

## QUESTION 1 A

In[1]:= **Qlist** = {{**q**, 0, 0}, {-2 **q**, 0, 1}, {**q**, 1, 1}}

Out[1]= {{**q**, 0, 0}, {-2 **q**, 0, 1}, {**q**, 1, 1}}

In[2]:= **Clear**[**x**, **y**]

In[3]:= **V**[**x\_**, **y\_**] :=  
 $\text{Sum}[\text{Qlist}[[i, 1]] / \text{Sqrt}[(\mathbf{x} - \text{Qlist}[[i, 2]])^2 + (\mathbf{y} - \text{Qlist}[[i, 3]])^2], \{i, 1, 3\}]$

In[4]:= **EF4**[**x\_**, **y\_**] := {D[V[**x**, **y**], **x**], D[V[**x**, **y**], **y**]}

In[25]:= **EF4**[**x**, **y**]

$$\text{Out[25]} = \left\{ -\frac{-1+x}{((-1+x)^2 + (-1+y)^2)^{3/2}} + \frac{2x}{(x^2 + (-1+y)^2)^{3/2}} - \frac{x}{(x^2 + y^2)^{3/2}}, \right. \\ \left. -\frac{-1+y}{((-1+x)^2 + (-1+y)^2)^{3/2}} + \frac{2(-1+y)}{(x^2 + (-1+y)^2)^{3/2}} - \frac{y}{(x^2 + y^2)^{3/2}} \right\}$$

In[39]:= **EF4**[**x**, **y**] /. {{**x** → 1}, {**y** → 1}}

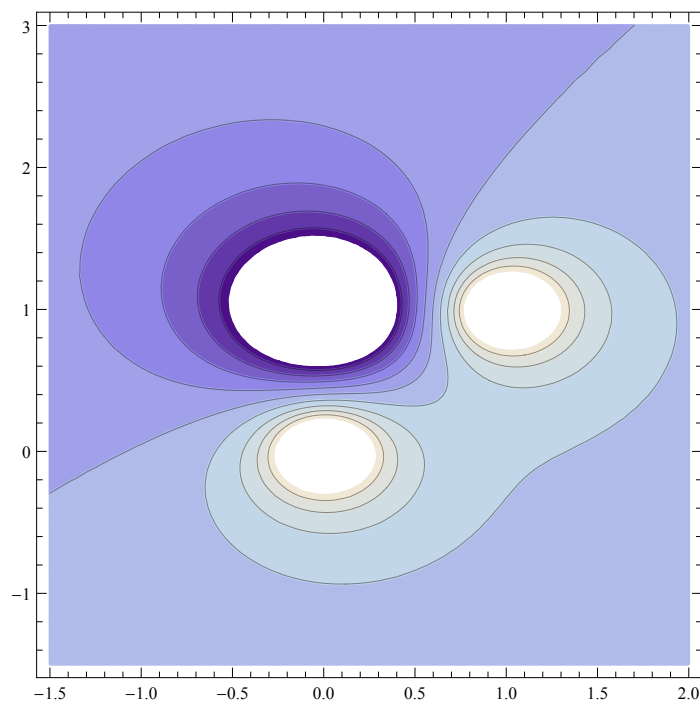
$$\text{Out[39]} = \left\{ \left\{ \frac{2}{(1 + (-1+y)^2)^{3/2}} - \frac{1}{(1+y^2)^{3/2}}, \frac{2(-1+y)}{(1 + (-1+y)^2)^{3/2}} - \frac{-1+y}{((-1+y)^2)^{3/2}} - \frac{y}{(1+y^2)^{3/2}} \right\}, \right. \\ \left. \left\{ -\frac{-1+x}{((-1+x)^2)^{3/2}} + \frac{2x}{(x^2)^{3/2}} - \frac{x}{(1+x^2)^{3/2}}, -\frac{1}{(1+x^2)^{3/2}} \right\} \right\}$$

## QUESTION 1 B

In[10]:= **q** = 1

Out[10]= 1

**ContourPlot**[V[**x**, **y**], {**x**, -1.5, 2}, {**y**, -1.5, 3}]



## QUESTION 1 C

```
NSolve[EF4[x, y] == 0, {x, y}]
```

```
{ {x → 0.251258 + 1.11931 i, y → 0.258734 - 0.419234 i},
  {x → 0.251258 - 1.11931 i, y → 0.258734 + 0.419234 i},
  {x → 0.741266 + 0.419234 i, y → 0.748742 - 1.11931 i},
  {x → 0.741266 - 0.419234 i, y → 0.748742 + 1.11931 i},
  {x → 0.213624 + 0.487227 i, y → 0.786376 - 0.487227 i},
  {x → 0.213624 - 0.487227 i, y → 0.786376 + 0.487227 i},
  {x → 0.810361, y → 0.189639}, {x → 0.640595 + 0.453806 i, y → 1.07411 + 0.0314305 i},
  {x → 0.640595 - 0.453806 i, y → 1.07411 - 0.0314305 i},
  {x → -0.0741101 - 0.0314305 i, y → 0.359405 - 0.453806 i},
  {x → -0.0741101 + 0.0314305 i, y → 0.359405 + 0.453806 i}}
```

QUESTION 1 D

```
Clear[q]
```

```
In[11]:= q1 = -1
```

```
Out[11]= -1
```

```
In[23]:= PE = q1 * V[1, 0]
```

```
Out[23]= -2 +  $\sqrt{2}$ 
```

```
In[40]:= F = q1 * EF4[x, y] /. {{x → 1}, {y → 0}}
```

```
Out[40]=  $\left\{ \left\{ -\frac{2}{(1 + (-1 + y)^2)^{3/2}} + \frac{1}{(1 + y^2)^{3/2}}, -\frac{2(-1 + y)}{(1 + (-1 + y)^2)^{3/2}} + \frac{-1 + y}{((-1 + y)^2)^{3/2}} + \frac{y}{(1 + y^2)^{3/2}} \right\}, \right.$   

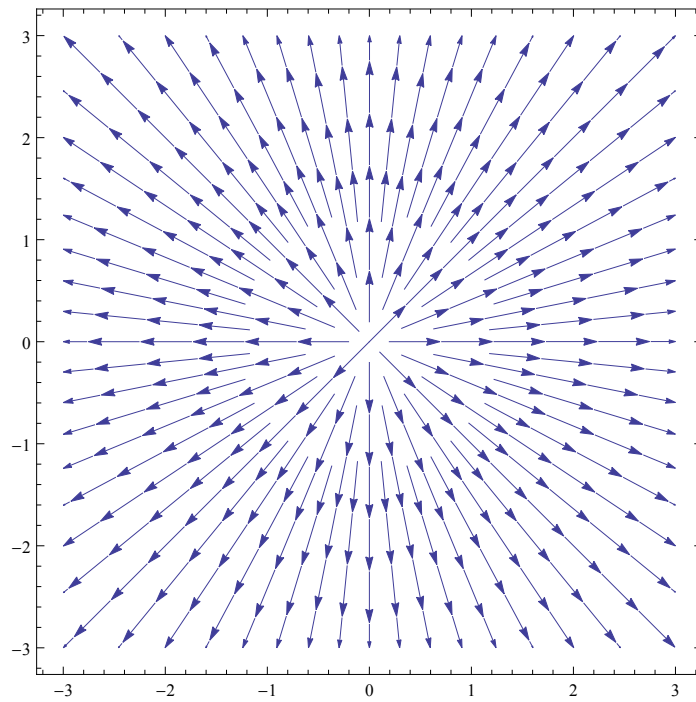
 $\left. \left\{ \frac{-1 + x}{(1 + (-1 + x)^2)^{3/2}} + \frac{x}{(x^2)^{3/2}} - \frac{2x}{(1 + x^2)^{3/2}}, -\frac{1}{(1 + (-1 + x)^2)^{3/2}} + \frac{2}{(1 + x^2)^{3/2}} \right\} \right\}$ 
```

QUESTION 2 A

```
In[15]:= EF[x_, y_] := {x / (x^2 + y^2)^(3 / 2), y / (x^2 + y^2)^(3 / 2)}
```

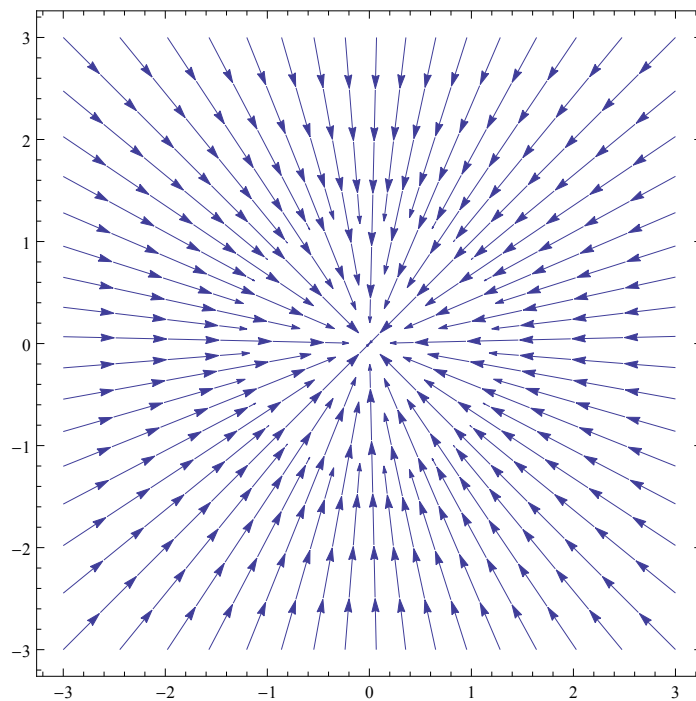
QUESTION 2 B

```
StreamPlot[EF[x, y], {x, -3, 3}, {y, -3, 3}]
```



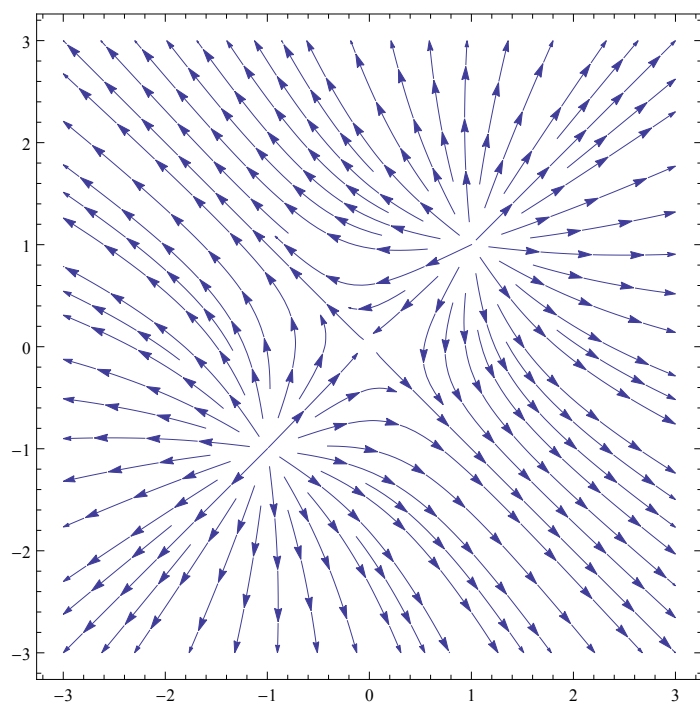
QUESTION 2 C

```
StreamPlot[-EF[x, y], {x, -3, 3}, {y, -3, 3}]
```



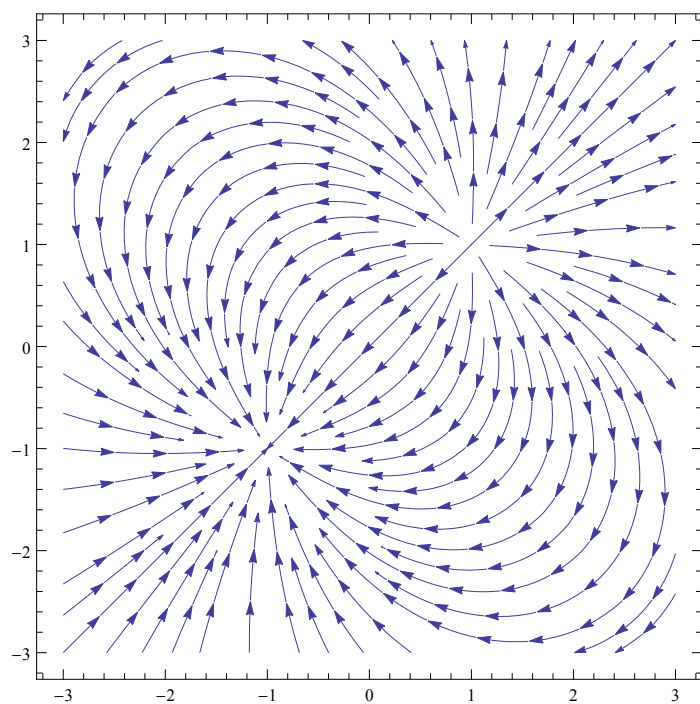
QUESTION 2 D

```
StreamPlot[EF[x + 1, y + 1] + EF[x - 1, y - 1], {x, -3, 3}, {y, -3, 3}]
```



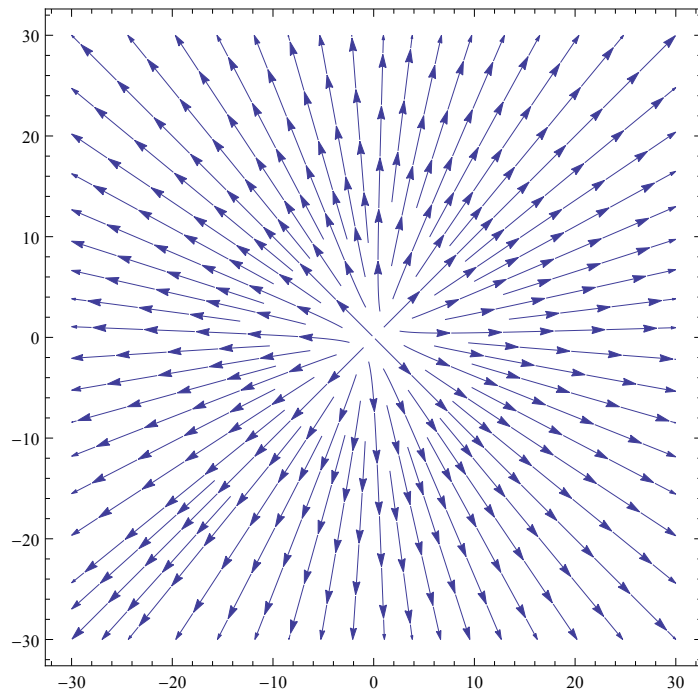
QUESTION 2 E

```
StreamPlot[-EF[x + 1, y + 1] + EF[x - 1, y - 1], {x, -3, 3}, {y, -3, 3}]
```



QUESTION 2 F (d)

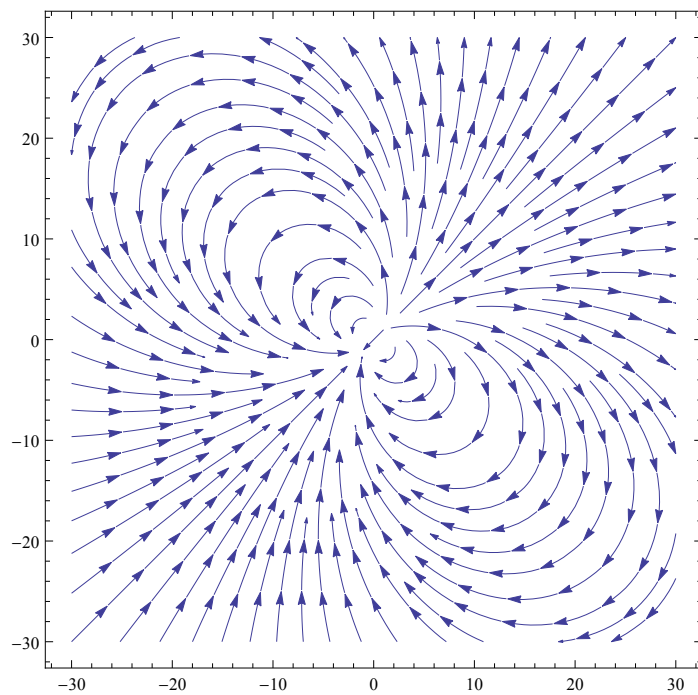
```
StreamPlot[EF[x + 1, y + 1] + EF[x - 1, y - 1], {x, -30, 30}, {y, -30, 30}]
```



Looks like a single point charge's field lines

QUESTION 2 F (e)

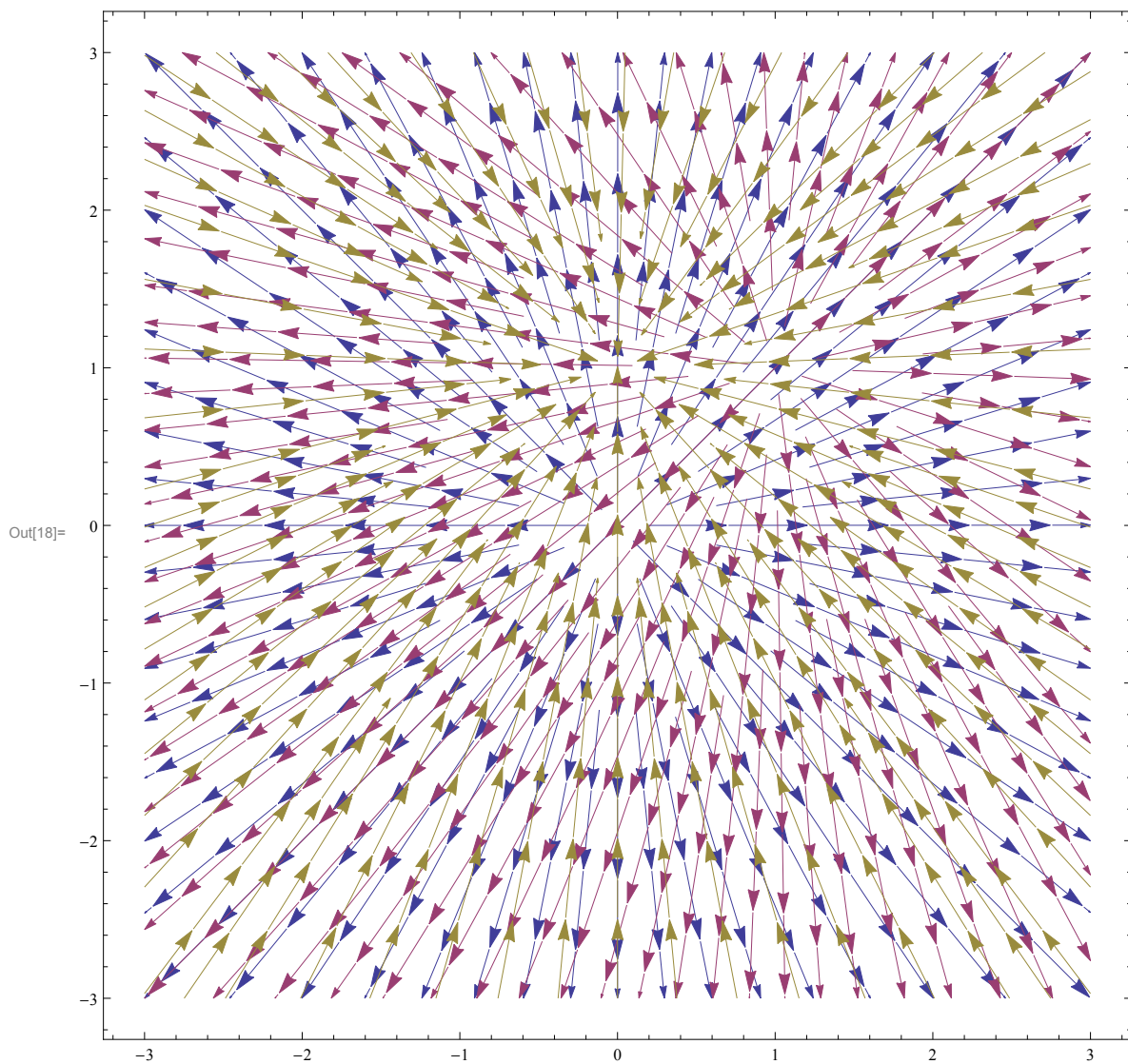
```
StreamPlot[-EF[x + 1, y + 1] + EF[x - 1, y - 1], {x, -30, 30}, {y, -30, 30}]
```



Looks like magnetic field lines

QUESTION 2 G

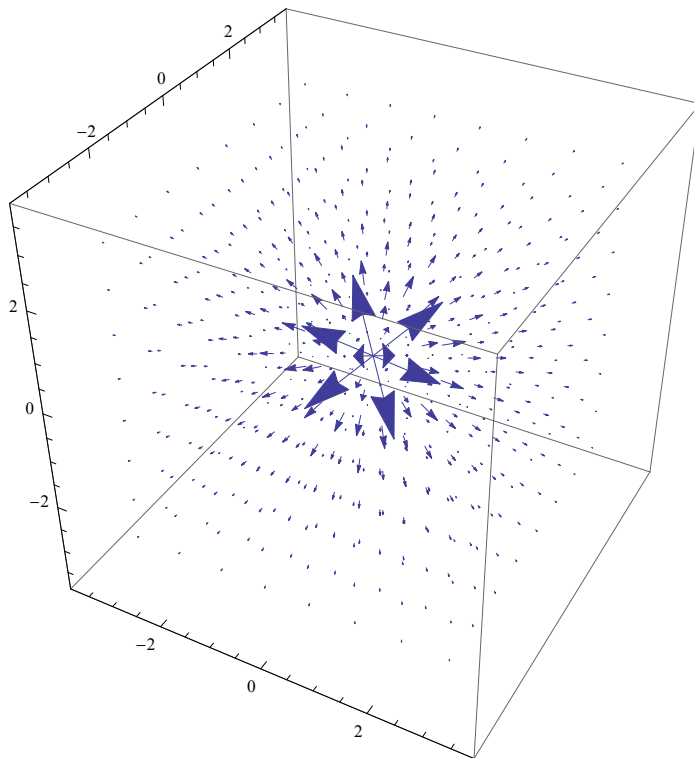
```
In[17]:= StreamPlot[{EF[x, y], EF[x - 1, y - 1], -2 * EF[x, y - 1]}, {x, -3, 3}, {y, -3, 3}]
```



QUESTION 2 H (I)

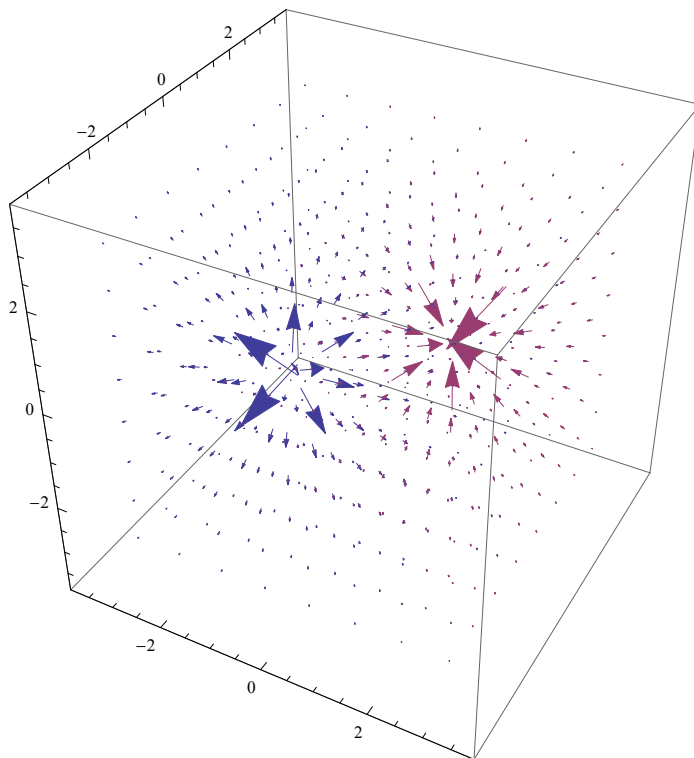
```
EF[x_, y_, z_] := {x / (x^2 + y^2 + z^2)^(3 / 2),  
  y / (x^2 + y^2 + z^2)^(3 / 2), z / (x^2 + y^2 + z^2)^(3 / 2)}
```

```
VectorPlot3D[{EF[x, y, z]], {x, -3, 3}, {y, -3, 3}, {z, -3, 3}]
```



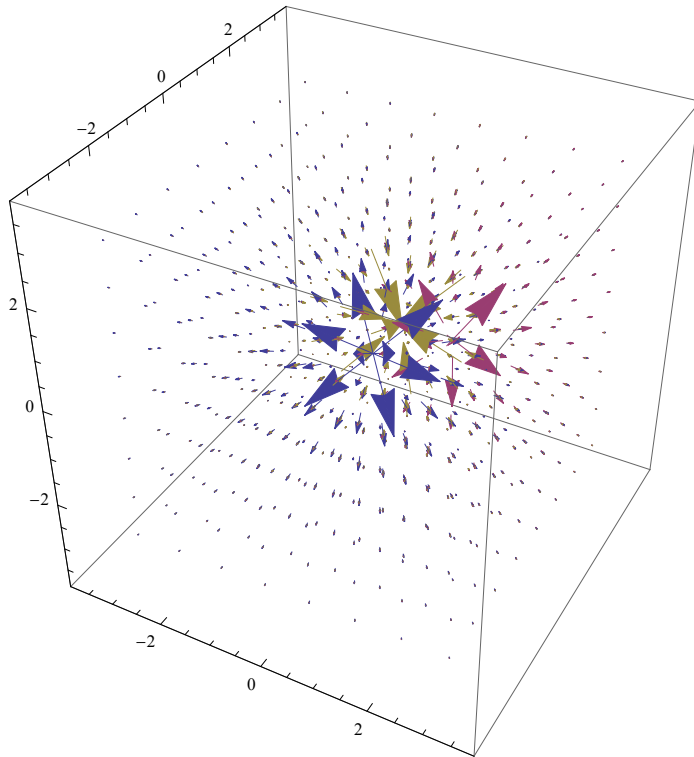
QUESTION 2 H (II)

```
VectorPlot3D[{EF[x + 1, y + 1, z], -EF[x - 1, y - 1, z]],  
{x, -3, 3}, {y, -3, 3}, {z, -3, 3}]
```



QUESTION 2 H (III)

```
VectorPlot3D[{EF[x, y, z], EF[x - 1, y - 1, z], -2 * EF[x, y - 1, z]},
  {x, -3, 3}, {y, -3, 3}, {z, -3, 3}]
```



#### QUESTION 2 H (IV)

```
In[19]:= R = 1 * Cos[45 * Pi / 180]
```

```
Out[19]=  $\frac{1}{\sqrt{2}}$ 
```

```
In[20]:= EF[x_, y_, z_] := {x / (x^2 + y^2 + z^2)^(3 / 2),
  y / (x^2 + y^2 + z^2)^(3 / 2), z / (x^2 + y^2 + z^2)^(3 / 2)}
```



```

In[22]:= VectorPlot3D[{EF[x - 1, y, z], EF[x + 1, y, z],
  EF[x, y - 1, z], EF[x, y + 1, z], EF[x + R, y + R, z], EF[x - R, y - R, z],
  EF[x + R, y - R, z], EF[x - R, y + R, z]}, {x, -3, 3}, {y, -3, 3}, {z, -3, 3}]

```

