1

NCERT-discrete: 10.5.3 - 2

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I. QUESTION

The laplace transform of $x_1(t) = e^{-t}u(t)$ is $X_1(s)$, where u(t) is the unit step function. The laplace transform of $x_2(t) = e^t u(-t)$ is $X_2(s)$. Which one of the following statements is TRUE?

- 1) The region of convergence of $X_1(s)$ is $Re(s) \ge 0$
- 2) The region of convergence of $X_2(s)$ is confined to the left half-plane of s.
- 3) The region of convergence of $X_1(s)$ is confined to the right half-plane of s.
- 4) the imaginary axis in the s-plane is included in both the region of convergence of $X_1(s)$ and the region of convergence of $X_2(s)$.

Solutions:

Symbols	Description
$X_1(s)$	Laplace transform of $x_1(t)$
$X_2(s)$	Laplace transform of $x_2(t)$
u(t)	Unit step function
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PARAMETERS, DESCRIPTIONS

Laplace transform of $x_1(t)$ is given by :

$$X_1(s) = \int_{-\infty}^{\infty} e^{-t} e^{-st} u(t) dt$$
 (1)

$$= \left[\frac{-e^{-t(s+1)}}{s+1} \right]_0^{\infty} \tag{2}$$

$$=\frac{1}{s+1},\tag{3}$$

ROC of
$$X_1(s) : Re(s) > -1$$
 (4)

Laplace transform of $x_2(t)$ is given by :

$$X_2(s) = \int_{-\infty}^{\infty} e^t e^{-st} u(-t) dt$$
 (5)

$$= \left[\frac{e^{t(1-s)}}{1-s} \right]_{-\infty}^{0}, (\because u(t) = 0, \forall t < 0)$$
 (6)

$$=\frac{1}{1-s},\tag{7}$$

ROC of
$$X_2(s) : Re(s) < 1$$
 (8)

Based on the regions of convergence of $X_1(s)$ and $X_2(s)$, we can conclude that option 4) is correct.

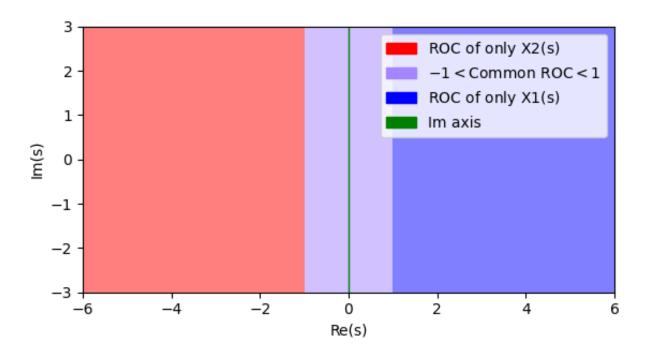


Fig. 1. ROC of $X_1(s)$ and $X_2(s)$