Prove the following identity.

$$\frac{\cos\alpha + \cos(\alpha + 2\beta)}{2} \equiv \sin\alpha \sin(\alpha + \beta)\cos(\alpha + \beta) + \cos\alpha \cos^2(\alpha + \beta)$$