

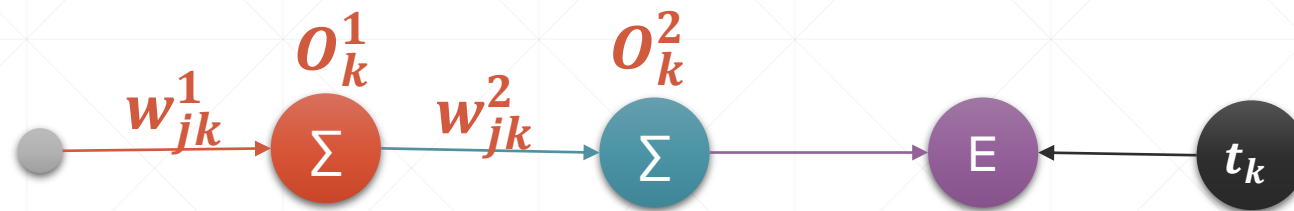


# MLP反向传播

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主讲人：龙良曲

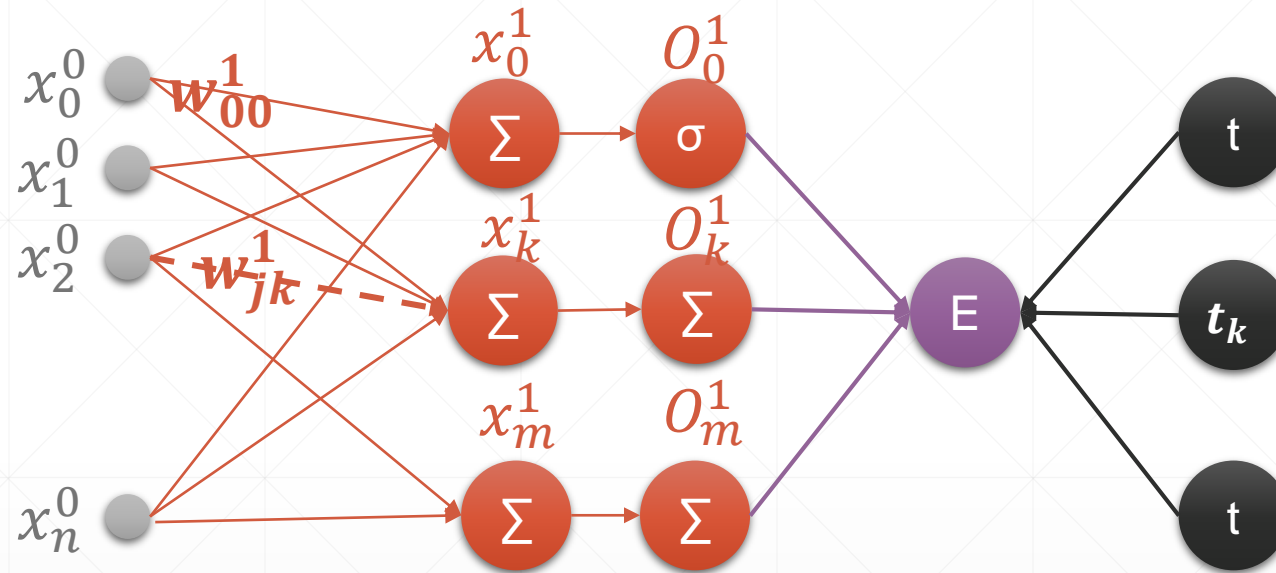
# Chain rule



$$\blacksquare \frac{\partial E}{\partial w_{jk}^1} = \frac{\partial E}{\partial O_k^1} \frac{\partial O_k^1}{\partial x} = \frac{\partial E}{\partial O_k^2} \frac{\partial O_k^2}{\partial O_k^1} \frac{\partial O_k^1}{\partial x}$$

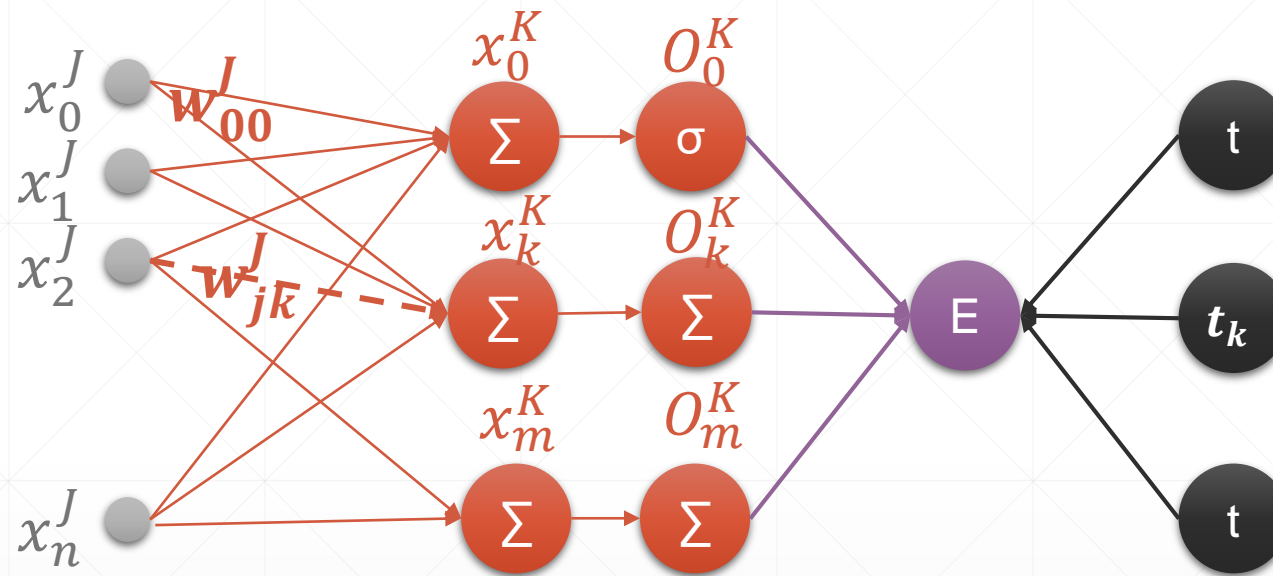
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# Multi-output Perceptron

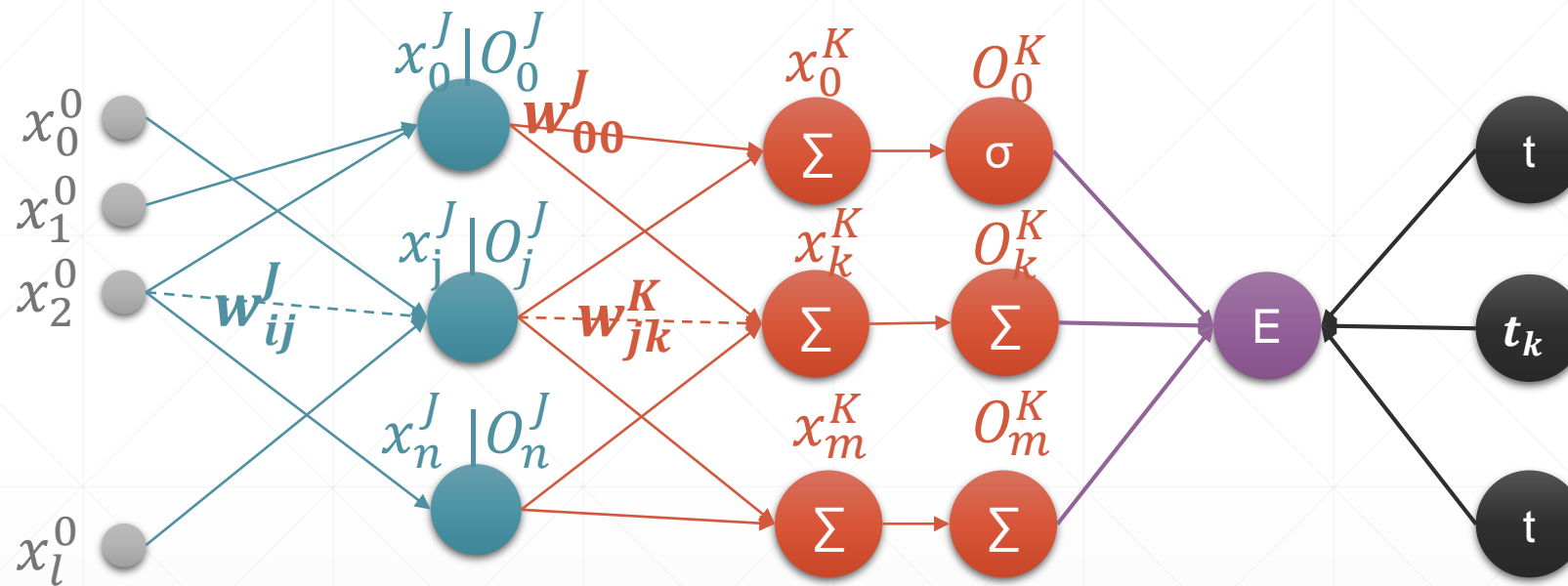


$$\frac{\partial E}{\partial w_{jk}} = (O_k - t_k) O_k (1 - O_k) x_j^0$$

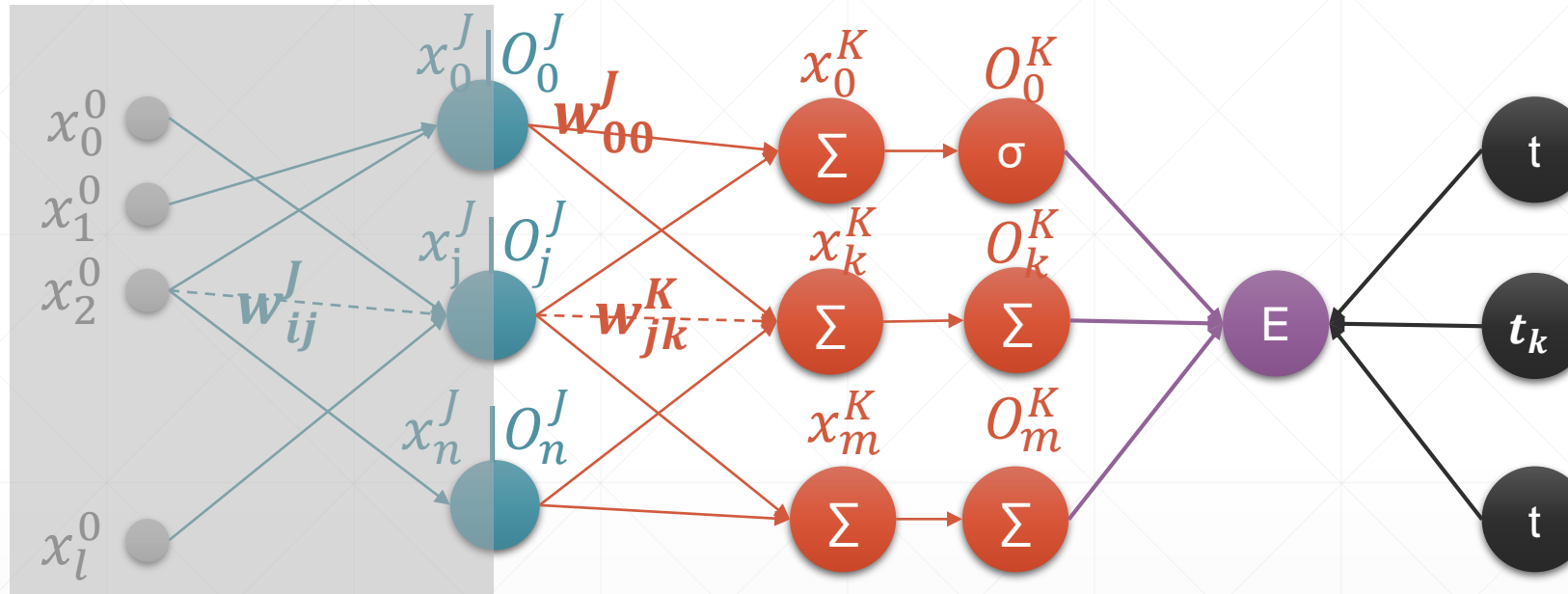
# Multi-Layer Perceptron



# Multi-Layer Perceptron



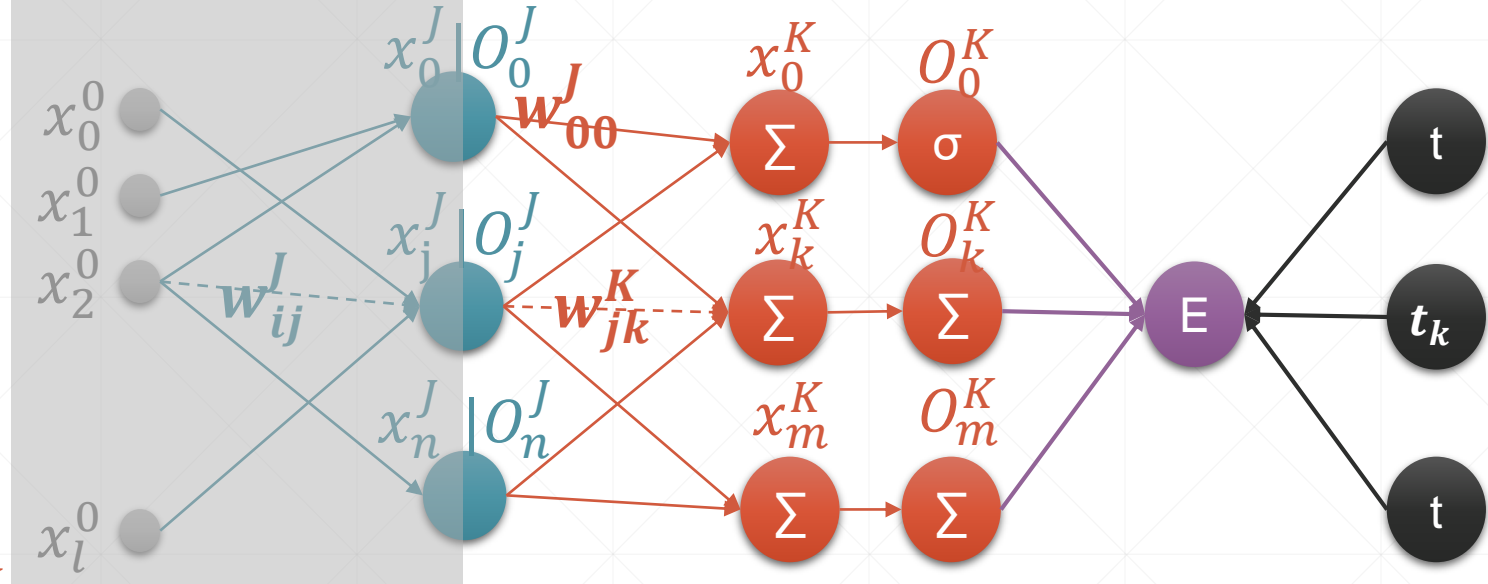
# Multi-Layer Perceptron



$$\frac{\partial E}{\partial w_{jk}} = (O_k - t_k) O_k (1 - O_k) x_j^0$$

$$\frac{\partial E}{\partial w_{jk}} = (O_k - t_k) O_k (1 - O_k) O_j^J$$

# Multi-Layer Perceptron



$$\frac{\partial E}{\partial w_{jk}} = (O_k - t_k) O_k (1 - O_k) O_j^J$$

$$\frac{\partial E}{\partial w_{jk}} = \delta_k^K O_j^J$$

$$\frac{\partial E}{\partial W_{ij}} = \frac{\partial}{\partial W_{ij}} \frac{1}{2} \sum_{k \in K} (\mathcal{O}_k - t_k)^2$$

$$\frac{\partial E}{\partial W_{ij}} = \sum_{k \in K} (\mathcal{O}_k - t_k) \frac{\partial}{\partial W_{ij}} \mathcal{O}_k$$

$$\frac{\partial E}{\partial W_{ij}} = \sum_{k \in K} (\mathcal{O}_k - t_k) \frac{\partial}{\partial W_{ij}} \sigma(x_k)$$

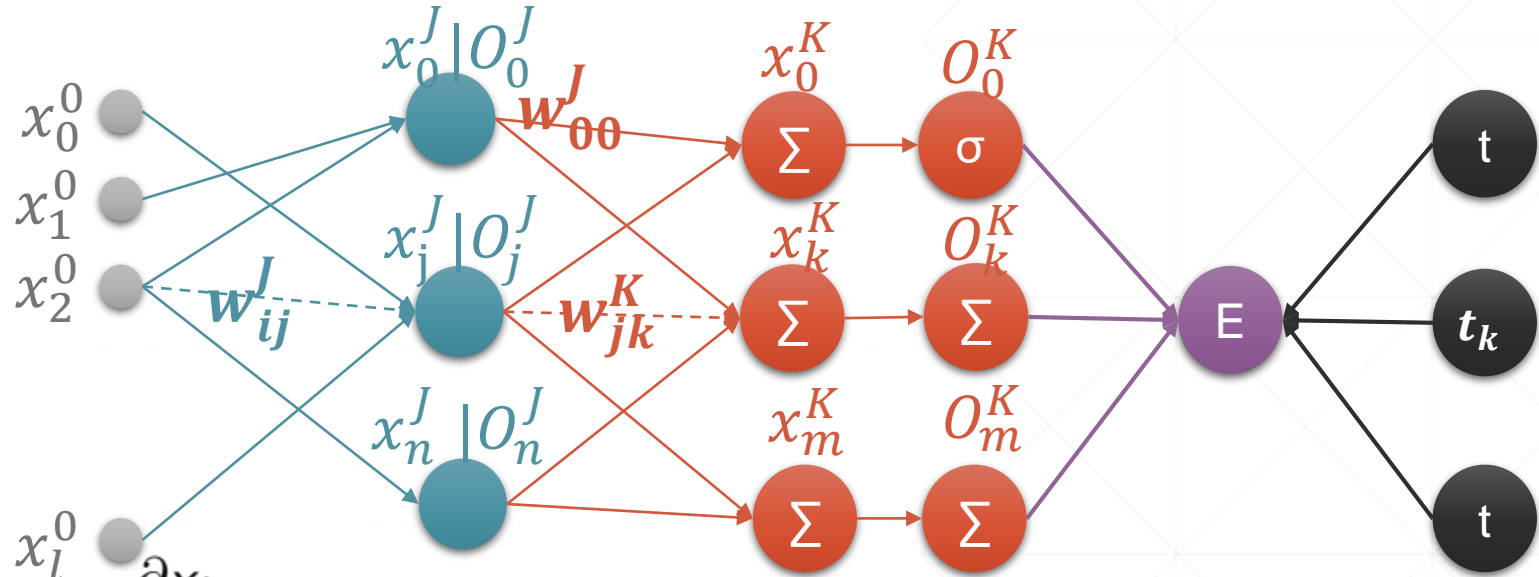
$$\frac{\partial E}{\partial W_{ij}} = \sum_{k \in K} (\mathcal{O}_k - t_k) \sigma(x_k) (1 - \sigma(x_k)) \frac{\partial x_k}{\partial W_{ij}}$$

$$\frac{\partial E}{\partial W_{ij}} = \sum_{k \in K} (\mathcal{O}_k - t_k) \mathcal{O}_k (1 - \mathcal{O}_k) \frac{\partial x_k}{\partial \mathcal{O}_j} \cdot \frac{\partial \mathcal{O}_j}{\partial W_{ij}}$$

$$\frac{\partial E}{\partial W_{ij}} = \sum_{k \in K} (\mathcal{O}_k - t_k) \mathcal{O}_k (1 - \mathcal{O}_k) W_{jk} \frac{\partial \mathcal{O}_j}{\partial W_{ij}}$$

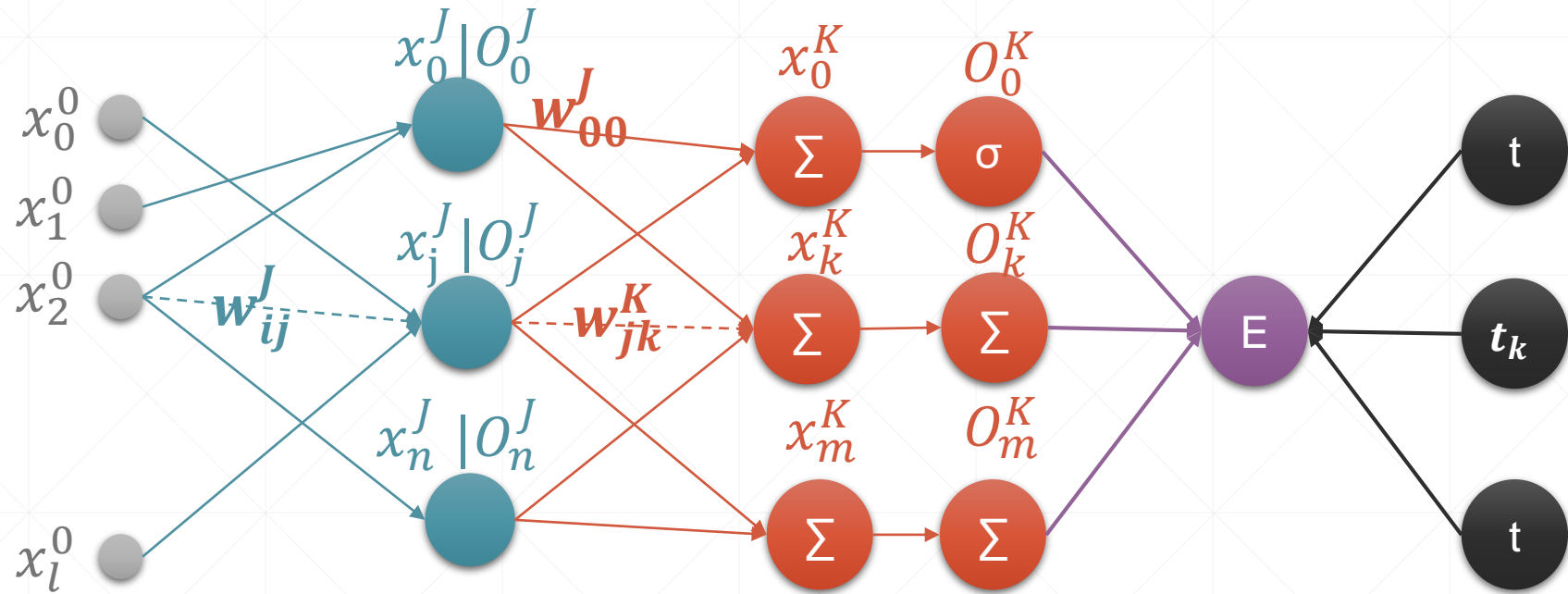
$$\frac{\partial E}{\partial W_{ij}} = \frac{\partial \mathcal{O}_j}{\partial W_{ij}} \sum_{k \in K} (\mathcal{O}_k - t_k) \mathcal{O}_k (1 - \mathcal{O}_k) W_{jk}$$

$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_j (1 - \mathcal{O}_j) \frac{\partial x_j}{\partial W_{ij}} \sum_{k \in K} (\mathcal{O}_k - t_k) \mathcal{O}_k (1 - \mathcal{O}_k) W_{jk}$$



$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_j (1 - \mathcal{O}_j) \mathcal{O}_i \sum_{k \in K} (\mathcal{O}_k - t_k) \mathcal{O}_k (1 - \mathcal{O}_k) W_{jk}$$





$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_j(1 - \mathcal{O}_j)\mathcal{O}_i \sum_{k \in K} (\mathcal{O}_k - t_k)\mathcal{O}_k(1 - \mathcal{O}_k)W_{jk}$$

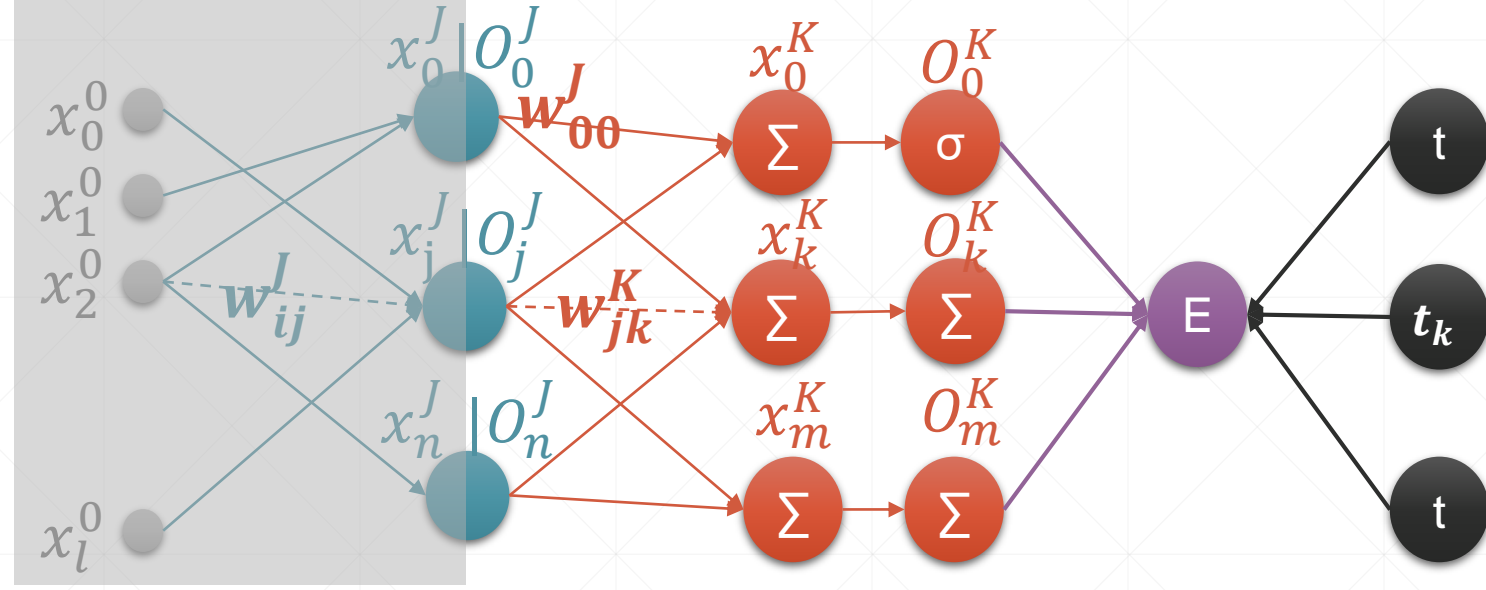
$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_i\mathcal{O}_j(1 - \mathcal{O}_j) \sum_{k \in K} \delta_k W_{jk}$$

$$\frac{\partial E}{\partial w_{jk}} = (O_k - t_k) O_k (1 - O_k) O_j^J$$

$$\frac{\partial E}{\partial w_{jk}} = \delta_k^K O_j^J$$

$$\frac{\partial E}{\partial W_{ij}} = O_j(1 - O_j) O_i \sum_{k \in K} (O_k - t_k) O_k (1 - O_k) W_{jk}$$

$$\frac{\partial E}{\partial W_{ij}} = O_i O_j (1 - O_j) \sum_{k \in K} \delta_k W_{jk}$$



For an output layer node  $k \in K$

$$\frac{\partial E}{\partial W_{jk}} = \mathcal{O}_j \delta_k$$

where

$$\delta_k = \mathcal{O}_k(1 - \mathcal{O}_k)(\mathcal{O}_k - t_k)$$

For a hidden layer node  $j \in J$

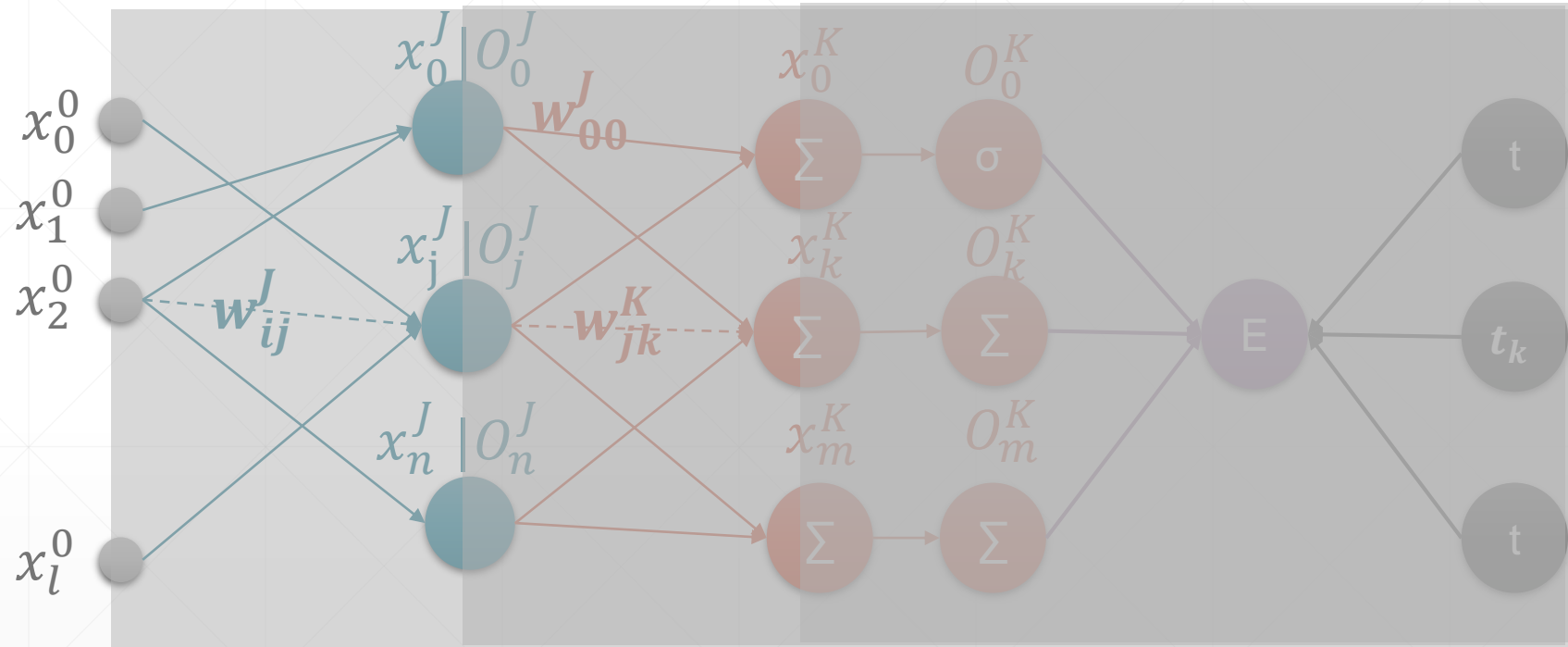
$$\frac{\partial E}{\partial W_{ij}} = \mathcal{O}_i \delta_j$$

where

$$\delta_j = \mathcal{O}_j(1 - \mathcal{O}_j) \sum_{k \in K} \delta_k W_{jk}$$

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- $\delta_k^K$
- $\frac{\partial E}{\partial w_{jk}}$
- $\delta_j^J$
- $\frac{\partial E}{\partial w_{ij}}$
- $\delta_i^I$
- $\frac{\partial E}{\partial w_{ni}}$



**GAME  
OVER**

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# 下一课时

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2D函数优化

**Thank You.**

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