

CDMA (Code Division Multiple Access) :-

CDMA works on codes and chip sequences which is different for different users. All the users are using the same frequency / bandwidth i.e., the bandwidth is not divided among various users unlike GSM.

The chip sequences are generated using DSSS (Direct Sequence Spread Spectrum).

Sender A:-

$$\text{Sends } A_d = 1 = 1$$

$$\text{Key } A_k = 010011 = -1, 1, -1, -1, 1, 1$$

(Assign $0 \rightarrow -1$ and $1 \rightarrow +1$)

$$\begin{aligned} \text{Sending signal } A_s &= A_d * A_k \\ &= (-1, 1, -1, -1, 1, 1) \end{aligned}$$

Sender B:-

$$\text{Sends } B_d = 0 = -1$$

$$\text{Key } B_k = 110101 = 1, 1, -1, 1, -1, 1$$

$$\therefore B_s = B_d * B_k = (-1, -1, +1, -1, +1, -1)$$

Both signals are superimposed in space.

$$\begin{aligned} \therefore A_e &= A_s + B_s = (-1, 1, -1, -1, 1, 1) + (-1, -1, +1, -1, +1, -1) \\ &= (-2, 0, 0, -2, 2, 0) \end{aligned}$$

Receiver wants to receive signal from sender A. Apply key A_k bit wise inner product. This will be A_e .

$$\begin{aligned} A_e &= (-2, 0, 0, -2, 2, 0) * A_k \\ &= (-2, 0, 0, -2, 2, 0) * (-1, 1, -1, -1, 1, 1) \\ &= (2, 0, 0, 2, 2, 0) \\ &= 6 \end{aligned}$$

(Adding all).

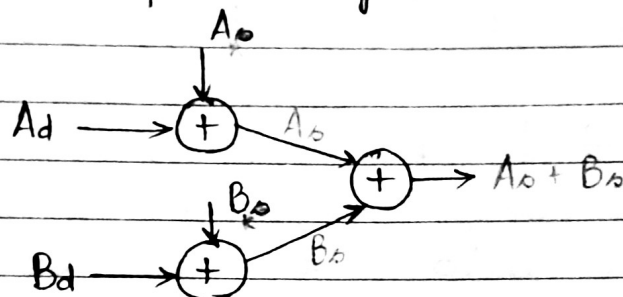
Result > 0 , therefore original bit was 1.

1ly, receiving signal from sender B.

$$\begin{aligned}
 B \text{ to } A &= (-2, 0, 0, -2, +2, 0) * B_k \\
 &= (-2, 0, 0, -2, +2, 0) * (1, 1, -1, 1, -1, 1) \\
 \therefore B_k &= (1, 1, 0, 1, 0, 1) \\
 &= (1, 1, -1, 1, -1, 1) \\
 &= (-2, 0, 0, -2, -2, 0) \\
 &= -6 \quad (\text{Adding all})
 \end{aligned}$$

Result < 0 , therefore original bit is 0.

If
 Result $< 0 \Rightarrow$ bit 0
 Result $= 0 \Rightarrow$ silent
 Result $> 0 \Rightarrow$ bit 1



FHSS (Frequency Hopped Spread Spectrum):-

Hopping between frequency bands so as to provide ne gaps in order to reduce bit error.

→ PN sequence generator in CDMA:-

PN sequence generator
 (Pseudo Number)

Walsh code: Walsh code Gold code

$$W_1 = [+1]$$

$$W_{2N} = \begin{bmatrix} W_N & W_N \\ W_N & \overline{W_N} \end{bmatrix}$$

E.g., $W_2 = \begin{bmatrix} +1 & +1 \\ +1 & -1 \end{bmatrix} \quad (N=1)$

$\therefore W_4 = W_{2(2)} = \begin{bmatrix} W_2 & W_2 \\ W_2 & \overline{W_2} \end{bmatrix} \quad (N=2)$

$$W_4 = \begin{bmatrix} +1 & +1 & +1 & +1 \\ +1 & -1 & +1 & -1 \\ +1 & +1 & -1 & -1 \\ +1 & -1 & -1 & +1 \end{bmatrix}$$

$$W_8 = W_{2(4)} = \begin{bmatrix} W_4 & W_4 \\ W_4 & W_4 \end{bmatrix} \quad (N=4)$$

$$W_8 = \begin{bmatrix} +1 & +1 & +1 & +1 & +1 & +1 & +1 & +1 \\ +1 & -1 & +1 & -1 & +1 & -1 & +1 & -1 \\ +1 & +1 & -1 & -1 & +1 & +1 & -1 & -1 \\ +1 & -1 & -1 & +1 & +1 & -1 & -1 & +1 \\ +1 & +1 & +1 & +1 & -1 & -1 & -1 & -1 \\ +1 & -1 & +1 & -1 & -1 & +1 & -1 & +1 \\ +1 & +1 & -1 & -1 & -1 & -1 & +1 & +1 \\ +1 & -1 & -1 & +1 & -1 & +1 & +1 & -1 \end{bmatrix}$$

Note that the matrices are symmetrical and every row (except first) has equal no. of +1s and -1s. So we say that the codes are orthogonal in nature, (i.e., $\text{prod} = 0$).

Q:- If the CDMA demux received the code $(-1, -1, -3, +1)$, find the bits sent by the different stations.

Sol:- Since we got 4 numbered chip code $(-1, -1, -3, +1)$

\therefore we would have used (4×4) Walsh matrix, i.e., W_4 .

For station A, we have Key $\begin{cases} +1, +1, +1, +1 \end{cases}$
 " " B, " " $\begin{cases} +1, -1, +1, -1 \end{cases}$
 " " C, " " $\begin{cases} +1, +1, -1, -1 \end{cases}$
 " " D, " " $\begin{cases} +1, -1, -1, +1 \end{cases}$

For A:

$$\begin{aligned} & (+1, +1, +1, +1) \cdot (-1, -1, -3, +1) \quad \text{Dot product} \\ & = (-1, -1, -3, +1) \\ & = -4 \quad \text{Adding all} \quad \text{i.e., bit 0} \end{aligned}$$

For B:

$$\begin{aligned} & (+1, -1, +1, -1) \cdot (-1, -1, -3, +1) \\ & = (-1, +1, -3, -1) \end{aligned}$$

For C:

$$\begin{aligned} & (+1, +1, -1, -1) \cdot (-1, -1, -3, +1) \\ &= (-1, -1, +3, -1) \\ &= 0 \quad \text{i.e., silent} \end{aligned}$$

For D:

$$\begin{aligned} & (+1, -1, -1, +1) \cdot (-1, -1, -3, +1) \\ &= (-1, +1, +3, +1) \\ &= 4 \quad \text{i.e., bit 1} \end{aligned}$$

Thus the stations have sent bits
0, 0, silent, 1 respectively.

Do from
slides

Gold code:-

It is a sequence of 0s and 1s.

It uses LFSR (Linear Feedback Shift Register operation).

MLSR (Maximal Length Shift Register Sequence).

Correlation:- Cross-Correlation and Auto-correlation.

110010

Shift by 0 bits.

110010

\therefore Do dot product with itself (Auto-correlation).

$$\begin{aligned} & (110010) \cdot (110010) \\ &= (110010) \cdot (110010) \\ &= (110010) \cdot (110010) \quad \text{Adding.} \\ &= 6 \quad \text{i.e., weightage.} \end{aligned}$$

Shift by 1 bit. (right shift).

011001

Do dot product with itself (Auto-correlation).

$$\begin{aligned} & (011001) \cdot (110010) \\ &= (-111001) \cdot (110010) \\ &= (-111001) \cdot (110010) \\ &= -2 \end{aligned}$$