# Report 1: Measurements

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Phys 207 Lab CD4

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# 1 Introduction

This lab is meant to explore the relationship between different variables, or the lack thereof, and how measuring those variables in the real-word effects those relationships. Almost all fields of science involve measuring different quantities and identifying the relationships between them, thus it is important to properly measure those quantites. Proper measurements do include using the right equipment in the correct way, but it also means determing a method of measurement best suited for the quantity. Questions such as:

- 1. At what intervals should data points be taken?
- 2. In what increments should a quantity be measured in?
- 3. What variables are accounted for and not accounted for in the given data?

Effective measurements allow us to accurately determine whether or not a relationship exists, and if there is one, what kind of relationship it is. Improper measurements or ineffective methods can result in inaccurate conclusions about the world we inhabit.

# 2 Procedure

### 2.1 Head Circumference and Heartbeat Time

Each group will pick one of their members to be their test subject. First, we will measure the circumference of their head by using a rope and a ruler in cm. Then, we will time between two of their heartbeats. We will enter this data onto the computer to use at the end of the lab.

### 2.2 Estimate $\pi$

We are meant to find the circumference and diameter of various objects, then calculate the ratio between the two using the formula:

$$\frac{C}{D} = \pi$$

The calculated value will only be an estimate of  $\pi$ , but it should be relatively close.

### 2.2.1 3 Objects

There are 3 circular objects:

- 1. A 500-gram mass.
- 2. A small circular disk.
- 3. A large circular disk.

For each object, we measure their circumference and diameter using a ruler, in which these values will be recorded in a Microsoft Excel spreadsheet. Then, we create a scatter plot in Excel, with the x-axis representing diameter and the y-axis representing circumference. Our estimate of  $\pi$  for this test will be the slope of the trendline of our plotted data.

### 2.2.2 Toothpicks

We form a circular shape using toothpicks. The circumference will be the amount of toothpicks used to form the shape and the diameter will be roughly the amount of toothpicks it takes to divide the shape in half. We then calculate our  $\pi$  estimate using these measurements.

#### 2.2.3 Google Maps

We will find a circular building or geographic location. Then, using the measure distance feature of Google Maps, plot points around the circumference of the object to find the circumference and plot two points perpendicular to each other as well as the center of the object to find the diameter. We will then calculate our estimate of  $\pi$  using these measurements.

### 2.3 Calculate Uncertainty in Measurements

We will calculate the potential uncertainty in measuring length using the formula:

$$A \pm \delta A = (A) \left[ 1 \pm \frac{\delta A}{A} \right] \tag{1}$$

and density using the formula:

$$\left(\frac{A \pm \delta A}{B \pm \delta B}\right) = \left(\frac{A}{B}\right) \left[1 \pm \left(\frac{\delta A}{A} + \frac{\delta B}{B}\right)\right]$$
(2)

#### 2.3.1 Measure the Fish

We will measure the length of a printed image of a fish using a ruler in centimeters. Then, we will calculate the uncertainty of this measurement by taking the  $\pm$  difference of the ticks on the ruler nearest to our measurement and dividing the difference in half.

For example, if our measurement was 10.2 cm, and assuming our ruler measured in intervals of 0.5 cm, we would subtract the tick to the left (10.0 cm) from the tick to the right (10.5 cm), and divide that difference (0.5 cm) by 2 to get 0.25 cm. Then, since our measurement could be greater or less than the actual length, we would write our value as  $\pm 0.25$  cm.

#### 2.3.2 Density of Wood Block

We will calculate the density of a mysterious wood block using the formula:

$$p = \frac{m}{v}$$

Where p is density, m is mass, and v is volume. We will calculate the mass in grams of the wood block using a digital scale. In order to calculate volume, we will measure the length, width, and height of the wood block in centimeters using a ruler, then multiply all three dimensions to get our volume in cm<sup>3</sup>.

### 2.4 Time of Oscillations

We will measure the time it takes for a pendulum to swing back and forth, which is known as the *period of oscillation*. The pendulum will be 1.5 m long, in which it will be a rope tied to a 500-gram weight, with the length of the pendulum being the length of the rope plus the distance from the end of the rope to the center of mass of our 500-gram weight.

We will record the time it takes for this pendulum to oscillate, then reduce the length of the pendulum. We will repeat this 4 more times until we have 5 measurements. Both the length and period of oscillation in a Excel spreadsheet, then plot the values in which the period of oscillation will be a function of length.

### 2.5 Experiment Analysis

Going back to the first part of the procedure, we will create a table in Excel using those measurements, and then create a scatter plot the measurements. The x-axis will be heartbeat time and the y-axis will be head circumference.

# 3 Data and Calculations

# 3.1 Figures and Tables

# 3.1.1 Pi Estimates

Figure 1: Circumference vs. Diameter of 3 Objects

Test 1: Pi Estimates

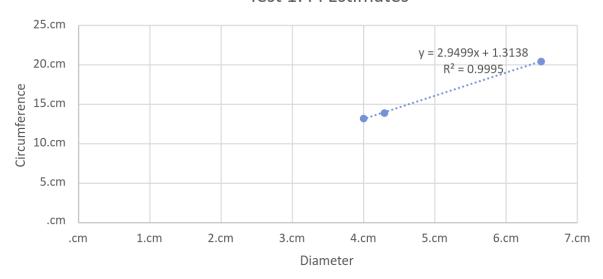


Table 1: Diameter and Circumference of 3 Objects

Object #	Diameter (cm)	Circumference (cm)
1	4.0 cm	13.2 cm
2	6.5 cm	20.5 cm
3	4.3 cm	13.9 cm

## 3.1.2 Oscillation and Pendulum Length

Figure 2: Period of Oscillation vs. Pendulum Length

# Time of Oscillation as a Function of Length

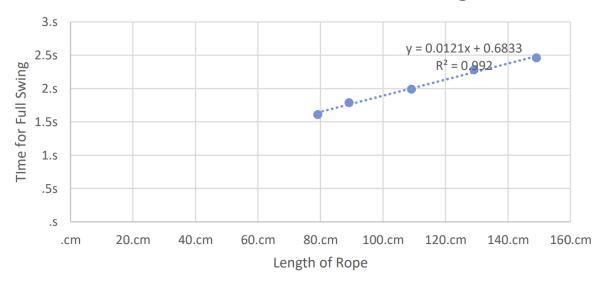


Table 2: Rope Length vs. Period of Oscillation

Rope Length (cm)	Period of Oscillation (s)
149.1 cm	2.46 s
129.1 cm	2.28 s
109.1 cm	1.99 s
89.1 cm	1.79 s
79.1 cm	1.61 s

# 3.1.3 Density of Wood

Table 3: Mass, Volume, and Density of Wood Block

Mass (g)	Volume $(cm^3)$	Density $(g/cm^3)$
72.3 g	$122.14~\mathrm{cm}^3$	$0.59~\mathrm{g/cm^3}$

### 3.1.4 Time Between Heartbeats vs Head Circumference

Figure 3: Heart Pulse vs. Head Circumference

# Time per Heartbeat vs. Head Circumfernece

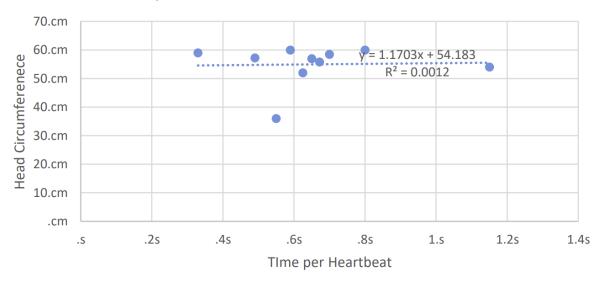


Table 4: Time Between Heartbeats vs. Head Circumference

Time Between Heartbeats (s)	Head Circumference (cm)
0.8 s	60.0 cm
0.59 s	60.0 cm
0.33 s	59.0 cm
0.7 s	58.5 cm
0.49 s	57.2 cm
$0.65 \mathrm{\ s}$	57.0 cm
0.67 s	55.8 cm
1.15 s	54.0 cm
0.63 s	52.0 cm
0.55 s	36.0 cm

# 3.2 Calculations

### 3.2.1 Density of Wood Block

The dimensions of the wood block were:

$$l = 23.8 \,\mathrm{cm}$$
  $w = 5.448 \,\mathrm{cm}$   $h = 0.942 \,\mathrm{cm}$ 

Thus the volume was:

$$v = l \cdot w \cdot h = 23.8 \,\mathrm{cm} \cdot 5.448 \,\mathrm{cm} \cdot 0.942 \,\mathrm{cm} \approx 122.14 \,\mathrm{cm}^3$$

The mass of the wood block was m = 72.3 g, thus the density was:

$$p = \frac{m}{v} = \frac{72.3 \,\mathrm{g}}{122.14 \,\mathrm{cm}^3} \approx 0.59 \,\mathrm{g/cm}^3$$

# 3.2.2 Uncertainty in Density of Wood Block

Since the density p consists of two quantities: mass m, which was measured using a scale measuring in increments of 0.01 grams, and volume v, which was calculated using the product of the 3 measured dimensions l, w, and h, all measured using a caliper measuring in increments of 0.001 centimeters.

The error propagation of the mass, which will be the  $\delta A$  of formula (2), can be calculated by dividing the increment of measurement by 2:

$$\delta A = \pm \frac{0.01 \,\mathrm{g}}{2} = \pm 0.05 \,\mathrm{g}$$

The error propagation of the volume  $\delta B$  will require us to calculate the relative uncertainties of all 3 measured dimensions. The absolute uncertainties of all 3 dimensions will be 0.0005 cm since they were all measured using the same caliper:

$$\delta l = \delta w = \delta h = \frac{0.001 \,\mathrm{cm}}{2} = 0.0005 \,\mathrm{cm}$$

The relative uncertainty of length l:

$$\delta l = \pm \frac{\delta l}{l} \cdot 100 = \pm \frac{0.0005 \,\text{cm}}{23.8 \,\text{cm}} \cdot 100 \approx \pm 0.0021008 \,\%$$

The relative uncertainty of length w:

$$\delta w = \pm \frac{\delta w}{w} \cdot 100 = \pm \frac{0.0005 \,\text{cm}}{5.448 \,\text{cm}} \cdot 100 \approx \pm 0.0091777 \,\%$$

The relative uncertainty of length h:

$$\delta h = \pm \frac{\delta h}{h} \cdot 100 = \pm \frac{0.0005 \,\text{cm}}{0.942 \,\text{cm}} \cdot 100 \approx \pm 0.0530786 \,\%$$

When we multiply all 3 dimensions, we will add the uncertainties:

$$v = (l \pm \delta l)(w \pm \delta w)(h \pm \delta h) = lwh \pm (\delta l + \delta w + \delta h)$$

When we substitute in our measurements, we get:

$$v = 122.14 \,\mathrm{cm}^3 \pm 0.0643571 \,\%$$

and converting to absolute uncertainty:

$$v = 122.14 \pm 0.07861 \,\mathrm{cm}^3$$

Using formula (2), we find that our uncertainty is:

$$\frac{72.3 \pm 0.05 \,\mathrm{g}}{122.14 \pm 0.07861 \,\mathrm{cm}^3} = \left(\frac{72.3}{122.14}\right) \left[1 \pm \left(\frac{0.05}{72.3} + \frac{0.07861}{122.14}\right)\right]$$

$$\Rightarrow (p) \left[1 \pm (0.001335)\right]$$

$$\rightarrow \left[\delta p = \pm 0.1335 \,\%\right]$$

# 4 Questions

1 Discuss the limitations of these methods for calculating  $\pi$ . Which method was the best? The worst? Are there improvements to be made? The best method for estimating  $\pi$  was taking the slope of the linear trendline from the plotted diameters and circumferences of the three objects. This is so because the value obtained from the slope had the least difference from  $\pi$  compared to the other methods.

Using Google Maps to calculate  $\pi$  turned out to be the worst method since the calculated value had the biggest difference from  $\pi$  compared to the other methods.

We could improve the first method of calculation by measuring more than just 3 objects. Perhaps 6 or 9 would give us a more accurate value. The second method of calculation, in which we used tooth picks to form a circular shape, would benefit from the use of more toothpicks in forming the circumference. It might also benefit from forming multiple circular shapes from different amounts of toothpicks, then taking the average of the calculated  $\pi$  estimates. The third and final method could benefit from plotting more points along the circumference of the circular object.

2 Try to match your piece of wood with a known tree. Discuss whether you can be certain of your identification. I narrowed down the identity of the wood to either Pine, jack and Sourwood as both types have a density roughly equivalent to the density of the wood,  $0.59 \text{ g/cm}^3$ .

While the uncertainty of the density was calculated to be  $\pm 0.1335 \,\%$ , that only means the true density of the wood block could be between 0.5892 and 0.5908 g/cm<sup>3</sup>, which both round to 0.59 g/cm<sup>3</sup>. Thus, I can be certain of this identification.

- 3 Based only on your experimental data, can you say how the time for one swing relates to the length of the pendulum? Is there a clear functional dependance? What could you do to make the experiment better? Based on my experimental data, the time for one swing seems to have a linear relationship to the length of the pendulum. Thus, it is clear that the period of oscillation depends on the length of the pendulum. The experiment would benefit from recording more than 5 data points as well as specifying a specific interval of rope length between data points.
- 4 Is there a correlation between the circumference of someone's head and the time between heartbeats? Would you expect there to be one? According to figure 3, there is no correlation between the circumference of someone's head and the time between heartbeats. The correlation coefficient  $R^2 = 0.0012$  of the trendline is quite low and visually, the data does not form any clear pattern.

However, I would expect there to be some kind of correlation because if there was no correlation, then head circumference would not average between 50 and 60 cm, with the exception of one outlier of 36 cm at a pulse of 0.55 s, see table 4. The two variables would need some kind of proportional relationship, most likely with a third unaccounted for variable, in order to for this average to appear.

# 5 Conclusion

Experiment 1: Estimating  $\pi$  While the results were not exactly  $\pi$ , it is clear that there is a relationship between circumference C and diameter D, in which the ratio between the two variables is always  $\pi$ . Regardless of the method used and its effectiveness, the result always remained close to  $\pi$ .

**Experiment 2: Calculating Uncertainty** The first part of this experiment, in which we calculated the uncertainty in measuring the length of the fish, did not reveal much as it did introduce us to the idea of measuring uncertainty.

However, the second part, calculating the density of the wood block, revealed that the relationships between variables also extends into their uncertainties. In this case, there were 6 variables: mass m, v volume, length l, width w, height h, and density p. p is the ratio between m and v, and so any uncertainties in those two variables will be reflected in p. However, v is the product of l, w, and h, which all have their own uncertainties. Thus, the uncertainties in those variables will be reflected in both v and p. Fortunately,

the uncertainties of l, w, and h were negligible enough that the uncertainty of v was also negligible. The uncertainty of m did not rely on any other variables and only on the equipment that was used. The same goes for l, w, and h. Thus, while uncertainty can be carried further down into variable relationships, the biggest impact on uncertainty is the equipment or method of measure used.

Looking back on experiment 1, where we used toothpicks and Google Maps to calculate  $\pi$ , the ineffectiveness of both methods, potentially due to more room for human error such as:

- 1. Not using enough toothpicks.
- 2. Not plotting enough points while using the Google Maps feature.

resulted in a less accurate estimate of  $\pi$ , which might mean that there was a higher level of uncertainty in these methods. In my experiment with the toothpicks, the last toothpick in the line of toothpicks used to measure the diameter of the shape extended out of the shape. Since both the circumference and diameter were to be measured in terms of toothpicks, we roughly estimated how much of the last toothpick remained in the shape. This was not a reliable method as we roughly measured this toothpick in tenths, meaning the uncertainty of the diameter could be quite significant.

**Experiment 3: Time of Oscillations** While we did find linear a relationship between oscillations and pendulum length, the domain of our graph, particularly the distance between data points, could have been larger. If you restrict almost any function to a small enough domain, it will appear linear, thus this could have been the case with our experiment. It is clear that a functional dependance exists, but whether that relation is linear or something else would require another trial.

Experiment 4: Graphing Head Circumference with Respect to Heartbeat Pulse Despite the lack of a correlation in our data, see figure 3, it is important to consider that there were only 10 data points, in which all individuals were around the same age group, young adults. With age being a potential variable, in which children see a lot of physical changes as they approach adulthood, we cannot conclude that there is no correlation, only that we did not find one given our available data pool.

# 6 References

(1) Oliver Seely "Physical Properties of Common Woods" http://www2.csudh.edu/oliver/chemdata/woods.htm