

77) Convex hull

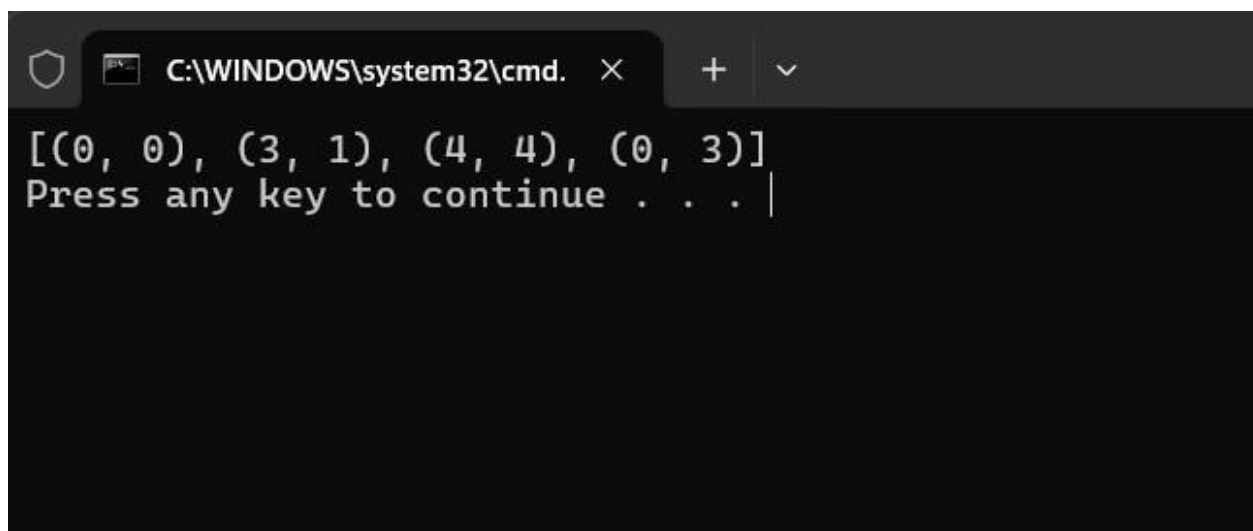
CODE:

```
def convex_hull(points):
    points = sorted(points)
    def cross(o, a, b):
        return (a[0] - o[0]) * (b[1] - o[1]) - (a[1] - o[1]) * (b[0] - o[0])
    lower = []
    for p in points:
        while len(lower) >= 2 and cross(lower[-2], lower[-1], p) <= 0:
            lower.pop()
        lower.append(p)
    upper = []
    for p in reversed(points):
        while len(upper) >= 2 and cross(upper[-2], upper[-1], p) <= 0:
            upper.pop()
        upper.append(p)
```

```
    return lower[:-1] + upper[:-1]
```

```
points = [(0, 3), (1, 1), (2, 2), (4, 4), (0, 0), (1, 2), (3, 1)] hull =
convex_hull(points) print(hull)
```

OUTPUT:



```
C:\WINDOWS\system32\cmd. x + v
[(0, 0), (3, 1), (4, 4), (0, 3)]
Press any key to continue . . . |
```

TIME COMPLEXITY : $O(n \log n)$