

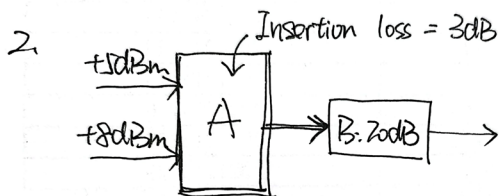
1. Delay distortion is one of the most significant impairments in transmission systems.
 - a) Present the reason of the occurrence of delay distortion. [50%]
 - b) Analysis the effects of delay distortion and the possible solutions to alleviate them, respectively. [50%]

1. a) Since ~~the~~ different components in the signal propagate at different speeds during transmission, it results in different arrival times at the receiver.

b) Effects: Some of the ~~signals~~ signal components of one bit position will spill over into other bit positions, causing intersymbol interference.

Equalizing techniques can alleviate them

2. Assume that a transmission system consists of two components A and B, A has two input ports with signal levels of 5 dBm and 8 dBm respectively, and the insertion loss of A is 3dB.
 - a) How many mW is the output signal of A? [50%]
 - b) If the output port of A is the input port of B, and the B has a gain of 20dB, how many W is the output signal of B? [50%]



a) $P_1 = \cancel{+5} + 5 \text{ dBm} = 10^{0.5} \text{ mW} = \cancel{3.16} 3.162 \text{ mW}$

$P_2 = +8 \text{ dBm} = 10^{0.8} \text{ mW} = 6.310 \text{ mW}$

Input power $P_i = P_1 + P_2 = 9.472 \text{ mW} = \cancel{9.764 \text{ dBm}}$

$10 \log(9.472 \text{ mW}) = \cancel{9.764} 9.764 \text{ dBm}$

Out power $P_o = P_i - 3 \text{ dB} = 6.764 \text{ dBm}$

b) $P_1 = 6.764 \text{ dBm}$

Output signal of B is: $P_2 = P_1 + 20 \text{ dB} = 26.764 \text{ dBm}$

3. Given that a company is deploying a metal cable as a transmission line, and the electrical properties are $58\Omega/\text{km}$, $34\mu\text{S}/\text{km}$, $48\text{nF}/\text{km}$, $0.37\text{mH}/\text{km}$. If the signal frequency is 60MHz .
- Calculate the characteristic impedance of this cable?
 - Calculate the propagation constant of this cable?

3. a) $R = 58\Omega/\text{km}$ $G = 34\mu\text{S}/\text{km}$ $L = 0.37\text{mH}/\text{km}$
 $C = 48\text{nF}/\text{km}$

Since $f = 60\text{MHz}$ is very high, so $Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}} \approx \sqrt{\frac{L}{C}}$
 the frequency

$$Z_0 = \sqrt{\frac{L}{C}} = \sqrt{\frac{0.37 \times 10^{-3}}{48 \times 10^{-9}}} = 87.81\Omega$$

b) Propagation constant: $\gamma = \sqrt{(R + j\omega L)(G + j\omega C)} = \alpha + j\beta$
 Since $f = 60\text{MHz} > 30\text{kHz}$.

$$\alpha = \left(\frac{R}{2} \sqrt{\frac{C}{L}} + \frac{G}{2} \sqrt{\frac{L}{C}} \right) (\text{Np}/\text{km})$$

$$\beta = \omega \sqrt{LC} \text{ (rad/km)}$$

$$\omega = 2\pi f = 3.77 \times 10^8 \text{ rad/s}$$

$$\alpha = \left(\frac{58}{2} \sqrt{\frac{48 \times 10^{-9}}{0.37 \times 10^{-3}}} + \frac{34 \times 10^{-6}}{2} \sqrt{\frac{0.37 \times 10^{-3}}{48 \times 10^{-9}}} \right) = 0.33 (\text{Np}/\text{km})$$

$$\beta = 3.77 \times 10^8 \cdot \sqrt{0.37 \times 10^{-3} \times 48 \times 10^{-9}} = 1587 \text{ (rad/km)}$$

$$\gamma = 0.33 + j1587$$

4. A microwave transmission system employs parabolic antennas as transmitter and receiver. The diameters of the transmitting and receiving antennas are 2.2meters and 3.5 meters , respectively. Assume that the transmitter power is 100W at 3.5 GHz , the receiving antenna is located 50 KM away from the transmitting antenna.
- What are the gains of the transmitting antenna and receiving antenna in decibels?
 - What is the available signal power out of the receiving antenna?

4. ~~a) Transmits~~

a) ~~Transmitter~~ Transmitting antenna: $r_1 = 1.1\text{m}$
Receiving antenna: $r_2 = 1.75\text{m}$

$$A_1 = \pi r_1^2 = 3.8\text{m}^2 \quad A_2 = \pi r_2^2 = 9.62\text{m}^2$$

$$A_{e1} = 0.56 A_1 = 2.128\text{m}^2 \quad A_{e2} = 0.56 A_2 = 5.39\text{m}^2$$

$$G_T = \frac{4\pi A_{e1}}{\lambda^2} \quad \lambda = \frac{c}{f} = \frac{3 \times 10^8 \text{ m/s}}{3.5 \times 10^9 \text{ Hz}} = 0.086\text{m}$$

$$G_T = \frac{4\pi A_{e1}}{\lambda^2} = 3615.6 \Rightarrow G_{T,dB} = 10 \lg(3615.6) = 35.58\text{dB}$$

$$G_R = \frac{4\pi A_{e2}}{\lambda^2} = 9158 \Rightarrow G_{R,dB} = 10 \lg(9158) = 39.62\text{dB}$$

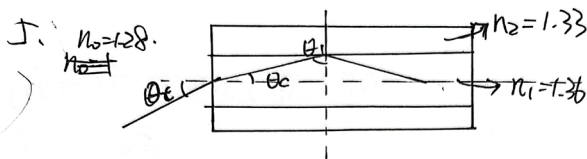
$$b) L_{dB} = 32.45 + 20 \lg(d) (\text{km}) + 20 \lg(f) (\text{MHz}) - G_{T,dB} - G_{R,dB} \\ = 62.11\text{dB}$$

$$P_T = 100\text{W} \Rightarrow P_{T,dB} = 10 \lg(100\text{W}) = 20\text{dBW}$$

$$P_R = P_{T,dB} - L_{dB} = 20\text{dBW} - 62.11\text{dB} = -42.11\text{dB}$$

5. Assume a step-index optical fiber with core refractive index $n_1 = 1.36$ and cladding refractive index $n_2 = 1.33$. The acceptance angle, refraction angle, and reflection angle are denoted as θ_i , θ_c , and θ_1 , respectively.

- If the interface of optical fiber is placed in vacuum with reflective index $n_0 = 1$, what is the numerical aperture?
- If the interface of optical fiber is placed in liquid with reflective index $n_0 = 1.28$, what is the maximum acceptance angle?



$$a) NA = \sqrt{n_1^2 - n_2^2} = \sqrt{1.36^2 - 1.33^2} = 0.28$$

$$b) n_0 \sin \theta_i = n_2 \sin \theta_0 \Rightarrow \sin \theta_1 = \frac{n_2}{n_1}$$

$$\theta_c = 90^\circ - \theta_1 \Rightarrow \sin \theta_c = \sin(90^\circ - \theta_1) = \cos \theta_1$$

$$\theta_c = 90^\circ - \theta_1 \Rightarrow \sin \theta_c = \sin(90^\circ - \theta_1) = \cos \theta_1$$

$$n_0 \sin \theta_c = n_1 \sin \theta_c = n_1 \cos \theta_1 = n_1 \sqrt{1 - \sin^2 \theta_1}$$

$$n_0 \sqrt{1 - \sin^2 \theta_1} = n_1 \sqrt{1 - \left(\frac{n_2}{n_1}\right)^2} = \sqrt{n_1^2 - n_2^2} = NA = 0.28$$

$$\text{so } \sin \theta_c = \frac{n_1 \sqrt{1 - \sin^2 \theta_1}}{n_0} = \frac{0.28}{1.28} = 0.219$$

The maximum acceptance angle:

$$\theta_c = \arcsin(0.219) = 12.65^\circ$$