missing_data_in_supervised_ML

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##

Missing data in supervised ML

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Brown University

https://github.com/brown-ccv/ODSC-Europe-2020

0.1 About me

- Born and raised in Hungary
- Astrophysics PhD at MPIA, Heidelberg, Germany
- Postdoctoral researcher at MIT (still in astrophysics at the time)
- Started at Brown in December 2015 as a Data Scientist
- Promoted to Lead Data Scientist in 2017
- Adjunct Lecturer in Data Science last fall and this fall
 - Teaching the course DATA1030: Hands-on data science, a mandatory course in the Data Science master's program at Brown

0.2 Data Science at Brown

- Center for Computation and Visualization (CCV) https://ccv.brown.edu/
- Institutional Data group
 - Data-driven decision support and predictive modeling for Brown's administrative units
 - Academic research on data-intensive projects
 - Data science consulting for industry partners

0.3 Learning Objectives

By the end of this workshop, you will be able to - Describe the three main types of missingness patterns - Evaluate simple approaches for handling missing values - Apply XGBoost to a dataset with missing values - Apply multivariate imputation - Apply the reduced-features model (also called the pattern submodel approach) - Decide which approach is best for your dataset

0.4 Before we start, a few words on our dataset: kaggle house price

- good for educational purposes
 - messy data that requires quite a bit of preprocessing
 - a nice mixture of continuous, ordinal, and categorical features, each feature type has missing values
- lots of excellent kernels on kaggle
 - check them out here
- dataset and description available in repo
 - let's take a look!

https://github.com/brown-ccv/ODSC-Europe-2020

0.5 Missing values often occur in datasets

- survey data: not everyone answers all the questions
- medical data: not all tests/treatments/etc are performed on all patients
- sensor can be offline or malfunctioning

0.6 Missing values are an issue for multiple reasons

Concenptual reason

- missing values can introduce biases
 - bias: the samples (the data points) are not representative of the underlying distribution/population
 - any conclusion drawn from a biased dataset is also biased.
 - rich people tend to not fill out survey questions about their salaries and the mean salary estimated from survey data tend to be lower than true value

Practical reason

- missing values (NaN, NA, inf) are incompatible with sklearn
 - all values in an array need to be numerical otherwise sklearn will throw a ValueError
- there are a few supervised ML techniques that work with missing values (e.g., XGBoost, CatBoost)
 - we will cover those later today

0.7 Learning Objectives

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1 Missing data patterns

- MCAR Missing Complete At Random
 - some people skip some survey questions by accident
- MAR Missing At Random

- males are less likely to fill out a survey on depression
- this has nothing to do with their level of depression after accounting for maleness
- MNAR Missing Not At Random
 - depressed people are less likely to fill out a survey on depression due to their level of depression

1.1 MCAR test

- MCAR can be diagnosed with a statistical test (Little, 1988)
 - python implementation available in the pymice package or in the skipped slide
- Caveat: it can differentiate between MCAR and MAR only, it misses MNAR

```
[1]: # from the pymice package
     # https://qithub.com/RianneSchouten/pymice
     import numpy as np
     import pandas as pd
     import math as ma
     import scipy.stats as st
     def checks_input_mcar_tests(data):
         """ Checks whether the input parameter of class McarTests is correct
                 Parameters
                 data:
                     The input of McarTests specified as 'data'
                 Returns
                 bool
                     True if input is correct
         if not isinstance(data, pd.DataFrame):
             print("Error: Data should be a Pandas DataFrame")
             return False
         if not any(data.dtypes.values == np.float):
             if not any(data.dtypes.values == np.int):
                 print("Error: Dataset cannot contain other value types than floats⊔
      →and/or integers")
                 return False
         if not data.isnull().values.any():
             print("Error: No NaN's in given data")
             return False
         return True
```

```
def mcar_test(data):
    """ Implementation of Little's MCAR test
    Parameters
    _____
    data: Pandas DataFrame
        An incomplete dataset with samples as index and variables as columns
    Returns
    ____
    p value: Float
        This value is the outcome of a chi-square statistical test, testing \Box
 ⇒whether the null hypothesis
        'the missingness mechanism of the incomplete dataset is MCAR' can be _{\! \sqcup}
 \hookrightarrow rejected.
    11 11 11
    if not checks_input_mcar_tests(data):
        raise Exception("Input not correct")
    dataset = data.copy()
    vars = dataset.dtypes.index.values
    n_var = dataset.shape[1]
    # mean and covariance estimates
    # ideally, this is done with a maximum likelihood estimator
    gmean = dataset.mean()
    gcov = dataset.cov()
    # set up missing data patterns
    r = 1 * dataset.isnull()
    mdp = np.dot(r, list(map(lambda x: ma.pow(2, x), range(n_var))))
    sorted_mdp = sorted(np.unique(mdp))
    n_pat = len(sorted_mdp)
    correct_mdp = list(map(lambda x: sorted_mdp.index(x), mdp))
    dataset['mdp'] = pd.Series(correct_mdp, index=dataset.index)
    # calculate statistic and df
    pj = 0
    d2 = 0
    for i in range(n_pat):
        dataset_temp = dataset.loc[dataset['mdp'] == i, vars]
        select_vars = ~dataset_temp.isnull().any()
        pj += np.sum(select_vars)
        select_vars = vars[select_vars]
        means = dataset_temp[select_vars].mean() - gmean[select_vars]
        select_cov = gcov.loc[select_vars, select_vars]
        mj = len(dataset_temp)
```

1.2 MCAR, MAR, MNAR are nice in theory, pretty useless in practice

- it can be challenging to infer the missingness pattern from an incomplete dataset
 - There is a statistical test to differentiate MCAR and MAR
 - MNAR is difficult/impossible to diagnose to the best of my knowledge
- multiple patterns can be present in the data
 - even worse, multiple patterns can be present in one feature!
 - missing values in a feature can occur due to a mix of MCAR, MAR, MNAR

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1.4 Simple approaches for handling missing values

- 1) categorical/ordinal features: treat missing values as another category
 - missing values in categorical/ordinal features are not a big deal
- 2) continuous features: this is the tough part
 - sklearn's SimpleImputer
- 3) exclude points or features with missing values
 - might be OK

1.4.1 1a) Missing values in a categorical feature

- YAY this is not an issue at all!
- Categorical feature needs to be one-hot encoded anyway
- Just replace the missing values with 'NA' or 'missing' and treat it as a separate category

1.4.2 1b) Missing values in a ordinal feature

- this can be a bit trickier but usually fine
- Ordinal encoder is applied to ordinal features

```
- where does 'NA' or 'missing' fit into the order of the categories?
```

- usually first or last

[2]: # read the data

import pandas as pd

• if you can figure this out, you are done

```
import numpy as np
     from sklearn.model_selection import train_test_split
     # Let's load the data
     df = pd.read_csv('data/train.csv')
     # drop the ID
     df.drop(columns=['Id'],inplace=True)
     # the target variable
     y = df['SalePrice']
     df.drop(columns=['SalePrice'],inplace=True)
     # the unprocessed feature matrix
     X = df.values
     print(X.shape)
     # the feature names
     ftrs = df.columns
    (1460, 79)
[3]: # let's split to train, test, and holdout
     X_other, X_holdout, y_other, y_holdout = train_test_split(df, y, test_size=0.2,__
     →random state=0)
     X_train, X_test, y_train, y_test = train_test_split(X_other, y_other, u_
     →test_size=0.25, random_state=0)
     print(X_train.shape)
     print(X_test.shape)
     print(X_holdout.shape)
    (876, 79)
    (292, 79)
    (292, 79)
[4]: # collect the various features
     cat_ftrs =_
      →['MSZoning','Street','Alley','LandContour','LotConfig','Neighborhood','Condition1','Conditi
      → 'BldgType', 'HouseStyle', 'RoofStyle', 'RoofMatl', 'Exterior1st', 'Exterior2nd', 'MasVnrType', 'Fo
      → 'Heating', 'CentralAir', 'Electrical', 'GarageType', 'PavedDrive', 'MiscFeature', 'SaleType', 'Sal
```

```
ordinal_ftrs =
→['LotShape','Utilities','LandSlope','ExterQual','ExterCond','BsmtQual','BsmtCond','BsmtExpo
 → 'BsmtFinType1', 'BsmtFinType2', 'HeatingQC', 'KitchenQual', 'Functional', 'FireplaceQu', 'GarageF
                'GarageQual', 'GarageCond', 'PoolQC', 'Fence']
ordinal_cats =
→[['Reg','IR1','IR2','IR3'],['AllPub','NoSewr','NoSeWa','ELO'],['Gtl','Mod','Sev'],\
→['Po','Fa','TA','Gd','Ex'],['Po','Fa','TA','Gd','Ex'],['NA','Po','Fa','TA','Gd','Ex'],\
→['NA','Po','Fa','TA','Gd','Ex'],['NA','No','Mn','Av','Gd'],['NA','Unf','LwQ','Rec','BLQ','A

→ ['NA', 'Unf', 'LwQ', 'Rec', 'BLQ', 'ALQ', 'GLQ'], ['Po', 'Fa', 'TA', 'Gd', 'Ex'], ['Po', 'Fa', 'TA', 'Gd', 'Ex']
 →['Sal','Sev','Maj2','Maj1','Mod','Min2','Min1','Typ'],['NA','Po','Fa','TA','Gd|,'Ex'],\
→['NA','Unf','RFn','Fin'],['NA','Po','Fa','TA','Gd','Ex'],['NA','Po','Fa','TA',|Gd','Ex'],
                ['NA', 'Fa', 'TA', 'Gd', 'Ex'], ['NA', 'MnWw', 'GdWo', 'MnPrv', 'GdPrv']]
num ftrs =
 →['MSSubClass','LotFrontage','LotArea','OverallQual','OverallCond','YearBuilt', YearRemodAdd
→ 'MasVnrArea', 'BsmtFinSF1', 'BsmtFinSF2', 'BsmtUnfSF', 'TotalBsmtSF', '1stFlrSF', '2ndFlrSF', \
 → 'LowQualFinSF', 'GrLivArea', 'BsmtFullBath', 'BsmtHalfBath', 'FullBath', 'HalfBath', 'BedroomAbvG
 → 'KitchenAbvGr', 'TotRmsAbvGrd', 'Fireplaces', 'GarageYrBlt', 'GarageCars', 'GarageArea', 'WoodDec
 → 'OpenPorchSF', 'EnclosedPorch', '3SsnPorch', 'ScreenPorch', 'PoolArea', 'MiscVal', 'MoSold', 'YrSo
```

[5]: df[ordinal_ftrs]

[5]:		LotShape	Utilities	LandSlope	ExterQual	${\tt ExterCond}$	${\tt BsmtQual}$	${\tt BsmtCond}$	\
	0	Reg	AllPub	Gtl	Gd	TA	Gd	TA	
	1	Reg	AllPub	Gtl	TA	TA	Gd	TA	
	2	IR1	AllPub	Gtl	Gd	TA	Gd	TA	
	3	IR1	AllPub	Gtl	TA	TA	TA	Gd	
	4	IR1	AllPub	Gtl	Gd	TA	Gd	TA	
		•••	•••		•••	•••	•••		
	1455	Reg	AllPub	Gtl	TA	TA	Gd	TA	
	1456	Reg	AllPub	Gtl	TA	TA	Gd	TA	
	1457	Reg	AllPub	Gtl	Ex	Gd	TA	Gd	
	1458	Reg	AllPub	Gtl	TA	TA	TA	TA	
	1459	Reg	AllPub	Gtl	Gd	TA	TA	TA	

1	Gd	ALQ	Unf	Ex	TA	Тур
2	Mn	GLQ	Unf	Ex	Gd	Тур
3	No	ALQ	Unf	Gd	Gd	Тур
4	Av	GLQ	Unf	Ex	Gd	Тур
•••	•••	•••		•••	•••	
1455	No	Unf	Unf	Ex	TA	Тур
1456	No	ALQ	Rec	TA	TA	Min1
1457	No	GLQ	Unf	Ex	Gd	Тур
1458	Mn	GLQ	Rec	Gd	Gd	Тур
1459	No	BLQ	LwQ	Gd	TA	Тур

	${\tt FireplaceQu}$	${\tt GarageFinish}$	${\tt GarageQual}$	${\tt GarageCond}$	${\tt PoolQC}$	Fence
0	NaN	RFn	TA	TA	NaN	NaN
1	TA	RFn	TA	TA	NaN	NaN
2	TA	RFn	TA	TA	NaN	NaN
3	Gd	Unf	TA	TA	NaN	NaN
4	TA	RFn	TA	TA	NaN	NaN
•••	•••	•••				
1455	TA	RFn	TA	TA	NaN	NaN
1456	TA	Unf	TA	TA	NaN	${\tt MnPrv}$
1457	Gd	RFn	TA	TA	NaN	${\tt GdPrv}$
1458	NaN	Unf	TA	TA	NaN	NaN
1459	NaN	Fin	TA	TA	NaN	NaN

[1460 rows x 19 columns]

```
[6]: # preprocess with pipeline and columntransformer
     from sklearn.compose import ColumnTransformer
     from sklearn.pipeline import Pipeline
     from sklearn.preprocessing import OneHotEncoder
     from sklearn.preprocessing import OrdinalEncoder
     from sklearn.preprocessing import StandardScaler
     from sklearn.impute import SimpleImputer
     # one-hot encoder
     categorical_transformer = Pipeline(steps=[
         ('imputer', SimpleImputer(strategy='constant',fill_value='missing')),
         ('onehot', OneHotEncoder(sparse=False,handle_unknown='ignore'))])
     # ordinal encoder
     ordinal_transformer = Pipeline(steps=[
         ('imputer2', SimpleImputer(strategy='constant',fill_value='NA')),
         ('ordinal', OrdinalEncoder(categories = ordinal_cats))])
     # standard scaler
     numeric_transformer = Pipeline(steps=[
         ('scaler', StandardScaler())])
```

```
# collect the transformers
     preprocessor = ColumnTransformer(
         transformers=[
             ('num', numeric_transformer, num_ftrs),
             ('cat', categorical_transformer, cat_ftrs),
             ('ord', ordinal_transformer, ordinal_ftrs)])
[7]: # fit_transform the training set
     X_prep = preprocessor.fit_transform(X_train)
     # little hacky, but collect feature names
     feature_names = preprocessor.transformers_[0][-1] + \
                     list(preprocessor.named_transformers_['cat'][1].
      →get_feature_names(cat_ftrs)) + \
                     preprocessor.transformers_[2][-1]
     df_train = pd.DataFrame(data=X_prep,columns=feature_names)
     print(df_train.shape)
     # transform the test
     df_test = preprocessor.transform(X_test)
     df_test = pd.DataFrame(data=df_test,columns = feature_names)
     print(df_test.shape)
     # transform the holdout
     df_holdout = preprocessor.transform(X_holdout)
     df_holdout = pd.DataFrame(data=df_holdout,columns = feature_names)
     print(df_holdout.shape)
    (876, 221)
    (292, 221)
    (292, 221)
[8]: df_train[ordinal_ftrs]
          LotShape Utilities LandSlope ExterQual ExterCond BsmtQual
[8]:
                                                                           BsmtCond \
               0.0
                                      0.0
                                                 2.0
                                                            2.0
                                                                       4.0
                          0.0
                                                                                 3.0
     0
     1
               0.0
                          0.0
                                      0.0
                                                 3.0
                                                            2.0
                                                                       4.0
                                                                                 3.0
     2
               1.0
                          0.0
                                      0.0
                                                 2.0
                                                            2.0
                                                                      4.0
                                                                                 3.0
     3
               0.0
                          0.0
                                      0.0
                                                 2.0
                                                            2.0
                                                                       3.0
                                                                                 3.0
                                      0.0
     4
               0.0
                          0.0
                                                 3.0
                                                            2.0
                                                                       4.0
                                                                                 3.0
     871
               0.0
                          0.0
                                      0.0
                                                 2.0
                                                            2.0
                                                                       3.0
                                                                                 3.0
               0.0
                                      0.0
                                                 3.0
                                                            2.0
                                                                      4.0
                                                                                 3.0
     872
                          0.0
     873
               0.0
                          0.0
                                      0.0
                                                 2.0
                                                            3.0
                                                                      3.0
                                                                                 3.0
               0.0
                                      0.0
                                                 3.0
                                                                      4.0
     874
                          0.0
                                                            2.0
                                                                                 3.0
     875
               1.0
                          0.0
                                      0.0
                                                 3.0
                                                            2.0
                                                                       4.0
                                                                                 3.0
```

	BsmtExposur	e BsmtFinType1	${ t BsmtFinTyp}$	e2 Heating ${\tt Q}$	C KitchenQu	al \
0	1.	0 1.0	1	.0 4.	0 2	2.0
1	3.	0 6.0	1	.0 4.	0 3	3.0
2	3.	0 5.0	2	.0 3.	0 3	3.0
3	1.	0 4.0	1	.0 2.	0 2	2.0
4	1.	0 6.0	1	.0 4.	0 3	3.0
		•••	•••			
871	1.	0 3.0	1	.0 2.	0 2	2.0
872	1.	0 1.0	1	.0 4.	0 3	.0
873	1.	0 1.0	1	.0 2.	0 2	2.0
874	2.	0 1.0	1	.0 3.	0 4	0
875	1.	0 1.0	1	.0 4.	0 3	.0
	Functional	FireplaceQu G	arageFinish	GarageQual	GarageCond	PoolQC \
0	7.0	0.0	2.0	3.0	3.0	0.0
1	7.0	4.0	2.0	3.0	3.0	0.0
2	7.0	0.0	2.0	3.0	4.0	0.0
3	7.0	2.0	2.0	3.0	3.0	0.0
4	7.0	0.0	2.0	3.0	3.0	0.0
	•••	•••	•••	•••		
871	7.0	0.0	1.0	3.0	3.0	0.0
872	7.0	0.0	2.0	3.0	3.0	0.0
873	5.0	0.0	2.0	3.0	3.0	0.0
874	7.0	4.0	2.0	3.0	3.0	0.0
875	7.0	4.0	2.0	3.0	3.0	0.0
	Fence					
0	0.0					
1	0.0					
2	3.0					
3	0.0					
4	0.0					
	•••					
871	3.0					

[876 rows x 19 columns]

0.0

0.0

0.0

0.0

872

873

874

875

1.4.3 2) Continuous features: mean or median imputation

- Imputation means you infer the missing values from the known part of the data
- sklearn's SimpleImputer can do mean and median imputation
- USUALLY A BAD IDEA!

- MCAR: mean/median of non-missing values is the same as the mean/median of the true underlying distribution, but the variances are different
- not MCAR: the mean/median and the variance of the completed dataset will be off
- supervised ML model is too confident (MCAR) or systematically off (not MCAR)

1.4.4 3) Exclude points or features with missing values

- easy to do with pandas
- it is an ACCEPTABLE approach under two conditions:
 - Little's test supports MCAR (p > 0.05)
 - only small fraction of points contain missing values (maybe a few percent?) OR the missing values are limited to one or a few features that can be dropped
- if the MCAR assumption is justified, dropping points will not introduce biases to your model
- due to the smaller sample size, the confidence of your model might suffer.
- what will you do with missing values when you deploy the model?

```
[9]: print('data dimensions:',df_train.shape)
      print('the p value of the mcar test:',mcar test(df train))
      perc_missing_per_ftr = df_train.isnull().sum(axis=0)/df_train.shape[0]
      print('fraction of missing values in features:')
      print(perc_missing_per_ftr[perc_missing_per_ftr > 0])
      frac missing = sum(df_train.isnull().sum(axis=1)!=0)/df_train.shape[0]
      print('fraction of points with missing values:',frac_missing)
     data dimensions: (876, 221)
     the p value of the mcar test: 1.0
     fraction of missing values in features:
     LotFrontage
                    0.173516
     MasVnrArea
                    0.004566
     GarageYrBlt
                    0.050228
     dtype: float64
     fraction of points with missing values: 0.2237442922374429
[10]: print(df train.shape)
      # by default, rows/points are dropped
      df r = df train.dropna()
      print(df_r.shape)
      # drop features with missing values
      df_c = df_train.dropna(axis=1)
      print(df_c.shape)
```

1.5 Learning Objectives

(876, 221) (680, 221) (876, 218)

By the end of this workshop, you will be able to - Describe the three main types of missingness patterns - Evaluate simple approaches for handling missing values - **Apply XGBoost to a dataset**

with missing values - Apply multivariate imputation - Apply the reduced-features model (also called the pattern submodel approach) - Decide which approach is best for your dataset

1.6 XGBoost and missing values

- sklearn raises an error if the feature matrix (X) contains nans.
- XGBoost doesn't!
- If a feature with missing values is split:
 - XGBoost tries to put the points with missing values to the left and right
 - calculates the impurity measure for both options
 - puts the points with missing values to the side with the lower impurity
- if missingness correlates with the target variable, XGBoost extracts this info!

```
[11]: import xgboost
      from sklearn.model_selection import ParameterGrid
      from sklearn.metrics import mean_squared_error
      param_grid = {"learning_rate": [0.03],
                    "n_estimators": [2000],
                    "seed": [0],
                    #"n_jobs": [-1],
                    #"reg_alpha": [0e0,0.1,0.31622777,1.,3.16227766,10.],
                    #"reg_lambda": [0e0,0.1,0.31622777,1.,3.16227766,10.],
                    "missing": [np.nan],
                    #"max_depth": [1,2,3,4,5],
                    "colsample bytree": [0.9],
                    "subsample": [0.66]}
      XGB = xgboost.XGBRegressor()
      XGB.set_params(**ParameterGrid(param_grid)[0])
      XGB.fit(df_train,y_train,early_stopping_rounds=50,eval_set=[(df_test, y_test)],_
       →verbose=False)
      print('the test RMSE:',XGB.evals_result()['validation_0']['rmse'][-1])
      y_holdout_pred = XGB.predict(df_holdout)
      print('the holdout RMSE:',np.sqrt(mean_squared_error(y_holdout,y_holdout_pred)))
```

the test RMSE: 23486.925781 the holdout RMSE: 31748.96283078089

1.7 Learning Objectives

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1.8 Multivariate Imputation

• models each feature with missing values as a function of other features

- at each step, a feature with nans is designated as target variable y and the other features are treated as feature matrix X
- a regressor is trained on (X, y) for known y
- then, the regressor is used to predict the missing values of y
- in the ML pipeline:
 - create n imputed datasets
 - run all of them through the ML pipeline
 - generate n holdout scores
 - the uncertainty in the holdout scores is due to the uncertainty in imputation
- works on MCAR and MAR, fails on MNAR
- paper here

2 sklearn's IterativeImputer

```
LotFrontage MasVnrArea GarageYrBlt
     0.424926
0
                -0.573303
                               0.979398
1
           {\tt NaN}
                 0.492835
                               1.018748
2
                -0.573303
           NaN
                               0.192399
3
    -0.049970
                0.810076
                              -0.476551
     -1.474659
               -0.022031
                               0.979398
  LotFrontage MasVnrArea GarageYrBlt
0
     0.424926
               -0.573303
                               0.979398
    -1.289018
                 0.492835
1
                               1.018748
2
    -0.287418
               -0.573303
                               0.192399
3
     -0.049970
                 0.810076
                              -0.476551
    -1.474659
                -0.022031
                               0.979398
```

/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.7/site-packages/sklearn/impute/_iterative.py:670: ConvergenceWarning:

[IterativeImputer] Early stopping criterion not reached.
" reached.", ConvergenceWarning)

the test RMSE: 23189.175781

the holdout RMSE: 32290.240629124994

2.1 Learning Objectives

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2.2 Reduced-features model (or pattern submodel approach)

- first described in 2007 in a JMLR article as the reduced features model
- in 2018, "rediscovered" as the pattern submodel approach in Biostatistics

My holdout set:

index	feature 1	feature 2	feature 3	target var
0	NA	45	NA	0
1	NA	NA	8	1
2	12	6	34	0
3	1	89	NA	0
4	0	NA	47	1
5	687	24	67	1
6	NA	23	NA	1

To predict points 0 and 6, I will use train and test points that are complete in feature 2.

To predict point 1, I will use train and test points that are complete in feature 3.

To predict point 2 and 5, I will use train and test points that are complete in features 1-3.

Etc. We will train as many models as the number of patterns in holdout.

2.3 How to determine the patterns?

```
[14]: mask = df_holdout[['LotFrontage','MasVnrArea','GarageYrBlt']].isnull()
unique_rows, counts = np.unique(mask, axis=0,return_counts=True)
print(unique_rows.shape) # 6 patterns, we will train 6 models
for i in range(len(counts)):
```

```
(6, 3)
     [False False False] 223
     [False False True] 21
     [False True False] 1
     [ True False False] 44
     [ True False True] 2
     [ True True False] 1
[15]: def xgb_model(X_train, Y_train, X_test, Y_test, X_holdout, Y_holdout,_
      →verbose=1):
          # make into row vectors to avoid an obnoxious sklearn/xqb warning
          Y_train = np.reshape(np.array(Y_train), (1, -1)).ravel()
          Y_test = np.reshape(np.array(Y_test), (1, -1)).ravel()
          Y_holdout = np.reshape(np.array(Y_holdout), (1, -1)).ravel()
          XGB = xgboost.XGBRegressor(n_jobs=1)
          # find the best parameter set
          param_grid = {"learning_rate": [0.03],
                        "n_estimators": [2000],
                        "seed": [0],
                        #"n_jobs": [6],
                        #"reg_alpha": [0e0,0.1,0.31622777,1.,3.16227766,10.],
                        #"reg_lambda": [0e0,0.1,0.31622777,1.,3.16227766,10.],
                        "missing": [np.nan],
                        #"max_depth": [1,2,3,4,5],
                        "colsample_bytree": [0.9],
                        "subsample": [0.66]}
          pg = ParameterGrid(param_grid)
          scores = np.zeros(len(pg))
          for i in range(len(pg)):
              if verbose >= 5:
                  print("Param set " + str(i + 1) + " / " + str(len(pg)))
              params = pg[i]
              XGB.set_params(**params)
              eval_set = [(X_test, Y_test)]
              XGB.fit(X_train, Y_train,
                      early_stopping_rounds=50, eval_set=eval_set, verbose=False)#_
       \rightarrow with early stopping
              Y_test_pred = XGB.predict(X_test, ntree_limit=XGB.best_ntree_limit)
              scores[i] = mean_squared_error(Y_test,Y_test_pred)
```

print(unique_rows[i],counts[i])

```
best_params = np.array(pg)[scores == np.max(scores)]
    if verbose >= 4:
       print('Test set max score and best parameters are:')
       print(np.max(scores))
       print(best_params)
    # test the model on the holdout set with best parameter set
   XGB.set params(**best params[0])
   XGB.fit(X_train,Y_train,
            early stopping rounds=50, eval set=eval set, verbose=False)
   Y_holdout_pred = XGB.predict(X_holdout, ntree_limit=XGB.best_ntree_limit)
   if verbose >= 1:
       print ('The MSE is:',mean squared_error(Y_holdout,Y_holdout_pred))
   if verbose >= 2:
       print ('The predictions are:')
       print (Y_holdout_pred)
    if verbose >= 3:
       print("Feature importances:")
       print(XGB.feature_importances_)
   return (mean_squared_error(Y_holdout,Y_holdout_pred), Y_holdout_pred, XGB.
→feature importances )
# Function: Reduced-feature XGB model
# all the inputs need to be pandas DataFrame
def reduced feature_xgb(X_train, Y_train, X_test, Y_test, X_holdout, Y_holdout):
    # find all unique patterns of missing value in holdout set
   mask = X_holdout.isnull()
   unique rows = np.array(np.unique(mask, axis=0))
   all_Y_holdout_pred = pd.DataFrame()
   print('there are', len(unique_rows), 'unique missing value patterns.')
   # divide holdout sets into subgroups according to the unique patterns
   for i in range(len(unique_rows)):
       print ('working on unique pattern', i)
        ## generate X_holdout subset that matches the unique pattern i
       sub_X_holdout = pd.DataFrame()
        sub_Y_holdout = pd.Series()
       for j in range(len(mask)): # check each row in mask
            row_mask = np.array(mask.iloc[j])
            if np.array_equal(row_mask, unique_rows[i]): # if the pattern_
 → matches the ith unique pattern
```

```
sub_X_holdout = sub_X_holdout.append(X_holdout.iloc[j])# append__
\rightarrow the according X_holdout row j to the subset
               sub_Y_holdout = sub_Y_holdout.append(Y_holdout.iloc[[j]])#_
\rightarrow append the according Y holdout row j
       sub_X_holdout = sub_X_holdout[X_holdout.columns[~unique_rows[i]]]
       ## choose the according reduced features for subgroups
       sub_X_train = pd.DataFrame()
       sub_Y_train = pd.DataFrame()
       sub_X_test = pd.DataFrame()
       sub_Y_test = pd.DataFrame()
       # 1.cut the feature columns that have nans in the according
\hookrightarrow sub X holdout
       sub_X_train = X_train[X_train.columns[~unique_rows[i]]]
       sub_X_test = X_test[X_test.columns[~unique_rows[i]]]
       # 2.cut the rows in the sub_X_train and sub_X_test that have any nans
       sub_X_train = sub_X_train.dropna()
       sub_X_test = sub_X_test.dropna()
       # 3.cut the sub_Y_train and sub_Y_test accordingly
       sub_Y_train = Y_train.iloc[sub_X_train.index]
       sub_Y_test = Y_test.iloc[sub_X_test.index]
       # run XGB
       sub_Y_holdout_pred = xgb_model(sub_X_train, sub_Y_train, sub_X_test,
                                       sub_Y_test, sub_X_holdout,_
→sub_Y_holdout, verbose=0)
       sub_Y_holdout_pred = pd.
→DataFrame(sub_Y_holdout_pred[1],columns=['sub_Y_holdout_pred'],
                                          index=sub_Y_holdout.index)
       print(' RMSE:',np.
→sqrt(mean_squared_error(sub_Y_holdout,sub_Y_holdout_pred)))
       # collect the holdout predictions
       all_Y_holdout_pred = all_Y_holdout_pred.append(sub_Y_holdout_pred)
   # rank the final Y holdout pred according to original Y holdout index
   all_Y_holdout_pred = all_Y_holdout_pred.sort_index()
   Y_holdout = Y_holdout.sort_index()
   # get global RMSE
   total_RMSE = np.sqrt(mean_squared_error(Y_holdout,all_Y_holdout_pred))
   return total_RMSE
```

2.3.1 A python implementation is available on the skipped slide

[16]: print('final RMSE:',reduced_feature_xgb(df_train, y_train, df_test, y_test, u → df_holdout, y_holdout))

there are 6 unique missing value patterns. working on unique pattern 0

/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.7/site-packages/ipykernel_launcher.py:76: DeprecationWarning: The default dtype for empty Series will be 'object' instead of 'float64' in a future version. Specify a dtype explicitly to silence this warning.

RMSE: 35277.53669207676 working on unique pattern 1

/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.7/site-packages/ipykernel_launcher.py:76: DeprecationWarning: The default dtype for empty Series will be 'object' instead of 'float64' in a future version. Specify a dtype explicitly to silence this warning.

RMSE: 11607.857261825593 working on unique pattern 2

/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.7/site-packages/ipykernel_launcher.py:76: DeprecationWarning: The default dtype for empty Series will be 'object' instead of 'float64' in a future version. Specify a dtype explicitly to silence this warning.

RMSE: 1134.5625 working on unique pattern 3

/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.7/site-packages/ipykernel_launcher.py:76: DeprecationWarning: The default dtype for empty Series will be 'object' instead of 'float64' in a future version. Specify a dtype explicitly to silence this warning.

RMSE: 18366.394043603428 working on unique pattern 4

/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.7/site-packages/ipykernel_launcher.py:76: DeprecationWarning: The default dtype for empty Series will be 'object' instead of 'float64' in a future version. Specify a dtype explicitly to silence this warning.

RMSE: 18521.340554971906 working on unique pattern 5

/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.7/site-packages/ipykernel_launcher.py:76: DeprecationWarning: The default dtype for empty Series will be 'object' instead of 'float64' in a future version. Specify a dtype explicitly to silence this warning.

RMSE: 65343.46875

final RMSE: 32061.23877235819

2.4 Learning Objectives

By the end of this workshop, you will be able to - Describe the three main types of missingness patterns - Evaluate simple approaches for handling missing values - Apply XGBoost to a dataset with missing values - Apply multivariate imputation - Apply the reduced-features model (also called the pattern submodel approach) - **Decide which approach is best for your dataset**

2.5 Which approach is best for my data?

- XGB: run n XGB models with n different seeds
- **imputation**: prepare n different imputations and run n XGB models on them
- reduced-features: run n reduced-features model with n different seeds
- rank the three methods based on how significantly different the corresponding mean scores are

Now you can - Describe the three main types of missingness patterns - Evaluate simple approaches for handling missing values - Apply XGBoost to a dataset with missing values - Apply multivariate imputation - Apply the reduced-features model (also called the pattern submodel approach) - Decide which approach is best for your dataset

#

Thanks for your attention!