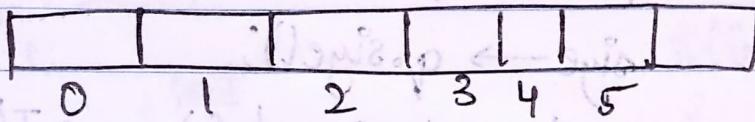


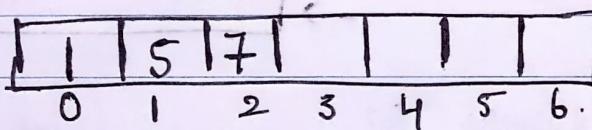
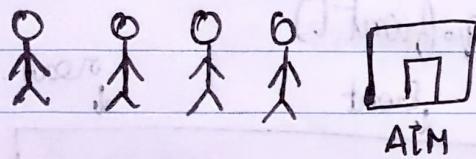
## Lec 60 :- Queue

trans. →  
queue → pop

Queue → Is a type of data structure where FIFO is followed.



FIFO → First in First Out.



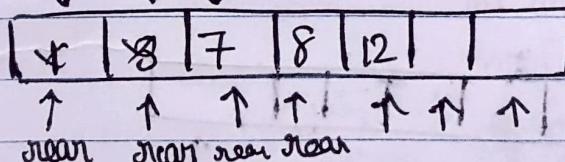
queue.push(i)

- push(5)
- push(8)

FIFO

(pop) → FIFO

(pop) front front front



push() → front

pop(), pop() → rear

push() → rear

pop() → front

queue → push / insert

pop / remove

{ size, isEmpty }

operation.

## STL Queue

push → insert

pop → remove

create → queue<int> q;

push → q.push(17);

pop → q.pop();

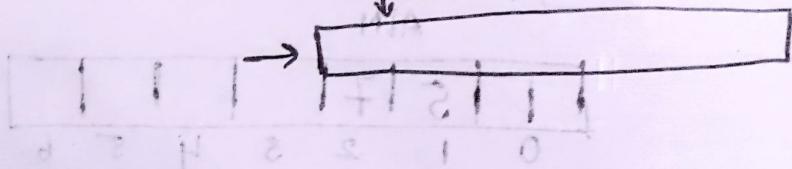
size → q.size();

isempty → q.isEmpty() → T/F

take front  
element

→ q.front()

Front



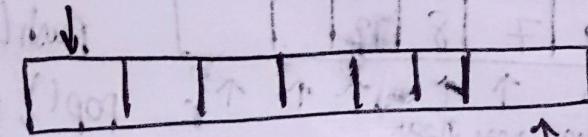
## Queue

→ Array

→ Linked List

Starting.

front



↑  
rear

↑ rear=n-1 → null.

push  
if full)

empty

front = rear

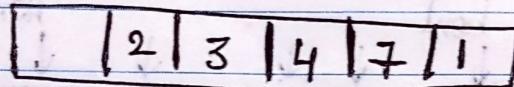
else arr[rear] = element;  
rear++;

Pop

if (empty) → Queue is empty.  
 else

arr[front] = -1;  
 front++;

↓ front



isempty → front == rear

front = rear  
 ↓  
 empty.

if (front == rear)

{

front = 0;  
 rear = 0;

→ Implementation.

void enqueue (int data)

{

if (front == rear)

{

cout << "Queue full";

}

else

{

arr[rear] = data;

rear++;

}

int dequeue()

{

if (front == rear)

{

return -1;

}

else

{

int ans = arr[front]; // Element to be removed

arr[front] = -1;

front++;

if (front == rear)

{

front = 0;

rear = 0;

}

return ans;

```

bool isEmpty()
{
    if (front == rear)
    {
        return true;
    }
    else
        return false;
}

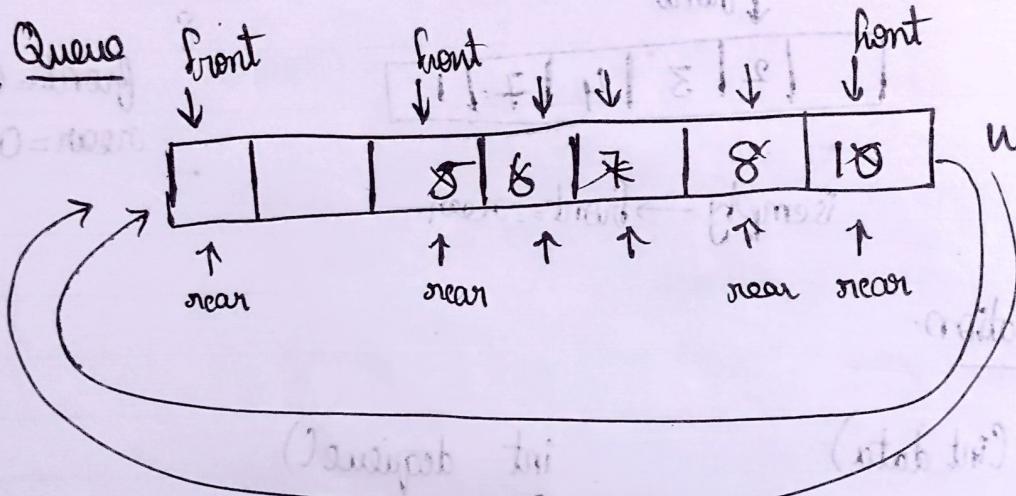
```

```

int front()
{
    if (front == rear)
    {
        return -1;
    }
    else
        return arr[front];
}

```

### Circular Queue



queue:

front = -1

rear = -1

push

if (full) → "Queue is full"

front = 0 & rear = size - 1

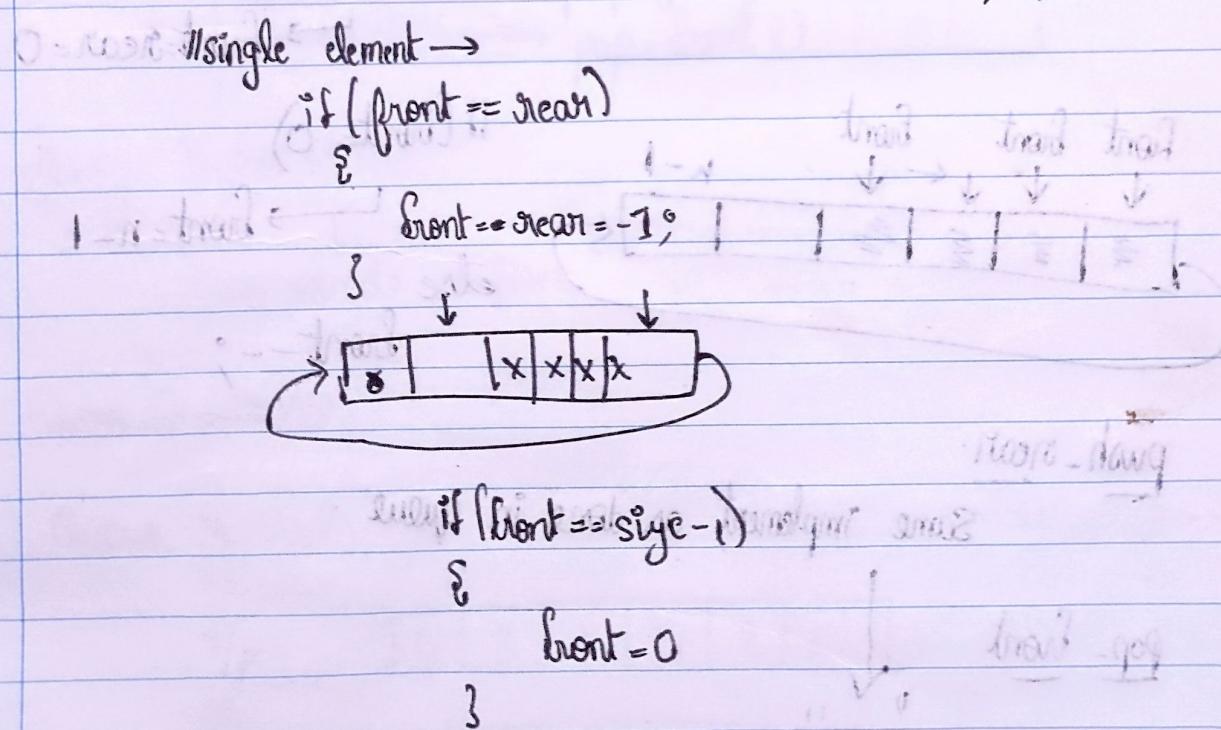
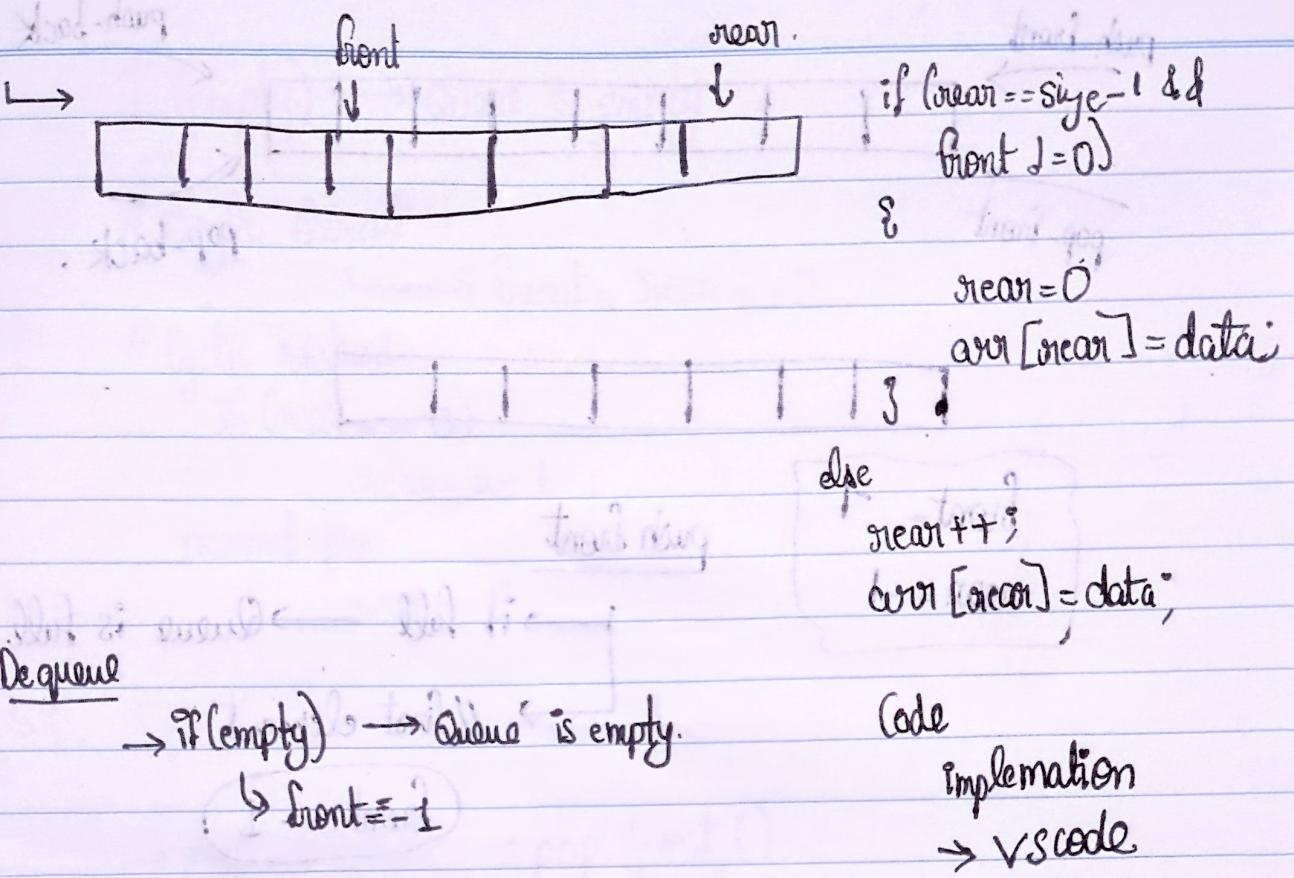
rear = ((front - 1) % (size - 1))

→ if front = -1

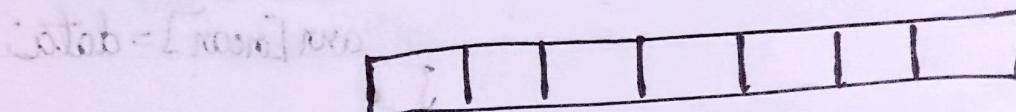
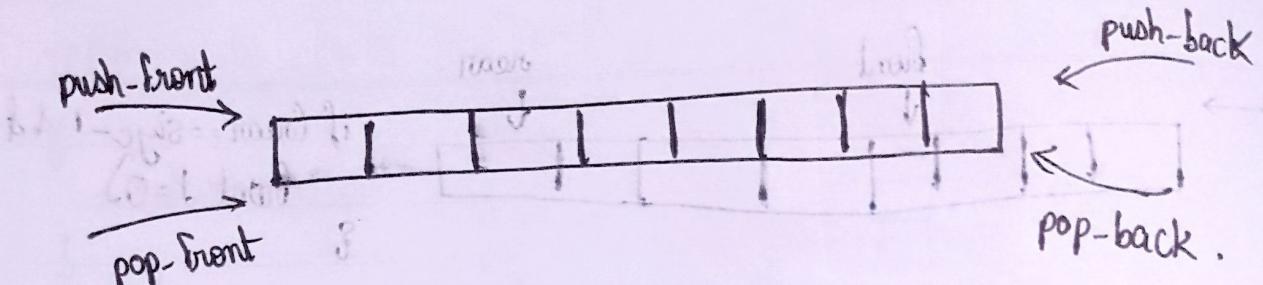
? front = 0

rear = 0

arr[queue] = data;



## Doubly Ended Queue



Front = -1  
rear = -1

push-front

if full → Queue is full.

// first-element

front = +1

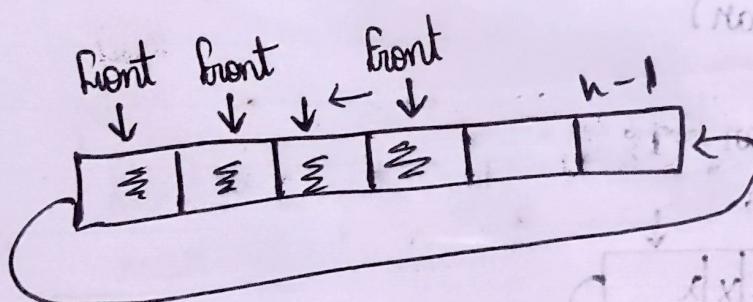
front = rear = 0

if (front = 0)

front = n - 1

else

front --;



push-rear

Some implement as done in queue

pop-front

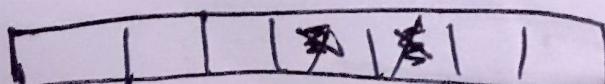
" "

o-front

rear-pop

pop-back

rear-rear  
↓ ↓ ↓



if (empty) → Queue is empty.

// single element

→ front = rear = -1

// Cyclic Nature:

if (rear == 0)

rear = n - 1

normal flow

rear--;

## STL Operations.

→ push-front() → pop-front()

→ push-back() → pop-front()

Array Implementation

→ vscode refer

## Queue Questions:

Queue reversals

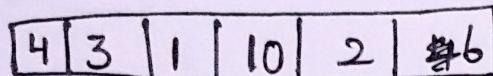
i/p      

4	3	1	10	2	6
---	---	---	----	---	---

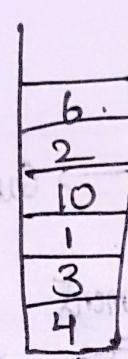
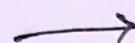
o/p      

6	2	10	1	3	4
---	---	----	---	---	---

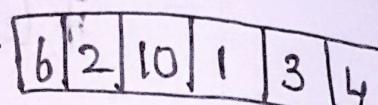
Approach 1.



Queue.



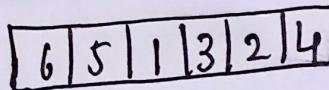
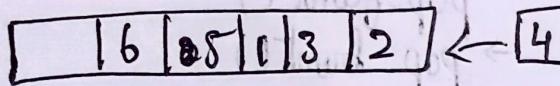
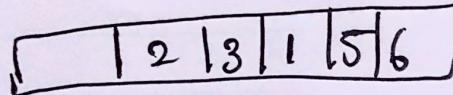
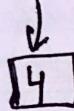
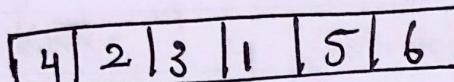
Stack



Queue.

2<sup>nd</sup>

Recursion.



Code

8. Recursion.

queue<int> rev(queue<int> q)

{

if(q.empty())

q = rev(q);

q.push(data);

return q;

}

return q;

3

int data = q.front();

q.pop();

### Approach!

```
queue<int> q;
stack<int> s;
while (!q.empty())
```

```
    int element = q.front();
```

```
    q.pop();
```

```
    s.push();
```

```
}
```

```
while (!s.empty())
```

```
}
```

```
    int element = s.top();
```

```
    s.pop();
```

```
    q.push();
```

```
3.
```

```
return q;
```

```
3
```

---

### Implement Stack using Queue.

#### Stack

#### Queue

first in first out, front

#### class Stack

```
queue<int> q1, q2;
```

```

public:
    void push(int x)
    {
        q2.push(x);
        while(!q1.empty())
        {
            q2.push(q1.front());
            q1.pop();
        }
    }

queue<int> q = q1; //swapping
q1 = q2;
q2 = q;
}

void pop()
{
    if(q1.empty())
    {
        return;
    }
    q1.pop();
}

int top()
{
    if(q1.empty())
    {
        return -1;
    }
    return q1.front();
}

int size()
{
    return q1.size();
}

```

```

int main()
{
    Stack s;
    s.push(1);
    s.push(2);
    s.push(3);
    s.top();
    s.top();
    s.top();
}

```

//Top of stack is always the last element pushed

Output :-

3  
2  
1

### Implement Queue Using Stack

```

struct Queue
{
    stack<int> s1, s2;
    void enqueue(int x)
    {
        while(!s1.empty())
        {
            s2.push(s1.top());
            s1.pop();
        }
        s1.push(x);
    }

    while(!s2.empty())
    {
        s1.push(s2.top());
        s2.pop();
    }
}

```

# BINARIA TRE

int deQueue()

{

if (S1.empty())

{

return -1;

}

int x = S1.top();

S1.pop();

return x;

}

};

int main()

{

Queue q;

q.enQueue(1);

q.enQueue(2);

q.enQueue(3);

cout << q.dequeue();

cout << q.dequeue();

cout << q.dequeue();

return 0;

3
2
1

*	x	x	3	2	1
---	---	---	---	---	---

*	x	x	3	2	x
---	---	---	---	---	---

1
2
3
x
x
*

2
1
x

S1

S2

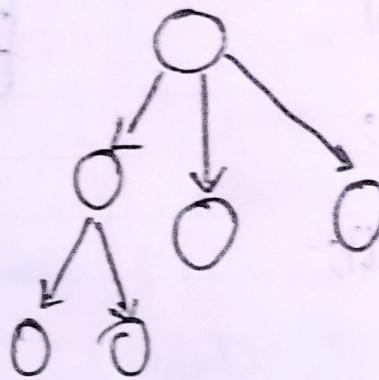
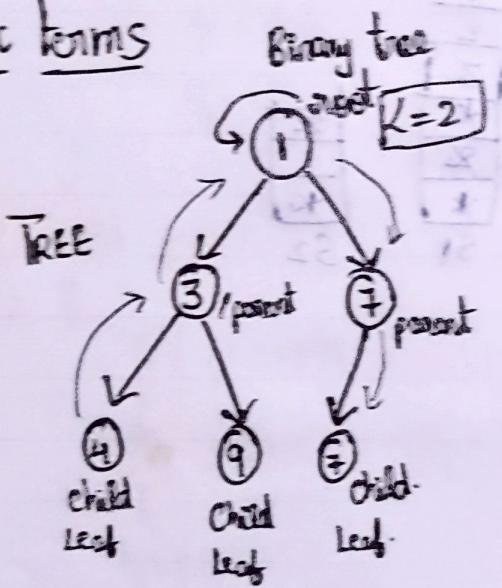
## #62. BINARY TREE

TREE → Non-linear Data Structure

linked list → DS Linear

□ → □ → □ → □ → x

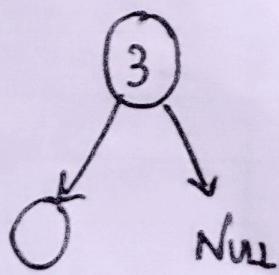
Basic terms



- ① Node
- ② Root
- ③ Children
- ④ Parent
- ⑤ Siblings
- ⑥ Ancestors
- ⑦ Descendant
- ⑧ Leaf → Doesn't have child

node

```
{
    int data;
    node *left;
    node *right;
}
```



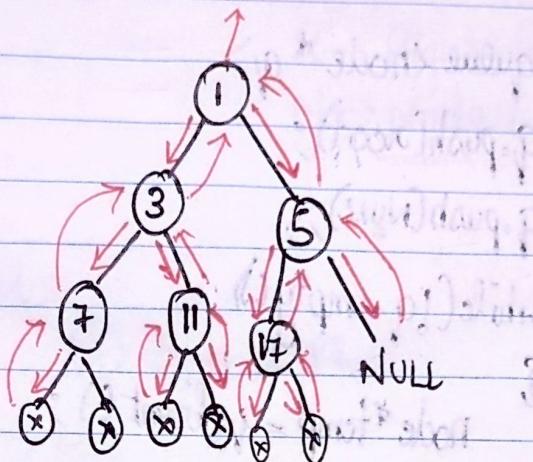
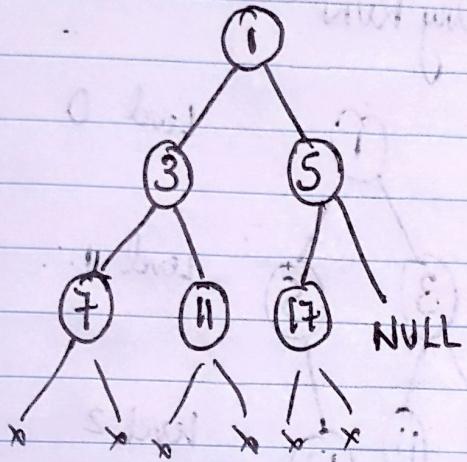
If Multiple Node allowed:

node

```
{
    int data
    list<node*> child;
}
```



## # Creation Binary Tree



class Node:

{

public:

int data;

int \*left;

int \*right;

node (int d)

{

this → data = d;

this → left = NULL;

this → right = NULL;

}

,

node \* buildTree (node \*\*root)

{

cout << "Enter data" << endl;

int data;

cin >> data;

root = new node (data);

if (data == -1)

{

return NULL;

3

cout << "Enter data left of " << data << endl;

root → left = buildTree (root → left);

cout << "Enter data Right of " << data << endl;

root → right = buildTree (root → right);

return root;

}

## LEVEL Order Traversal

```
void LevelOrder Traversal (Node *root)
```

```
{
```

```
queue <node *> q;
```

```
q.push(root);
```

```
q.push(NULL);
```

```
while (!q.empty ())
```

```
{
```

```
node *temp = q.front ();
```

```
q.pop();
```

```
if (temp == NULL)
```

```
{
```

```
cout << endl;
```

```
if (!q.empty ())
```

```
{
```

```
q.push(NULL);
```

```
3
```

```
else
```

```
{
```

```
cout << temp->data << " ";
```

```
if (temp->left)
```

```
{
```

```
q.push(temp->left);
```

```
3
```

```
if (temp->right)
```

```
{
```

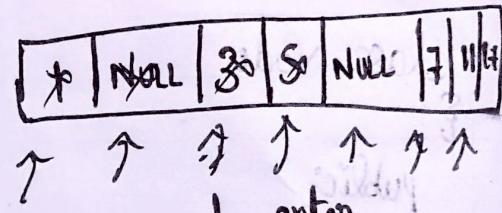
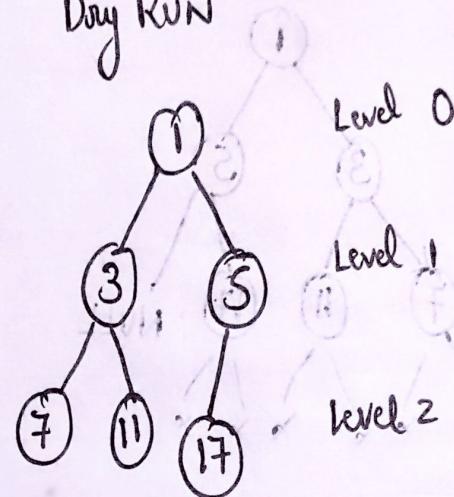
```
q.push(temp->right);
```

```
3
```

```
3
```

```
3
```

Day Run



ans

3, 5 enter

7, 11, 17 enter

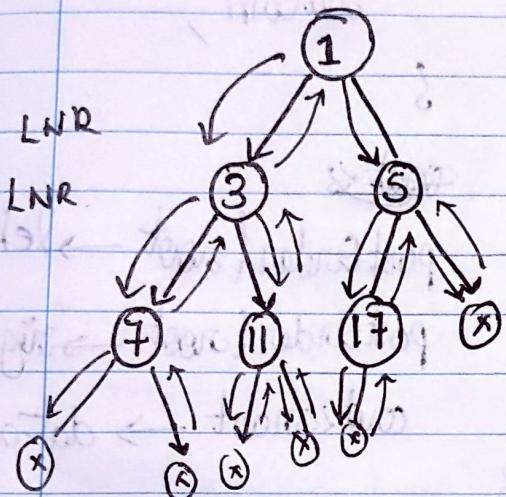
$\rightarrow$  InOrder / PreOrder / PostOrder

LNR

NLR

LRN

L  $\rightarrow$  Left Part  
R  $\rightarrow$  Right Part  
N  $\rightarrow$  Node (Point)

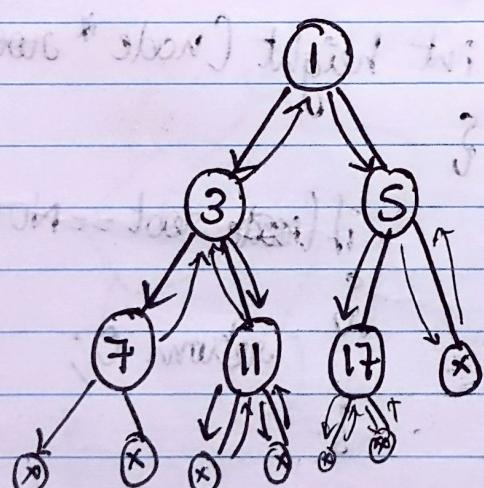


Inorder

⑦ 3 11 17 5

PreOrder

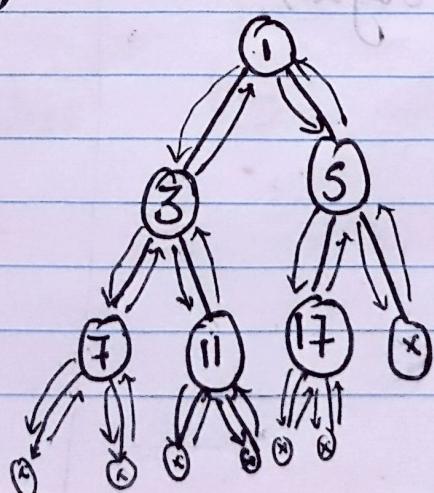
NLR



PreOrder  $\rightarrow$

1 3 7 11 5 17

Post Order LRN



7 11 3 17 5 1

Code LNR

void Inorder(node \* root)

```
{  
    if (root == NULL)  
    {  
        return;  
    }
```

Inorder (root → left);

cout << root → data << " "  
Inorder (root → right);

}

void preorder(node \* root) NLR

```
{  
    if (root == NULL)  
    {  
        return;  
    }
```

cout << root → data << " "  
preorder (root → left);  
preorder (root → right);

}

LRN void postorder(node \* root)

```
{  
    if (root == NULL)  
    {  
        return;  
    }
```

~~cout~~

postOrder (root → left);

postOrder (root → right);

cout << root → data << endl;

}

Height Tree Code TC → O(n)

int height (node \* root)

{

if (node, root == NULL)

{

return 0;

}

int left = height (root → left);

int right = height (root → right);

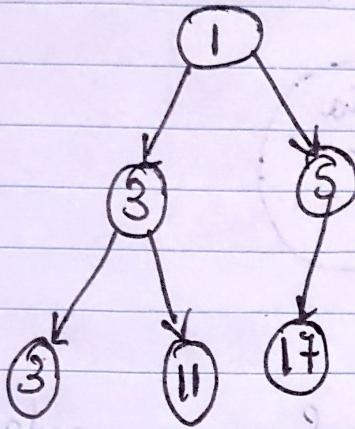
int ans = max(left, right) + 1

return (ans);

}

(Apoll)CS-27  
visit

→ Height of A Tree



height → 3

height = ?

Longest Path b/w root node & the leaf node.

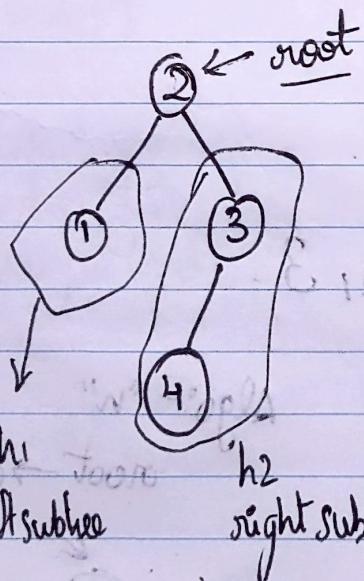
no. of nodes → height

approach

Recursion

I can solve

rest recursion



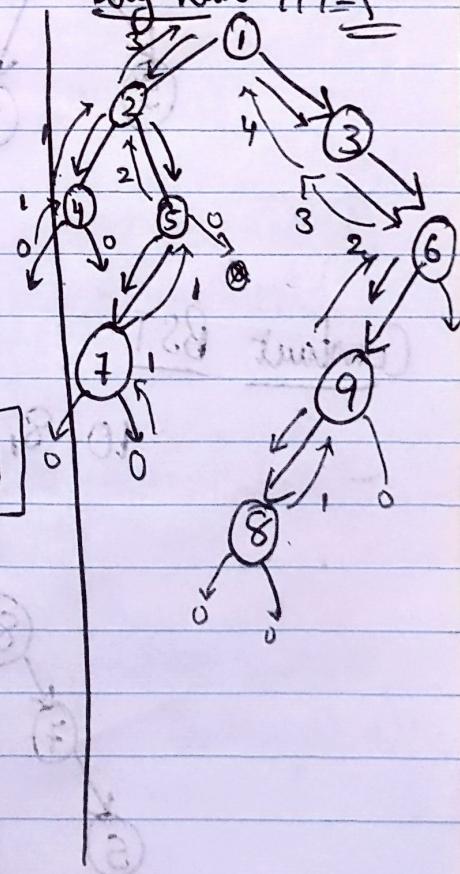
h1  
left subtree

h2  
right subtree

$$\max(h_1, h_2) + 1$$

height

Dry Run 4+1=5



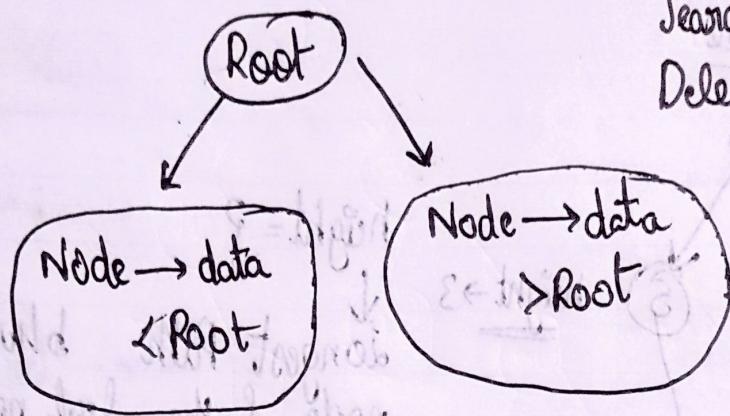
# BINARY SEARCH TREE

T.C  $\rightarrow O(\log n)$

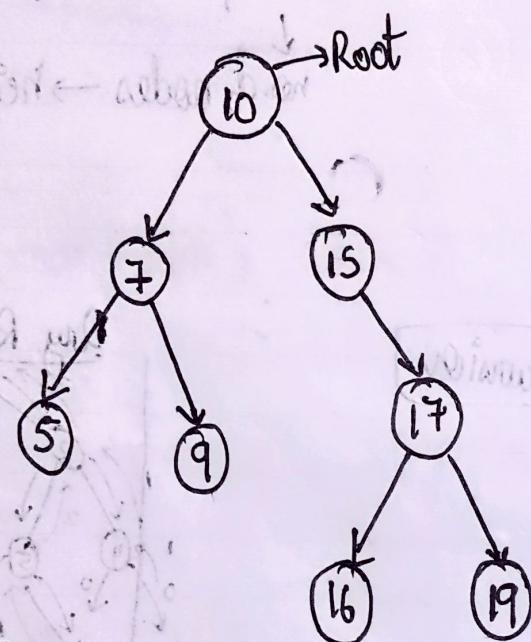
Inserion

Searching

Deletion



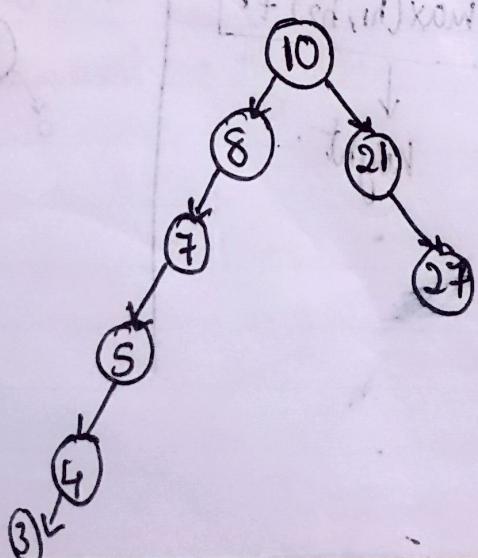
Eg:-



for every node  
the condition must satisfy

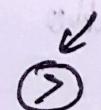
Construct BST

10, 8, 21, 7, 27, 5, 4, 3.

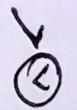


Algo:- "n"

root → data



right part



left part

## Insertion

```
class Node
```

```
{ public:
```

```
    int data;
```

```
    Node *left;
```

```
    Node *right;
```

```
Node (int d)
```

```
{
```

```
    this->data = d;
```

```
    this->left = NULL;
```

```
    this->right = NULL;
```

```
}
```

```
,
```

```
int main()
```

```
{
```

```
    Node *root = NULL;
```

```
    cout << "Enter data to create BST" << endl;
```

```
    takeInput (root);
```

```
,
```

```
void takeInput (Node *root)
```

```
{
```

```
    int data;
```

```
    cin >> data;
```

```
    while (data != -1)
```

```
{
```

```
    root = insertIntoBst (root, data);
```

```
    cin >> data;
```

```
,
```

```
Node * insertIntoBst (Node *root, int d)
```

```
{
```

```
    if (root == NULL)
```

```
{
```

```
    root = new Node (d);
```

```
    return root;
```

```
,
```

```
    if (d > root->data)
```

```
{
```

```
    root->right = insertIntoBst
```

```
(root->right, d);
```

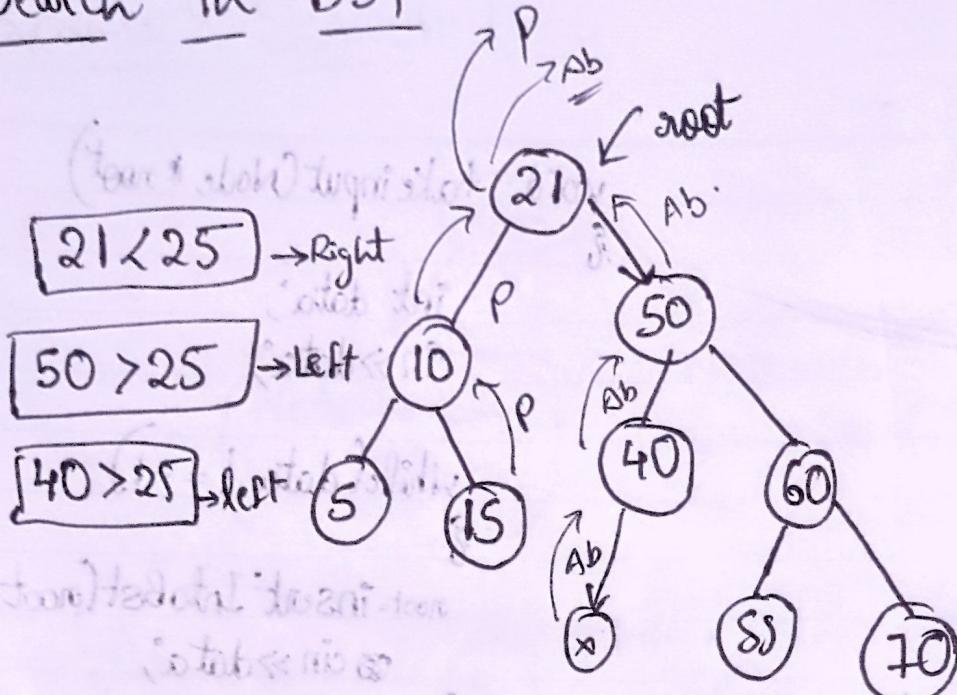
```
,
```

```
else {
```

```
    root->left = insertIntoBst
```

```
(root->left, d);
```

## Search in BST



$x = 21$

$x = 15$

$21 > 15$  Left.

$10 < 15$  Right.

$15 == 15$

base case.  
 $\Rightarrow \text{return } \rightarrow \text{False / Absent}$

if  $[\text{root} \rightarrow \text{data} > x]$  → Left.

else

right part

## Implementation // Recursive

```
bool searchInBst (BinaryTreeNode* root, int x)
{
    if (root == NULL) // Not found
    {
        return false;
    }
    if (root → data == x) // Found.
    {
        return true;
    }
    else // Right side.
    {
        return searchInBst (root → right, x);
    }
}
```

## II Iterative

bool searchInBst(BinaryTreeNode \*int > root, int x)

{

BinaryTreeNode \*int > temp = root;

while (temp != NULL)

{

if (temp -> data == x)

{

return true;

}

if (temp -> data > x)

{

temp = temp -> left;

}

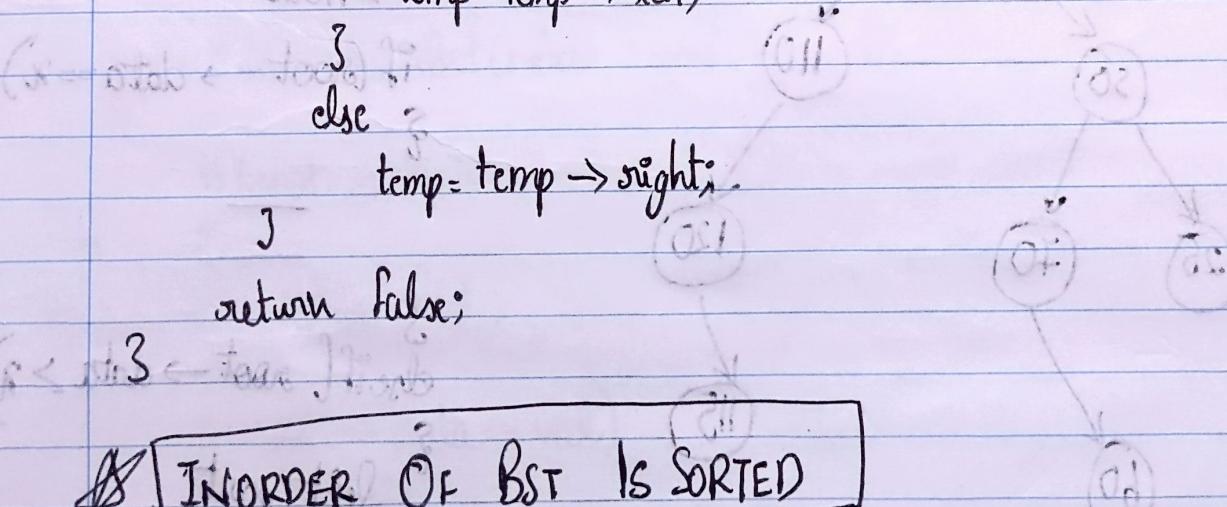
else

temp = temp -> right;

}

return false;

**INORDER OF BST IS SORTED**



## Max / Min In BST

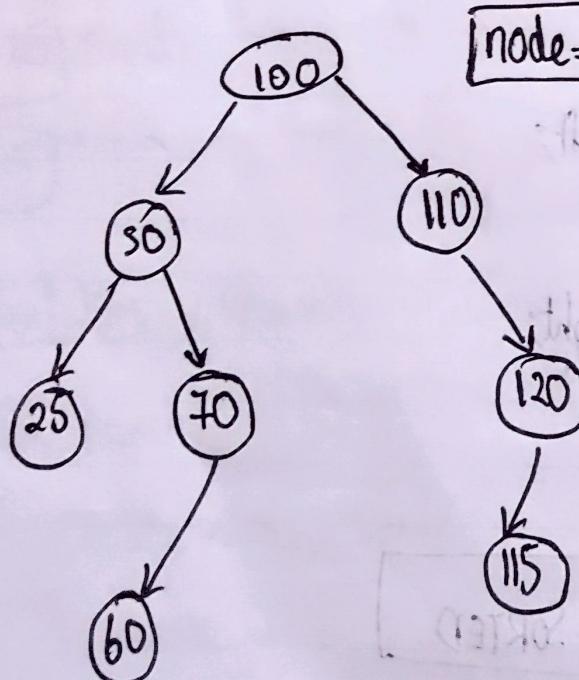
```

Node * minValue (Node * root) //MIN
{
    Node * temp = root;
    while (temp != NULL)
    {
        temp = temp->left;
    }
    return temp;
}

Node * maxValue (Node * root)
{
    Node * temp = root;
    while (temp != NULL)
    {
        temp = temp->right;
    }
    return temp;
}

```

## Deletion in BST



node = 120

Algo:-

→ node

if (root → data == x)

{

=

else if (root → data > x)

{

left part

{

else {

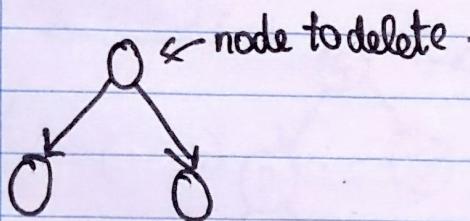
right part

Node to delete

O Child

→ delete node;  
return NULL

↳ 2 children.



Child

```

graph TD
    a((a)) --> b((b))
    a --> c((c))
    x((x)) --> y((y))
    x --> z((z))
  
```

Left Child

```
temp = root → left  
delete (root);  
return temp.
```

## Light

temp = root → right  
delete (root)  
return temp.

## Implementation

Node \* deletefrombst(Node \* root, int val)

毛

if (root == NULL)

3

return root;

if( $\text{root} \rightarrow \text{data} == \text{val}$ )

8 10 Child.

if ( $\text{root} \rightarrow \text{left} == \text{NULL}$  &&  $\text{root} \rightarrow \text{right} == \text{NULL}$ )

3

delete root

return NULL;

3

// 1 Child

// Left Child

if (root → left != NULL && root → right == NULL)

{

Node \*temp = root → left;

delete (root);

return temp;

}

Right

if (root → left == NULL && root → right != NULL) Right

{

Node \*temp = root → right;

delete (root);

return temp;

}

// 2 Child

if (root → left != NULL && root → right != NULL)

{

int mini = minValue (root → right) → data;

root → data = mini;

root → right = deletefromBst (root → right, mini);

return root;

}

## Question

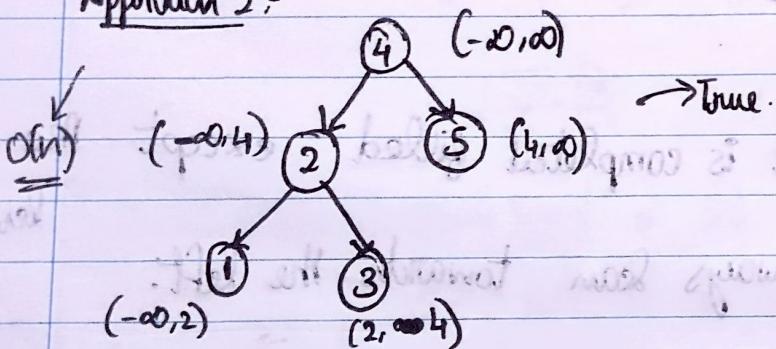
Valid BST (or) NOT

Approach 1 :-

Inorder traversal if sorted → T then BST  
→ F then false.

O(n)

Approach 2 :-



Code // Approach 2

```
bool validate(Node* root, int min, int max)
```

S

```
if (root == NULL)
```

```
{ return true; }
```

```
if (root->data > min & & root->data < max)
```

S

```
bool left = validate(root->left, min, root->data);
```

```
bool right = validate(root->right, root->data, max);
```

```
return left && right;
```

S

```
else
```

```
return false;
```

INT\_MIN

INT\_MAX

// Approach 1 - GeekForGeeks

```
do inorder (root, ans)
```

```
inorder (root->left, ans)
```

```
ans.push_back (root->data)
```

```
inorder (root->right, ans)
```

check arr

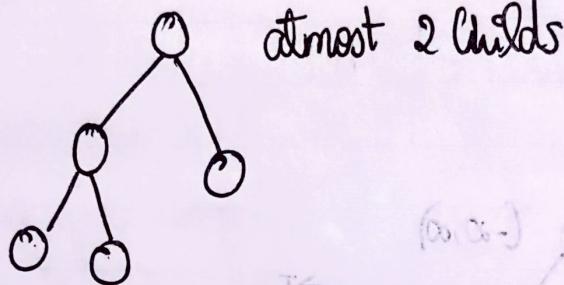
whether sorted  
(ii) not.

## #74 Heaps

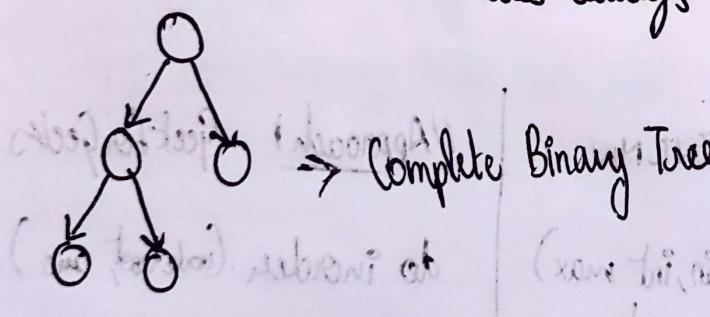
What is Heap?

↪ is a Complete Binary Tree that comes with a heap Order property.

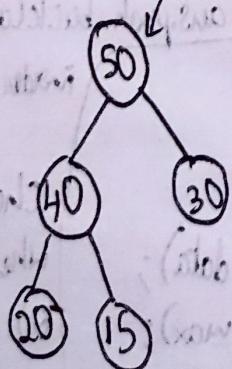
What's Complete Binary Tree?



CBT → Every level is completed filled except the last level  
→ Nodes always lean towards the left.



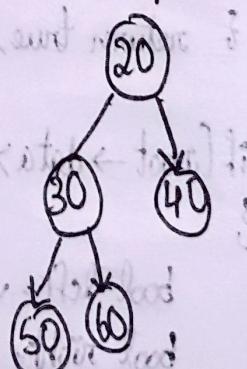
Max Heap: root is largest among all children



All Child nodes are smaller

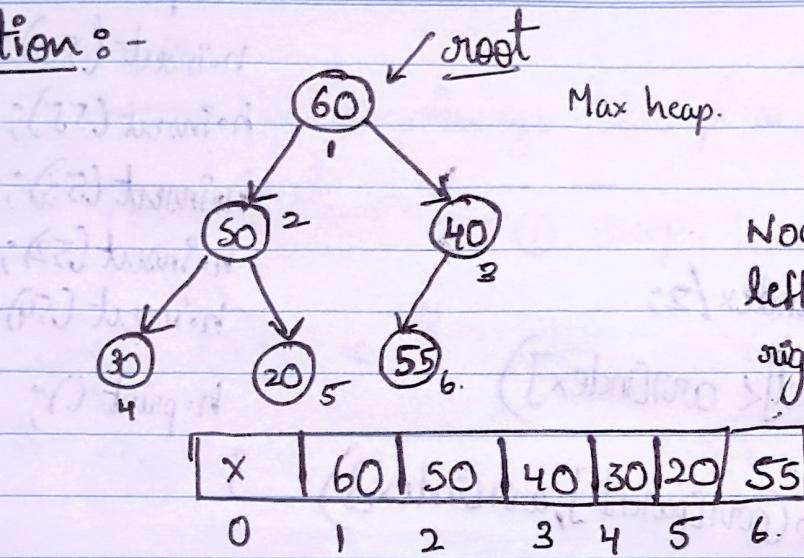
Min Heap:

Every node is smaller than its children



All Child nodes are bigger

## Inserion :-



Node  $\rightarrow$   $i^{\text{th}}$  index

left Child  $\rightarrow 2 \times i^{\text{th}}$  index.

right Child  $\rightarrow (2 \times i + 1)^{\text{th}}$  index.

$$\text{parent} = \underline{(i/2)}$$

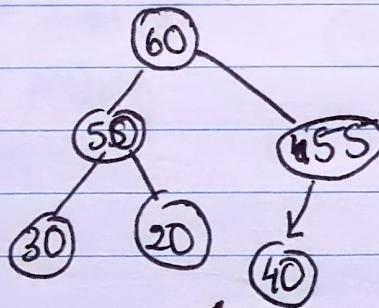
$$\text{Eg: } \underline{(5/2)} = 2^{\text{nd}} \text{ index}$$

val = 55



①  $\rightarrow$  insert at end

②  $\rightarrow$  take it to correct position



$\rightarrow$  Becomes like this

## Implementation Insertion

class Heap:

public:

int arr[100];

int size;

// Constructor Heap()

{ arr[0] = -1;

size = 0;

}

```
void insert(int val)
```

```
{
```

```
size = size + 1;
```

```
int index = size;
```

```
arr[index] = val;
```

```
while(index > 1)
```

```
{ int parent = index / 2;
```

```
if(arr[parent] < arr[index])
```

```
{
```

```
swap(arr[parent], arr[index]);
```

```
index = parent;
```

```
}
```

```
else
```

```
{
```

```
return;
```

```
}
```

```
}
```

```
void print()
```

```
{
```

```
for(int i=1; i<size; i++)
```

```
{ cout << arr[i] << " ";
```

```
cout << endl;
```

```
};
```

```
int main()
```

```
{
```

```
Heap h;
```

```
h.insert(50);
```

```
h.insert(55);
```

```
h.insert(53);
```

```
h.insert(52);
```

```
h.insert(54);
```

```
h.print();
```

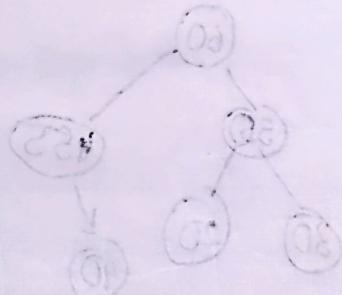
50 = root

55

53

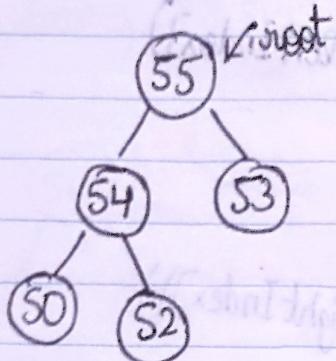
52

54

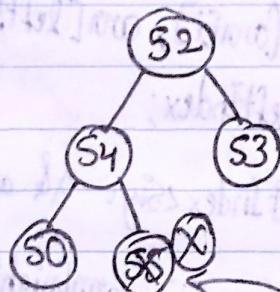


## Deletion in Heaps

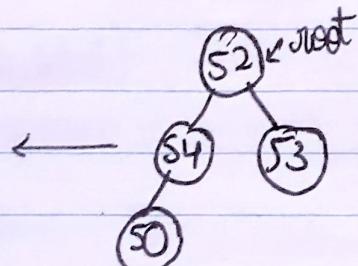
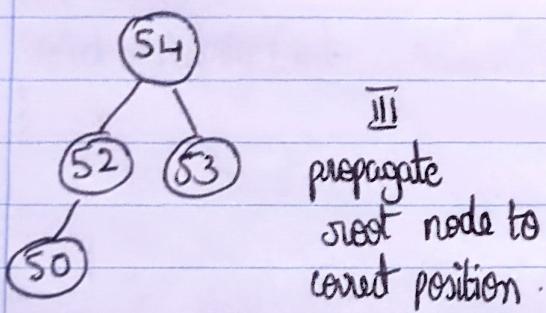
→ Deletion always takes place for ~~the~~ root node.



① swap first node with last node.



II Remove last node



## Implementation

void deleteFromHeap()

{

if (size == 0)

{

cout << "Nothing to delete";

return;

}

arr[1] = arr[size];

size--;

```

int i=1;
while(i<size)
{

```

```
    int leftIndex = 2*i;
```

```
    int rightIndex = 2*i+1; select greater child
```

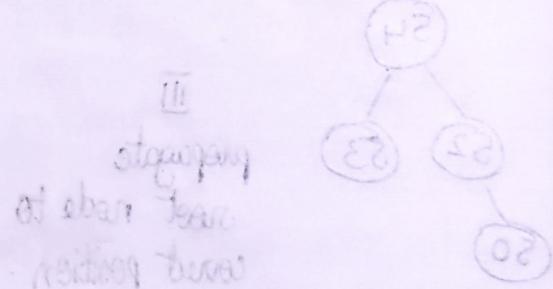
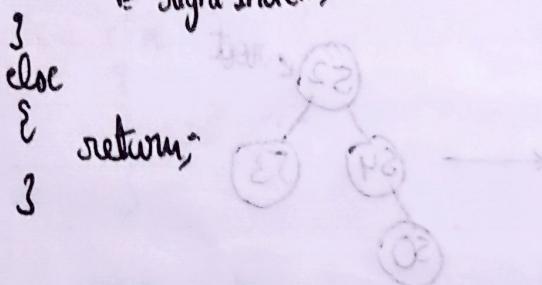
```
    if (leftIndex < size && arr[i] < arr[leftIndex])
```

```
    {
        swap(arr[i], arr[leftIndex]);
        i = leftIndex;
    }

```

```
    else if (rightIndex < size && arr[i] < arr[rightIndex])
```

```
    {
        swap(arr[i], arr[rightIndex]);
        i = rightIndex;
    }
}
else
{
    return;
}
```

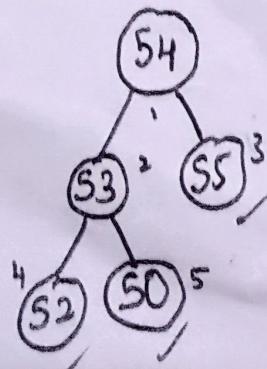


## Heapify Alg

i/p → 

54	53	55	52	50
1	2	3	4	5

↓  
Convert into Heap.



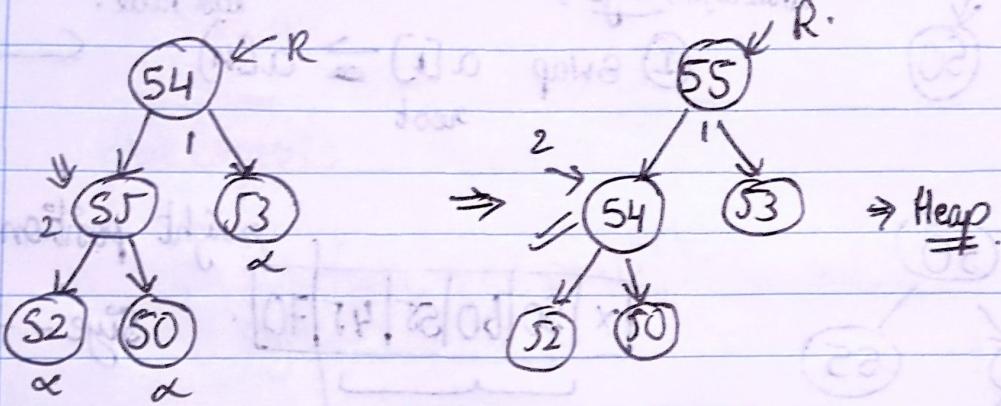
(CBT → leaf node)  
 $\rightarrow (n/2 + 1)$

$n/2 + 1$

:  
Focus :  $1 \rightarrow n/2$

for ( $n/2 \rightarrow >0$ )

    3 heapify (arr, size, i);



Implementation:

```
void heapify (int arr[], int n, int i)
```

```
{  
    int largest = i;  
    int left = 2 * i;  
    int right = 2 * i + 1;
```

```
    if (largest < n && arr[largest] < arr[left])  
    {
```

```
        largest = left;
```

```
    }  
    if (largest < n && arr[largest] < arr[right])  
    {
```

```
        largest = right;
```

```
    }  
    if (largest != i)  
    {
```

```
        swap (arr[largest], arr[i]);  
        heapify (arr, n, largest);
```

```
int main ()  
{
```

```
    int arr[6] = {81, 54,  
                 53, 55, 52, 50};
```

```
    int n = 5
```

```
    for (int i = n / 2; i > 0; i--)
```

```
{
```

```
    heapify (arr, n, i);
```

```
}
```

```
// printing
```

```
for (int i = 1; i <= n; i++)
```

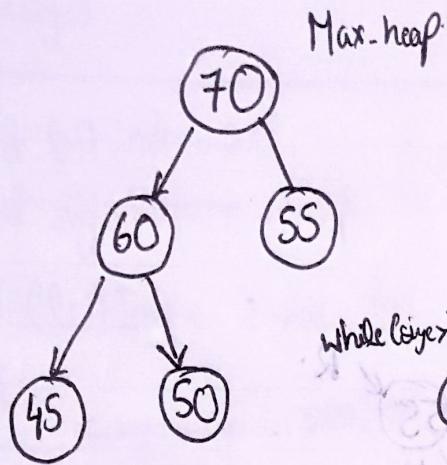
```
{
```

```
    cout << arr[i] << " ";
```

```
}
```

```
}
```

## Heap Sort:

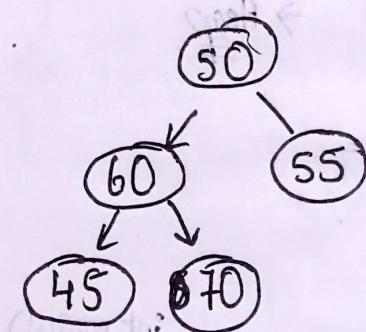


X	70	60	55	45	50
0	1	2	3	4	5

while( $i > 1$ ) Step :-

I) Swap  $a[i] \geq a[n]$   $\xrightarrow{\text{root}}$

last node.

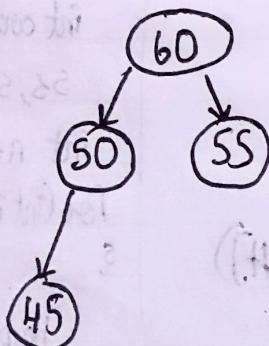


X	50	60	55	45	70

right position.

$i = i - 1$ ;

II) root node connection position

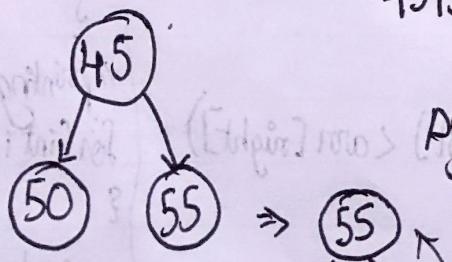


60 | 50 | 55 | 45

Again I)

45 | 50 | 55 | 60, 70

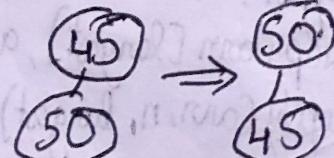
$\downarrow$  sorted



Again II)

55 | 50 | 45 | 60 | 70

Again I)



45 | 50 | 55 | 60  
 ↓  
 50 | 45 | 55 | 60  
 ↓  
 45, 50, 55, 60

## Implementation

```
void HeapSort(int arr[], int n)
{
```

int size = n;

while (size > 1)

{

    swap(arr[size], arr[1]); "last index" -> print

    size--;

    Heapify(arr, size, 1);

## PRIORITY QUEUE STL

(1) Max heap (how to use on

<int, greater<int>>)

priority\_queue<int> pq;

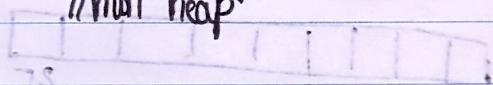
pq.push() top()

push()

empty()

pop()

// min heap



priority\_queue<int, vector<int>, greater<int>> minheap;

o < i - b

i < j - b

full habit

graph LR; gen --> qm; qm --> gen

no gen heap and

# Hashmaps



Data Structure



Type of D.S



Ins/ Del / Search

→ operations → T.C is very good. →  $O(1)$

## Question

String str = "abc bdeaaaf"

"Maximum Occuring Character"

a → 3

b → 2

c → 1

d → 1

e → 1

f → 1

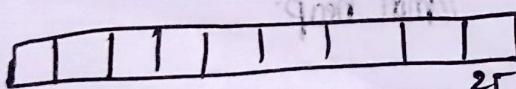
Possible Normally

for (i=0; i<str.size(); i++)

char ch = str[i];

count[ch-'a']++;

3



0 1 2  
↓ ↓ ↓  
'a' 'b' 'c'

'd' - 'a' → 0

'b' - 'a' → 1

if str = "My name is Ganesh  
name is Ganesh Ganesh";

My → 1

name → 2

Ganes → 3

Not possible  
So, hashmaps  
are used.

Max occurring word.

As we want to store like this

<name, 2>

<My, 1>

<Ganesh, 3>

## Inbuilt Stuff

→ map →  $O(\log n)$

→ unordered\_map →  $O(1)$

int main()  
{

map<string, int> m;

//

pair<string, int> p = make\_pair("ganesh", 3);

//

pair<string, int> pair2("name", 2);

//

m["Ny"] = 2;

// Size

cout << m.size(); → gives size.

// Count

cout << m.count("ganesh") → Returns 1

// Erase

m.erase("name"). → removes key

// Iteration

map<string, int> :: iterator it = m.begin();

while (it != m.end())

{

cout << it → first << " " << it → second; + Oxd

it++; ← N.D. E&C1-

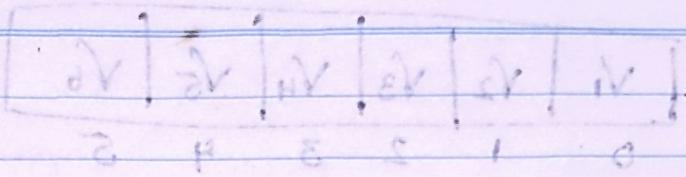
}

3.

gulabhi miallo

gulabhi ame ← gulabhi miallo

gulabhi bala ←



<value, val>

Gulabhi Jalebi

## Bucket Array

<key, value>

$V_1$	$V_2$	$V_3$	$V_4$	$V_5$	$V_6$
0	1	2	3	4	5

Chaining

Conversion to int

Unification.

→ Hash Code

→ identity function.

Conversion  
to int

Hash functions.

Hash Code

→ Compression Function

int hash code

brings into range

i/o/p      H.C      → 23 → O/p.

i/o/p "babbar" → H.C → 23 → O/p.

$$b + b + a + b + b + a + o$$

$$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$$

$$97 \quad 98 \quad 97 \quad 97 \quad 97 \quad 96$$

→ 606 → 23

b	b	b	b	a	o
0	1	2	3	4	5

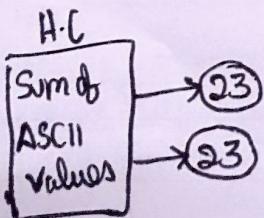
$$b \times 0 + a \times 1 + b \times 2 + b \times 3 + a \times 4 + o \times 5$$

$$= 1283 \% N \rightarrow 22$$

## Collision

"babbar"

"babbar"

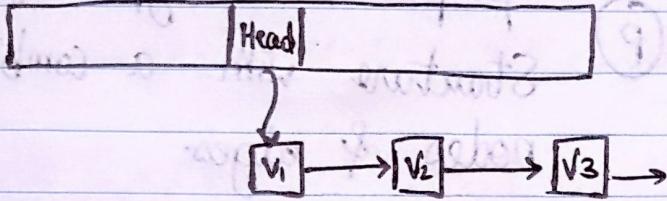


Collision Handling.

→ Open Hashing → same place put

→ closed Addressing.

## Open Hashing



separate Chaining

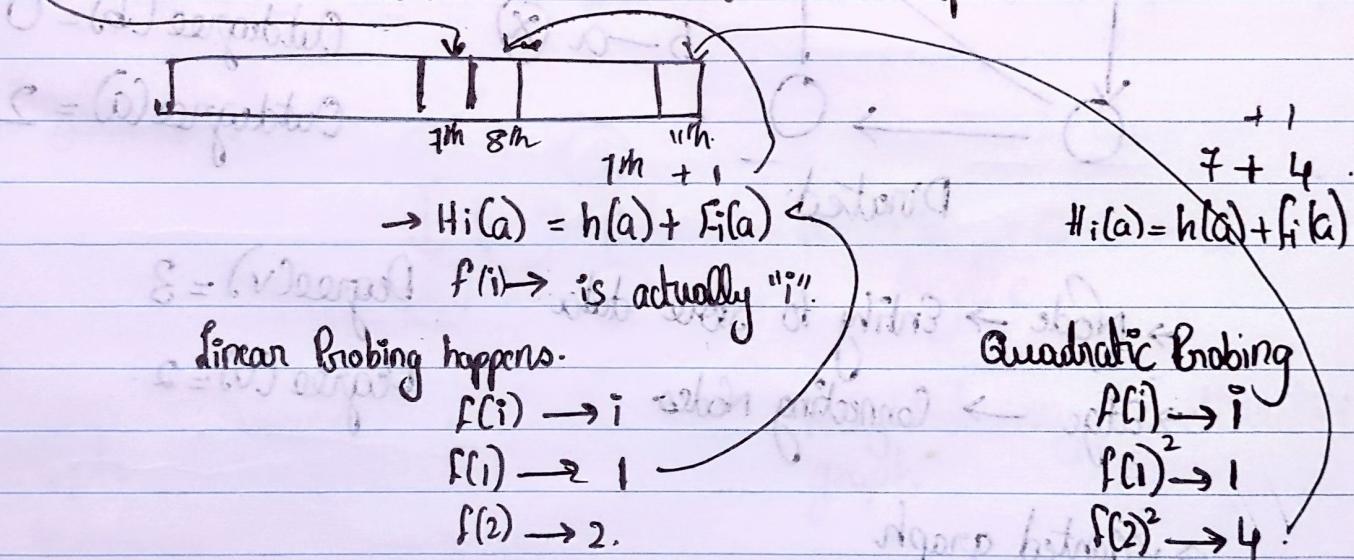
Closed

## Open Addressing

'A' → 7<sup>th</sup> index

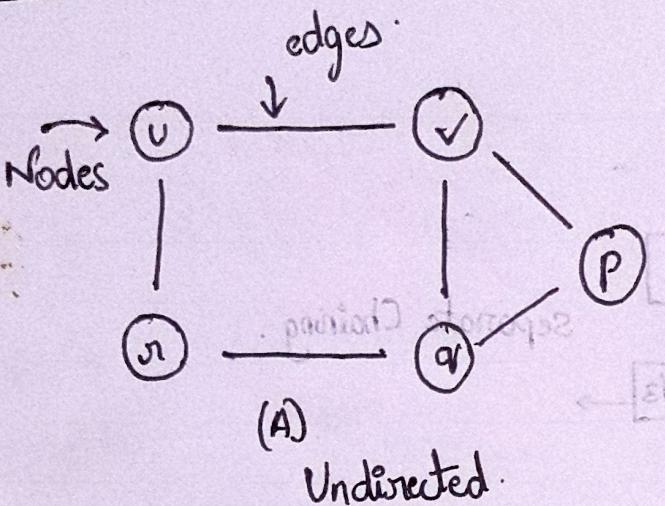
'B' → 7<sup>th</sup> index

Search for another space.



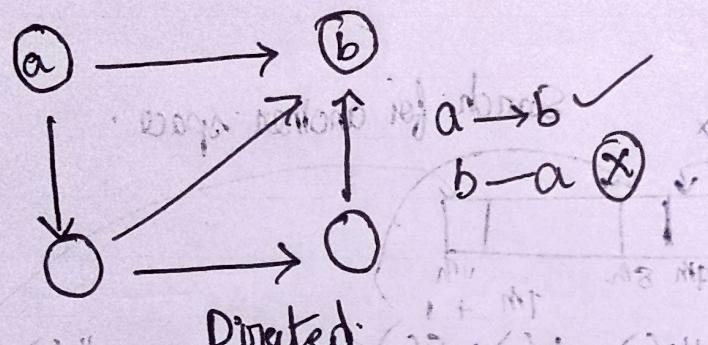
Complexity →  $O(k)$  →  $\sim O(1)$  if  $(n \gg k)$ .

# Graphs # 85



What - ?

Graph is a type of data structure with a combination of nodes & edges.



Directed:

Indegree ( $b$ ) = 3

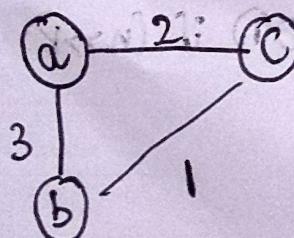
Outdegree ( $b$ ) = 0

Outdegree ( $a$ ) = 2

→ Node → Entity to store data      Degree( $v$ ) = 3

→ Edge → Connecting Nodes      Degree ( $u$ ) = 2

→ weighted graph



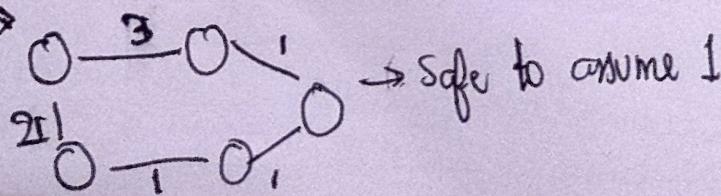
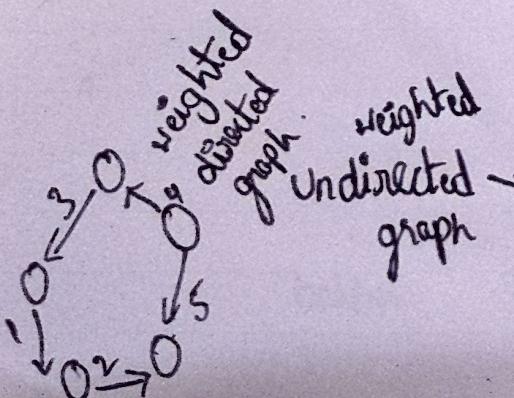
Degree( $v$ ) = 3

Degree ( $u$ ) = 2

$a - c \rightarrow 2$

$a - b \rightarrow 3$

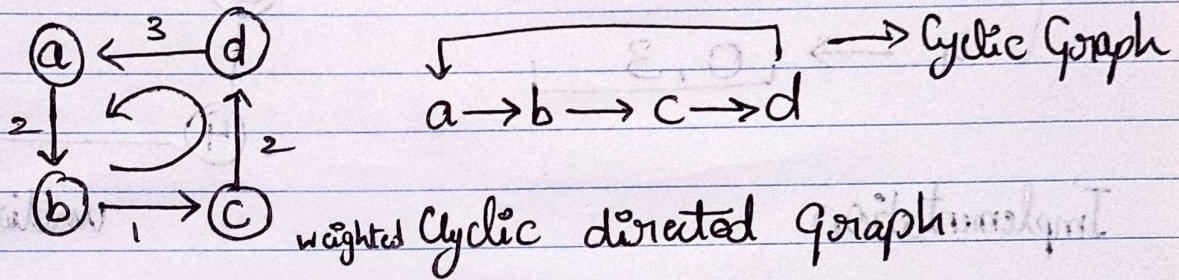
$b - c \rightarrow 1$



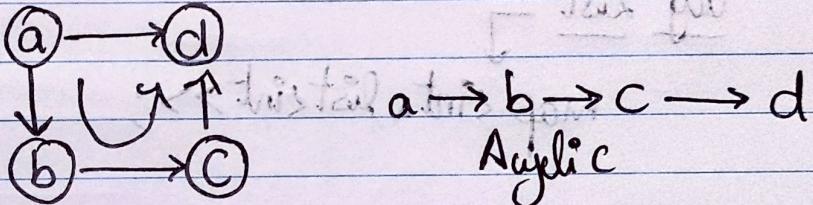
→ Safe to assume 1

$\Rightarrow \text{Path} = U-V-P$   
 $= P-Q-V:$   
 $- P-Q-V-P \times \text{NOT a path.}$

### Cyclic Graph.



### Acyclic Graph



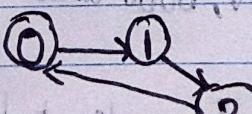
### Graph

- Adjacency Matrix
- Adjacency List

### ① → Adjacency Matrix

	0	1	2
0	0	1	0
1	0	0	1
2	1	0	0

S.C  $\rightarrow O(n^2)$



i/p  $\rightarrow$

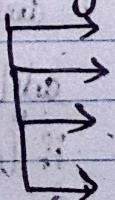
No. of nodes ( $n$ )  
 No. of edges ( $m$ )

$n=3, m=3$

0  $\rightarrow$  1

1  $\rightarrow$  2

2  $\rightarrow$  0

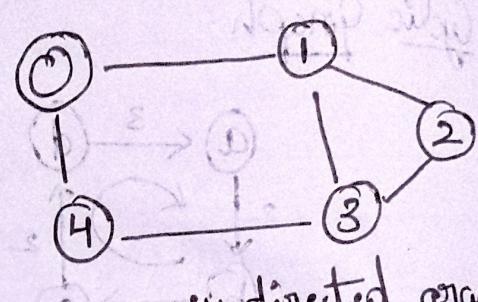
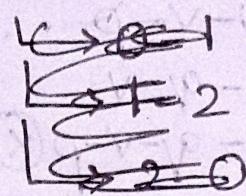


edges.

## ② Adjacency List

adj list

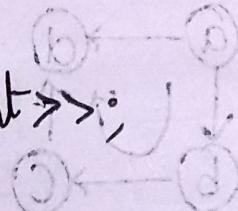
0 →	<u>1, 4</u>
1 →	<u>0, 3, 2</u>
2 →	<u>1, 3</u>
3 →	<u>4, 1, 2</u>
4 →	<u>0, 3</u>



Implementation: ~~bottom up approach~~ ~~top down approach~~ ~~iterative~~ ~~undirected graph~~

adj list ↴

~~b ← c~~ map<int, list<int>>;



Code :-

class graph

{

public:

unordered\_map<int, list<int>> adj;

void addEdge(int u, int v, bool direction)

{

// direction = 0 → undirected

// direction = 1 → directed

adj[u].push\_back[v];

if (direction == 0)

{ adj[v].push\_back(u); }

void printAdjList()

{

for (auto i : adj)

cout << i.first <<

i.second << endl;

for (auto j : i.second)

cout << j <<

endl;

cout << endl;

3

1,

0	1	3
1	0	3
3	1	0

184 Mark Mark  
(A)

```
int main() {  
    // Code  
}
```

*int n;*

```
cout << "Enter the number of nodes" << endl;  
cin >> n;
```

`int m;`

```
cout << "Enter the number of edges" << endl;
cin >> m;
```

graph g;

```
for(int i=0; i<m; i++)
```

3

int u,v;

`cin >> u >> v;`

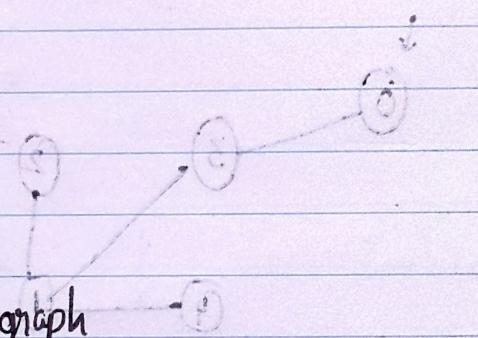
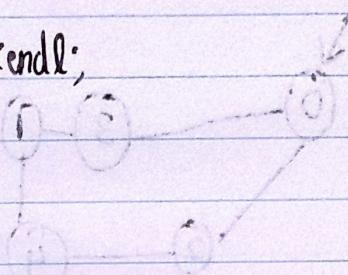
## 11 Creating An Undirected graph

g.addEdge(v, v, 0);

3.

g. printAdjList();

3



AP  
AS  
AT  
AE  
AQ

$\times$  short hand  $\times$  O. short hand

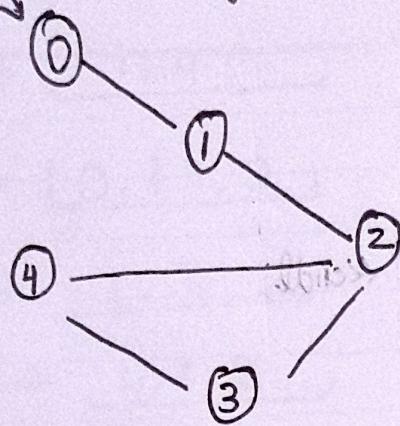
~~elbow to~~

## Construction

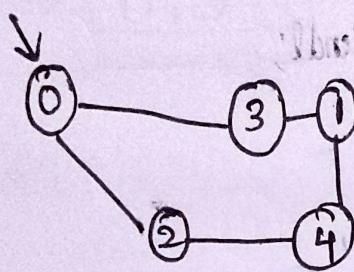
卷之三

# Breadth First Search #86

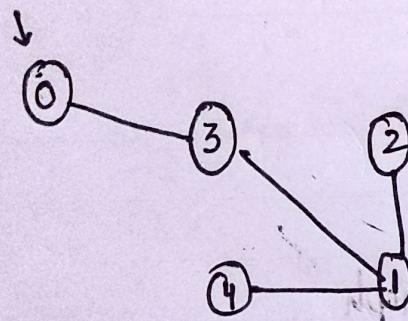
(BFS)



point  $\rightarrow 0, 1, 2, 3, 4$



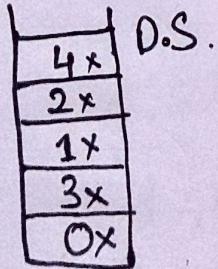
$\rightarrow 0, 2, 3, 4, 1$



visited  $\rightarrow 0, S$

unordered\_map<node, bool>;

queue  $\rightarrow$  FIFO



q

frontNode = 0  $\times$  frontNode = 3  $\times$

ans  $\rightarrow 0, 3, 1, 2, 4$

frontNode = 1  $\times$

frontNode = 2  $\times$

frontNode = 4

adj  $\rightarrow$  list

0  $\rightarrow$  3

1  $\rightarrow$  2, 3, 4

2  $\rightarrow$  1

3  $\rightarrow$  0, 1

4  $\rightarrow$  1

Visited

0  $\rightarrow$  f  $\rightarrow$  T

1  $\rightarrow$  f  $\rightarrow$  T

2  $\rightarrow$  f  $\rightarrow$  T

3  $\rightarrow$  f  $\rightarrow$  T

4  $\rightarrow$  f  $\rightarrow$  T

if (!visited[node])

{  
    bfs();  
}

## BFS Code Implementation

```
vector<int> bfsOfGraph (int V, vector<int> adj[ ])
```

```
vector<int> ans;
```

```
vector<int> vis(V, 0);
```

```
queue<int> q;
```

```
q.push(0);
```

```
vis[0] = 1
```

```
while (!q.empty())
```

```
int front = q.front();
```

```
q.pop();
```

```
ans.push_back(front);
```

for each

```
for (auto &it : adj[front])
```

```
{}
```

```
if (!vis[it])
```

```
{}
```

```
q.push(it);
```

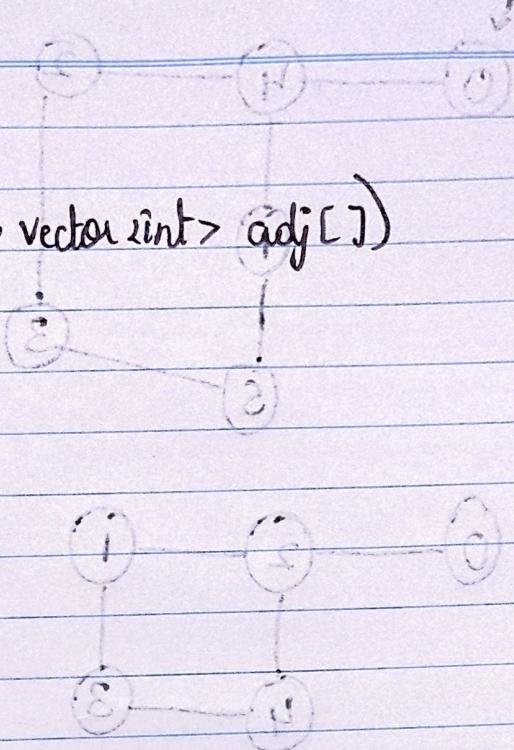
```
vis[it] = 1;
```

```
}
```

```
}
```

```
return ans;
```

```
}
```



(0) 2.16

(1) 2.16

(2) 2.16

(3) 2.16

(4) 2.16

(5) 2.16

2.16

2.16 0

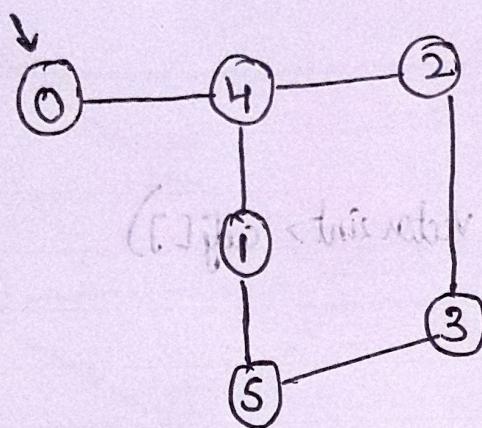
2.16 2.16

2.16 2.16 1

2.16 2.16 2

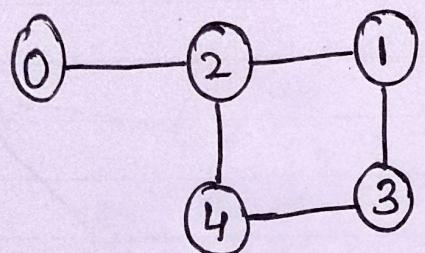
2.16 2.16 3

( Depth First Search (DFS) #87 T.C  $\rightarrow O(n)$



BFS - 0, 1, 2, 3, 4, 5

DFS - 0, 4, 2, 3, 5, 1



Ci      dfs()

for ( \_\_\_\_\_ )  
  {  
    if (!visited[Ci])  
      {

vist

0  $\rightarrow$  f  $\rightarrow$  T

2  $\rightarrow$  f  $\rightarrow$  T

1  $\rightarrow$  f  $\rightarrow$  T

3  $\rightarrow$  f  $\rightarrow$  T

4  $\rightarrow$  f  $\rightarrow$  T

dfs(0)



dfs(2)



dfs(1)



dfs(3)



dfs(4)

## Implementation

```
void dfs(int node, vector<int>& ans, vector<int>& visited, vector<int> adj[])
```

```
{
```

```
    ans.push_back(node);
```

```
    visited[node] = 1;
```

```
    for (auto it : adj[node])
```

```
{
```

```
        if (visited[it] == 0)
```

```
{
```

```
            dfs(it, ans, visited, adj)
```

```
}
```

```
}
```

```
}
```

```
vector<int> dfsOfGraph(int v, vector<int> adj[])
```

```
{
```

```
    vector<int> visited(v, 0);
```

```
    vector<int> ans;
```

```
    dfs(0, ans, visited, adj)
```

```
    return ans;
```

```
}
```