

Hebbian Learning

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20/15

* Based on Hebb's law

Training Algorithm

- 1) Initialise weights to zero $w_i = 0$ for all i .
- 2) Weight adjustments are performed.

$$w_i(n) = w_i(n) + \Delta x_i y_o$$

↓ Activity Product Rule

Pattern associatⁿ, categorisation & classificatⁿ

Using Hebb Rule, find weights required to perform the following classificatⁿs of given i/p patterns
'+' represent +1 & empty squares indicate -1.
Consider '1' belongs to the members of class (Target value 1) & '0' does not belong to the members of class (Target value -1)

+	+	+
1	+	
1	+	+

"1"

+	+	+
+	+	+
+	+	+

"0"

Solve 1- Pattern

Target Date
Page

x_1	x_2	x_3	x_4	x_5	x_6	x_7	x_8	x_9
1	1	1	-1	1	-1	1	1	1
1	1	1	1	-1	1	1	1	1

Case '1':

Initial Weights $w_1 = w_2 = w_3 = \dots = w_9 = 0$

$\alpha = 1$

Update the weights

$$w_{1(n)} = w_{1(n)} + \alpha x_i y_i$$

$$w_{1(n)} = 0 + 1 \times 1 = 1$$

$$w_2 = 1, w_3 = 1, w_4 = -1, w_7 = 1, w_8 = -1$$

$$w_5 = 1, w_6 = 1, w_9 = 1$$

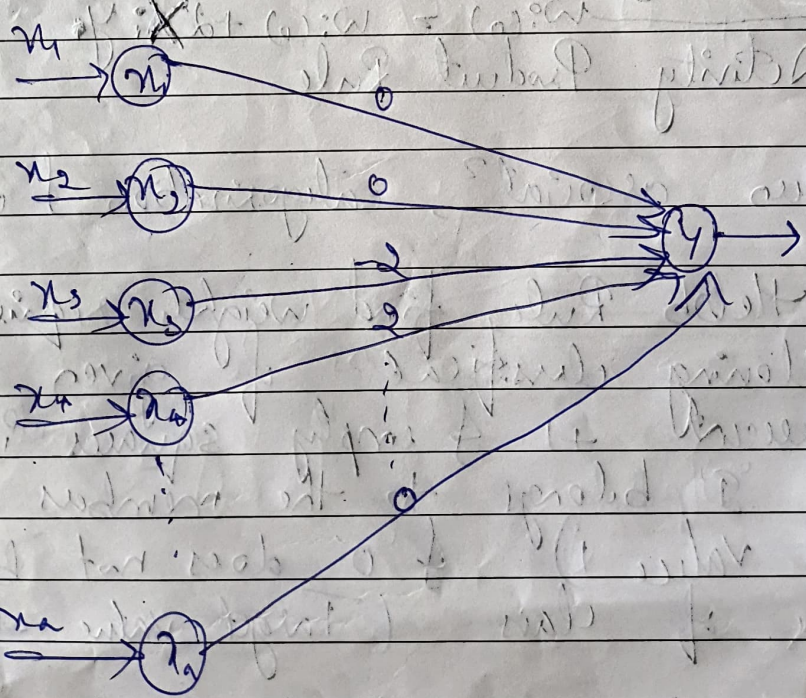
$$W(n) = \begin{bmatrix} 1 & 1 & 1 & -1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix}$$

Case '0': $w_{1(n)} = 1 + 1 \times (-1) = 0$

$$w_2(n) = 0, w_3(n) = 0, w_4 = -2, w_5 = 2$$

$$w_6 = -2, w_7 = 0, w_8 = 0, w_9 = 0$$

$$W(n) = \begin{bmatrix} 0 & 0 & 0 & -2 & 2 & -2 & 0 & 0 & 0 \end{bmatrix}$$



$$\begin{bmatrix} 1 & 1 & 1 & -1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} y = 2 + 2 + 2 = 6$$

$$y = -2 - 2 - 2 = -6$$

Step (6) $= 1$

Step (-6) $= -1$