

# Reading Notes of *Causal Inference*

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## Causal inference without models

### 1 A definition of causal effect

#### 1.1 Individual causal effects

Causal effect for individual  $i$ :

$$Y_i^{a=1} \neq Y_i^{a=0}$$

the treatment  $A$  has a causal effect on an individual's outcome  $Y$  if  $Y^{a=1} \neq Y^{a=0}$  for the individual.

That is, for individual  $i$ ,  $Y^{a=1}$  (is a random variable, read  $Y$  under treatment  $a = 1$ ), the outcome variable that would have been observed under the treatment value  $a = 1$  is not equal to the outcome variable that would have been observed under the treatment value  $a = 0$  ( $Y^{a=0}$ ). The variables  $Y^{a=1}$  and  $Y^{a=0}$  are referred to as *potential outcomes* or as *counterfactual outcomes*. In economics, we often refer “counterfactual outcomes” to outcomes that had not happen. But here, both  $Y^{a=0}$  and  $Y^{a=1}$  are counterfactual outcomes, no matter actually  $a = 0$  or  $a = 1$ .

the counterfactual outcomes that corresponds to the treatment value that the individual actually received is *actually factual*.

Consistency:

$$\text{if } A_i = a, \text{ then } Y_i^a = Y^{A_i} = Y_i$$

an individual with observed treatment  $A = a$ , has observed outcome  $Y$  equal to his counterfactual outcome  $Y^a$ .

That is, the observed outcome is equal to what (we think that) would have been observed.

In general, individual causal effects cannot be identified – that is, cannot be expressed as a function of the observed data – because of missing data.

#### 1.2 Average causal effects