



# Deep Forward Networks

Wednesday  
08h15 – 09h00

Géraldine Schaller, Bern Winter School on Machine Learning 2025, Muerren

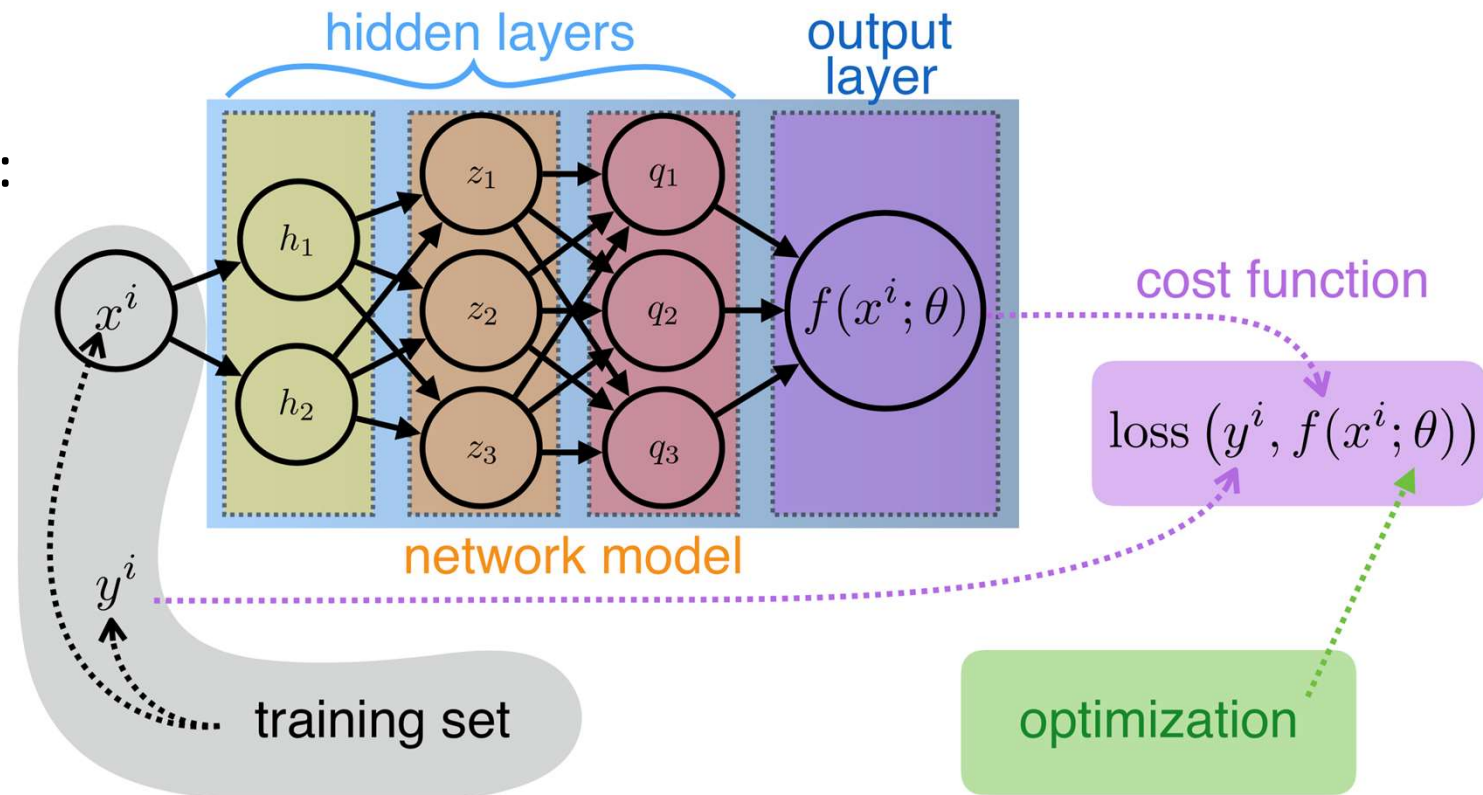
# Deploying a Neural Network

Given a task (in terms of **I/O mappings**), we need :

1) **Network model**

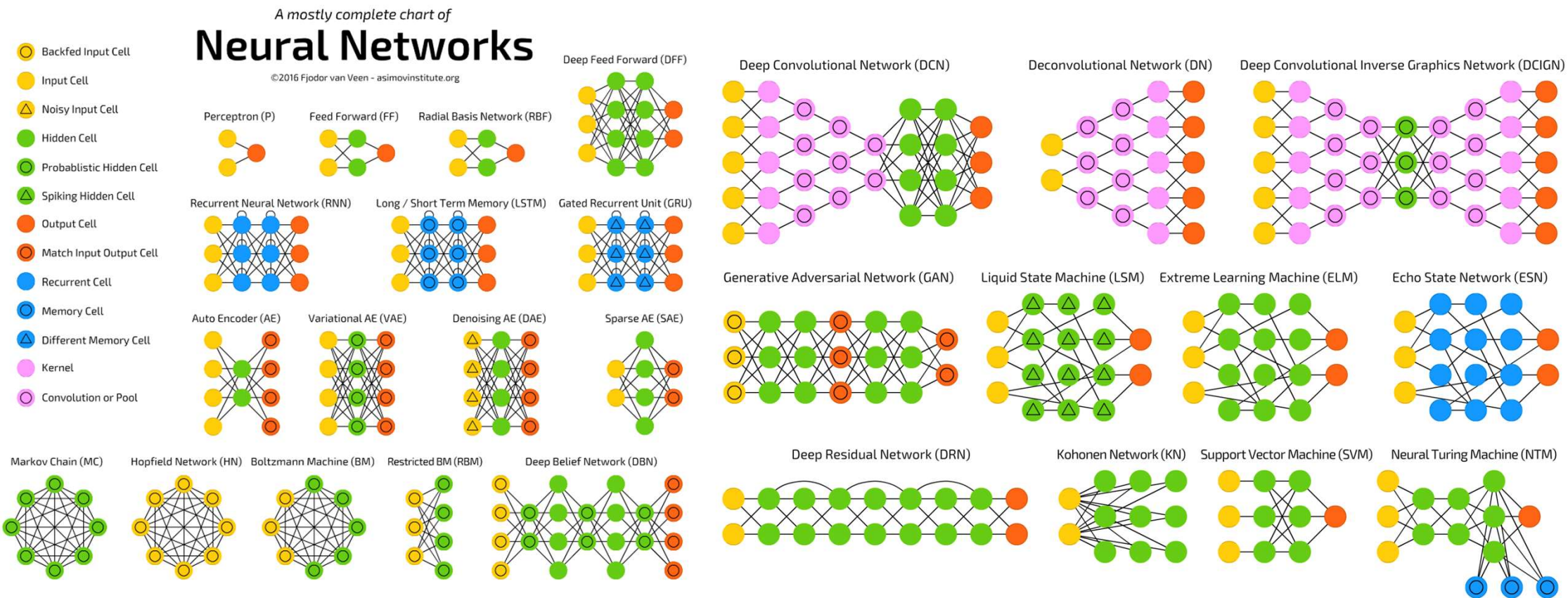
2) **Cost function**

3) **Optimization**





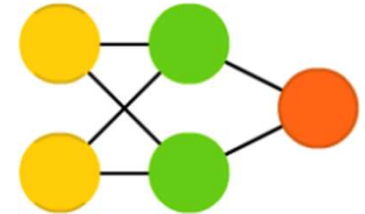
# 1) Network Model



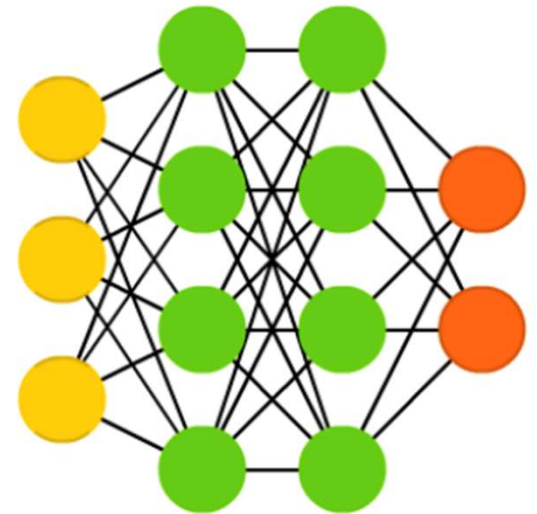
# (Deep) Feedforward NN (DFF)

- the **simplest type** of neural network
- All units are **fully connected** (between layers)
- information flows from **input** to **output** layer **without back loops**
- The first single-neuron network was proposed already in 1958 by AI pioneer Frank Rosenblatt
- **Deep** for “more than 1 **hidden layer**”

Feed Forward (FF)

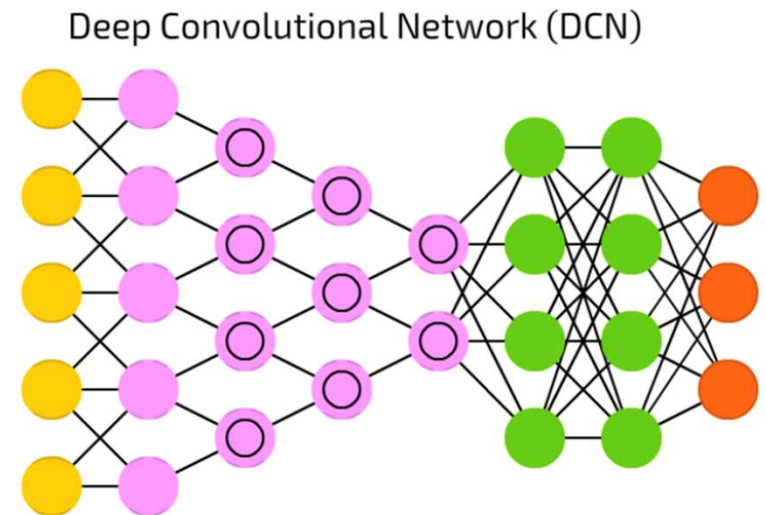


Deep Feed Forward (DFF)



# Convolutional Neural Networks (CNN)

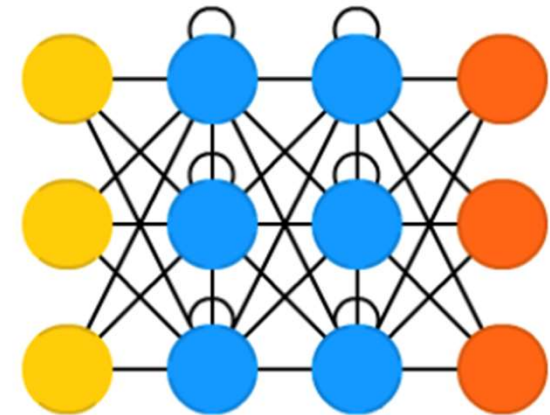
- inspired by the organization of the **animal visual cortex**
- **Kernel and convolution or pool cells** used to process and simplify input data
  - Weight sharing between *local regions*
- well suited for **computer vision** tasks
  - Image classification
  - Object detection



# Recurrent Neural Networks (RNN)

- connections between neurons include **loops**
- **Recurrent cells** (or memory cells) used
  - Weight sharing between *time-steps*
- well-suited for processing **sequences** of inputs, when **context is important**
  - Text analysis

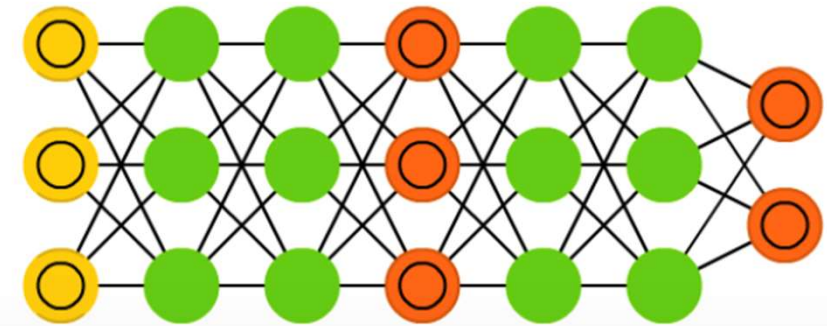
Recurrent Neural Network (RNN)



# Generative Adversarial Networks (GAN)

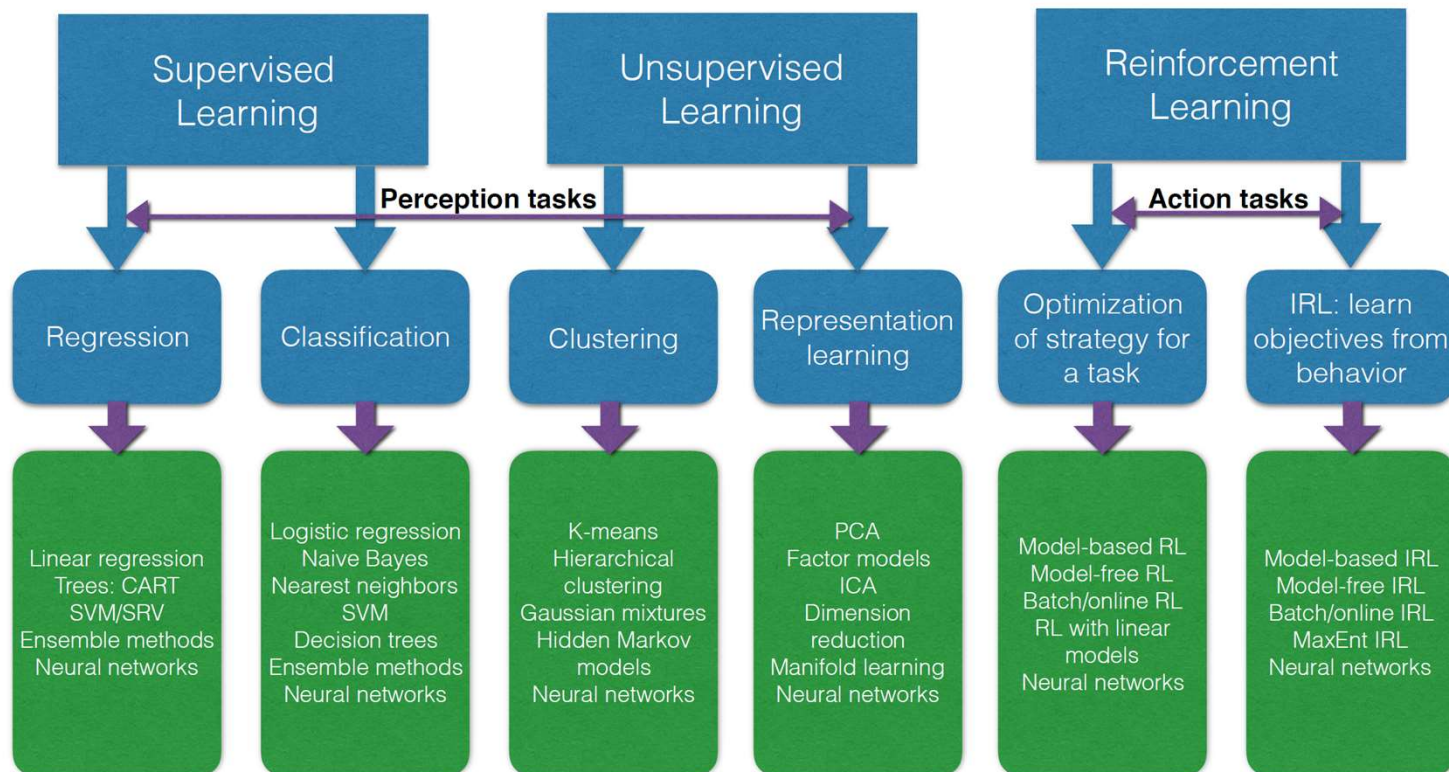
- More of a **Training Paradigm** rather than an architecture
- **Double** networks composed from generator and discriminator.
- They constantly try to fool each other, hence contain **backfed input cells** and **match input output cells**.
- well-suited for **generating real-life** images, text or speech

Generative Adversarial Network (GAN)





# Use cases





## 2) Loss and Cost functions

- **Loss function**  $L(\hat{y}^{(i)}, y^{(i)})$ , also called **error function**, measures **how different** the prediction  $\hat{y} = f(x)$  and the desired output  $y$  are

- **Cost function**  $J(w, b)$  is the average of the loss function on the **entire training set**

$$J(w, b) = \frac{1}{m} \sum_{i=1}^m L(\hat{y}^{(i)}, y^{(i)})$$

- Goal of the optimization is to find the **parameters**  $\theta = (w, b)$  that minimize the cost function

### 3) Optimization

- Given a task we define

- Training data

$$\{x^i, y^i\}_{i=1, \dots, m}$$

- Network

$$f(x; \theta)$$

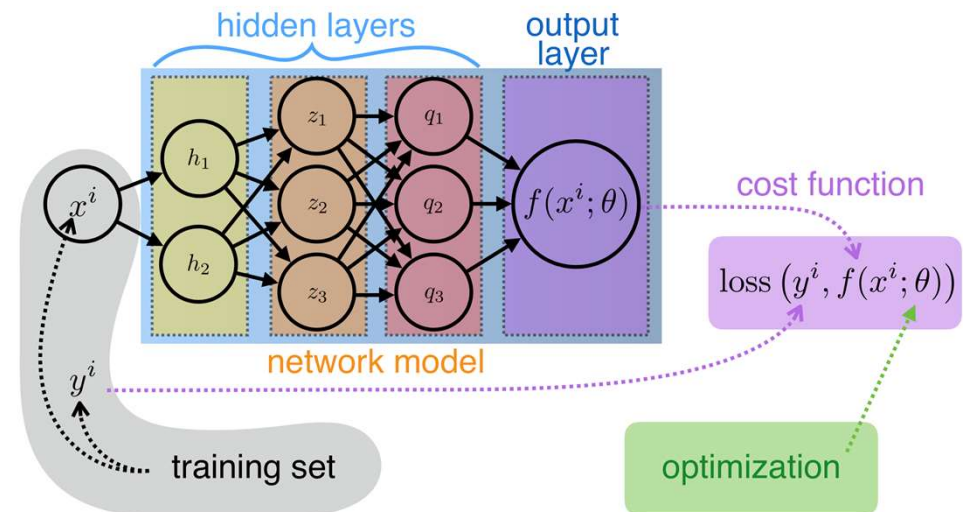
- Cost function

$$J(\theta) = \sum_{i=1}^m \text{loss}(y^i, f(x^i; \theta))$$

- Parameter initialization (weights, biases)

- random weights, biases initialized to small values (0.1)*

- Next, we *optimize the network parameters  $\theta$*  (training)
- In addition, we have to set values for hyperparameters



# Maximum Likelihood

- Given IID input/output samples :  $(x^i, y^i) \sim p_{\text{data}}(x, y)$
- **Conditional Maximum Likelihood estimate** (between model pdf and data pdf):

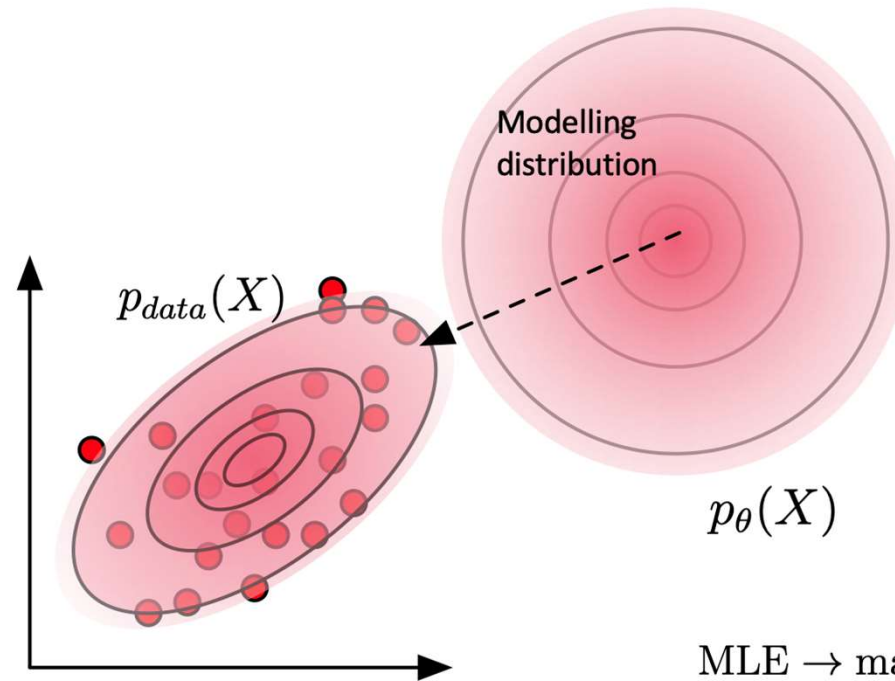
$$\begin{aligned}\theta_{\text{ML}} &= \arg \max_{\theta} \prod_{i=1}^m p_{\text{data}}(y^i | x^i; \theta) \\ &= \arg \max_{\theta} \sum_{i=1}^m \log p_{\text{data}}(y^i | x^i; \theta)\end{aligned}$$

- Mathematical tricks :

$$\min_{\theta} -E_{x, y \sim \hat{p}_{\text{data}}} [\log p_{\text{model}}(y | x; \theta)]$$

Maximize the likelihood == **Minimize the negative log-likelihood**

# Maximum Likelihood



$$\text{MLE} \rightarrow \max_{\theta \in \Theta} \frac{1}{N} \sum_{i=1}^N \log p_{\theta}(x_i)$$

Fisher 1922

$$\min_{\theta \in \mathcal{M}} KL(P_{\text{data}}, P_{\theta}) = \mathbb{E}_{\mathbf{x} \sim P_{\text{data}}} \left[ \log \frac{p_{\text{data}}(\mathbf{x})}{p_{\theta}(\mathbf{x})} \right]$$



# Loss function choice

- Choice determined by the **output representation**
  - Probability vector (**classification**) : **Cross-entropy**

$$\hat{y} = \sigma(w^\top h + b)$$

$$p(y|\hat{y}) = \hat{y}^y (1 - \hat{y})^{(1-y)}$$

$$L(\hat{y}, y) = -\log p(y|\hat{y}) = -(y \log(\hat{y}) + (1 - y)\log(1 - \hat{y}))$$

(binary classification)

- Mean estimate (**regression**) : **Mean Squared Error, L2 loss**

$$\hat{y} = W^\top h + b$$

$$p(y|\hat{y}) = N(y; \hat{y})$$

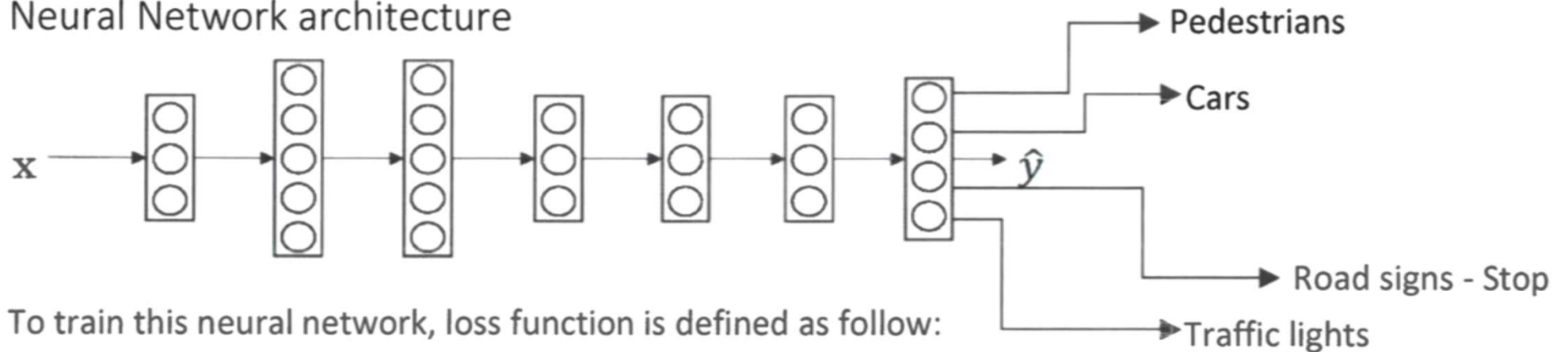
$$L_2(\hat{y}, y) = -\log p(y|\hat{y}) = \sum_{i=0}^m (y^i - \hat{y}^i)^2$$

# Loss function example

- NN does **simultaneously several tasks (multi-task)**



Neural Network architecture

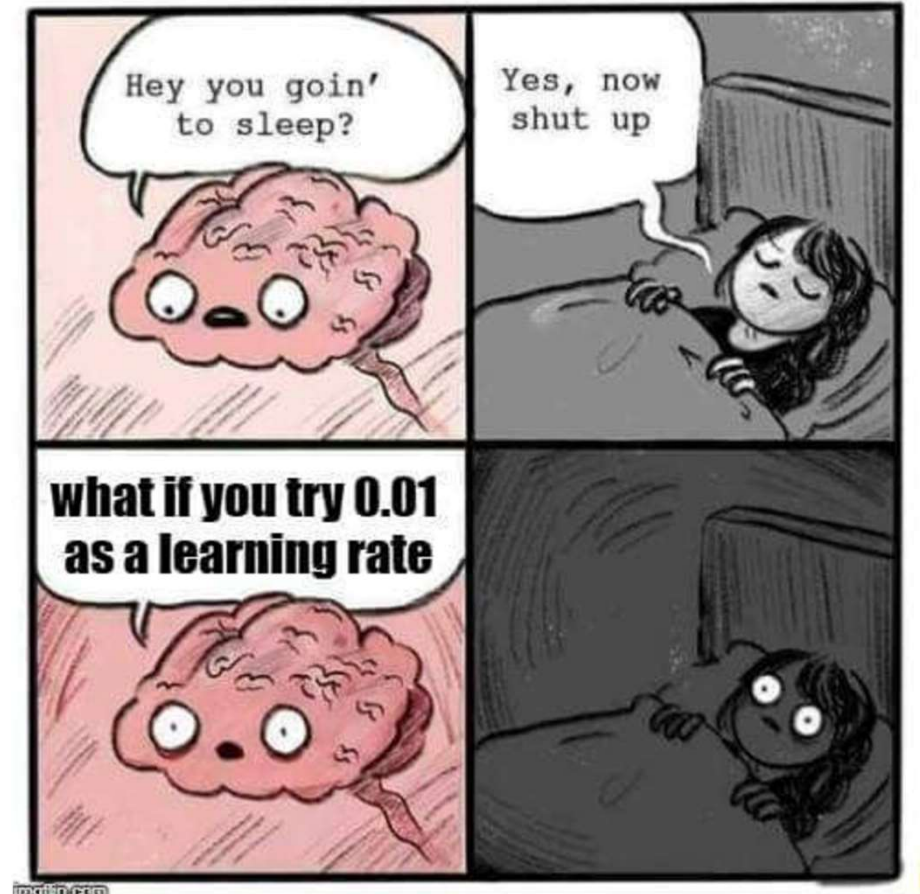


To train this neural network, loss function is defined as follow:

$$-\frac{1}{m} \sum_{i=1}^m \left[ \sum_{j=1}^4 \left( y_j^{(i)} \log(\hat{y}_j^{(i)}) + (1 - y_j^{(i)}) \log(1 - \hat{y}_j^{(i)}) \right) \right]$$

# Hyperparameters

- Parameters that **cannot be learnt** directly from training data
- A long list...
  - Learning rate  $\alpha$
  - Number of iterations (**epochs**)
  - Number of hidden layers
  - Number of hidden units
  - Choice of activation function
  - *More to come !*



# Training

- *Iterative* process



Forward propagation

$$Z = w^T x + b$$

$$A = \sigma(Z)$$



Cost function  
 $J(w, b) = J(\theta)$

epochs

Parameter update  
(gradient descent)

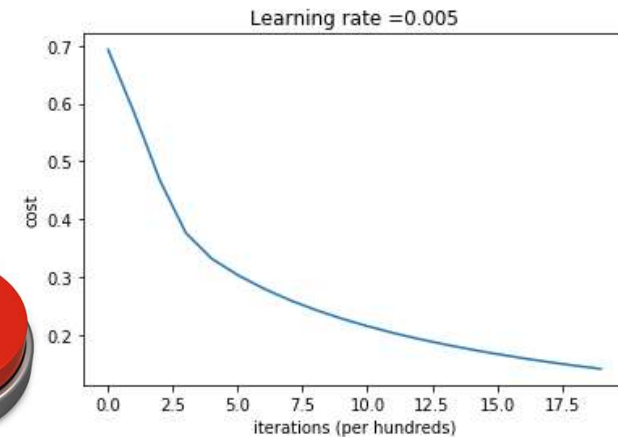
learning rate  $\alpha$

$$\theta_{t+1} = \theta_t - \alpha \nabla J(\theta_t)$$



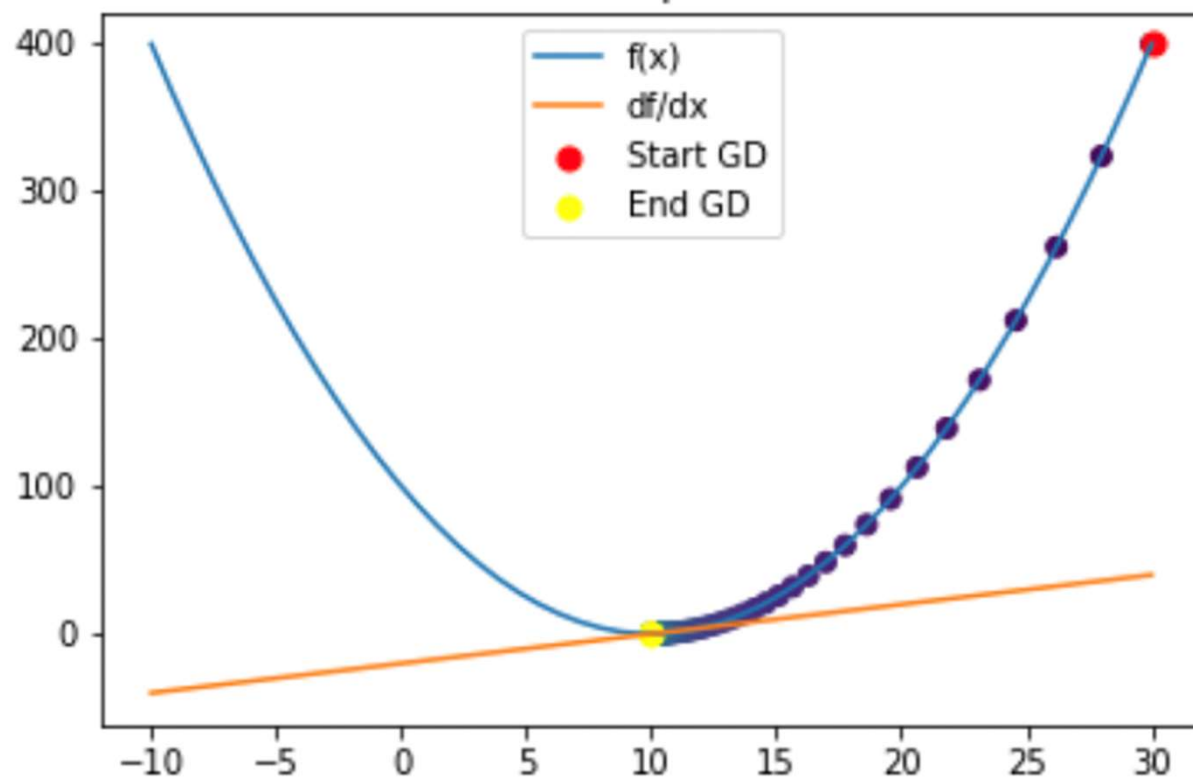
Backward propagation  
( $dJ/dw$ ,  $dJ/db$ )

Learning curve



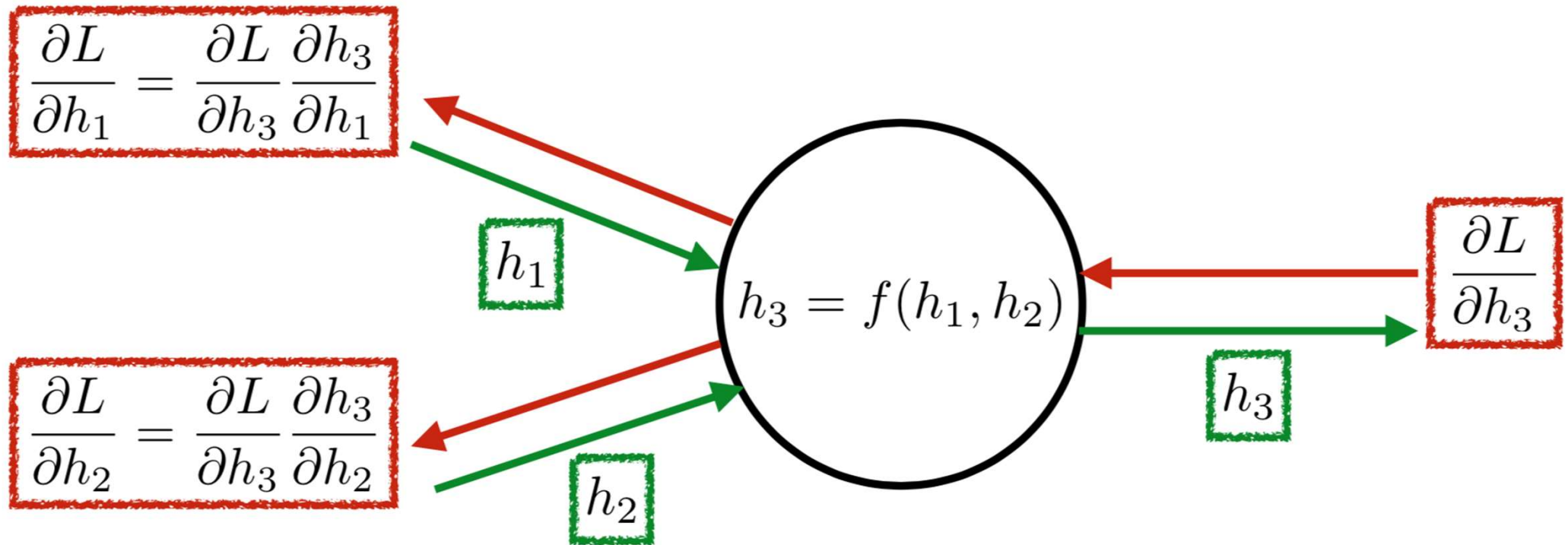


Gradient descent quadratic function



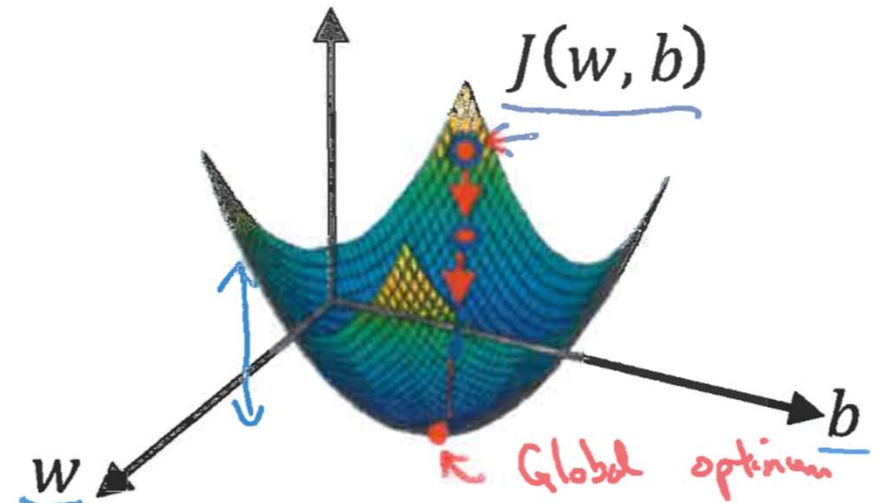
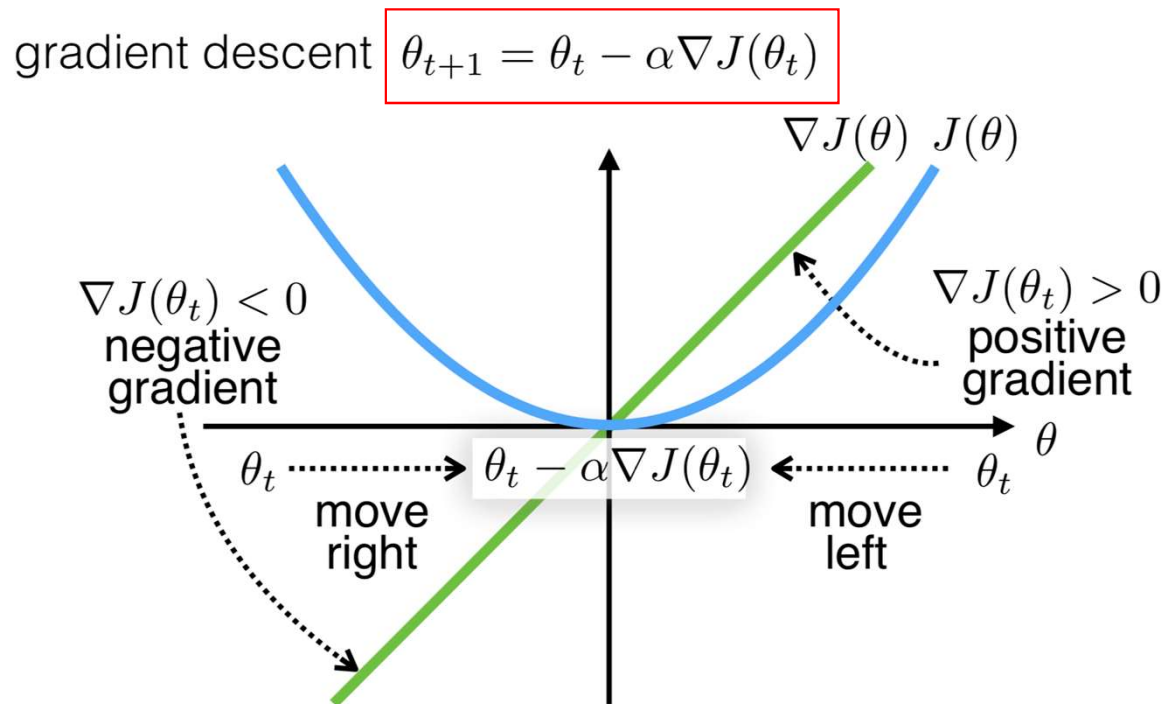
# Backpropagation

- Efficient implementation of the **chain-rule** to compute derivatives with respect to network weights



# Gradient Descent

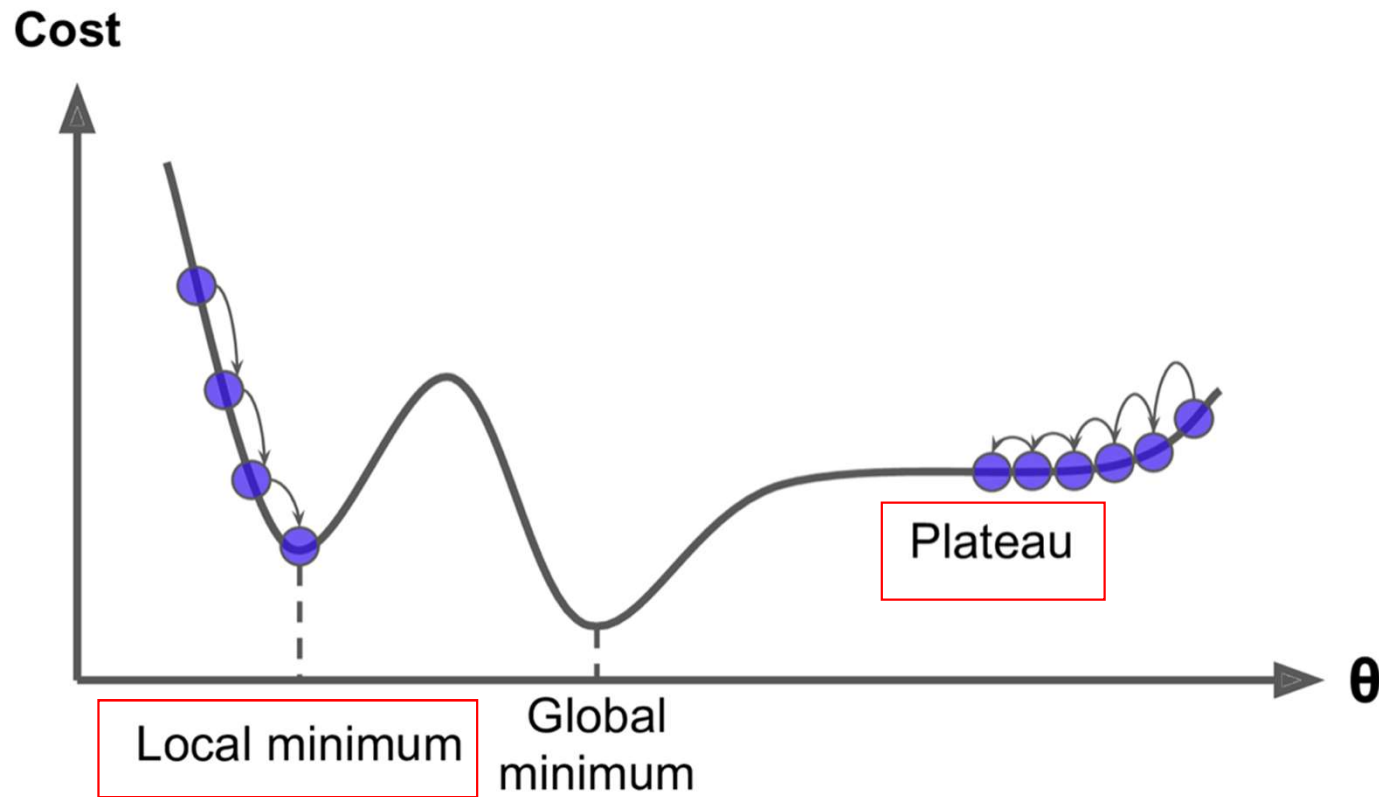
- **Iterative method** to find the parameters  $\theta = (w, b)$  that minimize  $J(\theta)$



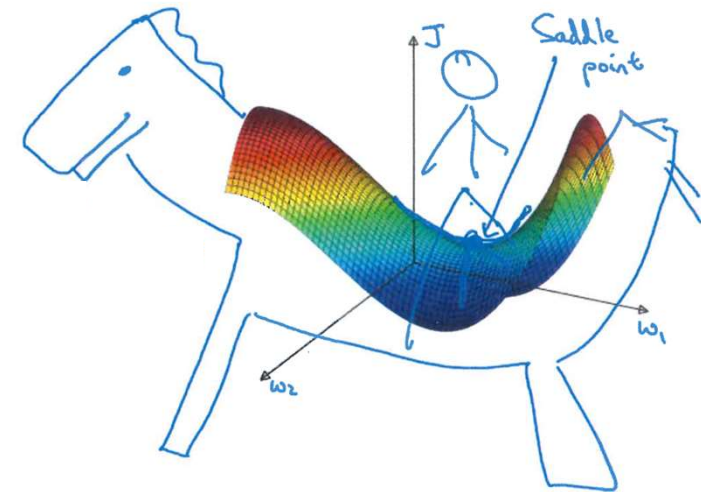
$$\nabla J(w) = \frac{dJ(w, b)}{dw}$$

$$\nabla J(b) = \frac{dJ(w, b)}{db}$$

# Optimization pitfalls

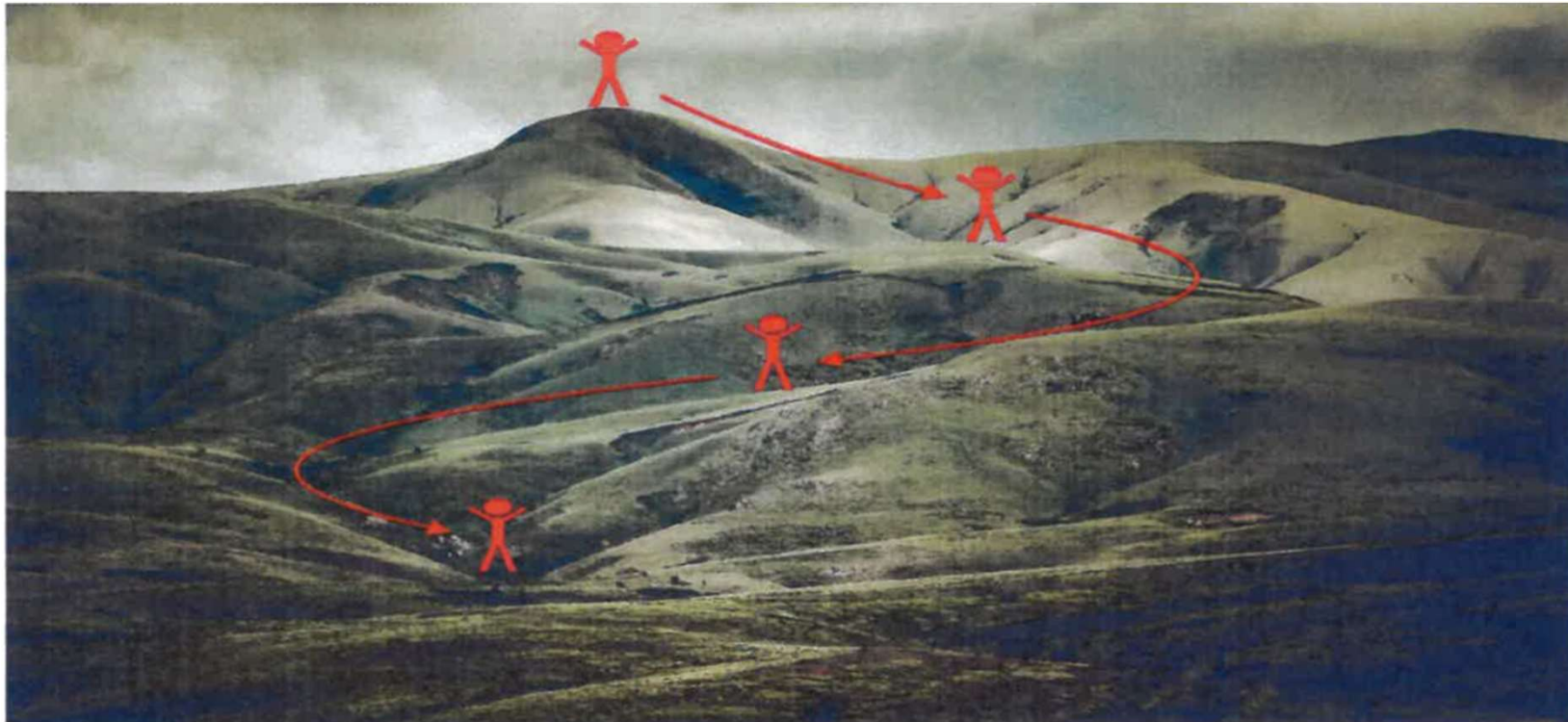


Saddle point





# Gradient Descent Illustration



# Tutorial / Practical

