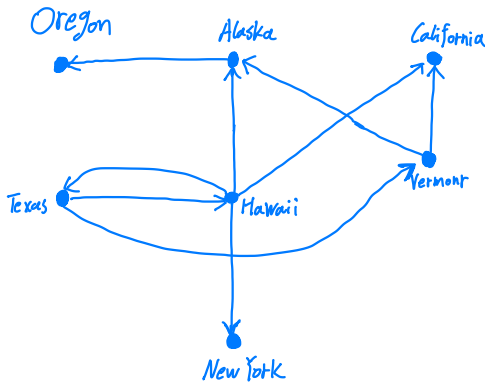


$V(\text{StateGraph}) = \{\text{Oregon, Alaska, Texas, Hawaii, Vermont, New York, California}\}$

$E(\text{StateGraph}) = \{(\text{Alaska, Oregon}), (\text{Hawaii, Alaska}), (\text{Hawaii, Texas}), (\text{Texas, Hawaii}), (\text{Hawaii, California}), (\text{Hawaii, New York}), (\text{Texas, Vermont}), (\text{Vermont, California}), (\text{Vermont, Alaska})\}$

1. Draw the StateGraph



1. Describe the graph pictured above, using the formal graph notation.

$V(\text{StateGraph}) =$

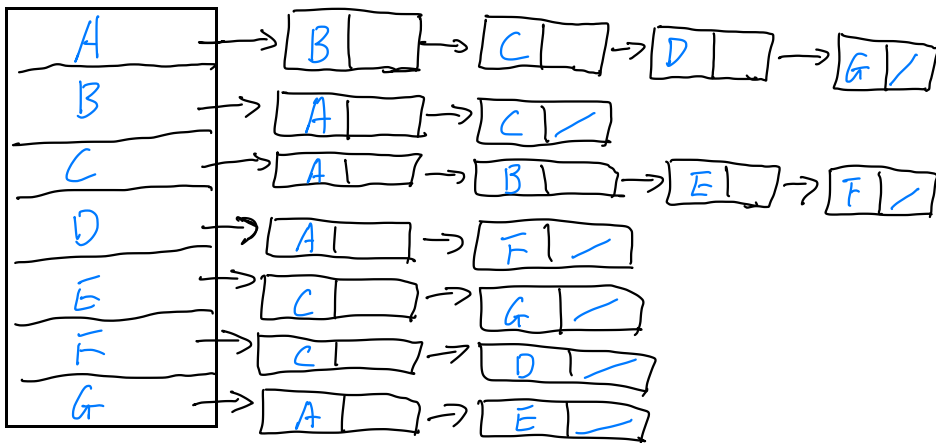
$E(\text{StateGraph}) =$

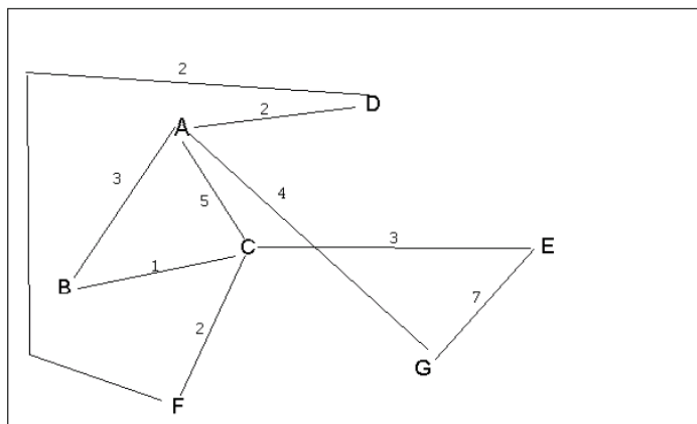
2. a. Is there a path from Oregon to any other state in the graph? *No*
- b. Is there a path from Hawaii to every other state in the graph? *Yes*
- c. From which state(s) in the graph is there a path to Hawaii? *Texas*

1. a. Show the adjacency matrix that would describe the edges in the graph.
Store the vertices in alphabetical order

States							
Alaska	0	0	0	0	1	0	0
California	0	0	0	0	0	0	0
Hawaii	1	1	0	1	0	1	0
New York	0	0	0	0	0	0	0
Oregon	0	0	0	0	0	0	0
Texas	0	0	1	0	0	0	1
Vermont	1	1	0	0	0	0	0

3. b. Show the adjacency lists that would describe the edges in the graph





4 a. Which of the following lists the graph nodes in depth first order beginning with E?

A) E, G, F, C, D, B, A

B) G, A, E, C, B, F, D

C) E, G, A, D, F, C, B ✓

D) E, C, F, B, A, D, G

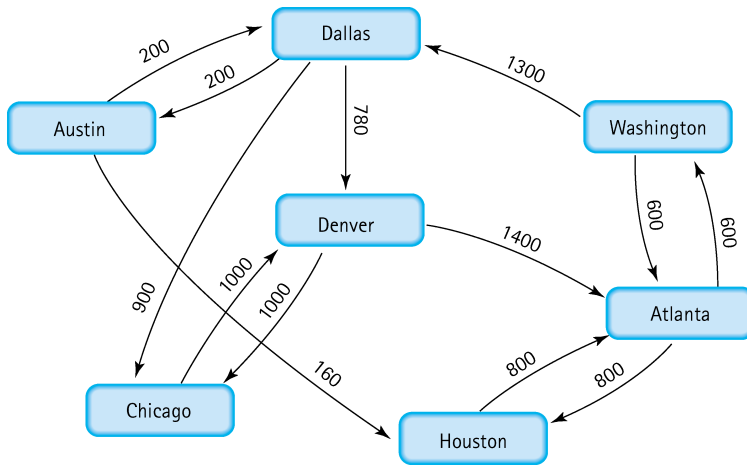
4 b. Which of the following lists the graph nodes in breadth first order beginning at F?

A) F, C, D, A, B, E, G

B) F, D, C, A, B, C, G

C) F, C, D, B, G, A, E

D) a, b, and c are all breadth first traversals ✓



5. Find the shortest distance from Atlanta to every other city

Atlanta to Washington : 600

Atlanta to Houston : 800

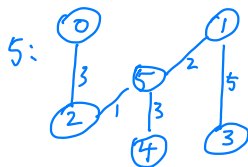
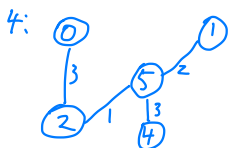
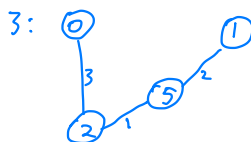
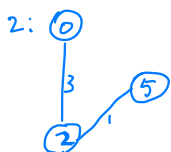
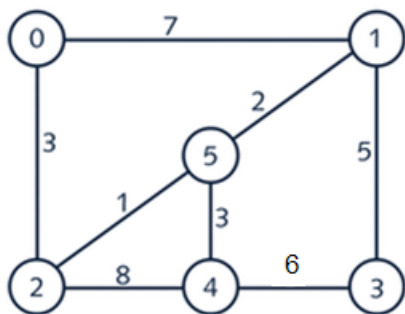
Atlanta to Dallas : $600 + 1300 = 1900$

Atlanta to Denver : $600 + 1300 + 780 = 2680$

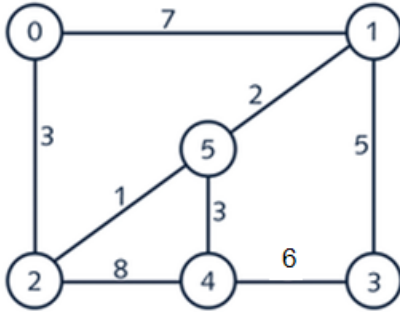
Atlanta to Austin : $600 + 1300 + 200 = 2100$

Atlanta to Chicago : $600 + 1300 + 900 = 2800$

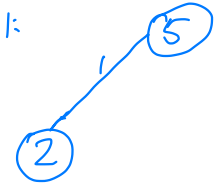
6. Find the minimal spanning tree using Prim's algorithm. Use 0 as the source vertex . Show the steps.



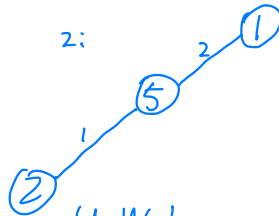
7. Find the minimal spanning tree using Kruskal's algorithm.
Show the weights in order and the steps.



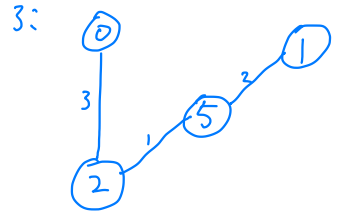
Weight_List = {1, 2, 3, 4, 5, 6, 7, 8}



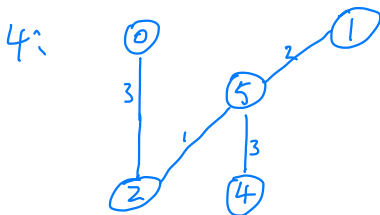
Updated Weight_List
= {2, 3, 3, 5, 6, 7, 8}



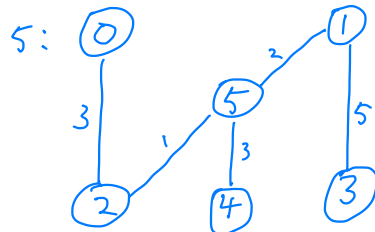
U.W.L
= {3, 3, 5, 6, 7, 8}



U.W.L
= {3, 5, 6, 7, 8}

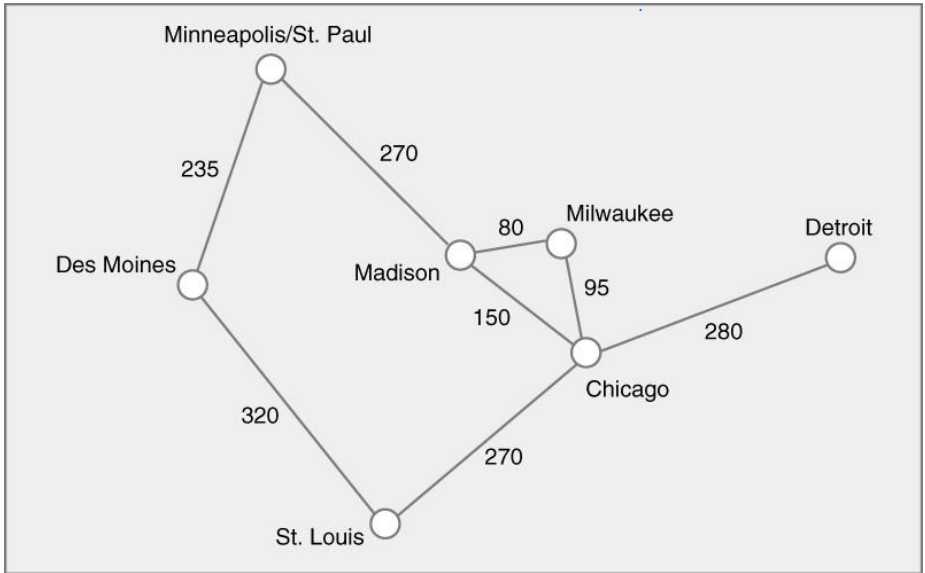


U.W.L
= {5, 6, 7, 8}

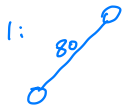


U.W.L
= {6, 7, 8}

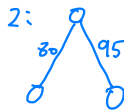
8. Find the minimal spanning tree using the algorithm you prefer. Use Minneapolis/St. Paul as the source vertex



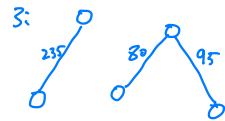
Weight_List = {80, 95, 150, 235, 270, 270, 280, 320}



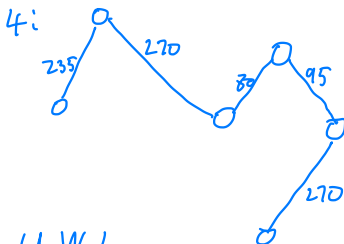
U.W.L
= {95, 150, 235, 270,
270, 280, 320}



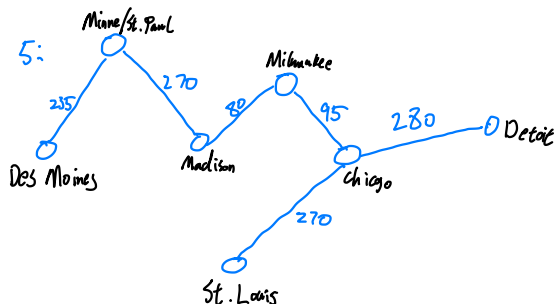
U.W.L
= {150, 235, 270,
270, 280, 320}



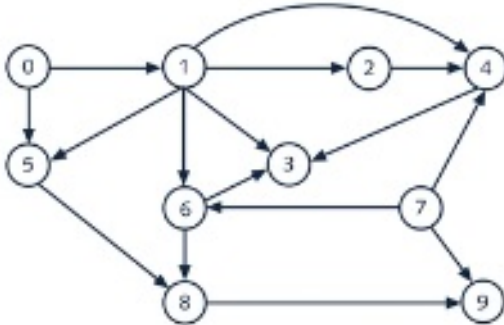
U.W.L
= {270, 270, 280, 320}



U.W.L
= {280, 320}



9. List the nodes of the graph in a breadth first topological ordering. Show the steps using arrays predCount, topologicalOrder and a queue



1: PredCount []

0	1	2	3	4	5	6	7	8	9
0	1	1	3	3	2	2	0	2	2

Queue

0	7			
---	---	--	--	--

↑
remove from f place in topological []

0									
---	--	--	--	--	--	--	--	--	--

Success node '0' over 1.5

$$\text{Predcount}[1] = \text{Predcount}[1] - 1$$

$$\text{Predcount}[5] = \text{Predcount}[5] - 1$$

2: Precount []

0	1	2	3	4	5	6	7	8	9
0	1	1	3	3	1	2	0	2	2

decrement

Queue

7	1	1			
---	---	---	--	--	--

front

t_sore

0	7								
---	---	--	--	--	--	--	--	--	--

Successors of node 7 are: 4, 6, 9

Successor precount of node = 4, 6, 9

3: Precount []

0	1	2	3	4	5	6	7	8	9
0	0	1	3	2	1	1	0	2	1

decremented

Queue :

1					
---	--	--	--	--	--

front

t_sore

0	7	1							
---	---	---	--	--	--	--	--	--	--

Successors of node 1: 2, 3, 4, 5, 6

Decrement Precount [] of node 2, 3, 4, 5, 6

4:

0	1	2	3	4	5	6	7	8	9
0	0	0	2	1	0	0	0	2	1

decrement

Decrement

Queue

2	5	6			
---	---	---	--	--	--

t_sore

0	7	1	2						
---	---	---	---	--	--	--	--	--	--

Sum of node: 2: 4

5:

0	1	2	3	4	5	6	7	8	9
0	0	0	2	0	0	0	0	2	1

↑

Sum of node: 8

Queue

5	6	4			
---	---	---	--	--	--

front

t_sore

0	7	1	2	5					
---	---	---	---	---	--	--	--	--	--

6: Predcount[] decrement Predcount[8]

0	1	2	3	4	5	6	7	8	9
0	0	0	2	0	0	0	0	1	1

Successor of node 6: 3, 8

Queue

6	4	1	1	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---

T-Sort

0	7	1	2	5	6				
---	---	---	---	---	---	--	--	--	--

7: Predcount[]

0	1	2	3	4	5	6	7	8	9
0	0	0	1	0	0	0	0	0	1

Queue

4	8	1	1	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---

T-Sort

0	7	1	2	5	6	4			
---	---	---	---	---	---	---	--	--	--

Successor of node 4: 3

8: Predcount[]

0	1	2	3	4	5	6	7	8	9
0	0	0	0	0	0	0	0	0	1

Queue

8	3	1	1	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---

T-Sort

0	7	1	2	5	6	4	8		
---	---	---	---	---	---	---	---	--	--

Successor of node 8: 9

9: Predcount

0	1	2	3	4	5	6	7	8	9
0	0	0	0	0	0	0	0	0	0

Queue

3	9	1	1	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---

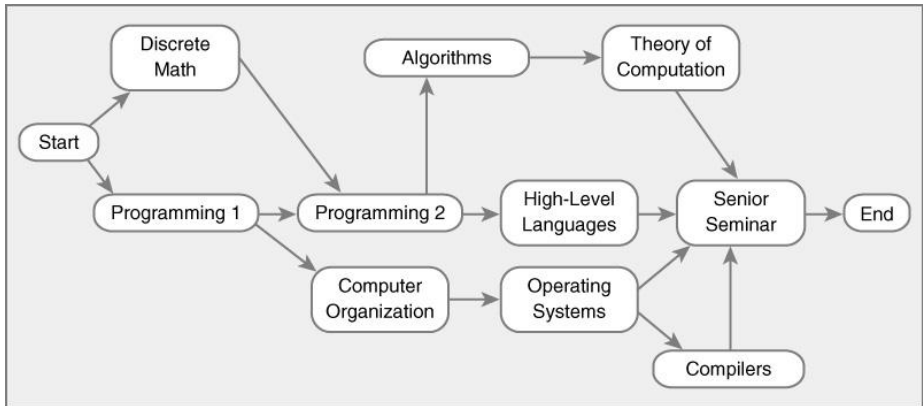
Final Sort

T-Sort

0	7	1	2	5	6	4	8	3	9
---	---	---	---	---	---	---	---	---	---

Successor of 3 and 9 all null.

10. List the nodes of the graph in a breadth first topological ordering.



Start

Discrete Math

Programming 1

Programming 2

Computer Organization

Algorithms

High-Level Languages

Operating Systems

Theory Computation

Senior Seminar

Compilers

End