

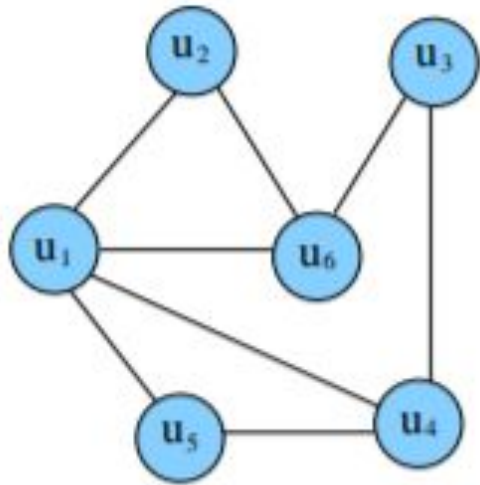
Kernelized Probabilistic Matrix Factorization

Alexeychuk Nikita
Belikova Kristina
Gazdieva Milena
Kuzin Mikhail
Maksimov Ivan

Problem statement

Matrix completion problem

1. Recommendation systems
2. Image restoration



(a) Social network graph

| | i_1 | i_2 | i_3 | i_4 |
|-------|-------|-------|-------|-------|
| u_1 | 3 | 5 | ? | 5 |
| u_2 | ? | 1 | ? | 4 |
| u_3 | 3 | ? | 4 | 1 |
| u_4 | ? | ? | 5 | 5 |
| u_5 | 5 | ? | ? | 2 |
| u_6 | ? | 4 | 2 | ? |

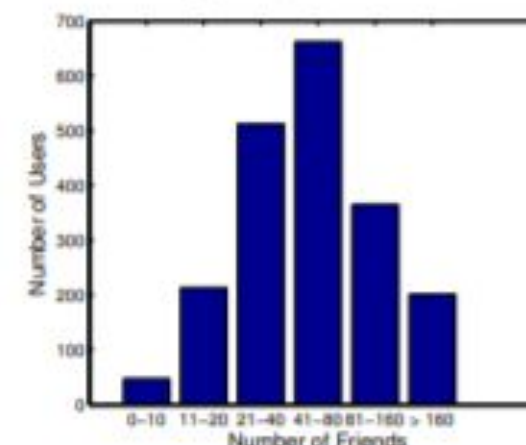
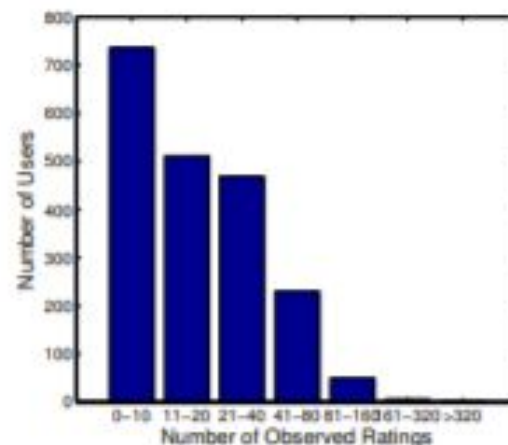
(b) Rating matrix



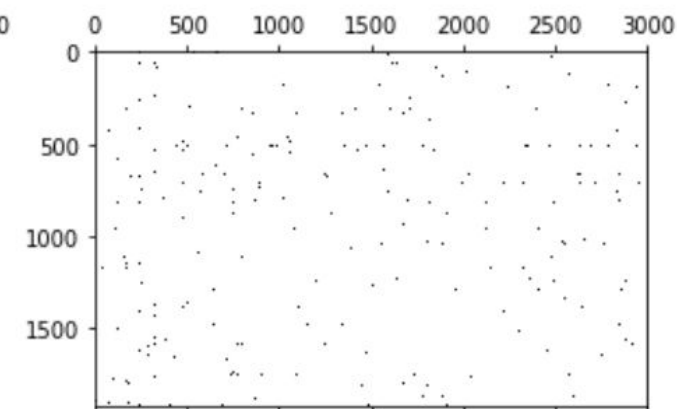
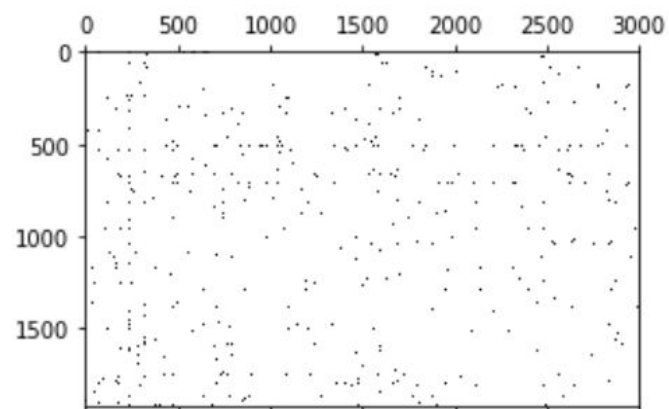
Methodology - Dataset

Dataset: Epinion

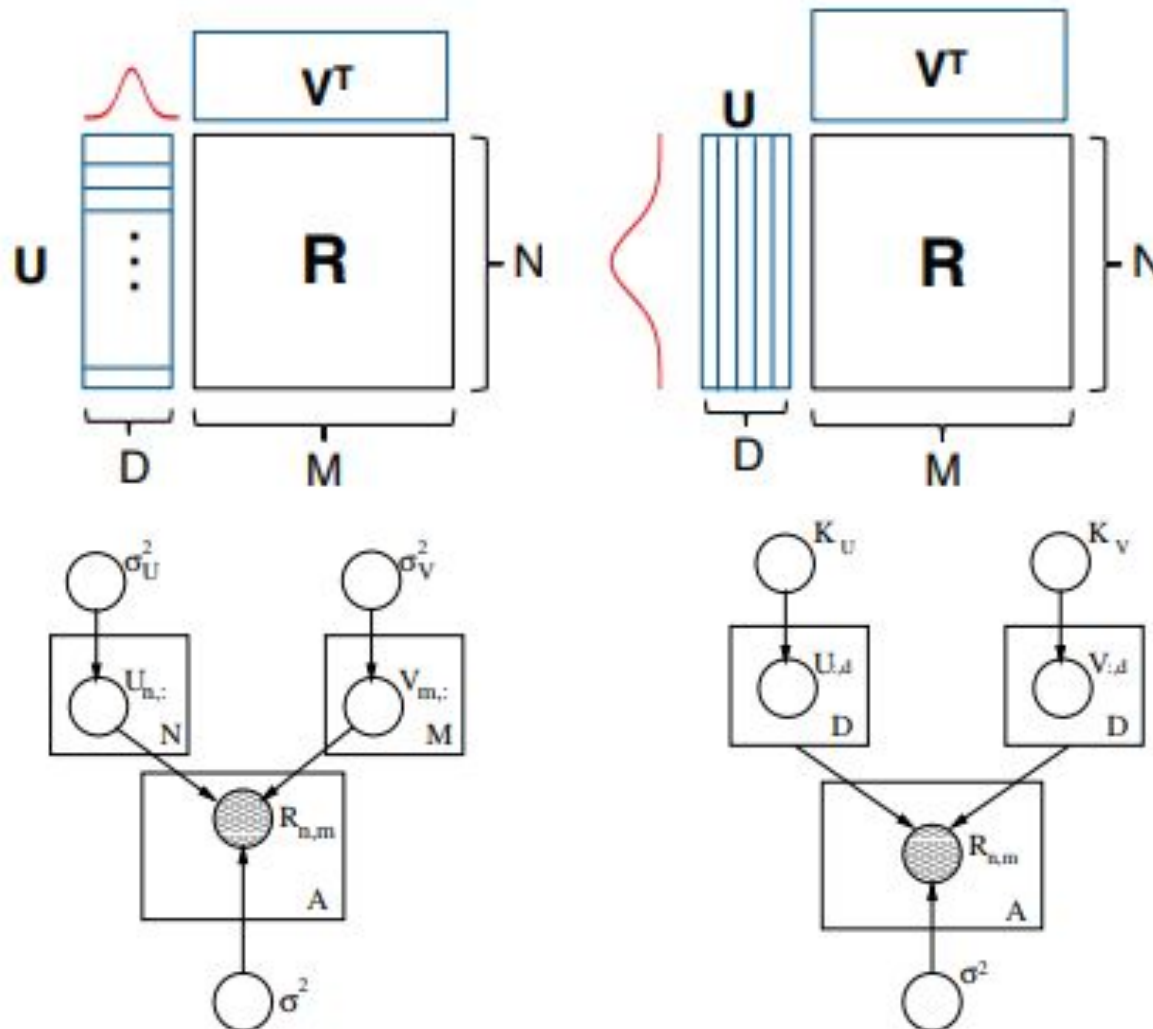
| | |
|--------------------------|--------|
| Number of Users | 2 000 |
| Number of Items | 3 000 |
| Number of Rating | 60 485 |
| Number of Relations | 32 548 |
| User-Item matrix density | 1.01% |



1. Get User-Item matrix (X_{full})
2. Drop randomly 25% of its elements (X_{trun})
3. Run decomposition on X_{trun} , trying to impute missing values $\Rightarrow X_{trun_imputed}$
4. $RMSE(X_{trun}; X_{trun_imputed})$



Methodology - PMF vs KPMF



- PMF
 - U is sampled in a “row-wise” manner
 - independent latent v . for each row
- KPMF
 - U is sample in a “column-wise”
 - latent vectors spanning all rows
 - uses side information

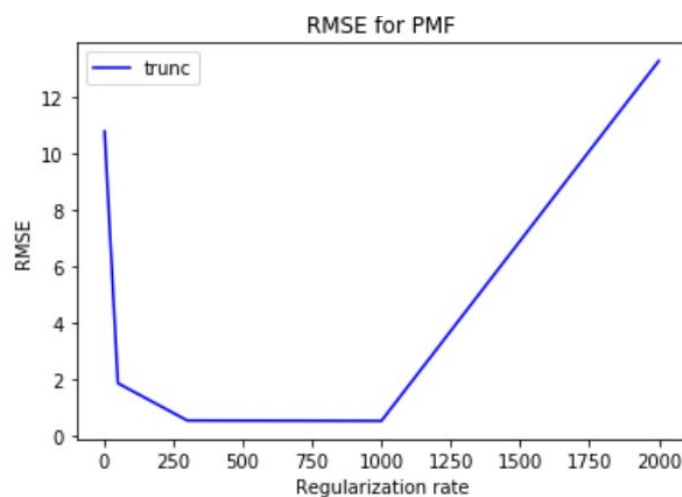
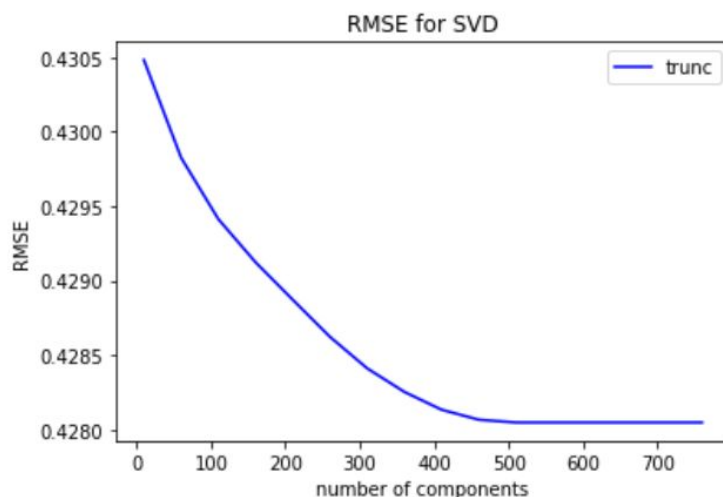
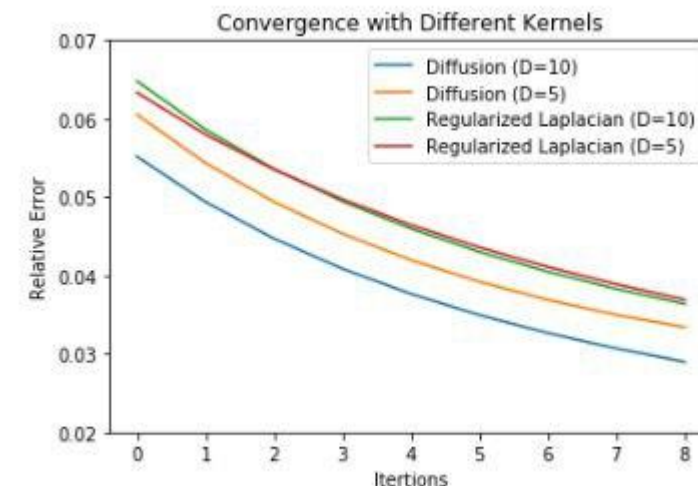
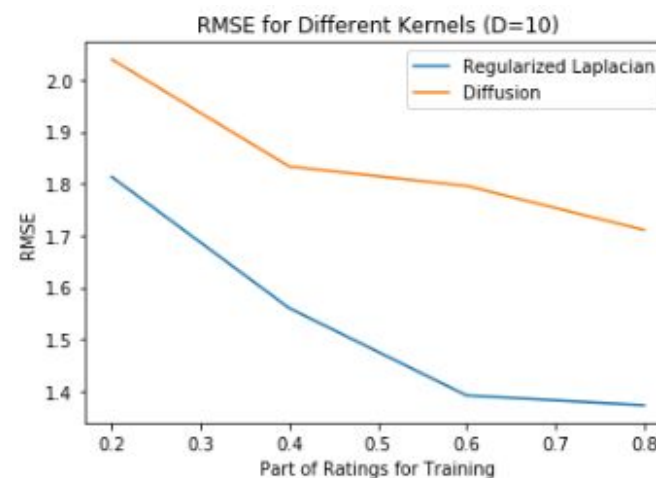
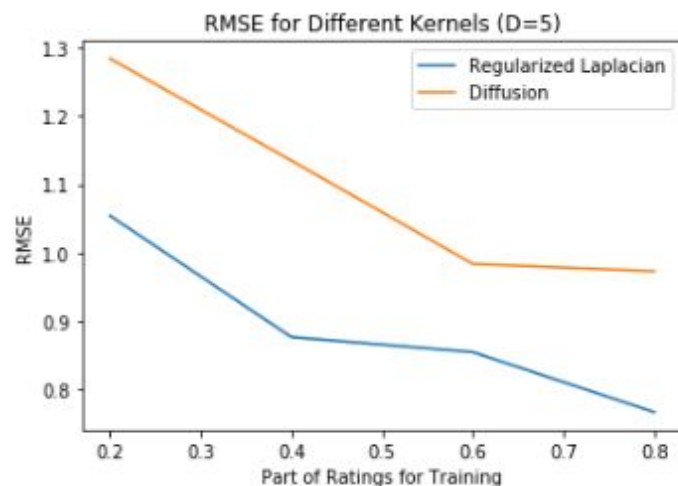
KPMF: Maximize the log-posterior

$$\begin{aligned} & \log p(U, V | R, \sigma^2, K_U, K_V) \\ &= -\frac{1}{2\sigma^2} \sum_{n=1}^N \sum_{m=1}^M \delta_{n,m} (R_{n,m} - U_{n,:} V_{m,:}^T)^2 \\ & \quad - \frac{1}{2} \sum_{d=1}^D U_{:,d}^T S_U U_{:,d} - \frac{1}{2} \sum_{d=1}^D V_{:,d}^T S_V V_{:,d} \\ & \quad - A \log \sigma^2 - \frac{D}{2} (\log |K_U| + \log |K_V|) + C, \end{aligned}$$

Define a similarity measure for users' taste

- Diffusion kernel $K_D = \lim_{n \rightarrow \infty} \left(1 - \frac{\beta L}{n}\right)^n = e^{-\beta L},$
- Regularized laplacian $K_{RL} = (I + \gamma L)^{-1},$

Results



| Model with top parameters | RMSE |
|--|-------|
| KPMF (D = 5; Kernel = 'Regularized Laplacian') (need more iteration!) | 0.763 |
| PMF (regularization_rate = 300) | 0.431 |
| SVD (n_comp = 550) | 0.423 |