

Medical Image Analysis

Week 3: Assignment Key and Solution

Answer key:

Q. No.	Ans. Key	Q. No.	Ans. Key
1	c	11	d
2	a	12	c
3	b	13	b
4	a	14	b
5	d	15	a
6	a	16	c
7	c	17	d
8	d	18	b
9	b	19	a
10	d	20	b

Solutions to selected questions:

Q1. Refer Lec. 3.1_3.2 Slide No. 13.

Node 1: $p(C1) = 15/25$, $p(C2) = 10/25$

Entropy (Node 1) = $-(p(C1)\log_{10}(p(C1))+p(C2)\log_{10}(p(C2))) = 0.29$

Node 2: $p(C1) = 8/12$, $p(C2) = 4/12$

Entropy (Node 2) = $-(p(C1)\log_{10}(p(C1))+p(C2)\log_{10}(p(C2))) = 0.28$

Node 3: $p(C1) = 7/13$, $p(C2) = 6/13$

Entropy (Node 3) = $-(p(C1)\log_{10}(p(C1))+p(C2)\log_{10}(p(C2))) = 0.30$

Q2. Refer Lec. 3.1_3.2 Slide No. 13.

Information gain = Entropy(Node 1) – (((12/25)*Entropy(Node 2))+((13/25)*Entropy(Node 3))) = 0

Q3. In the last layer only node no. 6 is the pure node and the other can be split further for getting pure node.

Q4. Refer Lec. 3.1_3.2 Slide No. 13. (Follow down steps from **Q1**)

Q5. Calculate the entropy for both the trees as discussed in Lec.3.1_3.2 Slide No. 13. (Follow down steps from **Q1**)

Q6. Calculate the information gain for both the nodes as discussed Lec.3.1_3.2 Slide No.13). (Follow down steps from **Q2**)

Q7. Calculate the posterior probability by no of sample for one particular class present in one node.

Such as, $p(\omega_1, n_5^1) = \frac{0}{6} = 0$ and $p(\omega_2, n_5^1) = \frac{6}{6} = 1$.

Q8. Calculate the values of posterior probability of class1 and class2 for the total forest as discussed in Lec. 3.1_3.2 Slide No.20.

$$P(\text{class1}) = (1/5) \times (0.375 + 0.625 + 0.5 + 0.555 + 0.667) = 0.54$$

Q9. Refer Lec. 3.3 Slide no. 3

Q10. $y = \frac{1}{1+e^{-x}}$

$$\frac{\partial y}{\partial x} = \frac{-1}{(1+e^{-x})^2} (-e^{-x}) = \frac{1+e^{-x}-1}{(1+e^{-x})^2} = \frac{1}{(1+e^{-x})} + \frac{1}{(1+e^{-x})^2} = \frac{1}{(1+e^{-x})} \left[1 - \frac{1}{(1+e^{-x})} \right] = y(1-y)$$

Q11. Output of node 1 = $0.2 + (0.1 \times 1) + (0.15 \times 2) + (0.3 \times 3) = 1.5$, after non-linearity = 0.82

Output of node 2 = $0.05 + (0.05 \times 1) + (0.01 \times 2) + (0.03 \times 3) = 0.21$, after non-linearity = 0.55

$$J(W) = \sum_n \|p_n - \hat{p}_n\| = 0.5 * \sqrt{(1 - 0.82)^2 + (0 - 0.55)^2} = 0.58$$

Q12. Refer Lec. 3.3 Slide no. 7, demonstration on neural network

Q13. Refer Lec. 3.4_3.5 Slide no. 17

Q15. For, module = nn.SpatialConvolution(nInputPlane, nOutputPlane, kW, kH, [dW], [dH], [padW], [padH])

$$\text{owidth} = \text{floor}((\text{width} + 2 * \text{padW} - \text{kW}) / \text{dW} + 1) = \text{floor}((32 + 2 * 0 - 5) / 1 + 1) = 28$$

$$\text{ohight} = \text{floor}((\text{height} + 2 * \text{padH} - \text{kH}) / \text{dH} + 1) = 28$$

$$\text{nChannels} = \text{nOutputPlane} = 6$$

Q16. Refer deep neural network demonstration

Q17. Refer Lec. 3.4_3.5 Slide no. 17

Q18. Refer Lec. 3.4_3.5 Slide no. 17

Q19. Refer Lec. 3.4_3.5 Slide no. 17

Q20. Refer Lec. 3.4_3.5 Slide no. 17