

ChocoPy v2.0: Language Manual and Reference

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1 Introduction

This manual describes the ChocoPy language, which is a statically typed dialect of Python 3.6. ChocoPy is intended to be used in a classroom setting. It has been designed to be small enough for students to implement a full ChocoPy compiler over one semester.

ChocoPy has been designed to be a subset of Python. Almost every valid ChocoPy program is also a valid Python 3.6 program. An execution of a ChocoPy program that does not result in error usually has the same observable semantics as the execution of that program in Python 3.6. Appendix A lists the small number of exceptions to this rule.

A ChocoPy program is contained in a single source file. At the top level, a ChocoPy program consists of a sequence of variable definitions, function definitions, and class definitions followed by a sequence of statements. A class consists of a sequence of attribute definitions and method definitions. A class creates a user-defined type. Function definitions can be nested inside other methods and functions. All class names and functions defined at the top level are globally visible. Classes, functions, and methods cannot be redefined. Program statements can contain expressions, assignments, and control-flow statements such as conditionals and loops. Evaluation of an expression results in a value that can be an integer, a boolean, a string, an object of user-defined class, a list, or the special value `None`. ChocoPy does not support dictionaries, first-class functions, and reflective introspection. All expressions are statically typed. Variables (global and local) and class attributes are statically typed, and have only one type throughout their lifetime. Both variables and attributes are explicitly typed using annotations. In function and method definitions, type annotations are used to explicitly specify return type and types of formal parameters.

For readers familiar with the Python language, Figure 1 contains a sample ChocoPy program illustrating top-level functions, statements, global variables, local variables, and type annotations. The type annotations are valid syntaxes in Python 3.6, though the Python interpreter simply ignores these annotations and leaves them as hints for other tools. In contrast, ChocoPy enforces static type checking at compile time. In Figure 1, the function `is_zero` is defined at the top level. Its formal parameters `items` and `idx` are explicitly typed as a list of integers and an integer, respectively. The return type of the function `is_zero` is `bool`. The function defines a local variable, `val`, whose type is `int`. At the top level, the program defines a global variable `mylist`, whose type is a list of integers. Function `is_zero` is invoked in a top level statement and its result is output using the predefined `print` function. Similarly, Figure 2 contains a ChocoPy program that defines two classes: `animal` and `cow`. The class `cow` inherits from `animal`, which in turn inherits from the predefined root class `object`. The Boolean attribute `makes_noise` is defined in `animal` and is therefore inherited by class `cow`. The class `cow` overrides the method `sound`. The constructor for class `cow` is invoked at line 19.

Section 2 provides a detailed but informal overview of the various language constructs in ChocoPy. Sections 3–6 provide formal descriptions of the lexical structure, grammatical syntax, typing rules, and operation semantics of ChocoPy.

2 A tour of ChocoPy

Notation In the rest of this section, we use:

- `{expr}` to denote an expression in the program.
- `{id}` to denote an identifier such as the name of a variable or function.
- `{stmts}` to denote a list of program statements, separated by newlines.
- `{declarations}` to denote a list of (possibly interleaved) declarations of functions, variables, attributes, and/or classes, where applicable.
- `{type}` to denote a static type annotation.
- `{literal}` to denote a constant literal such as an integer literal, a string literal, or the keywords `True`, `False` or `None`.

```

1 def is_zero(items: [int], idx: int) -> bool:
2     val:int = 0           # Type is explicitly declared
3     val = items[idx]
4     return val == 0
5
6 mylist: [int] = None
7 mylist = [1, 0, 1]
8 print(is_zero(mylist, 1)) # Prints 'True'

```

Figure 1: ChocoPy program illustrating functions, variables, and static typing.

2.1 The top level

A ChocoPy program consists of zero or more definitions followed by one or more statements, referred to as top-level definitions and statements respectively. Top-level definitions include global variable definitions, function definitions, and class definitions. These definitions create new mappings in a scope called the *global scope*. Global variables are defined using the syntax `{id}:{type} = {literal}`, where the identifier specifies the variable name, the type annotation specifies the static type of the variable, and the constant literal specifies the initial value of the variable upon program execution. The names of global variables, global functions, and classes must be distinct. Top-level statements execute in the global scope; that is, expressions in top-level statements may reference entities defined in the global scope using identifiers. A ChocoPy program’s execution begins with the first top-level statement and ends when the last top-level statement is executed completely. Function and class definitions are described in Section 2.2 and Section 2.3 respectively. Program statements are described in Section 2.8.

2.2 Functions

In ChocoPy, a function definition can appear at the top level of a program, or it could be nested inside other functions or methods. Functions cannot be redefined in the same scope. However, a function definition in the current scope can shadow a function defined in a surrounding scope of the function. A function definition has the following form:

```

def {id}({id}: {type}, ..., {id}: {type}) {return type}:
    {declarations}
    {stmts}

```

where `{return type}` is either empty or has the form `-> {type}`.

The first line defines the function’s name, a comma-separated list of zero or more formal parameters in parentheses, and the function’s return type after the `{code-`}` symbol. When the return type is empty, the function may only return the value `None`. Every formal parameter has a name and a static type annotation. The body of a function contains a sequence of zero or more declarations followed by a sequence of one or more program statements. A function definition creates a new scope.

Declarations in a function body include local variable definitions, global and nonlocal variable declarations, and definitions of nested functions. A local variable definition has the form `{id}:{type} = {literal}`. Such a definition declares a local variable with the name `id`, explicitly associates it with a static type, and specifies an initial value using a literal. The `global {id}` statement is used to bind a name to a global variable. Similarly, `nonlocal {id}` statement is used within a nested function to bind a name to a variable defined in the closest surrounding scope that is not the global scope. It is illegal for a `global` declaration to occur at the top level. Similarly, it is illegal for a `nonlocal` declaration to occur outside a nested function.

If a variable is not explicitly declared in a function, but is bound to some entity—variable, function, or class—in any surrounding scope, then its binding is implicitly inherited from the surrounding scope as a read-only variable—such a variable cannot be assigned to in any of the function’s statements.

```

1 class animal(object):
2     makes_noise:bool = False
3
4     def make_noise(self: "animal") -> object:
5         if (self.makes_noise):
6             print(self.sound())
7
8     def sound(self: "animal") -> str:
9         return "???"
10
11 class cow(animal):
12     def __init__(self: "cow"):
13         self.makes_noise = True
14
15     def sound(self: "cow") -> str:
16         return "moo"
17
18 c:animal = None
19 c = cow()
20 c.make_noise()           # Prints "moo"

```

Figure 2: ChocoPy program illustrating classes, attributes, methods, and inheritance.

2.3 Classes

In ChocoPy, a class definition can appear at the top level of a program. Classes cannot be redefined. Class names can never be shadowed; that is, a program may not define any variable or function with the same name as a class name. A class definition has the following form:

```

class {id}({id}):
    {declarations}

```

The first line specifies the name of the class followed by the name of its *superclass* in parentheses. The class name must not be bound to any other entity—class, function, or variable—in the program. The superclass must refer to a class that has been previously defined in the program, or be the predefined class `object`. The superclass may not be one of `int`, `str`, or `bool`.

The class body consists of a sequence of attribute definitions and method definitions. In ChocoPy, attributes and methods are associated with object instances of a class, and not with the classes themselves; that is, ChocoPy does not support the notion of *static* class members that some other languages support. Similar to variable definitions, an attribute definition has the form `{id}:{type} = {literal}`. A method definition has the same syntax as a function definitions (ref. Section 2.2), with two important restrictions: (1) a method definition must have at least one formal parameter, and (2) the first formal parameter must have the defining class as type.

A class defines attributes and methods. A class inherits attributes and methods of its superclass. Attributes, whether defined in the current class or inherited from the superclass, cannot be redefined. Methods cannot be redefined in the same class. Inherited methods can be redefined as long as the return type and the types of all formal parameters except the first parameter are exactly the same. Any reference to an attribute or method must be prefixed with an expression and the dot operator (ref. Section 2.6).

If a class `C` is defined to have a superclass `P`, then class `C` is a subclass of `P`. If `C` is a subclass of `P`, then `P` must either be a user-defined class that has been defined before `C` in the program, or be the predefined class `object`. The `object` class does not have a superclass. Since every ChocoPy class (except `object`) inherits attributes and methods from a single superclass, this scheme is called *single inheritance*. The subclass/superclass relation on classes defines a graph. Since a class can only subclass another class defined previously, this graph is a tree with `object` as the root.

In order to create an object `o` of type `C`, the expression `C()` is used. Upon execution, a new object is first created with attributes initialized to their defined values. Then, the `__init__` method in the class `C` is

invoked. If `__init__` method is not defined in class `C`, then the inherited `__init__` method is called. The root class `object` has a default `__init__` method whose body is empty.

2.4 Type hierarchy

In ChocoPy, every class name is also a type. The basic type rule in ChocoPy is that if a method or variable expects a value of type `P`, then any value of type `C` may be used instead, provided that `P` is an ancestor of `C` in the class hierarchy. In other words, if `C` inherits from `P`, either directly or indirectly, then a `C` can be used wherever a `P` would suffice. When an object of type `C` may be used in place of an object of type `P`, we say that `C` conforms to `P` or that $C \leq P$ (think: `C` is lower down in the inheritance tree). Conformance of class types is defined in terms of the inheritance graph. Let `A`, `C`, and `P` be types. Then conformance (i.e. \leq) is defined as follows:

- $A \leq A$ for all types `A`
- if `C` is a subclass of `P`, then $C \leq P$
- if $A \leq C$ and $C \leq P$, then $A \leq P$

The root of the class hierarchy is the predefined class `object`. The predefined types `int`, `bool`, and `str` are subclasses of `object`. Additionally, for every type `T` in a ChocoPy program, there is a list type `[T]`, which represents a list whose elements are of type `T`. For example, the type `[int]` represents a list of integers. List types are recursive: the type `[[int]]` represents a list whose elements are each a list of integers. List types are not related to each other by the \leq relation. Every list type conforms to `object`; that is, $[T] \leq \text{object}$ for any type `T`.

In addition to types that one can denote in ChocoPy programs, there are two special types: the type of `None`, which we denote `<None>`, and the type of `[]`, which we denote as `<Empty>`. Because there is no way to explicitly write these type names in ChocoPy, no variable, parameter, or function return value ever has either of these types. In the type hierarchy, $\text{<None>} \leq \text{object}$, $\text{<Empty>} \leq \text{object}$, and as usual $\text{<None>} \leq \text{<None>}$ and $\text{<Empty>} \leq \text{<Empty>}$, but otherwise these types are unrelated to any other type.

To describe assignments and function invocation, we will need a slightly different relation, which we'll call *assignment compatibility* and denote by the symbol \leq_a . Roughly, the idea is that we may assign or pass a quantity of type `T1` to something of type `T2` iff $T_1 \leq_a T_2$. More precisely, $T_1 \leq_a T_2$ iff at least one of the following is true:

- $T_1 \leq T_2$ (i.e., ordinary subtyping).
- T_1 is `<None>` and T_2 is not `int`, `bool`, or `str`.
- T_2 is a list type `[T]` and T_1 is `<Empty>`.
- T_2 is a the list type `[T]` and T_1 is `[<None>]`, where $\text{<None>} \leq_a T$.

The last case bears mention: it is the only case in which two different list types are assignment compatible. It is convenient for writing such things as

```
x: [A] = [None, None]
```

It is rather limited, admittedly. For example,

```
x: [[A]] = [[None]]
```

is still invalid, although it looks perfectly sensible. There is subtle danger lurking here, and it turns out we must restrict the places where we may assign objects of type `[<None>]`, as described under the `MULTI-ASSIGN-STMT` rule in Section 5.

In some situations, we will also need to use the concept of a *join* of two or more types. The join of two types `A` and `B` is the least type `C` (using the \leq_a ordering) such that `A` and `B` are assignment compatible with `C`. The join operator \sqcup can be formally defined as follows: $C = A \sqcup B$ if and only if:

$$(A \leq_a C) \wedge (B \leq_a C) \wedge (\forall D : (A \leq_a D) \wedge (B \leq_a D) \Rightarrow (C \leq_a D))$$

That is, C is the join of A and B if and only if both A and B are assignment compatible with C , and if there exists type D such that A and B are assignment compatible with D , then C also is also assignment compatible with D . The join of any two types always exists and is unique:

- If $A \leq_a B$, then $A \sqcup B = B \sqcup A = B$.
- Otherwise, $A \sqcup B$ is simply the *least common ancestor* of A and B in the tree-like type hierarchy defined by \leq .

2.5 Values

In ChocoPy, we can have the following kinds of values.

2.5.1 Integers

Integers are signed and are represented using 32 bits. The range of integers is from -2^{31} to $(2^{31} - 1)$. Although integers are **objects**, they are immutable. Arithmetic operations that cause overflow lead to undefined behavior in program execution.

2.5.2 Booleans

There are exactly two boolean values: **True** and **False**.

2.5.3 Strings

Strings are immutable sequences of characters. String literals are delimited with double quotes, e.g. **"Hello World"**. Strings support the following three operations: retrieving the length via the **len** function, indexing via the **s[i]** syntax, and concatenation via the **s1 + s2** syntax. As in Python, ChocoPy does not have a character type. Indexing into a string returns a new string of length 1. Concatenation returns a new string with length equal to the sum of the lengths of its operands.

2.5.4 Lists

Lists are mutable sequences with a fixed length. As such, lists in ChocoPy behave more like arrays in C. A list can be constructed using the square-brackets notation, e.g. **[1, 2, 3]**.

Like strings, lists of type **[T]** support three operations: **len**, indexing via the **lst[i]** syntax, and concatenation via the **lst1 + lst2** syntax. Indexing a list of type **[T]** returns a value of type **T**. Concatenation of two lists of type **[T₁]** and **[T₂]** respectively returns a new list of type **[T₃]**, where the element type of the new list is $T_3 = T_1 \sqcup T_2$. The concatenated list has length equal to the sum of the lengths of the two operands. Additionally, lists of type **[T]** are mutable and support a fourth operation: element assignment via the syntax **lst[i] = {expr}**, where the expression on the right-hand side must conform to the type **T**.

The rules of ChocoPy permit the construction of some rather odd (but harmless) lists with types such as **[<None>]** and **[<Empty>]**. The only variables and parameters these may be assigned to or passed as have declared type **object**, since it is not possible to write the specific type names **[<None>]** and **[<Empty>]** in ChocoPy. It is even possible (if not particularly useful) to index such values.

2.5.5 Objects of user-defined classes

Objects are manipulated using references. That is, **x = cow()** implies that variable **x** references an object of type **cow**. A subsequent assignment **y = x** implies that **x** and **y** reference the *same* **cow** object in memory. The **is** operator can be used to determine if two expression reference the same object in memory. Objects are destroyed when they are not reachable from any local, global, or temporary variable.

2.5.6 None

None is a special value that can be assigned to a variable or attribute of type **object**, any user-defined class type, or any list type. The **is** operator can be used to determine if an expression evaluates to the **None** value. For type-checking purposes, it has the type **<None>** (see section 2.4).

2.5.7 The empty list ([])

The expression **[]** creates a list that can be assigned to a variable having type **object** or any list type. For type-checking purposes, it has type **<Empty>**.

2.6 Expressions

ChocoPy supports the following categories of expressions: literals, identifiers, arithmetic expressions, logical expressions, relational expressions, concatenation expressions, access expressions, and call expressions.

2.6.1 Literals and identifiers

The basic expression is a constant literal or a variable. Literals of type **str**, **bool**, and **int** have been described briefly in Section 2.5, and their lexical structure is described in Section 3.4. Variables evaluate to the value contained in the variable. If an identifier is bound to a global function or class, then it is not a valid expression by itself—it can appear only in specific expressions such as call expressions. This is because ChocoPy does not support first-class functions and classes.

2.6.2 List expressions

Lists may be constructed using a comma-separated sequence of expressions delimited by square brackets: **[{expr}, ...]**. The type of a list expression containing one or more elements is **[T]**, where **T** is the *least common ancestor* of the types of the list elements in the program's type hierarchy. In other words, **T** is the least type such that the type of each element expression conforms to **T**. Using the *join* operator \sqcup defined in Section 2.4, we can say that an expression of the form **[{expr}_1, {expr}_2, ..., {expr}_n]**, where each expression **{expr}_i** has the type **T_i**, results in a list of type **[T]** where **T** = **T_1** \sqcup **T_2** \sqcup ... \sqcup **T_n**.

The empty list expression **[]** has the special type **<Empty>**, which allows it to be assigned to (passed as) to a variable (parameter) of any list type. For example, if variable **x** has type **[int]**, then the assignment **x = []** is legal; **x** will contain an empty list of integers after this assignment.

2.6.3 Arithmetic expressions

ChocoPy supports the following arithmetic expressions on two operands each of type **int**: **{expr} + {expr}**, **{expr} - {expr}**, **{expr} * {expr}**, **{expr} // {expr}**, and **{expr} % {expr}**. These operators perform integer addition, subtraction, multiplication, division quotient, and division remainder, respectively. ChocoPy does not support the **{expr} / {expr}** expression, which in Python evaluates to a **float** value. The unary expression **-{expr}** evaluates to the negative of the integer-valued operand. Arithmetic operations return an **int** value.

2.6.4 Logical expressions

ChocoPy supports the following logical operations on operands of type **bool**: **not {expr}**, **{expr} and {expr}**, and **{expr} or {expr}**, which evaluate to the logical negation, conjunction, and disjunction of their operands, respectively. Logical expressions return a **bool** value. The binary logical expressions are also *short-circuiting*. If the left operand of an **and** expression evaluates to **False**, then a result of **False** is returned without evaluating the right operand at all. Similarly, if the left operand of an **or** expression evaluates to **True**, then a result of **True** is returned without evaluating the right operand at all. These semantics are important when the expressions in the right-hand side operands contain side-effects.

2.6.5 Relational expressions

ChocoPy supports the following relational expressions on operands of type `int`: `{expr} < {expr}`, `{expr} <= {expr}`, `{expr} > {expr}`, `{expr} >= {expr}`. Additionally, the operands in the expressions of the form `{expr} == {expr}` and `{expr} != {expr}` can be of types `int`, `bool`, or `str`, as long as both operands are of the same type. In contrast, the operands in the expressions of the form `{expr} is {expr}` can be the `None` literal or expressions of any static type other than `int`, `bool`, `str`. The `==` and `!=` operators return `true` if and only if their operands evaluate to respectively equal or unequal values of integers, booleans, or strings. The `is` operator returns `True` if and only if both operands evaluate to the same object or if both operands evaluate to `None`.

2.6.6 Conditional expressions

The expression `{expr1} if {expr0} else {expr2}` first evaluates `{expr0}`, which must have type `bool`. If the result is `True`, then `{expr1}` is evaluated and its result is the value of the expression. Otherwise, `{expr2}` is evaluated and its value is the value of the expression.

2.6.7 Concatenation expressions

The expression `{expr} + {expr}` can be used to concatenate two strings or two lists; the result is a new string or list, respectively.

2.6.8 Access expressions

An attribute of an object can be accessed using the dot operator: `{expr}.{id}`. For example, `x.y.z` returns the value stored in the attribute `z` of the object obtained by evaluating the expression `x.y`. An element of a string or list can be accessed using the index operator: `{expr}[{expr}]`. For example, `"Hello"[2+2]` returns the string `"o"`. Accessing a string or list `x` with an index `i` such that `i < 0` or `i >= len(x)` aborts the program with an appropriate error message.

2.6.9 Call expressions

A call expression is of the form `{id}({expr},...)`, where `{expr},...` is a comma-separated list of zero or more expressions provided as arguments to the call. If the identifier is bound to a globally declared function, the expression evaluates to the result of the function call. If the identifier is bound to a class, the expression results in the construction of a new object of that class, whose `__init__` method is invoked with the provided arguments.

An expression of the form `{expr}.{id}({expr},...)` invokes a method with name `{id}` on the object returned by evaluating the expression to the left of the dot operator. The first argument is implicit and is the object whose method is being invoked; the remaining arguments are explicitly provided in parentheses. Methods are invoked using dynamic dispatch: if the dynamic type of the object, i.e. the type at the time of execution, is `T`, then the method `{id}` defined in `T` or inherited by `T` is invoked.

2.7 Type annotations

In ChocoPy, static type annotations are used to explicitly provide types for variables, attributes, formal parameters and return types of functions and methods. A type annotation can either refer to a class type `T`, or a list type `[T]` such that `T` is the type annotation corresponding to the type of the elements of the list. Class-type annotations can be provided in one of two forms: as identifiers or as string literals containing the name of a class. In ChocoPy, one can use either of the two forms for annotations. However, in Python, the former form cannot be used to refer to a class type that has not yet been defined, because Python is interpreted line by line. Since we want ChocoPy to behave similarly as Python, we will use the latter form of annotation in the above described scenario. In particular, string literals are always needed in type annotations for the first formal parameter in method definitions, since the type of that parameter is always the same as the enclosing class, which is not yet fully defined.

2.8 Statements

2.8.1 Expression statements

The simplest statement is a standalone expression. The expression is evaluated and its result is discarded. These types of statements are useful when they have side-effects, e.g. `print("Hello")`.

2.8.2 Compound statements: conditionals and loops

ChocoPy supports the Python-like `if-elif-else` syntax for conditional control-flow, with `elifs` and `else` being optional:

The following code:

```
if {expr1}:
    {body1}
elif {expr2}:
    {body2}
elif {expr3}:
    {body3}
```

is equivalent to:

```
if {expr1}:
    {body1}
else:
    if {expr2}:
        {body2}
    else:
        if {expr3}:
            {body3}
```

The expressions in the `if` and `elif` conditions must have type `bool`. The body immediately following an `if` or `elif` condition is only evaluated if the expression evaluates to `True`. If the expression evaluates to `False`, then subsequent `elif` or `else` blocks are considered. The body following the `else` arm is only evaluated if all of the preceding condition expressions evaluate to `False`.

ChocoPy supports two types of loops: simple `while` loops and `for` loops over lists and strings. `while` loops have the following structure:

```
while {expr}:
    {body}
```

The expression must be of type `bool`. The body is repeatedly evaluated as long as the expression evaluates to `True` between iterations.

`for` loops can be used to iterate over elements of a list or characters of a string. They take the following form:

```
for x in {expr}:
    {body}
```

`for` loops are syntactic sugar; the structure above is equivalent to the following de-sugaring:

```
itr = {expr}
idx = 0
while idx < len(itr):
    x = itr[idx]
    {body}
    idx = idx + 1
```

where `len` is the predefined *length* function, and `itr/idx` are temporary variables that are not defined in the original scope. A `for` loop does not create new declarations for the loop variable (`x` in the above example); the loop variable must be declared before the `for` statement.

2.8.3 Assignment statements

An assignment statement can be one of the following three forms: (1) `{id} = {expr}` assigns a value to the variable bound to the identifier `{id}`, (2) `{expr}.{id} = {expr}` assigns a value to an attribute of an object, and (3) `{expr}[{expr}] = {expr}` assigns a value to an element of a list. When assigning a value to index `i` of a list `x`, if `i < 0` or `i >= len(x)` then the program aborts after printing an appropriate error message.

A single assignment may assign the same value to several different destinations. For example, the code `x = y.f = z[0] = 1` assigns the integer value 1 to three memory locations: (1) the variable `x`, (2) the attribute `f` of the object referenced by variable `y`, (3) and the first element of the list `z`, in that order. That is, the final expression (the *right-hand side*) is evaluated first. The result is then assigned to the *left-hand sides* (left of the `=` symbols, that is), evaluating these from left to right.

2.8.4 Pass statement

The `pass` statement is a no-op. The program state does not change and control flow simply continues on to the next statement.

2.8.5 Return statement

The `return` statement terminates the execution of a function and optionally returns a value using the `return {expr}` syntax. If a return value is not specified, then the `None` value is returned. It is illegal for a return statement to occur at the top level outside a function or method body. During a function's execution, if control flow reaches the end of the function body without encountering a `return` statement, then the `None` value is implicitly returned. Consider the following example:

```
def bar(x: int) -> object:
    if x > 0:
        return
    elif x == 0:
        return None
    else:
        pass
```

In function `bar`, the execution of the function can terminate either because (1) `x > 0` and a `return` statement with no return value is executed, or (2) `x == 0` and an explicit `return None` is executed, or (3) `x < 0` and the control flow reaches the end of the function, implicitly returning `None`.

In functions or methods that declare a return type of `int`, `str`, or `bool`, all execution paths must contain a `return` statement with an expression that is not a `None` literal. In class definitions, `__init__` methods must have an empty return type (indicating that they always return `None`).

2.8.6 Predefined classes and functions

The functions `print`, `input` and `len` are provided by the runtime.

print takes an argument of type `object`, and outputs its printed form to the standard output, returning the value `None`. The valid arguments are restricted to `str`, `int`, or `bool`. Other arguments cause the program to abort with an error message.

input takes no arguments and returns a value of type `str` by reading a line of input from the standard input.

len takes an argument `x` of type `object`, returning its length if it is a `str` or a list. Other arguments cause the program to abort with an error message.

The predefined classes `object`, `int`, `bool`, and `str` each define an `__init__` method. “Calling” these classes yield an empty object, the value 0, the value `False`, and the value `""` (empty string) respectively.

3 Lexical structure

This section describes the details required to implement a lexical analysis for ChocoPy. A lexical analysis reads an input file and produces a sequences of *tokens*. Tokens are matched in the input string using lexical rules that are expressed using regular expressions. Where ambiguity exists, a token comprises the longest possible string that forms a legal token, when read from left to right.

The following categories of tokens exist: line structure, identifiers, keywords, literals, operators, and delimiters.

3.1 Line structure

In ChocoPy, like in Python, whitespace may be significant both for terminating a statement and for reasoning about the indentation level of a program statement. To accommodate this, ChocoPy defines three lexical tokens that are derived from whitespace: `NEWLINE`, `INDENT`, and `DEDENT`. The rules for when such tokens are generated are described next using the concepts of physical and logical lines.

3.1.1 Physical lines

A physical line is a sequence of characters terminated by an end-of-line sequence. In source files and strings, the following line termination sequences can be used: the Unix form using ASCII LF (`\n`), the Windows form using the sequence ASCII CR LF (`\r\n`), or the old Macintosh form using the ASCII CR (`\r`) character. All of these forms can be used equally, regardless of platform. The end of input also serves as an implicit terminator for the final physical line.

3.1.2 Logical lines

A logical line is a physical line that contains at least one token that is not whitespace or comments. The end of a logical line is represented by the lexical token `NEWLINE`. Statements cannot cross logical line boundaries except where `NEWLINE` is allowed by the syntax (e.g., between statements in control-flow structures such as `while` loops).

3.1.3 Comments

A comment starts with a hash character (`#`) that is not part of a string literal, and ends at the end of the physical line. Comments are ignored by the lexical analyzer; they are not emitted as tokens.

3.1.4 Blank lines

A physical line that contains only spaces, tabs, and possibly a comment, is ignored (i.e., no `NEWLINE` token is generated).

3.1.5 Indentation

The description of indentation is borrowed from the Python 3 documentation¹.

“Leading whitespace (spaces and tabs) at the beginning of a logical line is used to compute the indentation level of the line, which in turn is used to determine the grouping of statements. Tabs are replaced (from left to right) by one to eight spaces such that the total number of characters up to and including the replacement is a multiple of eight (this is intended to be the same rule as used by Unix). The total number of spaces preceding the first non-blank character then determines the line’s indentation.”

“The indentation levels of consecutive lines are used to generate `INDENT` and `DEDENT` tokens, using a stack, as follows: Before the first line of the input program is read, a single zero is pushed on the stack; this will never be popped off again. The numbers pushed on the stack will always be strictly increasing from bottom to top. At the beginning of each logical line, the line’s indentation level is compared to the top of the stack. If it is equal, nothing happens. If it is larger, it is pushed on the stack, and one `INDENT` token is

¹https://docs.python.org/3/reference/lexical_analysis.html

generated. If it is smaller, it must be one of the numbers occurring on the stack; all numbers on the stack that are larger are popped off, and for each number popped off a `DEDENT` token is generated. At the end of the input program, a `DEDENT` token is generated for each number remaining on the stack that is larger than zero.”

3.1.6 Whitespace between tokens

Except at the beginning of a logical line or in string literals, the whitespace characters space and tab can be used interchangeably to separate tokens. Whitespace is needed between two tokens only if their concatenation could otherwise be interpreted as a different token (e.g., `ab` is one token, but `a b` is two tokens). Whitespace characters are not tokens; they are simply ignored.

3.2 Identifiers

Identifiers are defined as a contiguous sequence of characters containing the uppercase and lowercase letters A through Z, the underscore `_` and, except for the first character, the digits 0 through 9.

3.3 Keywords

The following strings are not recognized as identifiers, and are instead recognized as distinct keyword tokens:

`False`, `None`, `True`, `and`, `as`, `assert`, `async`, `await`, `break`, `class`, `continue`, `def`, `del`, `elif`, `else`, `except`, `finally`, `for`, `from`, `global`, `if`, `import`, `in`, `is`, `lambda`, `nonlocal`, `not`, `or`, `pass`, `raise`, `return`, `try`, `while`, `with`, `yield`.

Not all keywords have special meaning in ChocoPy. For example, ChocoPy does not support `async` or `await`. However, ChocoPy uses the same list of keywords as Python in order to avoid cases where an identifier is legal in ChocoPy but not in Python. Consequently, some keywords (such as `async`) do not appear anywhere in the grammar and will simply lead to a syntax error.

An identifier may contain a keyword as a substring; for example, `classic` is a valid identifier even though it contains the substring `class`. This follows from the longest match rule.

3.4 Literals

String and integer literals are matched at the lexical analysis stage and are represented by string-valued and integer-valued tokens, respectively. The structure of these literals is described below. Boolean literals `True` and `False` are represented simply by their keyword tokens.

3.4.1 String literals

String literals in ChocoPy are greatly simplified from that in Python. In ChocoPy, string literals are simply a sequence of ASCII characters delimited by (and including) double quotes: `"..."`. The ASCII characters must lie within the decimal range 32-126 inclusive—that is, higher than or equal to the *space* character and up to *tilde*. The string itself may contain double quotes escaped by a preceding backslash, e.g. `\"`.

Because string literals are used both for values and for type names, it is convenient to distinguish two categories: string literals whose content has the syntax of an identifier (`IDSTRING` in the syntax), and other string literals (denoted `STRING`).

The value of a string token is the sequence of characters between the delimiting double quotes, with any escape sequences applied. The following escape sequences are recognized: `\"`, `\n`, `\t`, `\\`, which correspond to a literal double quote, a newline, a tab, and a literal backslash respectively. Any other escape sequence is considered illegal. Some examples follow:

Literal	Value
<code>"Hello"</code>	<code>Hello</code>
<code>"He\"ll\"o"</code>	<code>He"ll"o</code>
<code>"He\\\\"llo"</code>	<code>He\\"llo</code>
<code>"Hell\o"</code>	(error: <code>"\o"</code> not recognized)

3.4.2 Integer literals

Integer literals in ChocoPy are composed of a sequence of one or more digits 0–9, where the leftmost digit may only be 0 if it is the only character in the sequence. That is, non-zero valued integer literals may not have leading zeros. The integer value of such literals is interpreted in base 10. The maximum interpreted value can be $2^{31} - 1$ for the literal 2147483647. A literal with a larger value than this limit results in a lexical error.

3.5 Operators and delimiters

The following is a space-separated list of symbols that correspond to distinct ChocoPy tokens: + - * // % < > <= >= == != = () [] , : . ->

4 Syntax

Figure 3 lists the grammar of ChocoPy using an extended BNF notation. Keyword tokens are represented in a **boldfaced font**. Literals and whitespace tokens are represented in UPPERCASE. Nonterminals are formatted *lowercase italics*. Operators and delimiters are formatted as-is. The notation $\llbracket \dots \rrbracket$ is used to group one or more symbols in a production rule and are not tokens in the input language. Symbols or groups may be annotated as follows: ‘?’ denotes that the preceding symbol or group is optional, ‘*’ denotes zero or more repeating occurrences and ‘+’ denotes one or more repeating occurrences.

The puzzling division of expressions into *expr* and *cexpr* captures the obscure point that ChocoPy (like Python) only allows logical binary or unary expressions as operands of logical operators (and, or, not). As a result, the expression `True == not False` is supposed to produce a syntax error (the correct expression being `True == (not False)`).

4.1 Precedence

Operators in ChocoPy have the same precedence as they do in Python. The following list summarizes the precedence of operators in ChocoPy, from lowest precedence (least binding) to highest precedence (most binding).

- `· if · else ·`
- `or`
- `and`
- `not`
- `==, !=, <, >, <=, >=, is`
- `+, -` (binary)
- `*, //, %`
- `-` (unary)
- `., []`

The arithmetic, comparison, and dot binary operators are left associative. The comparison operators are nonassociative (so ChocoPy, unlike Python 3, does not allow expressions such as `x < y < z`.)

```

program ::=  $\llbracket$ var_def | func_def | class_def $\rrbracket^*$  stmt*
class_def ::= class ID ( ID ) : NEWLINE INDENT class_body DEDENT
class_body ::= pass NEWLINE
              |  $\llbracket$ var_def | func_def $\rrbracket^*$ 

func_def ::= def ID (  $\llbracket$ typed_var  $\llbracket$ , typed_var $\rrbracket^*$  $\rrbracket^?$  )  $\llbracket$ -> type $\rrbracket^?$  : NEWLINE INDENT func_body DEDENT
func_body ::=  $\llbracket$ global_decl | nonlocal_decl | var_def | func_def $\rrbracket^*$  stmt+
typed_var ::= ID : type
            type ::= ID | IDSTRING | [ type ]
global_decl ::= global ID NEWLINE
nonlocal_decl ::= nonlocal ID NEWLINE
var_def ::= typed_var = literal NEWLINE
stmt ::= simple_stmt NEWLINE
        | if expr : block  $\llbracket$ elif expr : block  $\rrbracket^*$   $\llbracket$ else : block $\rrbracket^?$ 
        | while expr : block
        | for ID in expr : block
simple_stmt ::= pass
              | return  $\llbracket$ expr $\rrbracket^?$ 
              |  $\llbracket$ target =  $\rrbracket^+$  expr
block ::= NEWLINE INDENT stmt+ DEDENT
literal ::= None
           | True
           | False
           | INTEGER
           | IDSTRING | STRING
expr ::= cexpr
        | not expr
        | expr  $\llbracket$ and | or $\rrbracket$  expr
        | expr if expr else expr
cexpr ::= ID
         | literal
         | [  $\llbracket$ expr  $\llbracket$ , expr $\rrbracket^*$  $\rrbracket^?$  ]
         | ( expr )
         | member_expr
         | index_expr
         | member_expr (  $\llbracket$ expr  $\llbracket$ , expr $\rrbracket^*$  $\rrbracket^?$  )
         | ID (  $\llbracket$ expr  $\llbracket$ , expr $\rrbracket^*$  $\rrbracket^?$  )
         | cexpr bin_op cexpr
         | - cexpr
bin_op ::= + | - | * | // | % | == | != | <= | >= | < | > | is
member_expr ::= cexpr . ID
index_expr ::= cexpr [ expr ]
target ::= ID
          | member_expr
          | index_expr

```

Figure 3: Grammar describing the syntax of the ChocoPy language.

5 Type rules

This section formally defines the type rules of ChocoPy. The type rules define the type of every ChocoPy expression in a given context. The context is the type environment, which describes the type of every unbound identifier appearing in an expression. The type environment is described in Section 5.1. Section 5.2 gives the type rules.

5.1 Type environments

To a first approximation, type checking in ChocoPy can be thought of as a bottom-up algorithm: the type of an expression e is inferred from the (previously inferred) types of e 's sub-expression. For example, an integer 1 has type `int`; there are no sub-expression in this case. As another example, if the types of e_1 and e_2 are `int`, then the expression $e_1 > e_2$ has type `bool`.

A complication arises in the case of an expression v , where v is a variable or a function. It is not possible to say what the type of v is in a strictly bottom-up algorithm; we need to know the type declared for v in the larger expression. Such a declaration must exist for every variable and function in valid ChocoPy programs.

To capture information about the types of identifiers, we use a *type environment*. The type environment consists of four parts: O a local environment, M a method/attribute environment M , C the name of the current class in which the expression or statement appears, and R the return type of the function or method in which the expression or statement appears. C is \perp when the expression or statement appears outside a class, i.e. as a statement or expression in the top level. Similarly, M is \perp when the expression or statement appears outside a function or method, i.e. as a statement or expression in the top level. The local environment and the method/attribute environment are both maps. The local environment is a function of the form:

$$O(v) = T$$

which assigns the type T to a variable v . The same environment also holds information about function signatures. For example,

$$O(f) = \{\$ret : T_0, x_1 : T_1, \dots, x_n : T_n, v_1 : T'_1, \dots, v_m : T'_m\}$$

gives the “type” of f and denotes that identifier f has formal parameters x_1, \dots, x_n of types T_1, \dots, T_n , respectively, and has return type T_0 . The identifiers v_1, \dots, v_m are the variables and nested functions declared in the body of f and their types are T'_1, \dots, T'_m , respectively. The method/attribute environment similarly maps a class and its attributes and methods to their types. For example,

$$M(C, a) = T$$

maps the attribute a in the class C to the type T . Similarly,

$$M(C, m) = \{\$ret : T_0, x_1 : T_1, \dots, x_n : T_n, v_1 : T'_1, \dots, v_m : T'_m\}$$

maps the method m of class C to its type. Specifically, it denotes that method m in class C has formal parameters x_1, \dots, x_n of types T_1, \dots, T_n , respectively, and has return type T_0 . The identifiers v_1, \dots, v_m are the variables and nested functions declared in the body of m and their types are T'_1, \dots, T'_m , respectively.

The third component of the type environment is the name of the class containing the expression or statement to be type checked. The fourth component of the type environment is the return type R of the function or method containing the expression or statement to be type checked.

When type checking function and method definitions, we need to propagate the typing environment from an outer scope to the function scope, where the binding of any identifier is inherited unless the function declares a formal parameter, variable, or a nested function with the same name. Let O be the current local environment and f be a function with type definitions $\{\$ret : T_0, x_1 : T_1, \dots, x_n : T_n, v_1 : T'_1, \dots, v_m : T'_m\}$. When type checking the definition of f , we type check its body using the local environment $O[T_1/x_1][T_2/x_2] \dots [T_n/x_n][T'_1/v_1] \dots [T'_m/v_m]$, where the notation $O[T/c]$ is used to construct a new mapping as follows:

$$\begin{aligned} O[T/c](c) &= T \\ O[T/c](d) &= O(d) \text{ if } d \neq c \end{aligned}$$

5.2 Type checking rules

The general form of a type checking rule is:

$$\frac{\vdots}{O, M, C, R \vdash e : T}$$

The rule should be read: in the type environment with local environment O , method/attribute environment M , containing class C , and return type R , the expression e has type T . The line below the bar is a typing judgment: the turnstyle “ \vdash ” separates context (O, M, C, R) from a proposition $e : T$. The dots above the horizontal bar stand for other judgments about the types of sub-expressions of e . These other judgments are hypotheses of the rule; if the hypotheses are satisfied, then the judgment below the bar is true.

Variables. The rule for variables is simply that if the environment assigns an identifier id a type T , then the expression id has type T .

$$\frac{O(id) = T}{O, M, C, R \vdash id : T} \quad [\text{VAR-READ}]$$

Variable and Attribute Definitions and Assignments. This assignment rule—as well as others—uses the relation \leq_a (ref. Section 2.4). The rule says that the assigned expression e_1 must have a type T_1 that is assignment compatible with the type T of the identifier id in the type environment.

$$\frac{\begin{array}{l} O, M, C, R \vdash e_0 : T_0 \\ O, M, C, R \vdash e_1 : T_1 \\ T_1 \leq_a T_0 \end{array}}{O, M, C, R \vdash e_0 = e_1} \quad [\text{ASSIGN-STMT}]$$

Variable and attribute definitions obey a similar rule:

$$\frac{\begin{array}{l} O(id) = T \\ O, M, C, R \vdash e_1 : T_1 \\ T_1 \leq_a T \end{array}}{O, M, C, R \vdash id : T = e_1} \quad [\text{VAR-INIT}]$$

The colon used below the line in the rule for VAR-INIT is the colon in the syntax for type annotations.

Multiple assignment is similar, with a small twist.

$$\frac{\begin{array}{l} n > 1 \\ O, M, C, R \vdash e_0 : T_0 \\ O, M, C, R \vdash e_1 : T_1 \\ \vdots \\ O, M, C, R \vdash e_n : T_n \\ T_0 \neq [\text{<None>}] \\ \text{For all } 1 \leq i \leq n, T_0 \leq_a T_i \end{array}}{O, M, C, R \vdash e_1 = e_2 = \dots = e_n = e_0} \quad [\text{MULTI-ASSIGN-STMT}]$$

The restriction that $T_0 \neq [\text{<None>}]$ avoids a subtle type-safety issue. It is dangerous to allow there to be two different views of a list with differing element types. The type $[\text{<None>}]$ can only arise from list displays. As long as the value of such a display is immediately consumed by assignment to a single variable, parameter, or operand (+ for lists), there will be only be one opinion as to its type subsequently. But multiple assignment opens the possibility of programs like this:

```
x: [A] = None
y: [[int]] = None
x = y = [None]      # Trouble ahead!
x[0] = A()
print(y[0][0])      # ???
```

Java, for example, gets itself into this bind and therefore needs a runtime `ArrayStoreException`. To avoid it in ChocoPy, we conservatively forbid values of the type $[\text{<None>}]$ to be multiply assigned.

There is another very subtle point lurking here in the case where e_0 has type <Empty> (the type of the empty list). In this case, however, we need no special rule because in ChocoPy, there is no `.append` method to allow elements to be added to an empty list. Were that not the case, we could get this situation:

```
A: [int] = None
B: [str] = None
A = B = []
A.append(3)
```

and we'd subsequently have `B[0]` returning the value 3, which is certainly not a string.

Statement and Definition Lists. These type check if all the component definitions and statements type check.

$$\frac{\begin{array}{c} O, M, C, R \vdash s_1 \\ O, M, C, R \vdash s_2 \\ \vdots \\ O, M, C, R \vdash s_n \\ n \geq 1 \end{array}}{O, M, C, R \vdash s_1 \text{ NEWLINE } s_2 \text{ NEWLINE } \dots s_n \text{ NEWLINE}} \quad [\text{STMT-DEF-LIST}]$$

Pass Statements.

$$\frac{}{O, M, C, R \vdash \text{pass}} \quad [\text{PASS}]$$

Expression Statements.

$$\frac{O, M, C, R \vdash e : T}{O, M, C, R \vdash e} \quad [\text{EXPR-STMT}]$$

Literals.

$$\frac{}{O, M, C, R \vdash \text{False} : \text{bool}} \quad [\text{BOOL-FALSE}]$$

$$\frac{}{O, M, C, R \vdash \text{True} : \text{bool}} \quad [\text{BOOL-TRUE}]$$

$$\frac{i \text{ is an integer literal}}{O, M, C, R \vdash i : \text{int}} \quad [\text{INT}]$$

$$\frac{s \text{ is a string literal}}{O, M, C, R \vdash s : \text{str}} \quad [\text{STR}]$$

The `None` literal is assigned the (unmentionable) type `<None>`:

$$\frac{}{O, M, C, R \vdash \text{None} : \text{<None>}} \quad [\text{NONE}]$$

Arithmetic and Numerical Relational Operators.

$$\frac{O, M, C, R \vdash e : \text{int}}{O, M, C, R \vdash -e : \text{int}} \quad [\text{NEGATE}]$$

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : \text{int} \\ O, M, C, R \vdash e_2 : \text{int} \\ op \in \{+, -, *, //, \%\} \end{array}}{O, M, C, R \vdash e_1 op e_2 : \text{int}} \quad [\text{ARITH}]$$

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : \text{int} \\ O, M, C, R \vdash e_2 : \text{int} \\ \bowtie \in \{<, <=, >, >=, ==, !=\} \end{array}}{O, M, C, R \vdash e_1 \bowtie e_2 : \text{bool}} \quad [\text{INT-COMPARE}]$$

Logical Operators.

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : \text{bool} \\ O, M, C, R \vdash e_2 : \text{bool} \\ \bowtie \in \{==, !=\} \end{array}}{O, M, C, R \vdash e_1 \bowtie e_2 : \text{bool}} \quad [\text{BOOL-COMPARE}]$$

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : \text{bool} \\ O, M, C, R \vdash e_2 : \text{bool} \end{array}}{O, M, C, R \vdash e_1 \text{ and } e_2 : \text{bool}} \quad [\text{AND}]$$

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : \text{bool} \\ O, M, C, R \vdash e_2 : \text{bool} \end{array}}{O, M, C, R \vdash e_1 \text{ or } e_2 : \text{bool}} \quad [\text{OR}]$$

$$\frac{O, M, C, R \vdash e : \text{bool}}{O, M, C, R \vdash \text{not } e : \text{bool}} \quad [\text{NOT}]$$

Conditional Expressions.

$$\frac{\begin{array}{l} O, M, C, R \vdash e_0 : \text{bool} \\ O, M, C, R \vdash e_1 : T_1 \\ O, M, C, R \vdash e_2 : T_2 \end{array}}{O, M, C, R \vdash e_1 \text{ if } e_0 \text{ else } e_2 : T_1 \sqcup T_2} \quad [\text{COND}]$$

String Operations.

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : str \\ O, M, C, R \vdash e_2 : str \\ \bowtie \in \{==, !=\} \end{array}}{O, M, C, R \vdash e_1 \bowtie e_2 : bool} \quad [\text{STR-COMPARE}]$$

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : str \\ O, M, C, R \vdash e_2 : str \end{array}}{O, M, C, R \vdash e_1 + e_2 : str} \quad [\text{STR-CONCAT}]$$

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : str \\ O, M, C, R \vdash e_2 : int \end{array}}{O, M, C, R \vdash e_1[e_2] : str} \quad [\text{STR-SELECT}]$$

The ‘is’ Operator.

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : T_1 \\ O, M, C, R \vdash e_2 : T_2 \\ T_1, T_2 \text{ are not one of } int, str, bool \end{array}}{O, M, C, R \vdash e_1 \text{ is } e_2 : bool} \quad [\text{IS}]$$

Object Construction. If T is the name of a class, then object-construction expressions of that class can be typed as follows:

$$\frac{T \text{ is a class}}{O, M, C, R \vdash T() : T} \quad [\text{NEW}]$$

List Displays.

$$\frac{\begin{array}{l} n \geq 1 \\ O, M, C, R \vdash e_1 : T_1 \\ O, M, C, R \vdash e_2 : T_2 \\ \vdots \\ O, M, C, R \vdash e_n : T_n \\ T = T_1 \sqcup T_2 \sqcup \dots \sqcup T_n \end{array}}{O, M, C, R \vdash [e_1, e_2, \dots, e_n] : [T]} \quad [\text{LIST-DISPLAY}]$$

The empty list is a special case:

$$\frac{}{O, M, C, R \vdash [] : \langle \text{Empty} \rangle} \quad [\text{NIL}]$$

List Operators.

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : [T_1] \\ O, M, C, R \vdash e_2 : [T_2] \\ T = T_1 \sqcup T_2 \end{array}}{O, M, C, R \vdash e_1 + e_2 : [T]} \quad [\text{LIST-CONCAT}]$$

$$\frac{O, M, C, R \vdash e_1 : [T] \quad O, M, C, R \vdash e_2 : \text{int}}{O, M, C, R \vdash e_1[e_2] : T} \quad [\text{LIST-SELECT}]$$

Attribute Accesses. For attribute access, we use the class-member environment M :

$$\frac{O, M, C, R \vdash e_0 : T_0 \quad M(T_0, id) = T}{O, M, C, R \vdash e_0.id : T} \quad [\text{ATTR-READ}]$$

$$\frac{M(C, id) = T \quad O, M, C, R \vdash e_1 : T_1 \quad T_1 \leq_a T}{O, M, C, R \vdash id : T = e_1} \quad [\text{ATTR-INIT}]$$

Function Applications.

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : T_1'' \\ O, M, C, R \vdash e_2 : T_2'' \\ \vdots \\ O, M, C, R \vdash e_n : T_n'' \\ n \geq 0 \\ O(f) = \{\$ret : T_0, x_1 : T_1, \dots, x_n : T_n, v_1 : T_1', \dots, v_m : T_m'\} \\ \forall 1 \leq i \leq n : T_i'' \leq_a T_i \end{array}}{O, M, C, R \vdash f(e_1, e_2, \dots, e_n) : T_0} \quad [\text{INVOKE}]$$

To type check a function invocation, each of the arguments to the function must be first type checked. The type of each argument must conform to the types of the corresponding formal parameter of the function. The invocation expression is assigned the function's declared return type.

Method dispatch expressions are type checked in a similar fashion. The key difference from the function invocation expression is that the target method is determined by consulting the method/attribute environment using the type of the receiver object expression:

$$\frac{\begin{array}{l} O, M, C, R \vdash e_1 : T_1'' \\ O, M, C, R \vdash e_2 : T_2'' \\ \vdots \\ O, M, C, R \vdash e_n : T_n'' \\ n \geq 1 \\ M(T_1'', f) = \{\$ret : T_0, x_1 : T_1, \dots, x_n : T_n, v_1 : T_1', \dots, v_m : T_m'\} \\ T_1'' \leq_a T_1 \\ \forall 1 \leq 2 \leq n : T_i'' \leq_a T_i \end{array}}{O, M, C, R \vdash e_1.f(e_2, \dots, e_n) : T_0} \quad [\text{DISPATCH}]$$

Return Statements. This is where the return-type environment comes into play:

$$\frac{O, M, C, R \vdash e : T \quad T \leq_a R}{O, M, C, R \vdash \text{return } e} \quad [\text{RETURN-E}]$$

$$\frac{\langle \text{None} \rangle \leq_a R}{O, M, C, R \vdash \text{return}} \quad [\text{RETURN}]$$

Conditional Statements.

$$\frac{\begin{array}{l} O, M, C, R \vdash e_0 : \text{bool} \\ O, M, C, R \vdash b_0 \\ O, M, C, R \vdash e_1 : \text{bool} \\ O, M, C, R \vdash b_1 \\ \vdots \\ O, M, C, R \vdash e_n : \text{bool} \\ O, M, C, R \vdash b_n \\ n \geq 0 \\ O, M, C, R \vdash b_{n+1} \end{array}}{O, M, C, R \vdash \text{if } e_0 : b_0 \text{ elif } e_1 : b_1 \dots \text{ elif } e_n : b_n \text{ else } : b_{n+1}} \quad [\text{IF-ELIF-ELSE}]$$

While Statements.

$$\frac{\begin{array}{l} O, M, C, R \vdash e : \text{bool} \\ O, M, C, R \vdash b \end{array}}{O, M, C, R \vdash \text{while } e : b} \quad [\text{WHILE}]$$

For Statements.

$$\frac{\begin{array}{l} O, M, C, R \vdash e : \text{str} \\ O(id) = T \\ \text{str} \leq_a T \\ O, M, C, R \vdash b \end{array}}{O, M, C, R \vdash \text{for } id \text{ in } e : b} \quad [\text{FOR-STR}]$$

$$\frac{\begin{array}{l} O, M, C, R \vdash e : [T_1] \\ O(id) = T \\ T_1 \leq_a T \\ O, M, C, R \vdash b \end{array}}{O, M, C, R \vdash \text{for } id \text{ in } e : b} \quad [\text{FOR-LIST}]$$

Function Definitions. To type a function definition for f , we check the body of the function f in an environment where O is extended with bindings for the names explicitly declared by f .

$$\frac{\begin{array}{l} T = \begin{cases} T_0, & \text{if } \rightarrow \text{ is present,} \\ \langle \text{None} \rangle, & \text{otherwise.} \end{cases} \\ O(f) = \{ \$ret : T, x_1 : T_1, \dots, x_n : T_n, v_1 : T'_1, \dots, v_m : T'_m \} \\ n \geq 0 \quad m \geq 0 \\ O[T_1/x_1] \dots [T_n/x_n][T'_1/v_1] \dots [T'_m/v_m], M, C, T \vdash b \end{array}}{O, M, C, R \vdash \text{def } f(x_1 : T_1, \dots, x_n : T_n) \llbracket \rightarrow T_0 \rrbracket^? : b} \quad [\text{FUNC-DEF}]$$

$$\begin{array}{l}
T = \begin{cases} T_0, & \text{if } \rightarrow \text{ is present,} \\ \langle \text{None} \rangle, & \text{otherwise.} \end{cases} \\
O(C, f) = \{\$ret : T_0, x_1 : T_1, \dots, x_n : T_n, v_1 : T'_1, \dots, v_m : T'_m\} \\
n \geq 1 \quad m \geq 0 \\
C = T_1 \\
\frac{O[T_1/x_1] \dots [T_n/x_n][T'_1/v_1] \dots [T'_m/v_m], M, C, T \vdash b}{O, M, C, R \vdash \text{def } f(x_1 : T_1, \dots, x_n : T_n) \llbracket \rightarrow T_0 \rrbracket^? : b} \quad [\text{METHOD-DEF}]
\end{array}$$

Class Definitions. Class definitions are type checked by propagating the appropriate typing environment:

$$\frac{O, M, C, R \vdash b}{O, M, \perp, R \vdash \text{class } C(S) : b} \quad [\text{CLASS-DEF}]$$

The Global Typing Environment. The following functions and class methods are predefined globally:

$$\begin{aligned}
O(len) &= \{\$ret : int, arg : object\} \\
O(print) &= \{\$ret : object, arg : object\} \\
O(input) &= \{\$ret : str\} \\
M(object, _init_) &= \{\$ret : \langle \text{None} \rangle, self : object\} \\
M(str, _init_) &= \{\$ret : \langle \text{None} \rangle, self : object\} \\
M(int, _init_) &= \{\$ret : \langle \text{None} \rangle, self : object\} \\
M(bool, _init_) &= \{\$ret : \langle \text{None} \rangle, self : object\}
\end{aligned}$$

6 Operational semantics

This section contains the formal operational semantics for the ChocoPy language. The operational semantics define how every definition, statement, or expression in a ChocoPy program should be evaluated in a given context. The context has four components: a global environment, a local environment, a store, and a return value. Section 6.1 describes these components. Section 6.2 defines the syntax used to refer to ChocoPy values, and Section 6.3 defines the syntax used to refer to class definitions.

Keep in mind that a formal semantics is a specification only—it does not describe an implementation. The purpose of presenting the formal semantics is to make clear all the details of the behavior of a ChocoPy program. How this behavior is implemented is another matter.

6.1 Evaluation context

The value of a ChocoPy expression depends on the context in which it is evaluated. The context comprises of an *environment*, which maps variable identifiers to *locations*. Intuitively, an environment tells us for a given identifier the address of the memory location where that identifier’s value is stored. For a given expression, the environment must assign a location to all identifiers to which the expression may refer. For the expression $a + b$, we need an environment that maps a to some location and b to some location. We’ll use the following syntax to describe environments, which is very similar to the syntax of type environments defined in Section 5.1.

$$E = [a : l_1, b : l_2]$$

This environment maps variable a to location l_1 and variable b to location l_2 .

The second component of the evaluation context is the *store* (memory). The store maps locations to values, where values in ChocoPy are objects or functions. Intuitively, a store tells us what value is stored in a given memory location. For the moment, assume all values are integers. A store is similar to an environment:

$$S = [l_1 \mapsto 42, l_2 \mapsto 7]$$

This store maps location l_1 to the value 42 and the location l_2 to the value 7. Given an environment and a store, the value of a variable can be retrieved by first looking up the location of a variable in the environment E , and then looking up the value stored at this location in the store S . For example, the value of variable a can be looked up in the following way:

$$\begin{aligned} E(a) &= l_1 \\ S(l_1) &= 42 \end{aligned}$$

Together, the environment and the store define the execution state at a particular step of the evaluation of a ChocoPy program. The double indirection from identifiers to locations to values allows us to model variables. Consider what happens if the value 11 is assigned to variable a in the environment and store defined above. Assigning to a variable means changing the value to which it refers but not its location. To perform the assignment, we look up the location for a in the environment E and then change the mapping for the obtained location to the new value, giving a new store S' .

$$\begin{aligned} E(a) &= l_1 \\ S' &= S[11/l_1] \end{aligned}$$

Where the syntax $S' = S[v/l]$ denotes a new store S' that is identical to the store S , except that S' maps location l to value v . It is formally defined as follows:

$$\begin{aligned} S[v/l](l) &= v \\ S[v/l](l') &= S(l') \text{ if } l' \neq l \end{aligned}$$

There are also situations in which the environment is modified. Consider the definition of a variable in ChocoPy:

$$x : \text{int} = 36$$

When evaluating this definition, we must introduce a new identifier x into the environment, which will be valid for the rest of the scope in which definition occurs. If the current environment and store are E and S respectively, then the new environment and store after evaluating this definition are E' and S' respectively, which are defined by:

$$\begin{aligned} l_x &= \text{newloc}(S) \\ E' &= E[l_x/x] \\ S' &= S[36/l_x] \end{aligned}$$

The first step is to allocate a location for the variable x . The location should be fresh, meaning that the current store should not have a mapping for it. The function *newloc* applied to a store gives us an unused location in that store. We then create a new environment E' , which maps x to l_x but also contains all of the mappings of E for identifiers other than x . If x already has a mapping in E , the new environment E' hides this old mapping. We must also update the store to map the new location to a value. In this case l_x maps to the value 36, which is the initial value for x specified in the variable's definition.

The example in this subsection oversimplifies ChocoPy environments and stores a bit, because simple integers are not ChocoPy values. Even integers are full-fledged objects in ChocoPy.

In ChocoPy, the evaluation context consists of an additional component: a global environment G . G is an environment similar to E , but it always contains mappings for variables and functions defined at the global scope. This environment is useful for handling cases where a nested function references a global variable x via the `global x` declaration, bypassing any inherited mappings for variable x from the enclosing function.

6.2 Syntax for values

To describe ChocoPy semantics, we use the following categories of values: objects that are instances of classes, list objects, the `None` value, and functions (or methods).

6.2.1 Class instances

Let v be a value corresponding to an object belonging to class X . The value v is represented by the syntax:

$$v = X(a_1 = l_1, a_2 = l_2, \dots, a_n = l_n)$$

where each a_i for $1 \leq i \leq n$ is an attribute or method (including those inherited) of class X , and each l_i is the location where the value of attribute or method a_i is stored. Each a_i is distinct in a semantically valid ChocoPy program.

For base objects of ChocoPy (i.e., `int`, `str`, `bool`), we use a special case of the above syntax. Base objects have a class name, but their attributes are not like attributes of normal classes, because they cannot be modified. Therefore, we describe base objects using the following syntax:

$$\begin{aligned} &int(5) \\ &bool(True) \\ &str(7, \text{"ChocoPy"}) \end{aligned}$$

Integers and booleans contain just one component: the integer or boolean value respectively. Strings contain two components: a length and the actual sequence of ASCII characters.

6.2.2 List objects

A list object v of length n is represented by the syntax:

$$v = [l_0, l_1, \dots, l_{n-1}]$$

where each l_i is the element at index i .

6.2.3 None

The special value `None` is represented simply as `None`.

6.2.4 Functions

Functions are not first-class values in ChocoPy; that is, ChocoPy variables cannot store references to functions and ChocoPy expressions cannot evaluate to a function. However, functions are represented as values in the formal semantics and are the result of evaluating function and method definitions. Global functions, nested functions, and methods of classes are all represented by the same syntax, which is as follows:

$$v = (x_1, \dots, x_n, y_1 = e_1, \dots, y_k = e_k, b_{body}, E_f)$$

Here, v is a function having n formal parameters x_1, \dots, x_n and k local definitions y_1, \dots, y_k . Local definitions include local variables and nested functions. The term e_i represents the definition corresponding to the identifier y_i . For variable definitions, e_i is the literal expression that gives its initial value. For nested functions, e_i is the function definition itself. The term b_{body} is the function's body, which is a sequence of statements. The term E_f is the environment in which the function is defined, with appropriate substitutions for `global` declarations within the function.

6.3 Syntax for class definitions

When referring to class definitions, we need to use an additional notation. The mapping *class* is used to get the attributes and methods defined in a particular class. The syntax is as follows:

$$\text{class}(A) = (a_1 = e_1, \dots, a_m = e_m)$$

where each a_i is an attribute or method belonging to the class A (including inherited members). If a_i is an attribute, then the corresponding e_i is the literal expression that specifies the attribute's initial value. If a_i is a method name, then e_i is the corresponding method definition (which has the same syntax as a function definition).

For classes that inherit the method `__init__` from its definition in class `object`, we assume that the method body contains a single statement: `pass`.

6.4 Operational rules

Equipped with the notation for environments, stores, and the syntax for values and class definitions, we can now present the formal operational semantics rules for ChocoPy. The general form of a rule is:

$$\frac{\vdots}{G, E, S \vdash e : v, S', R'}$$

This rule should be read as follows: in a context with global environment G , local environment E , and store S , the program fragment e evaluates to value v , after which the new store is S' and the returned value is R' . Program fragments include expressions, definitions, statements, and sequences of statements. The value v will only be meaningful when e is an expression or function/method definition; in other cases, we represent the value v by the ‘ $_$ ’ (underscore) symbol to denote the absence of any value.

Literals.

$$\frac{}{G, E, S \vdash \text{None} : \text{None}, S, _} \quad [\text{NONE}]$$

$$\frac{}{G, E, S \vdash \text{False} : \text{bool}(\text{false}), S, _} \quad [\text{BOOL-FALSE}]$$

$$\frac{}{G, E, S \vdash \text{True} : \text{bool}(\text{true}), S, _} \quad [\text{BOOL-TRUE}]$$

$$\frac{i \text{ is an integer literal}}{G, E, S \vdash i : \text{int}(i), S, _} \quad [\text{INT}]$$

$$\frac{\begin{array}{l} s \text{ is a string literal} \\ n \text{ is the length of the string } s \end{array}}{G, E, S \vdash s : \text{str}(n, s), S, _} \quad [\text{STR}]$$

Pass Statements.

$$\frac{}{G, E, S \vdash \text{pass} : _, S, _} \quad [\text{PASS}]$$

Expression Statements. Here, we evaluate an expression, which may modify the store, and then discard its value:

$$\frac{G, E, S \vdash e : v, S', -}{G, E, S \vdash e : -, S', -} \quad [\text{EXPR-STMT}]$$

Variable Accesses. The values of variables involve finding their location in the environment and then reading or writing their values in the store.

$$\frac{\begin{array}{l} E(id) = l_{id} \\ S(l_{id}) = v \end{array}}{G, E, S \vdash id : v, S, -} \quad [\text{VAR-READ}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e : v, S_1, - \\ E(id) = l_{id} \\ S_2 = S_1[v/l_{id}] \end{array}}{G, E, S \vdash id = e : -, S_2, -} \quad [\text{VAR-ASSIGN-STMT}]$$

The last rule should be read as follows: the right-hand side of the assignment is first evaluated with the context $G, E, S, -$ to produce value v ; this evaluation may result in a modified store S_1 . After evaluating the variable assignment, the new store is S_2 , which is a modification of S_1 where the location l_{id} maps to the evaluated value of the right-hand-side: v .

Numerical Operations. These relate ChocoPy operators to corresponding mathematical operators.

$$\frac{\begin{array}{l} G, E, S \vdash e : \text{int}(i_1), S_1, - \\ v = \text{int}(-i_1) \end{array}}{G, E, S \vdash -e : v, S_1, -} \quad [\text{NEGATE}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e_1 : \text{int}(i_1), S_1, - \\ G, E, S \vdash e_2 : \text{int}(i_2), S_1, - \\ op \in \{+, -, *, //, \%\} \\ op \in \{//, \%\} \Rightarrow i_2 \neq 0 \\ v = \text{int}(i_1 \text{ op } i_2) \end{array}}{G, E, S \vdash e_1 \text{ op } e_2 : v, S_2, -} \quad [\text{ARITH}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e_1 : \text{int}(i_1), S_1, - \\ G, E, S_1 \vdash e_2 : \text{int}(i_2), S_2, - \\ \bowtie \in \{<, <=, >, >=, ==, !=\} \\ v = \begin{cases} \text{bool}(true) & \text{if } i_1 \bowtie i_2 \\ \text{bool}(false) & \text{otherwise} \end{cases} \end{array}}{G, E, S \vdash e_1 \bowtie e_2 : v, S_2, -} \quad [\text{INT-COMPARE}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e_1 : \text{bool}(b_1), S_1, - \\ G, E, S_1 \vdash e_2 : \text{bool}(b_2), S_2, - \\ \bowtie \in \{==, !=\} \\ v = \begin{cases} \text{bool}(true) & \text{if } b_1 \bowtie b_2 \\ \text{bool}(false) & \text{otherwise} \end{cases} \end{array}}{G, E, S \vdash e_1 \bowtie e_2 : v, S_2, -} \quad [\text{BOOL-COMPARE}]$$

String Operations.

$$\begin{array}{c}
G, E, S \vdash e_1 : \text{str}(n_1, s_1), S_1, - \\
G, E, S_1 \vdash e_2 : \text{str}(n_2, s_2), S_2, - \\
\bowtie \in \{=, !=\} \\
v = \begin{cases} \text{bool}(\text{true}) & \text{if } \bowtie \text{ is } = \text{ and } s_1 = s_2 \\ \text{bool}(\text{true}) & \text{if } \bowtie \text{ is } != \text{ and } s_1 \neq s_2 \\ \text{bool}(\text{false}) & \text{otherwise} \end{cases} \\
\hline
G, E, S \vdash e_1 \bowtie e_2 : v, S_2, - \quad [\text{STR-COMPARE}]
\end{array}$$

$$\begin{array}{c}
G, E, S \vdash e_1 : \text{str}(n_1, s_1), S_1, - \\
G, E, S_1 \vdash e_2 : \text{str}(n_2, s_2), S_2, - \\
v = \text{str}(n_1 + n_2, s_1.s_2) \quad \text{where } s_1.s_2 \text{ is the concatenated string} \\
\hline
G, E, S \vdash e_1 + e_2 : v, S_2, - \quad [\text{STR-CONCAT}]
\end{array}$$

$$\begin{array}{c}
G, E, S \vdash e_1 : \text{str}(n, c_1.c_2 \dots c_n), S_1, - \\
G, E, S_1 \vdash e_2 : \text{int}(i), S_2, - \\
0 \leq i < n \\
v = \text{str}(1, c_{i+1}) \\
\hline
G, E, S \vdash e_1[e_2] : v, S_2, - \quad [\text{STR-SELECT}]
\end{array}$$

Object Identity.

$$\begin{array}{c}
G, E, S \vdash e_1 : v_1, S_1, - \\
G, E, S_1 \vdash e_2 : v_2, S_2, - \\
v = \begin{cases} \text{bool}(\text{true}) & \text{if } v_1 = \text{None} \text{ and } v_2 = \text{None} \\ \text{bool}(\text{true}) & \text{if } v_1 \text{ and } v_2 \text{ are the same object in memory} \\ \text{bool}(\text{false}) & \text{otherwise} \end{cases} \\
\hline
G, E, S \vdash e_1 \text{ is } e_2 : v, S_2, - \quad [\text{IS}]
\end{array}$$

Logical Operators. The rule for the unary logical operator **not** is simple: the operand's value is negated. The binary logical operators perform short-circuit evaluation: if the result of logical conjunction or disjunction is apparent from evaluating the first operand (because the operand corresponds to **False** or **True** respectively), then the second operand is not evaluated at all. Otherwise, the result of the conjunction or disjunction is equal to the value of the second operand.

$$\begin{array}{c}
G, E, S \vdash e : \text{bool}(b), S_1, - \\
v = \begin{cases} \text{bool}(\text{false}) & \text{if } b = \text{true} \\ \text{bool}(\text{true}) & \text{otherwise} \end{cases} \\
\hline
G, E, S \vdash \text{not } e : v, S_1, - \quad [\text{NOT}]
\end{array}$$

$$\begin{array}{c}
G, E, S \vdash e_1 : \text{bool}(\text{false}), S_1, - \\
\hline
G, E, S \vdash e_1 \text{ and } e_2 : \text{bool}(\text{false}), S_1, - \quad [\text{AND-1}]
\end{array}$$

$$\begin{array}{c}
G, E, S \vdash e_1 : \text{bool}(\text{true}), S_1, - \\
G, E, S_1 \vdash e_2 : v, S_2, - \\
\hline
G, E, S \vdash e_1 \text{ and } e_2 : v, S_2, - \quad [\text{AND-2}]
\end{array}$$

$$\frac{G, E, S \vdash e_1 : \text{bool}(\text{true}), S_1, -}{G, E, S \vdash e_1 \text{ or } e_2 : \text{bool}(\text{true}), S_1, -} \quad [\text{OR-1}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e_1 : \text{bool}(\text{false}), S_1, - \\ G, E, S_1 \vdash e_2 : v, S_2, - \end{array}}{G, E, S \vdash e_1 \text{ or } e_2 : v, S_2, -} \quad [\text{OR-2}]$$

Conditional Statements and Expressions. conditional (**if-else** and **if-elif-else**) statements and conditional expressions are evaluated by first evaluating the condition, and then deciding which branch to evaluate. The body of a conditional statement may contain a **return** statement, which is propagated by the enclosing **if** statement as well.

$$\frac{\begin{array}{l} G, E, S \vdash e : \text{bool}(\text{true}), S_1, - \\ G, E, S_1 \vdash b_1 : -, S_2, R \end{array}}{G, E, S \vdash \text{if } e : b_1 \text{ else: } b_2 : -, S_2, R} \quad [\text{IF-ELSE-TRUE}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e : \text{bool}(\text{false}), S_1, - \\ G, E, S_1 \vdash b_2 : -, S_2, R \end{array}}{G, E, S \vdash \text{if } e : b_1 \text{ else: } b_2 : -, S_2, R} \quad [\text{IF-ELSE-FALSE}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e_0 : \text{bool}(\text{true}), S_1, - \\ G, E, S_1 \vdash b_0 : -, S_2, R \end{array}}{G, E, S \vdash \text{if } e_0 : b_0 \text{ elif } e_1 : b_1 \dots \text{ elif } e_n : b_n \text{ else: } b_{n+1} : -, S_2, R} \quad [\text{IF-ELIF-TRUE}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e_0 : \text{bool}(\text{false}), S_1, - \\ G, E, S_1 \vdash \text{if } e_1 : b_1 \dots \text{ elif } e_n : b_n \text{ else: } b_{n+1} : -, S_2, R \end{array}}{G, E, S \vdash \text{if } e_0 : b_0 \text{ elif } e_1 : b_1 \dots \text{ elif } e_n : b_n \text{ else: } b_{n+1} : -, S_2, R} \quad [\text{IF-ELIF-FALSE}]$$

$$\frac{G, E, S \vdash \text{if } e : b_1 \text{ else: } \text{pass} : -, S_1, R}{G, E, S \vdash \text{if } e : b_1 : -, S_1, R} \quad [\text{IF-NO-ELSE}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e : \text{bool}(\text{true}), S_1, - \\ G, E, S_1 \vdash b_1 : v, S_2, - \end{array}}{G, E, S \vdash b_1 \text{ if } e \text{ else } b_2 : v, S_2, -} \quad [\text{IF-ELSE-EXPR-TRUE}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e : \text{bool}(\text{false}), S_1, - \\ G, E, S_1 \vdash b_2 : v, S_2, - \end{array}}{G, E, S \vdash b_1 \text{ if } e \text{ else } b_2 : v, S_2, -} \quad [\text{IF-ELSE-EXPR-FALSE}]$$

While Loops. Evaluating a **while** loop first evaluates the condition. If the condition is false, the loop terminates. If the condition is true, then the loop body is executed and the **while** loop is then evaluated again unless the loop body returns a value.

$$\frac{G, E, S \vdash e : \text{bool}(\text{false}), S_1, -}{G, E, S \vdash \text{while } e : b : -, S_1, -} \quad [\text{WHILE-FALSE}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e : \text{bool}(\text{true}), S_1, - \\ G, E, S_1 \vdash b : -, S_2, - \\ G, E, S_2 \vdash \text{while } e : b : -, S_3, R \end{array}}{G, E, S \vdash \text{while } e : b : -, S_3, R} \quad [\text{WHILE-TRUE-LOOP}]$$

$$\frac{\begin{array}{l} G, E, S \vdash e : \text{bool}(\text{true}), S_1, - \\ G, E, S_1 \vdash b : -, S_2, R \\ R \text{ is not } - \end{array}}{G, E, S \vdash \text{while } e : b : -, S_2, R} \quad [\text{WHILE-TRUE-RETURN}]$$

Return Statements. **return** statements explicitly or implicitly set the return value R , which then propagates upward, preventing further execution until the nearest enclosing function call is reached.

$$\frac{G, E, S \vdash e : v, S_1, -}{G, E, S \vdash \text{return } e : -, S_1, v} \quad [\text{RETURN-E}]$$

$$\frac{}{G, E, S \vdash \text{return} : -, S_1, \text{None}} \quad [\text{RETURN}]$$

Statement Sequences. A sequence of statements is evaluated by evaluating each statement in turn, either until some statement returns a value or until the last statement in the sequence is evaluated.

$$\frac{\begin{array}{l} n \geq 0 \\ G, E, S_0 \vdash s_1 : -, S_1, - \\ G, E, S_1 \vdash s_2 : -, S_2, - \\ \vdots \\ G, E, S_{n-1} \vdash s_n : -, S_n, - \end{array}}{G, E, S_0 \vdash s_1 \text{ NEWLINE } s_2 \text{ NEWLINE } \dots s_n \text{ NEWLINE } : -, S_n, -} \quad [\text{STMT-SEQ}]$$

$$\frac{\begin{array}{l} n \geq 0 \\ G, E, S_0 \vdash s_1 : -, S_1, - \\ G, E, S_1 \vdash s_2 : -, S_2, - \\ \vdots \\ G, E, S_{k-1} \vdash s_k : -, S_k, R \\ k \leq n, \quad R \text{ is not } - \end{array}}{G, E, S_0 \vdash s_1 \text{ NEWLINE } s_2 \text{ NEWLINE } \dots s_n \text{ NEWLINE } : -, S_k, v} \quad [\text{STMT-SEQ-RETURN}]$$

Function Invocation and Method Dispatching. These are two of the three most complex operational rules (the other being object creation, [NEW]). First, simple function invocation.

$$\begin{array}{c}
S_0(E(f)) = (x_1, \dots, x_n, y_1 = e'_1, \dots, y_k = e'_k, b_{body}, E_f) \\
n, k \geq 0 \\
G, E, S_0 \vdash e_1 : v_1, S_1, - \\
\vdots \\
G, E, S_{n-1} \vdash e_n : v_n, S_n, - \\
l_{xi} = \text{newloc}(S_n), \text{ for } i = 1, \dots, n \text{ and each } l_{xi} \text{ is distinct} \\
l_{yi} = \text{newloc}(S_n), \text{ for } i = 1, \dots, k \text{ and each } l_{yi} \text{ is distinct} \\
E' = E_f[l_{x1}/x_1] \dots [l_{xn}/x_n][l_{y1}/y_1] \dots [l_{yk}/y_k] \\
G, E', S_n \vdash e'_1 : v'_1, S_n, - \\
\vdots \\
G, E', S_n \vdash e'_k : v'_k, S_n, - \\
S_{n+1} = S_n[v_1/l_{x1}] \dots [v_n/l_{xn}][v'_1/l_{y1}] \dots [v'_k/l_{yk}] \\
G, E', S_{n+1} \vdash b_{body} : -, S_{n+2}, R \\
R' = \begin{cases} \text{None, if } R \text{ is } - \\ R, \text{ otherwise} \end{cases} \\
\hline
G, E, S_0 \vdash f(e_1, \dots, e_n) : R', S_{n+2}, - \quad [\text{INVOKE}]
\end{array}$$

First, the function's value is fetched from the current store. Second, the arguments to the function call are evaluated in left-to-right order. Then, new locations are allocated for the function's formal parameters, local variables and nested functions. A new environment E' is created for the function call, which maps the formal parameters, local variables, and the names of nested functions to their corresponding locations. The store S_{n+1} maps these locations to their corresponding arguments, initial values, and function values respectively. Finally, the body of the function is evaluated with this new environment E' and initial state S_{n+1} . The function invocation expression evaluates to the value returned by the function body, or the value **None** if the function body was completely evaluated without encountering a **return** statement.

$$\begin{array}{c}
G, E, S \vdash e_0 : v_0, S_0, - \\
v_0 = X(a_1 = l_1, \dots, f = l_f, \dots, a_m = l_m) \\
S_0(l_f) = (x_0, x_1, \dots, x_n, y_1 = e'_1, \dots, y_k = e'_k, b_{body}, E_f) \\
n, k \geq 0 \\
G, E, S_0 \vdash e_1 : v_1, S_1, - \\
\vdots \\
G, E, S_{n-1} \vdash e_n : v_n, S_n, - \\
l_{xi} = \text{newloc}(S_n), \text{ for } i = 0, \dots, n \text{ and each } l_{xi} \text{ is distinct} \\
l_{yi} = \text{newloc}(S_n), \text{ for } i = 1, \dots, k \text{ and each } l_{yi} \text{ is distinct} \\
E' = E_f[l_{x0}/x_0] \dots [l_{xn}/x_n][l_{y1}/y_1] \dots [l_{yk}/y_k] \\
G, E', S_n \vdash e'_1 : v'_1, S_n, - \\
\vdots \\
G, E', S_n \vdash e'_k : v'_k, S_n, - \\
S_{n+1} = S_n[v_0/l_{x0}] \dots [v_n/l_{xn}][v'_1/l_{y1}] \dots [v'_k/l_{yk}] \\
G, E', S_{n+1} \vdash b_{body} : -, S_{n+2}, R \\
R' = \begin{cases} \text{None, if } R \text{ is } - \\ R, \text{ otherwise} \end{cases} \\
\hline
G, E, S \vdash e_0.f(e_1, \dots, e_n) : R', S_{n+2}, - \quad [\text{DISPATCH}]
\end{array}$$

The rule for dynamic dispatch is similar to the rule for function invocation, with two main differences: (1) the target method is determined by first evaluating the object expression and then retrieving the function

value that the method slot in the resulting object maps to; (2) the object itself is passed as the first argument to the method, before any of the arguments in the method-call expression.

Function Definitions. Function definitions result in the creation of function values. The rule is exactly the same for the definition of a globally defined function, a nested function, or a method defined in a class:

$$\frac{\begin{array}{l} g_1, \dots, g_L \text{ are the variables explicitly declared as global in } f \\ y_1 = e_1, \dots, y_k = e_k \text{ are the local variables and nested functions defined in } f \\ E_f = E[G(g_1)/g_1] \dots [G(g_L)/g_L] \\ v = (x_1, \dots, x_n, y_1 = e_1, \dots, y_k = e_k, b_{body}, E_f) \end{array}}{G, E, S \vdash \mathbf{def } f(x_1:T_1, \dots, x_n:T_n) \llbracket \rightarrow T_0 \rrbracket^? : b : v, S, -} \quad [\text{FUNC-METHOD-DEF}]$$

The function value captures the environment E in which it is defined. This allows a nested function to refer to local variables and functions defined in enclosing scopes. The captured environment E is slightly modified as E_f , which overrides the mapping for variables explicitly declared as global within the function's body using the `global` declaration. This modification allows a nested function to reference a global variable even if there exists a local variable defined with the same name in an enclosing scope.

Accessing Class Attributes. The rules for accessing class attributes are relatively simpler:

$$\frac{\begin{array}{l} G, E, S_0 \vdash e : v_1, S_1, - \\ v_1 = X(a_1 = l_1, \dots, id = l_{id}, \dots, a_m = l_m) \\ v_2 = S_1(l_{id}) \end{array}}{G, E, S_0 \vdash e.id : v_2, S_1, -} \quad [\text{ATTR-READ}]$$

$$\frac{\begin{array}{l} G, E, S_0 \vdash e_2 : v_r, S_1, - \\ G, E, S_1 \vdash e_1 : v_l, S_2, - \\ v_l = X(a_1 = l_1, \dots, id = l_{id}, \dots, a_m = l_m) \\ S_3 = S_2[v_r/l_{id}] \end{array}}{G, E, S_0 \vdash e_1.id = e_2 : -, S_3, -} \quad [\text{ATTR-ASSIGN-STMT}]$$

In the rule for attribute assignment, the expression on the right-hand side is evaluated before the expression on the left-hand side.

Object Instantiation. This is the only rule that uses the syntax for class definitions described in Section 6.3:

$$\begin{array}{l}
class(T) = (a_1 = e_1, \dots, a_m = e_m) \quad m \geq 1 \\
l_{ai} = newloc(S), \text{ for } i = 1, \dots, m \text{ and each } l_{ai} \text{ is distinct} \\
v_0 = T(a_1 = l_{ai}, \dots, a_m = l_{am}) \\
G, G, S \vdash e_1 : v_1, S, - \\
G, G, S \vdash e_2 : v_2, S, - \\
\vdots \\
G, G, S \vdash e_m : v_m, S, - \\
S_1 = S[v_1/l_{a1}] \dots [v_m/l_{am}] \\
l_{init} = l_{ai} \text{ such that } a_i = \text{--init--} \\
S_1(l_{init}) = (x_0, y_1 = e'_1, \dots, y_k = e'_k, b_{body}, E_f) \quad k \geq 0 \\
l_{x0} = newloc(S_1) \\
l_{yi} = newloc(S_1), \text{ for } i = 1, \dots, k \text{ and each } l_{yi} \text{ is distinct} \\
E' = E_f[l_{x0}/x_0][l_{y1}/y_1] \dots [l_{yk}/y_k] \\
G, E, S_1 \vdash e'_1 : v'_1, S_1, - \\
\vdots \\
G, E, S_1 \vdash e'_k : v'_k, S_1, - \\
S_2 = S_1[v_0/l_{x0}][v'_1/l_{y1}] \dots [v'_k/l_{yk}] \\
G, E', S_2 \vdash b_{body} : -, S_3, - \\
\hline
G, E, S \vdash T() : v_0, S_3, - \quad \text{[NEW]}
\end{array}$$

This rule performs the following operations. First, a new object v_0 with class T is created by allocating locations for each attribute and method that is defined or inherited by class T . Second, the attribute initializers and method definitions are evaluated using the *global environment*; this distinction is important since method definitions do not capture the environment E in which the object is being constructed. Third, a new store S_1 is created by modifying the current store S with mappings for the newly allocated attributes and methods of v_0 . Finally, the `--init--` method of the object v_0 is invoked via dynamic dispatch. The steps required to invoke this method are similar to that of general dynamic dispatch, with the exception that the `--init--` method does not accept any arguments apart from the object on which it is invoked.

List Displays. A list display creates a sequence of new locations in the store, which house the values of the list elements.

$$\begin{array}{l}
n \geq 0 \\
G, E, S_0 \vdash e_1 : v_1, S_1, - \\
G, E, S_1 \vdash e_2 : v_2, S_2, - \\
\vdots \\
G, E, S_{n-1} \vdash e_n : v_n, S_n, - \\
l_i = newloc(S_n), \text{ for } i = 1, \dots, n \text{ and each } l_i \text{ is distinct} \\
v = [l_1, l_2, \dots, l_n] \\
S_{n+1} = S_n[v_1/l_1][v_2/l_2] \dots [v_n/l_n] \\
\hline
G, E, S_0 \vdash [e_1, e_2, \dots, e_n] : v, S_{n+1}, - \quad \text{[LIST-DISPLAY]}
\end{array}$$

Operations on Lists. The rules for list selection, concatenation, and element update all use the locations corresponding to list elements and the values they map to in the store.

$$\begin{array}{c}
G, E, S_0 \vdash e_1 : v_1, S_1, - \\
G, E, S_1 \vdash e_2 : \text{int}(i), S_2, - \\
v_1 = [l_1, l_2, \dots, l_n] \\
0 \leq i < n \\
v_2 = S_2(l_{i+1}) \\
\hline
G, E, S_0 \vdash e_1[e_2] : v_2, S_2, - \quad [\text{LIST-SELECT}]
\end{array}$$

$$\begin{array}{c}
G, E, S_0 \vdash e_1 : v_1, S_1, - \\
G, E, S_1 \vdash e_2 : v_2, S_2, - \\
v_1 = [l_1, l_2, \dots, l_n] \\
v_2 = [l'_1, l'_2, \dots, l'_m] \\
n, m \geq 0 \\
l''_i = \text{newloc}(S_2), \text{ for } i = 1, \dots, (m+n) \text{ and each } l''_i \text{ is distinct} \\
v_3 = [l''_1, l''_2, \dots, l''_{n+m}] \\
S_3 = S_2[S_2(l_1)/l''_1] \dots [S_2(l_n)/l''_n][S_2(l'_1)/l''_{n+1}] \dots [S_2(l'_m)/l''_{n+m}] \\
\hline
G, E, S_0 \vdash e_1 + e_2 : v_3, S_3, - \quad [\text{LIST-CONCAT}]
\end{array}$$

$$\begin{array}{c}
G, E, S_0 \vdash e_3 : v_r, S_1, - \\
G, E, S_1 \vdash e_1 : v_l, S_2, - \\
G, E, S_2 \vdash e_2 : \text{int}(i), S_3, - \\
v_l = [l_1, l_2, \dots, l_n] \\
0 \leq i < n \\
S_4 = S_3[v_r/l_{i+1}] \\
\hline
G, E, S_0 \vdash e_1[e_2] = e_3 : -, S_4, - \quad [\text{LIST-ASSIGN-STMT}]
\end{array}$$

In the last rule, the expression on the right-hand side of the assignment operator is evaluated before the expressions on the left-hand side.

Multiple Assignment. We can describe multiple assignments by a kind of rewriting, breaking them down into a sequence of simple assignments and taking care to evaluate the right-hand side exactly once.

$$\begin{array}{c}
n > 1 \\
l = \text{newloc}(S) \\
X \text{ is a unique identifier not in the program} \\
G, E, S \vdash e_0 : v, S', - \\
G, E[l/X], S'[v/l] \vdash e_1 = X \text{ NEWLINE } e_2 = X \text{ NEWLINE } \dots e_n = X : -, S'', - \\
\hline
G, E, S \vdash e_1 = e_2 = \dots = e_n = e_0 : -, S'', - \quad [\text{MULTI-ASSIGN-STMT}]
\end{array}$$

Predefined Functions. The predefined functions `print` and `input` perform IO.

$$\begin{array}{c}
G, E, S \vdash e : v, S_1, - \\
v = \text{int}(i) \text{ or } v = \text{bool}(b) \text{ or } v = \text{str}(n, s) \\
\hline
G, E, S \vdash \text{print}(e) : \text{None}, S_1, - \quad [\text{PRINT}]
\end{array}$$

$$\begin{array}{c}
s \text{ is a user-provided input string of length } n \\
v = \text{str}(n, s) \\
\hline
G, E, S \vdash \text{input}() : v, S, - \quad [\text{INPUT}]
\end{array}$$

The predefined function `len` retrieves the length of a list or a string.

$$\frac{\begin{array}{l} G, E, S_0 \vdash e : v, S_1, - \\ v = [l_1, l_2, \dots, l_n] \\ n \geq 0 \end{array}}{G, E, S_0 \vdash \text{len}(e) : \text{int}(n), S_1, -} \quad [\text{LEN-LIST}]$$

$$\frac{\begin{array}{l} G, E, S_0 \vdash e : v, S_1, - \\ v = \text{str}(n, s) \end{array}}{G, E, S_0 \vdash \text{len}(e) : \text{int}(n), S_1, -} \quad [\text{LEN-STR}]$$

For Loops. The rules for `for` loops on lists and strings update the store after each iteration to map the loop variable's location to a value corresponding to a list element or substring respectively. In each case, we have a special version for early termination due to a return from the loop body.

$$\frac{\begin{array}{l} G, E, S_0 \vdash e : v, S'_0, - \\ v = [l_1, l_2, \dots, l_n] \\ n \geq 0 \\ l_{id} = E(id) \\ S_1 = S'_0[S'_0(l_1)/l_{id}] \\ G, E, S_1 \vdash b : -, S'_1, - \\ S_2 = S'_1[S'_1(l_2)/l_{id}] \\ G, E, S_2 \vdash b : -, S'_2, - \\ \vdots \\ S_n = S'_{n-1}[S'_{n-1}(l_n)/l_{id}] \\ G, E, S_n \vdash b : -, S'_n, - \end{array}}{G, E, S_0 \vdash \text{for } id \text{ in } e : b : -, S'_n, -} \quad [\text{FOR-LIST}]$$

$$\frac{\begin{array}{l} G, E, S_0 \vdash e : v_l, S'_0, - \\ v_l = [l_1, l_2, \dots, l_n] \\ n \geq 0 \\ l_{id} = E(id) \\ S_1 = S'_0[S'_0(l_1)/l_{id}] \\ G, E, S_1 \vdash b : -, S'_1, - \\ S_2 = S'_1[S'_1(l_2)/l_{id}] \\ G, E, S_2 \vdash b : -, S'_2, - \\ \vdots \\ S_k = S'_{k-1}[S'_{k-1}(l_k)/l_{id}] \\ G, E, S_k \vdash b : -, S'_k, R \\ 1 \leq k \leq n \quad R \text{ is not } - \end{array}}{G, E, S_0 \vdash \text{for } id \text{ in } e : b : -, S'_k, R} \quad [\text{FOR-LIST-RETURN}]$$

$$\begin{array}{c}
G, E, S_0 \vdash e : v, S'_0, - \\
v = \text{str}(n, c_1.c_2 \dots c_n) \\
n \geq 0 \\
l_{id} = E(id) \\
S_1 = S'_0[\text{str}(1, c_1)/l_{id}] \\
G, E, S_1 \vdash b : -, S'_1, - \\
S_2 = S'_1[\text{str}(1, c_2)/l_{id}] \\
G, E, S_2 \vdash b : -, S'_2, - \\
\vdots \\
S_n = S'_{n-1}[\text{str}(1, c_n)/l_{id}] \\
G, E, S_n \vdash b : -, S'_n, - \\
\hline
G, E, S_0 \vdash \text{for } id \text{ in } e : b : -, S'_n, - \quad [\text{FOR-STR}]
\end{array}$$

$$\begin{array}{c}
G, E, S_0 \vdash e : v_s, S'_0, - \\
v_s = \text{str}(n, c_1.c_2 \dots c_n) \\
n \geq 0 \\
l_{id} = E(id) \\
S_1 = S'_0[\text{str}(1, c_1)/l_{id}] \\
G, E, S_1 \vdash b : -, S'_1, - \\
S_2 = S'_1[\text{str}(1, c_2)/l_{id}] \\
G, E, S_2 \vdash b : -, S'_2, - \\
\vdots \\
S_k = S'_{k-1}[\text{str}(1, c_k)/l_{id}] \\
G, E, S_k \vdash b : -, S'_k, R \\
1 \leq k \leq n \quad R \text{ is not } - \\
\hline
G, E, S_0 \vdash \text{for } id \text{ in } e : b : -, S'_k, R \quad [\text{FOR-STR-RETURN}]
\end{array}$$

Programs. Finally, the rule for evaluating a ChocoPy program involves first initializing a global environment and the initial store with globally defined variables and functions, and then evaluating the sequence of top-level statements. Let \emptyset represent an empty mapping. Then, the top-level rule is:

$$\begin{array}{c}
g_1 = e_1, \dots, g_k = e_k \text{ are the global variable and function definitions in the program} \\
P \text{ is the sequence of statements in the program} \\
l_{gi} = \text{newloc}(\emptyset) \text{ for } i = 1, \dots, k \text{ and each } l_{gi} \text{ is distinct} \\
G = \emptyset[l_{g1}/g_1] \dots [l_{gk}/g_k] \\
G, G, \emptyset \vdash e_1 : v_1, \emptyset, - \\
\vdots \\
G, G, \emptyset \vdash e_k : v_k, \emptyset, - \\
S = \emptyset[v_k/l_{g1}] \dots [v_k/l_{gk}] \\
G, G, S \vdash P : -, S', - \\
\hline
\emptyset, \emptyset, \emptyset \vdash P : -, S', - \quad [\text{PROGRAM}]
\end{array}$$

When no valid rule can be applied to a given expression, the program aborts after printing an appropriate error message. Due to the myriad of semantic checks and typing rules enforced at compile-time, the set of errors that can occur at run-time is limited. The following is the standard set of run-time errors that can occur during the execution of a ChocoPy program:

1. Invalid argument (during invocation of `print` or `len`)

2. Division by zero
3. Index out of bounds (during string selection or list element access)
4. Operation on `None` (during method dispatch, attribute access, or list operations)
5. Out of memory (when allocating a new object)

The operational semantics do not specify what happens in the event of arithmetic integer overflow. This manual only specifies semantics for signed integer arithmetic that fits within 32 bits. Overflow is considered undefined behavior, and implementations may handle such situations in any manner of their choosing.

7 Acknowledgements

ChocoPy is a dialect of Python, version 3.6. The set of Python language features to include in ChocoPy were influenced by Cool (Classroom Object-Oriented Language), which itself is based on Sather164, a dialect of the Sather language. This language manual is largely based off the Cool reference manual.

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A Known incompatibilities with Python

The following are the known cases where a valid ChocoPy program either does not correspond to a valid Python program, or has different semantics:

- Python 3 does not allow forward references to classes that have not yet been defined. For example, the variable definition `x:A = None` is invalid in Python if this line appears before the class `A` has been completely defined. In ChocoPy, this is valid as long as the class `A` is defined anywhere in the program. A compromise is to use quoted type annotations: the syntax `x:"A" = None` is valid in both ChocoPy and Python, and has exactly the same meaning. In Python 3.7, forward references can be enabled by running `from __future__ import annotations`².
- Since integer overflow leads to undefined behavior in ChocoPy, there is no compatibility with Python when dealing with integer values less than 2^{31} or at least as large as 2^{31} .

²PEP 563 mentions that forward references will be allowed by default in Python 4.0.