AdaBoost (Adaptive Boosting):

- · AdaBoost (Adaptive Boosting) is an ensemble learning algorithm that combines multiple weak learners
- (e.g., decision trees with limited depth) to create a strong classifier.
- · It assigns weights to data points, focuses on misclassified samples, and iteratively builds weak models to correct errors.
- The final prediction is a weighted combination of weak learners outputs, and it is highly effective in improving classification accuracy.

The code below is implementing a boosting algorithm i.e AdaBoost (Adaptive Boosting), in a step-by-step manner for a binary classification problem. Here are the main steps and points of what is being done:

1. Data Preparation:

- A dataset is created with two features (X1 and X2) and a binary label (0 or 1).
- The dataset is visualized using a scatter plot to observe the distribution of data points.

2. Assigning Weights:

Initial weights are assigned to each data point. In this case, all weights are set to 0.1, as there are ten data points in total.

3. Base Model (Weak Learner):

- A decision tree classifier with a maximum depth of 1 (a stump) is trained on the dataset. This is considered a weak learner.
- The decision tree's structure is visualized using the plot tree function.

4. Weighted Prediction:

The weak learner predicts labels for the data points, and these predictions are stored in the 'y_pred' column of the DataFrame.

5. Calculating Model Weight (Alpha):

- A function is defined to calculate the weight (alpha) of the current weak learner based on its error rate.
- · The calculated alpha value represents the contribution of the weak learner to the final ensemble model.

6. Updating Data Point Weights:

• The weights of the data points are updated based on whether the weak learner's predictions match the true labels. Data points with correct predictions have their weights reduced, while those with incorrect predictions have their weights increased.

7. Normalizing Weights:

The updated data point weights are normalized to ensure they sum up to 1, which is a requirement for AdaBoost.

8. Creating a New Dataset:

· A new dataset is sampled by randomly selecting data points from the original dataset, with probabilities proportional to their normalized weights. This process is known as up-sampling, and it gives more importance to the misclassified points.

9. Iterative Model Building:

• The steps from 3 to 8 are repeated for a specified number of iterations or until a certain condition is met. Each iteration involves training a new weak learner, calculating its weight, updating data point weights, and normalizing weights.

10. Ensemble Model Prediction:

- To make predictions using the ensemble model, each weak learner's output (1 or -1) is scaled by its alpha value, and the results are summed to produce a final prediction.
- If the sum is positive, the ensemble predicts class 1; if it's negative, the ensemble predicts class 0.

11. Testing New Data Points:

• The code demonstrates how to use the trained ensemble model to make predictions on new data points.

In summary, this code is implementing the AdaBoost algorithm from scratch, which is an ensemble learning technique that combines the predictions of multiple weak learners (in this case, decision trees with depth 1) to create a strong classifier. It iteratively adjusts the weights of data points to focus on the misclassified samples, and the final prediction is a weighted combination of the weak learners predictions. This process continues for several iterations to improve classification accuracy.

```
In [1]:
        import pandas as pd
        import numpy as np
        from mlxtend.plotting import plot decision regions
In [2]: df = pd.DataFrame()
In [3]:
        df['X1'] = [1,3,3,4,5,6,7,7,8,9]
        df['X2'] = [10,6,5,6,1,2,8,9,2,5]
        df['label'] = [0,1,1,1,0,0,1,1,0,0]
```

```
3
                  5
                        1
              4
                  6
              6 2
                        0
              7
                  8
                        1
              8
                  2
                        0
              9
                  5
                        0
 In [5]: import seaborn as sns
          sns.scatterplot(x=df['X1'], y=df['X2'], hue=df['label'])
 Out[5]: <Axes: xlabel='X1', ylabel='X2'>
              10 -
                                                                                  label
                                                                                       1
               8
               6
           \aleph
               4
               2
                            2
                                                                     7
                                     3
                                             4
                                                     5
                                                             6
                                                                                      9
                                                    X1
 In [6]: #Step -1 : Assigining weights
    df['weight'] = 1/df.shape[0]
 In [7]: df
             X1 X2 label weight
 Out[7]:
              1 10
                              0.1
              3 6
                             0.1
          2
              3
                  5
                              0.1
                  6
                              0.1
              5
                 1
                        0
                              0.1
                 2
                        0
              6
                              0.1
                              0.1
              7 9
                             0.1
          8
              8
                 2
                              0.1
          9 9 5
                              0.1
 In [8]: from sklearn.tree import DecisionTreeClassifier
 In [9]: dt1 = DecisionTreeClassifier(max_depth = 1)
In [10]: X = df.iloc[:, 0:2].values
y = df.iloc[:,2].values
In [11]: dt1.fit(X, y)
```

Out[4]: X1 X2 label

1 10

```
In [12]: from sklearn.tree import plot_tree
         plot_tree(dt1)
         [Text(0.5, 0.75, 'x[1] <= 3.5\ngini = 0.5\nsamples = 10\nvalue = [5, 5]'), Text(0.25, 0.25, 'gini = 0.0\nsamples = 3\nvalue = [3, 0]'), Text(0.75, 0.25, 'gini = 0.408\nsamples = 7\nvalue = [2, 5]')]
Out[12]:
                            x[1] <= 3.5
                             gini = 0.5
                          samples = 10
                           value = [5, 5]
               gini = 0.0
                                     gini = 0.408
            samples = 3 \mid \text{samples} = 7
           value = [3, 0] | value = [2, 5]
In [13]: plot_decision_regions(X, y, clf = dt1, legend = 2)
         <Axes: >
Out[13]:
          10 -
           8 -
```

8

10

Out[11]: v

2 -

In [15]: df

2

In [14]: df['y_pred'] = dt1.predict(X)

DecisionTreeClassifier
DecisionTreeClassifier(max depth=1)

```
3
                 5
                       1
                             0.1
                                      1
              4
                 6
                             0.1
                                      1
              5
                             0.1
                                      0
              6 2
                                     0
                       0
                             0.1
             7
                 8
                             0.1
                             0.1
              8
                 2
                       0
                                     0
                             0.1
             9
                 5
                       0
                             0.1
In [16]: \# 3 mistakes i.e. 3/10 = 0.3
In [17]: def calculate_model_weight(error):
               return 0.5*np.log((1-error)/(error))
In [18]:
          #Step 3 - calculate model weight
          alpha1 = calculate model weight(0.3)
          alpha1
          0.42364893019360184
Out[18]:
          #Step 4 - Update weights
In [19]:
          def update_row_weights(row, alpha = 0.423):
              if row['label'] == row['y_pred']:
    return row['weight'] * np.exp(-alpha)
               else:
                   return row['weight'] * np.exp(alpha)
In [20]: df['updated_weights'] = df.apply(update_row_weights, axis = 1)
In [21]: df
Out[21]:
             X1 X2 label weight y_pred updated_weights
              1
                 10
                             0.1
                                               0.152653
                             0.1
                                               0.065508
              3
                 6
          2
              3
                 5
                             0.1
                                               0.065508
                             0.1
                                               0.065508
                 6
                                     0
                                               0.065508
              5
                 1
                       0
                             0.1
              6
                 2
                       0
                             0.1
                                     0
                                               0.065508
              7
                  8
                             0.1
                                      1
                                               0.065508
              7
                 9
                             0.1
                                      1
                                               0.065508
             8
                 2
                             0.1
                                               0.065508
                       0
                                     0
              9 5
                       0
                                               0.152653
In [22]: df['updated weights'].sum()
Out[22]: 0.8293697656827363
In [23]: df['normalized weights'] = df['updated weights']/df['updated weights'].sum()
In [24]: df
```

X1 X2 label weight y_pred

0.1

0.1

1 10

3

Out[15]:

```
3
                               0.1
                                                  0.065508
                                                                     0.078985
           2
               3
                   5
                                                  0.065508
                                                                     0.078985
                         1
                               0.1
                                        1
           3
               4
                   6
                         1
                               0.1
                                        1
                                                  0.065508
                                                                     0.078985
               5
                                        0
                                                                     0.078985
                         0
                               0.1
                                                  0.065508
               6
                  2
                                        0
                                                                     0.078985
           5
                         0
                               0.1
                                                  0.065508
           6
               7
                   8
                         1
                               0.1
                                        1
                                                  0.065508
                                                                     0.078985
                   9
                               0.1
                                                  0.065508
                                                                     0.078985
               8
                   2
                         0
                                        0
                                                                     0.078985
                               0.1
                                                  0.065508
               9
                   5
                         0
                               0.1
                                                  0.152653
                                                                     0.184060
In [25]: df['normalized_weights'].sum()
           1.0
In [26]: # Calculating range of values
           df['cumsum_upper'] = np.cumsum(df['normalized_weights'])
In [28]:
           df['cumsum_lower'] = df['cumsum_upper'] - df['normalized_weights']
In [29]:
           df
              X1 X2 label
                           weight y_pred updated_weights normalized_weights cumsum_upper cumsum_lower
Out[29]:
           0
               1
                  10
                               0.1
                                        1
                                                  0.152653
                                                                     0.184060
                                                                                    0.184060
                                                                                                   0.000000
           1
               3
                  6
                         1
                               0.1
                                        1
                                                  0.065508
                                                                     0.078985
                                                                                    0.263045
                                                                                                   0.184060
           2
               3
                   5
                               0.1
                                        1
                                                  0.065508
                                                                     0.078985
                                                                                    0.342030
                                                                                                   0.263045
                   6
                               0.1
                                                  0.065508
                                                                     0.078985
                                                                                    0.421015
                                                                                                   0.342030
               5
                         0
                                        0
                   1
                               0.1
                                                  0.065508
                                                                     0.078985
                                                                                    0.500000
                                                                                                   0.421015
           5
               6
                   2
                         0
                               0.1
                                        0
                                                  0.065508
                                                                     0.078985
                                                                                    0.578985
                                                                                                   0.500000
               7
                   8
                         1
                               0.1
                                        1
                                                  0.065508
                                                                     0.078985
                                                                                    0.657970
                                                                                                   0.578985
               7
                   9
                         1
                               0.1
                                        1
                                                  0.065508
                                                                     0.078985
                                                                                    0.736955
                                                                                                   0.657970
               8
                   2
                         0
                               0.1
                                        0
                                                  0.065508
                                                                     0.078985
                                                                                    0.815940
                                                                                                   0.736955
                   5
                               0.1
                                                  0.152653
                                                                     0.184060
                                                                                     1.000000
                                                                                                   0.815940
In [30]: def create_new_dataset(df):
                indices = []
                for i in range(df.shape[0]):
                    a = np.random.random()
                    for index, row in df.iterrows():
    if row['cumsum_upper'] > a and a > row['cumsum_lower']:
                              indices.append(index)
                return indices
In [31]: index_values = create_new_dataset(df)
           index_values
           [5, 7, 9, 5, 0, 6, 8, 5, 0, 5]
Out[31]:
           # weight of those rows have increased where errors occurred. this is called up sampling
In [32]:
           second_df = df.iloc[index_values, [0,1,2,3]]
In [33]:
In [34]:
           second_df
```

X1 X2 label weight y_pred updated_weights normalized_weights

0.152653

0.184060

Out[24]:

10

0.1

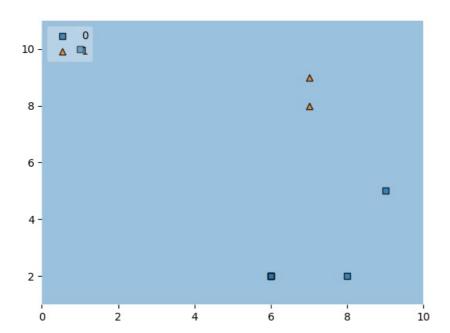
```
9
               5
                         0.1
              2
                         0.1
                         0.1
            7 8
                         0.1
            8
              2
                         0.1
                         0.1
            1 10
                         0.1
           6 2
                         0.1
In [35]: dt2 = DecisionTreeClassifier(max_depth = 1)
In [36]: X = second_df.iloc[:, 0:2].values
        y = second_df.iloc[:,2].values
In [37]: dt2.fit(X,y)
Out[37]: v
                DecisionTreeClassifier
        DecisionTreeClassifier(max depth=1)
In [38]: plot_tree(dt2)
        [Text(0.5, 0.75, 'x[0] \le 6.5 \cdot gini = 0.32 \cdot gles = 10 \cdot gles = [8, 2]'),
Out[38]:
         Text(0.25, 0.25, 'gini = 0.0\nsamples = 6\nvalue = [6, 0]'), Text(0.75, 0.25, 'gini = 0.5\nsamples = 4\nvalue = [2, 2]')]
                           x[0] <= 6.5
                          gini = 0.32
samples = 10
                          value = [8, 2]
                                             gini = 0.5
              gini = 0.0
            samples = 6 samples = 4
                                         value = [2, 2]
           value = [6, 0]
In [39]: plot_decision_regions(X, y , clf = dt2, legend =2)
```

X1 X2 label weight

0.1

Out[34]:

Out[39]: <Axes: >



In [44]: alpha2

```
In [40]: # One mistake
In [41]: second_df['y_pred'] = dt2.predict(X)
In [42]: second_df
            X1 X2 label weight y_pred
Out[42]:
                2
                           0.1
             7
                9
                           0.1
                                   0
                           0.1
                                   0
             9
                5
                      0
               2
                           0.1
                                   0
             6
             1 10
                      0
                           0.1
                                   0
                                   0
                8
                           0.1
                2
                           0.1
                                   0
             6 2
                      0
                           0.1
                                   0
                                   0
            1 10
                           0.1
         5 6 2
                           0.1
                                   0
In [43]: alpha2 = calculate_model_weight(0.1)
```

```
Out[44]: 1.0986122886681098

In [45]: # Update weights
def update_row_weights(row, alpha = 1.09):
    if row['label'] == row['y_pred']:
        return row['weight'] * np.exp(-alpha)
    else:
        return row['weight'] * np.exp(alpha)
```

```
In [46]: second_df['updated_weights'] = second_df.apply(update_row_weights, axis = 1)
           second_df
In [47]:
             X1 X2 label weight y_pred updated_weights
Out[47]:
               6
                  2
                        0
                              0.1
                                        0
                                                 0.033622
                                        0
           7
               7
                  9
                        1
                              0.1
                                                 0.297427
                                                 0.033622
           9
               9
                  5
                        0
                              0.1
                                        0
           5
               6
                  2
                        0
                              0.1
                                        0
                                                 0.033622
               1
                 10
                        0
                              0.1
                                        0
                                                 0.033622
              7
                  8
                        1
                              0.1
                                       0
                                                 0.297427
           8
               8
                  2
                        0
                              0.1
                                        0
                                                  0.033622
               6
                  2
                        0
                              0.1
                                        0
                                                 0.033622
              1 10
                              0.1
                                        0
                                                 0.033622
                        0
               6
                  2
                        0
                              0.1
                                        0
                                                  0.033622
In [48]: second_df['normalized_weights'] = second_df['updated_weights']/second_df['updated_weights'].sum()
In [49]: second df
Out[49]:
             X1 X2 label
                           weight y_pred updated_weights normalized_weights
              6
                  2
                        0
                              0.1
                                       0
                                                 0.033622
                                                                    0.038922
                                        0
               7
                  9
                              0.1
                                                 0.297427
                                                                    0.344313
               9
                  5
                        0
                              0.1
                                        0
                                                 0.033622
                                                                    0.038922
               6
                  2
                        0
                              0.1
                                       0
                                                 0.033622
                                                                    0.038922
           0
              1 10
                        0
                              0.1
                                        0
                                                                    0.038922
                                                 0.033622
               7
                  8
                        1
                              0.1
                                        0
                                                 0.297427
                                                                    0.344313
               8
                  2
                        0
                              0.1
                                        0
                                                 0.033622
                                                                    0.038922
               6
                  2
                        0
                              0.1
                                        0
                                                 0.033622
                                                                    0.038922
           0
               1 10
                        0
                              0.1
                                        0
                                                  0.033622
                                                                    0.038922
              6
                  2
                        0
                                       0
                                                 0.033622
                                                                    0.038922
                              0.1
In [50]: second df['cumsum upper'] = np.cumsum(second df['normalized weights'])
In [51]: second df['cumsum lower'] = second df['cumsum upper'] - second df['normalized weights']
In [52]: second_df[['X1','X2','label', 'weight','y_pred','updated_weights','normalized_weights','cumsum_lower','cumsum_u
Out[52]:
             X1 X2 label weight y_pred updated_weights normalized_weights cumsum_lower cumsum_upper
                  2
           5
              6
                        0
                              0.1
                                        0
                                                 0.033622
                                                                    0.038922
                                                                                   0.000000
                                                                                                  0.038922
                  9
                              0.1
                                       0
                                                 0.297427
                                                                    0.344313
                                                                                   0.038922
                                                                                                  0.383235
               9
                  5
                        0
                              0.1
                                        0
                                                 0.033622
                                                                    0.038922
                                                                                   0.383235
                                                                                                  0.422157
           5
               6
                  2
                        0
                              0.1
                                       0
                                                 0.033622
                                                                    0.038922
                                                                                   0.422157
                                                                                                  0.461078
           0
               1
                 10
                              0.1
                                        0
                                                 0.033622
                                                                    0.038922
                                                                                   0.461078
                                                                                                  0.500000
               7
                  8
                                        0
                              0.1
                                                 0.297427
                                                                    0.344313
                                                                                   0.500000
                                                                                                  0.844313
               8
                  2
                        0
                              0.1
                                       0
                                                 0.033622
                                                                    0.038922
                                                                                   0.844313
                                                                                                  0.883235
               6
                  2
                        0
                                       0
                                                 0.033622
                                                                    0.038922
                                                                                   0.883235
                                                                                                  0.922157
                              0.1
           0
              1 10
                        0
                              0.1
                                        0
                                                 0.033622
                                                                    0.038922
                                                                                   0.922157
                                                                                                  0.961078
           5 6 2
                        0
                              0.1
                                       0
                                                 0.033622
                                                                    0.038922
                                                                                   0.961078
                                                                                                  1.000000
In [53]: index values = create new dataset(second df)
          third df = second df.iloc[index values, [0,1,2,3]]
In [54]:
In [55]: third_df
```

```
8
               2
                         0.1
                         0.1
            6 2
                         0.1
               8
                         0.1
                         0.1
            7 8
                         0.1
                         0.1
In [56]: dt3 = DecisionTreeClassifier(max_depth = 1)
In [57]: X = third_df.iloc[:, 0:2].values
y = third_df.iloc[:,2].values
In [58]: dt3.fit(X,y)
Out[58]: v
                DecisionTreeClassifier
         DecisionTreeClassifier(max depth=1)
In [59]: plot_tree(dt3)
         [Text(0.5, 0.75, 'x[1] \le 5.0 \cdot gini = 0.32 \cdot gsamples = 10 \cdot gsamples = [8, 2]'),
Out[59]:
         Text(0.25, 0.25, 'gini = 0.0\nsamples = 8\nvalue = [8, 0]'), Text(0.75, 0.25, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]')]
                            x[1] \le 5.0
                           gini = 0.32
                          samples = 10
                          value = [8, 2]
                                             gini = 0.0
               gini = 0.0
            samples = 8 | samples = 2
           value = [8, 0]
                                         value = [0, 2]
In [60]: plot_decision_regions(X, y , clf = dt3, legend =2)
```

X1 X2 label weight

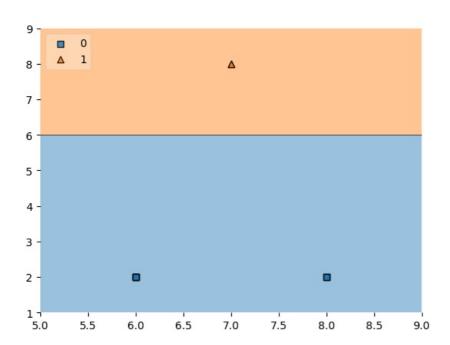
0

6 2

Out[60]: <Axes: >

0.1

0.1



```
In [61]: third_df['y_pred'] = dt3.predict(X)
```

In [62]: third_df

X1 X2 label weight y_pred Out[62]: 8 2 0.1 **5** 6 2 0 0.1 0 6 2 0.1 0 0 8 2 0 0.1 0 6 2 0 0 0.1 6 2 0.1 0 8 0.1 1 6 2 0.1 0 8 1 0.1 1 8 2 0.1 0

```
In [63]: #here error is 0. to avoid infinity case
error = 0.0000001
alpha3 = calculate_model_weight(error)
```

In [64]: alpha3

Out[64]: 8.059047775479158

In [65]: print(alpha1, alpha2, alpha3)

 $0.42364893019360184 \ 1.0986122886681098 \ 8.059047775479158$

Predictionn

```
In [66]: | query = np.array([3,6]).reshape(1,2)
         dt1.predict(query)
         array([1], dtype=int64)
Out[66]:
In [67]: dt2.predict(query)
Out[67]: array([0], dtype=int64)
In [68]: dt3.predict(query)
Out[68]: array([1], dtype=int64)
In [69]: # -1 for 0 and 1 for 1
         alpha1*1 + alpha2*(-1) + alpha3*1
         7.38408441700465
Out[69]:
In [70]: np.sign(7.38)
Out[70]:
In [71]: #Predicts 1
         query = np.array([9,5]).reshape(1,2)
In [72]:
         dt1.predict(query)
         array([1], dtype=int64)
Out[72]:
In [73]: dt2.predict(query)
         array([0], dtype=int64)
Out[73]:
In [74]: dt3.predict(query)
         array([0], dtype=int64)
Out[74]:
In [75]: alpha1*1 + alpha2*(-1) + alpha3*(-1)
         -8.734011133953667
Out[75]:
In [76]: np.sign(-8.73)
Out[76]: -1.0
In [77]: #Predicts 0
 In [ ]:
```

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