SRM Institute of Science and Technology Department of Mathematics

21MAB206T- Numerical Methods and Analysis

Unit IV: - Numerical Solution of Ordinary Differential Equations Tutorial Sheet – III

- 1. Apply the fourth order Runge Kutta method to find y(0.2) given that y' = x + y, y(0)=1. Ans: y(0.1) = 1.11034, y(0.2) = 1.2428
- 2. Apply the fourth order Runge Kutta method to find y(0.3) given that $y' = y + xy^2$, y(0)=1, by taking h=0.1 correct to four decimal places.

Ans:
$$y(0.1) = 0.9006$$
, $y(0.2) = 0.8046$, $y(0.3) = 0.7144$

- 3. Write Milne's Predictor and Corrector Formula
- 4. Write Adam Bashforth Predictor and Corrector Formula.
- 5. Determine the value of y(0.4) using Milne's method given that $y' = xy + y^2$, y(0) = 1. Use Taylor series to get the values of y(0.1), y(0.2) and y(0.3). **Ans.** Y(0.4) = 1.83698
- 6. Using Adam's method find y(0.4) given that $\frac{dy}{dx} = \frac{xy}{2}$, y(0)=1, y(0.1)=1.01, y(0.2)=1.022, y(0.3)=1.023. **Ans: 1.0410**
- 7. Given y' = 1 y, and y(0) = 0 find
 - (i) y (0.1) by Euler's method.
 - (ii) y (0.2) by Modified Euler's method.
 - (iii) y (0.3) by Improved Euler's method.
 - (iv) y (0.4) by Milne's method.

Ans: 0.1, 0.1855, 0.2629, $y_{4,p} = 0.3280$, $y_{4,c} = 0.3333$.