Prove the following identity.

$$\frac{\cos \alpha + \cos(\alpha + 2\beta)}{2} \equiv \sin \alpha \sin(\alpha + \beta) \cos(\alpha + \beta) + \cos \alpha \cos^2(\alpha + \beta)$$

GONDRO