, hence value $2^{m/2}$ determines strength of hash code against brute-force attacks
 - 128-bits inadequate, 160-bits suspect



Definition

Birthday attacks are a class of brute-force techniques that target the cryptographic hash functions. The goal is to take a cryptographic hash function and find two different inputs that produce the same output.



The Birthday Problem

What is the probability that at least two of *k* randomly selected people have the same birthday? (Same month and day, but not necessarily the same year.)



The Birthday Paradox

How large must *k* be so that the probability is greater than 50 percent?

The answer is 23

It is a paradox in the sense that a mathematical truth contradicts common intuition.



Birthday paradox

- What's the chances that two people in a class of 43 have the same birthday?
- Approximate solution:

$$p = 1 - e^{\frac{-k^2}{2N}} = 1 - e^{\frac{-43^2}{2*365}} \approx 0.92$$

Where k = 43 people, and N = 365 choices



Birthday Calendar Wall

Equivalence to our hashing space

Jan	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
Feb	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28			
Mar	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
Apr	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
May	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
Jun	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
Jul	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
Aug	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
Sep	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
Oct	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
Nov	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
Dec	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31

GRIFFITH COLCEA COLLINIA THE Probability-1

- Assumptions
 - Nobody was born on February 29
 - People's birthdays are equally distributed over the other 365 days of the year

GRIFFITH COLCAICULating the Probability-2

In a room of k people

q: the prob. all people have different birthdays

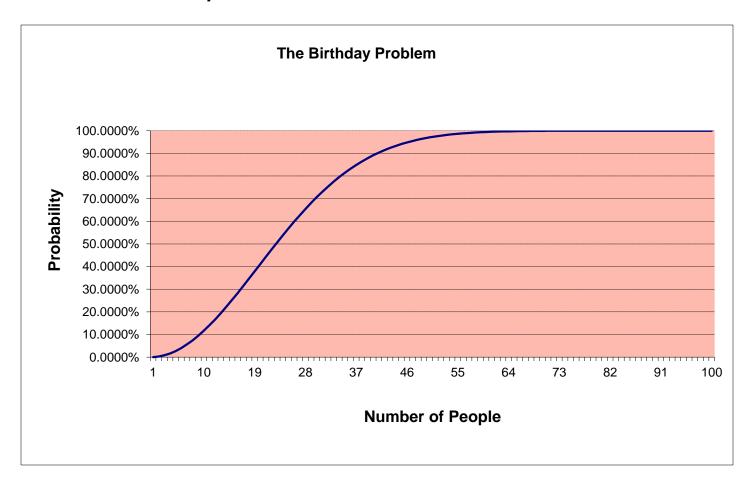
$$q = \frac{365}{365} \cdot \frac{364}{365} \cdot \frac{363}{365} \cdot \frac{362}{365} \cdot \dots \frac{365 - (k-1)}{365}$$
$$q = \frac{365!/(365 - k)!}{365^k}$$

p: the prob. at least two of them have the same birthdays

$$p=1-q=0.5 \Rightarrow k=23$$



Shared Birthday Probabalities





Attack Prevention

The important property is the length in bits of the message digest produced by the hash function.

If the number of *m* bit hash , the cardinality *n* of the hash function is

$$n = 2^{m}$$

The 0.5 probability of collision for m bit hash, expected number of operation k before finding a collision is very close to

$$k \approx \sqrt{n} = 2^{m/2}$$

m should be large enough so that it's not feasible to compute hash values!!!

he need of new Hash standard

- ➤ MD5 and SHA-0 already broken
- ➤ SHA-1 not yet fully "broken"
 - but similar to broken MD5 & SHA-0
 - so considered insecure and be fade out
- >SHA-2 (esp. SHA-512) seems secure
 - shares same structure and mathematical operations as predecessors so have concern
- ➤ NIST announced in 2007 a competition for the SHA-3 next gen hash function
 - goal to have in place by 2012



SHA-3 Requirements

- replace SHA-2 with SHA-3 in any use
 - so use same hash sizes
- preserve the nature of SHA-2
 - so must process small blocks (512 / 1024 bits)
- evaluation criteria
 - security close to theoretical max for hash sizes
 - cost in time & memory
 - characteristics: such as flexibility & simplicity



COLLISION IMPROVEMENTS

Rogue CA construction (<2048 bits)

- Cluster of 215 PlayStation3s
 - Performing like 8600 pc cores
- Complexity 2⁵⁰ using 30GB:
 - 1 day on cluster
- Complexity 2^{48.2} using a few TBs:
 - 1 day on 20 PS3s and 1 pc
 - 1 day on 8 NVIDIA GeForce GTX280s
 - 1 day on Amazon EC2 at the cost of \$2,000
- Normal CPC
 - Complexity approx. 2³⁹ (<1 day on quadcore pc)





MD5 Breakers

- Xiaoyun Wang (China)
 - collisions for MD5 in 2004
 - in a few hours on a big computer

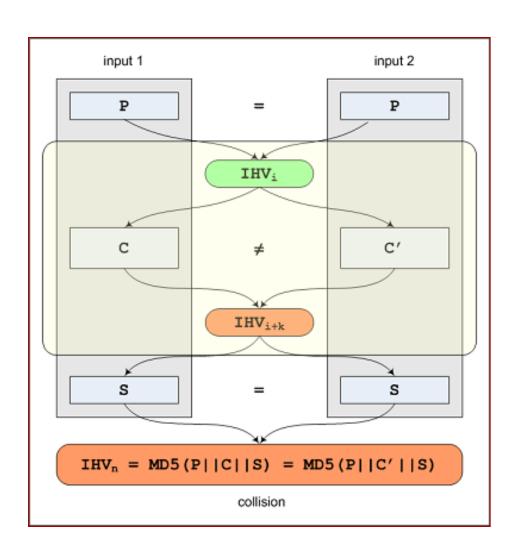


- Marc Stevens (Amsterdam)
 - MSc thesis 2007, TU/e
 - improved method, fully automated
 - collisions can now be found in about 1 second on a standard laptop





GRIFFITH COLLEGE Wang's Collisions: Identical Prefix

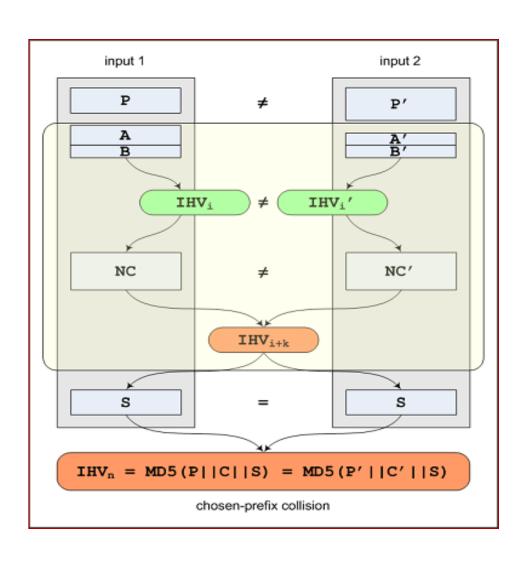


 identical prefix P

 different collision blocks C, C'

 identical suffix S

Steven's Collisions: Chosen Prefix



- Different prefixes P, P'
- different collision blocks NC, NC'
- identical suffix S



SHA-0 Attack

- 1998
 - Possible collisions attack with 2⁶¹ operations
- 2004
 - Full collisions found with 2⁵¹ operations
 - 80,000 CPU hours with Itanium2
- 2004
 - Collisions with 2⁴⁰ operations for SHA-0, MD5 and other
- 2005
 - Collisions with 2³⁹ operations



SHA-1 Attack

- 2005
 - Collisons found in 2⁸⁰ operations of reduced version of SHA-1--53 out of 80 rounds
- 2006
 - SHA-1-64 with 2³⁵ operations
- 2010
 - SHA-1-73 with 2³⁵ operations
 - Project HashClash: claim fully near collision attack
 with estimated complexity of 2^{57.5}



Progress of Collision Attacks

Attack complexities for MD5, SHA-1 and SHA-

	ME)5	SHA	\-1	SHA-2(256)					
jaar	identical prefix	chosen prefix	identical prefix	chosen prefix	identical prefix	chosen prefix				
– 2003	64	64	80	80	128	128				
2004	40		69							
2005	37		63							
2006	32	49		3 - 08						
2007	25	42 ₂	61							
2008	21									
2009	16	39 R	52	N.						



MD5 vectors

```
e6 ee c4 69 3d 9a
                                       06
                     7e
                            40
                                    58
                                       3e
                         ab
                                04
                                           b8
              09
                  f4
                     b3
                         02
                            83
                                    88
                                       83
                                e4
                            d9
          e8
              f7
                     c 9
                         9 f
                                       f2
                  cd
                                1 d
                                   bd
              56
                         5b
                                           36
                  34
                     8f
                                6d
                                       d4
                            ae
                                   ac
                     03
                                39
                 da
                         fd
                            02
                                    63
                                           d2
dd
          b4
                     7e
                         e8
                                54
                                    b6
                                           80
                            ce
          bc b6 a8
                     83 93 96 f9 65 2b
                                           6f
                  e6 ee c4 69 3d 9a
                                       06
       b5
                     7e
                         ab
                            40
                                04
                                    58
                                       3e
                  46
                  f4
                     b3
                         02
                            83
                                e4
                                    88
                                       83
          e8
              f7
                  cd
                     c9
                         9f
                            d9
                                1d
                                    bd
                         5b
              56
                     8f
                  34
                            ae
                                6d
                                       d4
                                           36
                                    ac
                     03
                         fd
                                    63
dd
          34
              87
                  da
                            02
                                39
                                       06
                                           d2
                     7e e8
                                54
                                       70
                                    b6
                                           80
                            ce
                     83
                        93
                            96 f9
          bc b6
                 a8
                                   65
                                       ab
                                           6f
```

Each of these blocks has MD5 hash
 79054025255fb1a26e4bc422aef54eb4



MD5 Collision demo

GRIFFITH COLLEGE Concat File Equivalence

```
$ ls >f1
$ cat v1 f1 >w1
$ cat v2 f1 >w2
$ ls -al
total 40
drwxr-xr-x 7 admin staff 238 Jul 16 17:07.
drwxr-xr-x 9 admin staff 306 Jul 16 16:40 ..
                             9 Jul 16 17:06 f1
           1 admin staff
-rw-r--r--
          1 admin staff 128 Jul 14 11:34 v1
-rwxr--r--
-rwxr--r-- 1 admin staff 128 Jul 14 11:35 v2
-rw-r--r- 1 admin staff 137 Jul 16 17:07 w1
-rw-r--r-- 1 admin staff
                          137 Jul 16 17:07 w2
$ md5 w*; openssl dgst -sha1 w*
MD5 (w1) = e9dc7f025001005370d9140168895489
MD5 (w2) = e9dc7f025001005370d9140168895489
SHA1(w1) = d867ab657437652d1cd9df9b4c89d9810f35fc24
SHA1(w2) = 2e05a71ff6c16f57d6ca935a47360de6aefcfad5
```



But how's about

```
$ md5 -s windows
```

 $MD5 \quad ("windows") = 0f4137ed1502b5045d6083aa258b5c42$

http://md5.rednoize.com/

