

Formal Verification of the c-kzg library: Establishing the Basis

Audit Report

Grant ID FY24-1544 — Ethereum Foundation

Brett Decker decker@galois.com Ryan McCleeary mccleeary@galois.com Roberto Saltini roberto.saltini@consensys.net Thanh-Hai Tran thanh-hai.tran@consensys.net

> Galois, Inc. 421 SW 6th Ave., Ste. 300 Portland, OR 97204

Consensys Software, Inc.



Contents

1	Audit Report		3
	1.1	Audit of the c-kzg Implementation	3
	1.2	Table 1: Comparing c-kzg vs. Python KZG Specification	5
2	Nex	t Steps	6

consensys

1. Audit Report

The goal of this audit report is to determine the adherence of the structure of the c-kzg implementation to the structure of its stated reference, the Polynomial Commitments section of the Python Deneb consensus specification (Python KZG Specification, hereafter) which encodes the KZG commitment scheme.

Identifying similarities and possible discrepancies between the two structures is key to the next two phases of this project. This comparison will guide us in structuring the Cryptol version of the Python KZG Specification in a way that enables subsequent verification against both the Python KZG specification itself and the c-kzg implementation.

It is important to note that determining the correctness of the c-kzg implementation with respect to the Python KZG Specification is beyond the scope of this document

1.1. Audit of the c-kzg Implementation

The Python KZG Specification entails 28 functions from four categories: Bit-reversal permutation, BLS12-381 helpers, Polynomials, and KZG. The following table identifies all of these functions, according to their category, with the GitHub references to Python specification and the c-kzg implementation.

In most cases the names of the functions in the Python specification match the c-kzg implementation. The differences include:

- The Python function multi_exp is represented in the c-kzg implementaion by splitting multiplication into two functions, g1_mul and g2_mul, to have separate functions handle multiplication for the two groups, G1 and G2, separately, followed by a call to blst_doub;
- 2. A naming convention difference between the Python function bls_field_to_bytes and the c-kzg implementation function bytes_from_bls_field;
- 3. Two instances where the c-kzg implementation provides two implementing functions (for speed reasons) with g1_lincomb_naive and g1_lincomb_fast for Python function g1_lincomb, and similarly in the case of functions blst_fr_inverse and blst_fr_eucl_inverse for Python function blst_modular_inverse (though there appears currently to be no difference between these two BLST imported functions as defined in the BLST repository).
- 4. One instance where the c-kzg implementaion has the prefix fr_, for fr_div

In addition, there are a couple of other slight differences. The computation specified in the Python function compute_quotient_eval_within_domain is handled inside the c-kzg implementation of the function compute_kzg_proof_impl instead of as a subroutine.

Another difference is that the function blst_modular_inverse uses the builtin Python function pow, whereas the corresponding BLST functions, as implented in reciprocal_fr, use BLST utility functions ct_inverse_mod_256, redc_mont_256, and mul_mont_sparse_256.

galois

consensys

Finally, while both the Python spec and the c-kzg implementation have a function named reverse_bits, the c-kzg function does not match the spec. The spec for reverse_bits defines the computation as reversing the bits of a value for some specified bit length. The c-kzg function defines the computation as reversing all the bits of the value as defined by the size of the memory representation (in this case a 64-bit integer). The c-kzg implementation has a separate function, reverse_bits_limited that does match the Python spec. It should be noted that this spec equivalent function is not used in the implementation of bit_reversal_permutation. Instead bit_reversal_permutation calls the non-equivalent reverse_bits function, but it handles the result in a way that conforms to the Python spec, so that the overall computation is equivalent.

consensys

1.2. Table 1: Comparing c-kzg vs. Python KZG Specification

Category	Python KZG Specification	c-kzg implementation
Bit-reversal	is_power_of_two	is_power_of_two
	reverse_bits	reverse_bits
permutation	bit_reversal_permutation	bit_reversal_permutation
	multi_exp	g1_mul , g2_mul
	hash_to_bls_field	hash_to_bls_field
	bytes_to_bls_field	bytes_to_bls_field
	bls_field_to_bytes	bytes_from_bls_field
	validate_kzg_g1	validate_kzg_g1
	bytes_to_kzg_commitment	bytes_to_kzg_commitment
RI C12 201 halpare	bytes_to_kzg_proof	bytes_to_kzg_proof
BLS12-381 helpers	blob_to_polynomial	blob_to_polynomial
	compute_challenge	compute_challenge
	bls_modular_inverse	blst_fr_inverse , blst_fr_eucl_inverse
	div	fr_div
	g1_lincomb	g1_lincomb_naive , g1_lincomb_fast
	compute_powers	compute_powers
	compute_roots_of_unity	compute_roots_of_unity
Polynomials	evaluate_polynomial	evaluate_polynomial
1 Olyffolinais	_in_evaluation_form	_in_evaluation_form
	blob_to_kzg_commitment	blob_to_kzg_commitment
	verify_kzg_proof	verify_kzg_proof
	verify_kzg_proof_impl	verify_kzg_proof_impl
	verify_kzg_proof_batch	verify_kzg_proof_batch
	compute_kzg_proof	compute_kzg_proof
KZG	compute_quotient _eval_within_domain	compute_kzg_proof_impl
	compute_kzg_proof_impl	compute_kzg_proof_impl
	compute_blob_kzg_proof	compute_blob_kzg_proof
	verify_blob_kzg_proof	verify_blob_kzg_proof
	verify_blob_kzg_proof_batch	verify_blob_kzg_proof_batch

2. Next Steps

The next phase of this grant's work is to create a Cryptol specification that matches the Python KZG Specification.

After this second milestone, we will create a test bench that will verify the Cryptol specification against the Python specification, using the Python as the oracle for property based testing of the Cryptol. We will also verify properties for KZG correct construction, e.g. calling compute_kzg_proof with valid inputs for blob and z_bytes always results in successful verification when the output proof is passed to verify_kzg_proof.

After this third milestone, we will create a script using the Software Analysis Workbench (SAW) to attempt to formally verify and prove one or more of the Python KZG Specification functions as implemented in c-kzg is functionally equivalent to the corresponding Cryptol specification function, as well as memory safe.

After this fourth milestone, we will deliver a final report with our results and conclusions.