Unit 3: Foundations for inference

2. Confidence intervals

GOVT 3990 - Spring 2017

Cornell University

Outline

1. Housekeeping

2. Main ideas
    1. Statistical inference methods based on the CLT depend on the same conditions as the CLT
    2. Use confidence intervals to estimate population parameters
    3. Critical value depends on the confidence level
    4. Calculate the sample size a priori to achieve desired margin of error

3. Summary

Announcements

- Tips for project: be mindful of the two big deadlines, read over the assignment and start asking questions, don't save the work till the last night – this is not a project you can complete by pulling an all nighter
- Peer eval feedback:
  - Lateness / absence, mental presence, communication, commitment
  - Tips: Move seats around in class and lab, give your best, and don't assume the worst
  - Instructions: Give scores that reflect your verbal comments
- Discussion section tomorrow: CLT, CIs, HTs

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1. Statistical inference methods based on the CLT depend on the same conditions as the CLT

Always check these in context of the data and the research question!

1. *Independence:* Sampled observations must be independent.
   * This is difficult to verify, but is more likely if
     - random sampling/assignment is used, and,
     - if sampling without replacement, $n <$ 10% of the population.
2. *Sample size/skew:* Either the population distribution is normal or $n > 30$ and the population distribution is not extremely skewed (the more skewed the distribution, the higher n necessary for the CLT to apply).
   * This is also difficult to verify for the population, but we can check it using the sample data, and assume that the sample mirrors the population.

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2. Use confidence intervals to estimate population parameters

$$CI : point\ estimate \pm margin\ of\ error$$

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If the parameter of interest is the population mean, and the point estimate is the sample mean,

$$\bar{x} \pm Z^{\star} \frac{s}{\sqrt{n}}$$

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3. Critical value depends on the confidence level

Your turn

What is the critical value ($Z^\star$) for a confidence interval at the 91% confidence level?

(a) $Z^\star = 1.34$

(b) $Z^\star = 1.65$

(c) $Z^\star = 1.70$

(d) $Z^\star = 1.96$

(e) $Z^\star = 2.33$

3. Critical value depends on the confidence level

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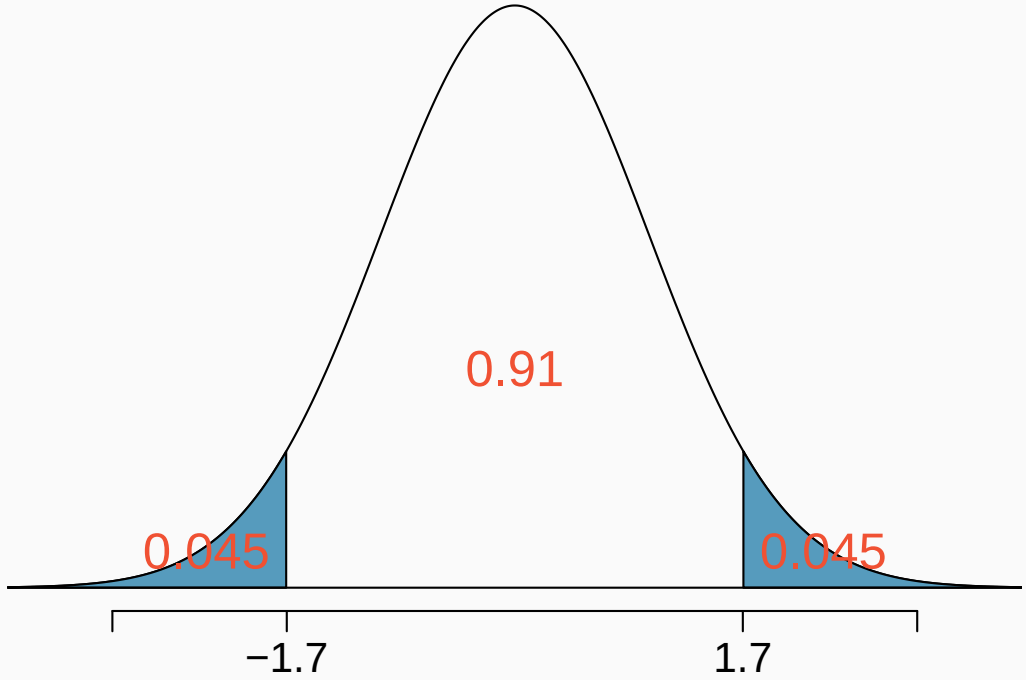

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3. A wider interval means less confidence.
   This is incorrect since it is possible to make very precise statements with very little confidence.

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4. Calculate the sample size a priori to achieve desired margin of error

$$ME = z^\star \frac{s}{\sqrt{n}}$$

So if we know the desired ME, and confidence level (and hence $z^\star$), and the sample standard deviation, we can solve for n.

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$$n = (\frac{z\star\, s}{ME})^2$$

Application exercise: 3.1 Confidence interval for a single mean

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Summary of main ideas

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