

第一讲: MatLab 基础

数学模型和算法的应用与 MATLAB 实现

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微信公众号: 超级数学建模

Part I

MatLab 快速入门

简介

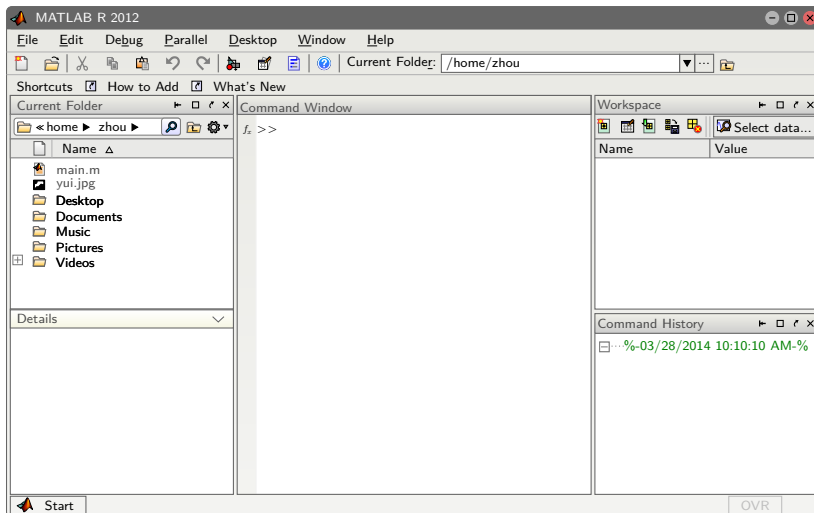
简史

- MATLAB (矩阵实验室) 是 **MAT**rix **LAB**oratory 的缩写;
- 最初由美国的 Clever Moler 教授于 1980 年开发, 初衷是为了解决“线性代数”课程的矩阵运算问题;
- 是一款由 MathWorks 公司 (1984 年成立) 出品的数学软件.

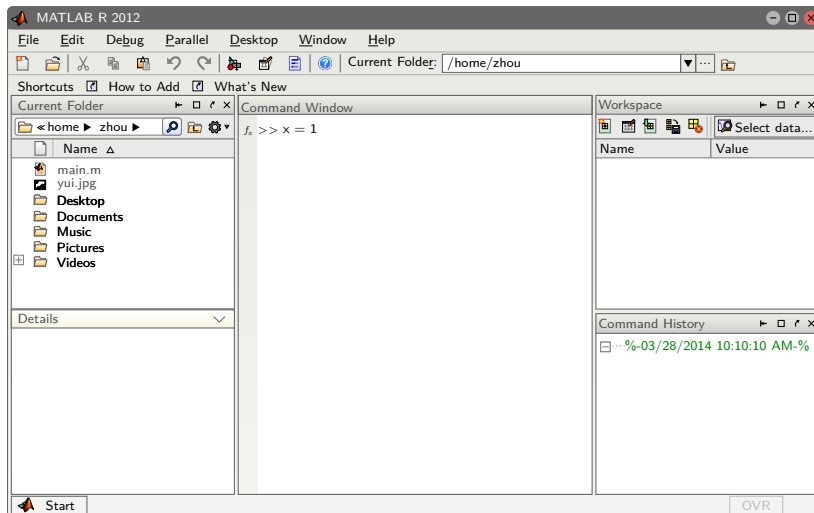
特性

- MATLAB 是一种用于算法开发, 数据可视化, 数据分析以及数值计算的高级技术计算语言和交互式环境.
- MATLAB 可用来创建用户界面及调用其它语言编写的程序.
- MATLAB 中包含众多的附加工具箱, 适合不同领域的应用.

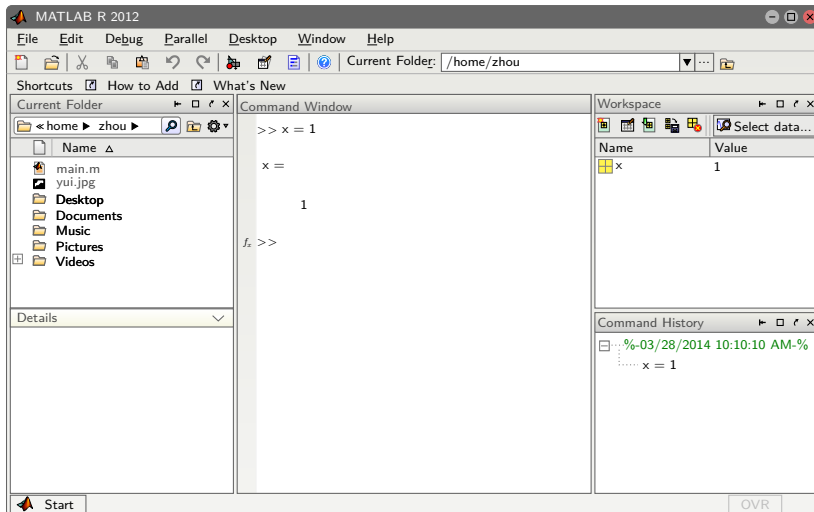
主窗介绍



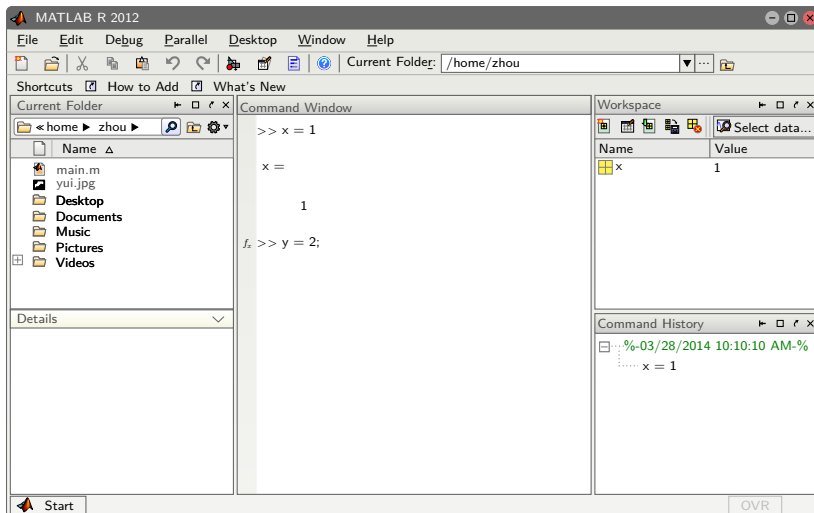
主窗介绍



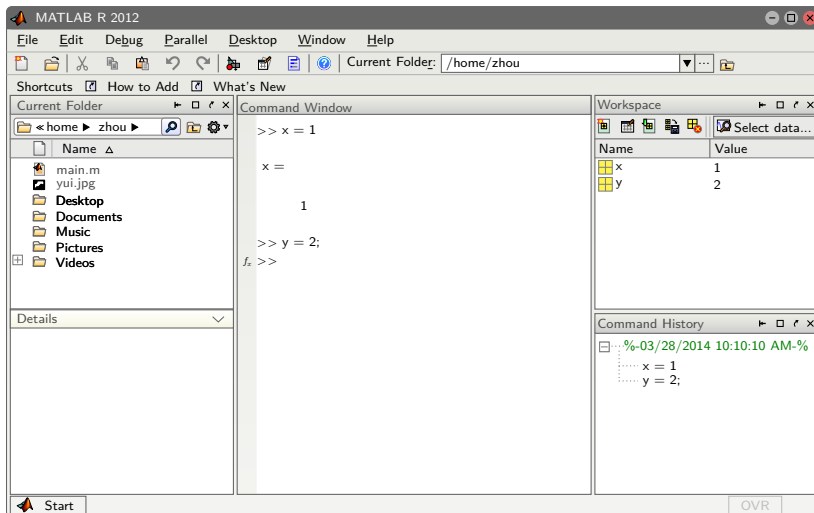
主窗介绍



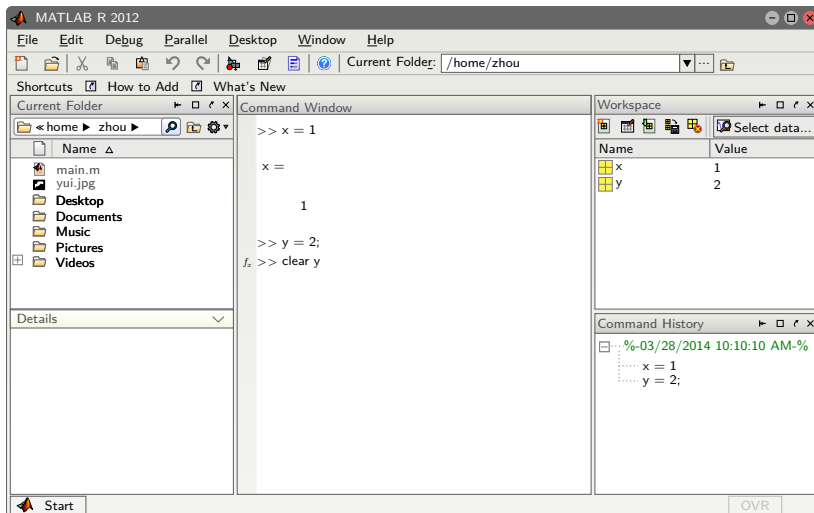
主窗介绍



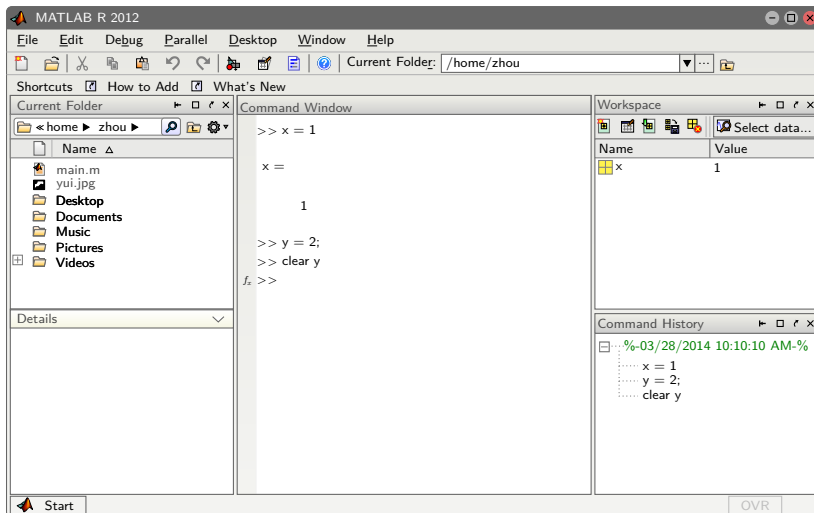
主窗介绍



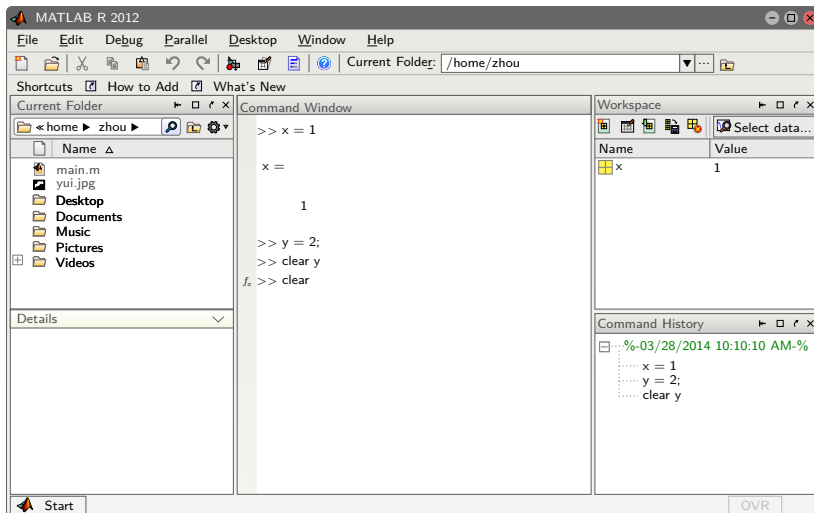
主窗介绍



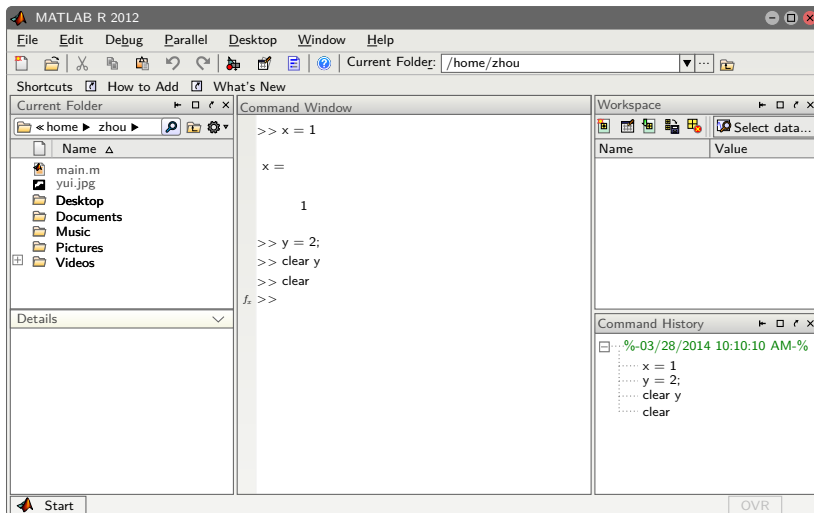
主窗介绍



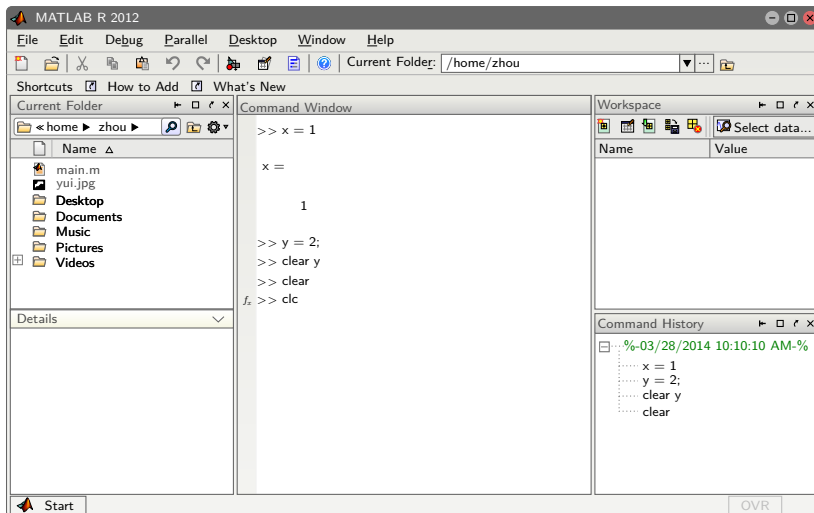
主窗介绍



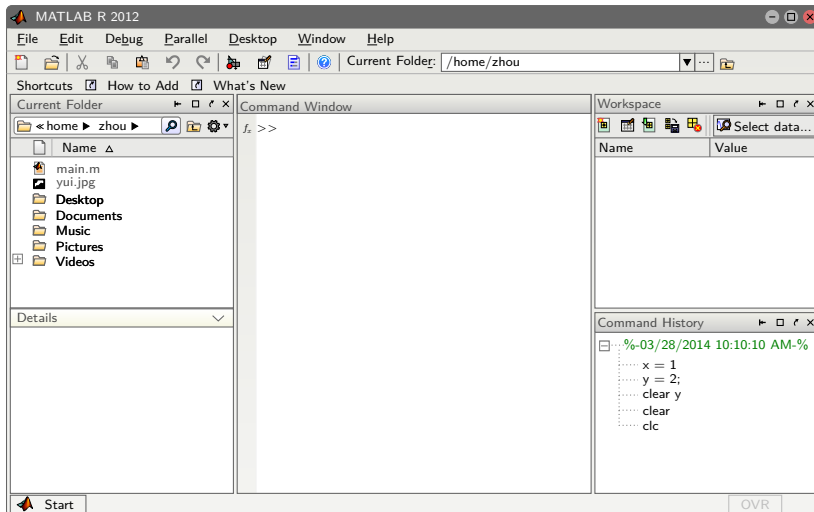
主窗介绍



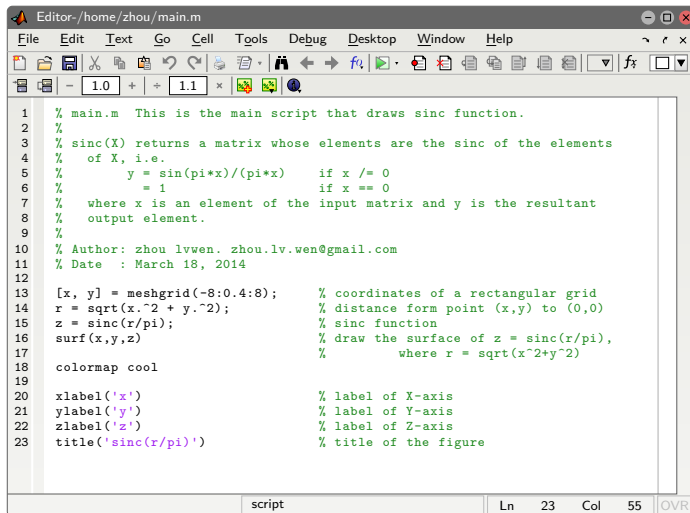
主窗介绍



主窗介绍



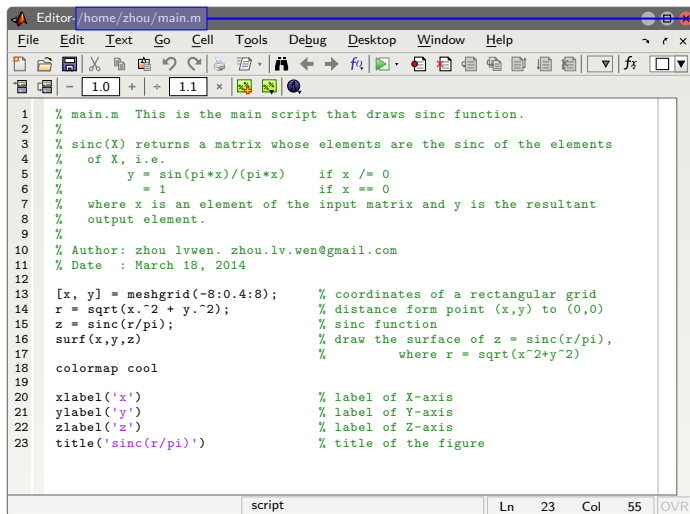
脚本窗口



```
Editor-/home/zhou/main.m
File Edit Text Go Cell Tools Debug Desktop Window Help
1 % main.m This is the main script that draws sinc function.
2 %
3 % sinc(X) returns a matrix whose elements are the sinc of the elements
4 % of X, i.e.
5 %     y = sin(pi*x)/(pi*x)    if x /= 0
6 %     = 1                    if x == 0
7 % where x is an element of the input matrix and y is the resultant
8 % output element.
9 %
10 % Author: zhou lvwen. zhou.lv.wen@gmail.com
11 % Date : March 18, 2014
12
13 [x, y] = meshgrid(-8:0.4:8); % coordinates of a rectangular grid
14 r = sqrt(x.^2 + y.^2); % distance from point (x,y) to (0,0)
15 z = sinc(r/pi); % sinc function
16 surf(x,y,z) % draw the surface of z = sinc(r/pi),
17 % where r = sqrt(x^2+y^2)
18 colormap cool
19
20 xlabel('x') % label of X-axis
21 ylabel('y') % label of Y-axis
22 zlabel('z') % label of Z-axis
23 title('sinc(r/pi)') % title of the figure

script Ln 23 Col 55 OVR
```

脚本窗口



Editor: /home/zhou/main.m

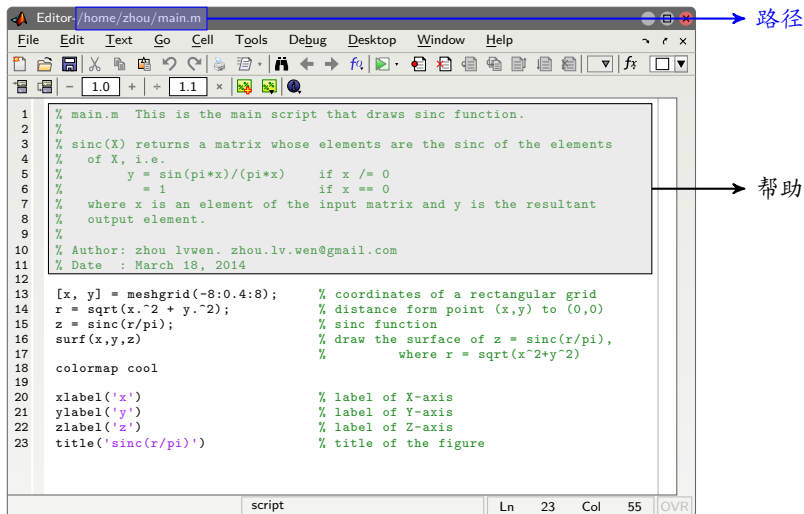
File Edit Text Go Cell Tools Debug Desktop Window Help

```
1 % main.m This is the main script that draws sinc function.
2 %
3 % sinc(X) returns a matrix whose elements are the sinc of the elements
4 % of X, i.e.
5 %     y = sin(pi*x)/(pi*x)    if x /= 0
6 %     = 1                    if x == 0
7 % where x is an element of the input matrix and y is the resultant
8 % output element.
9 %
10 % Author: zhou lvwen. zhou.lv.wen@gmail.com
11 % Date : March 18, 2014
12
13 [x, y] = meshgrid(-8:0.4:8); % coordinates of a rectangular grid
14 r = sqrt(x.^2 + y.^2);      % distance from point (x,y) to (0,0)
15 z = sinc(r/pi);             % sinc function
16 surf(x,y,z)                 % draw the surface of z = sinc(r/pi),
17                             % where r = sqrt(x^2+y^2)
18
19 colormap cool
20
21 xlabel('x')                  % label of X-axis
22 ylabel('y')                  % label of Y-axis
23 zlabel('z')                  % label of Z-axis
24 title('sinc(r/pi)')          % title of the figure
```

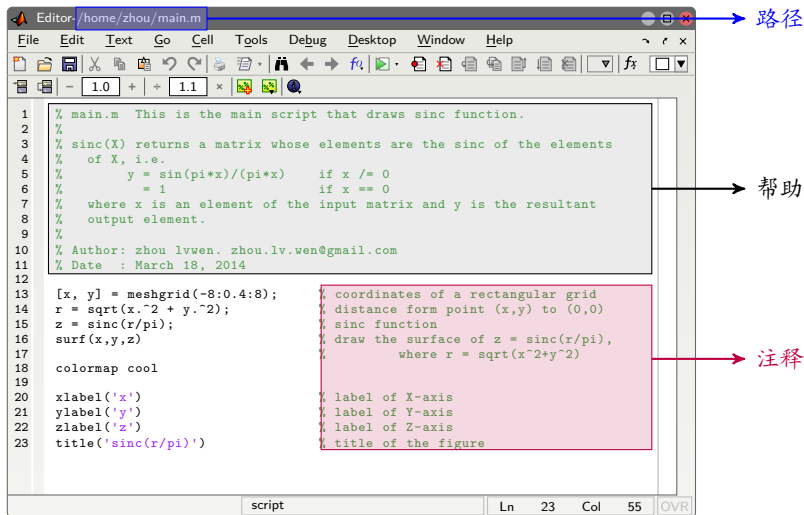
script Ln 23 Col 55 OVR

路径

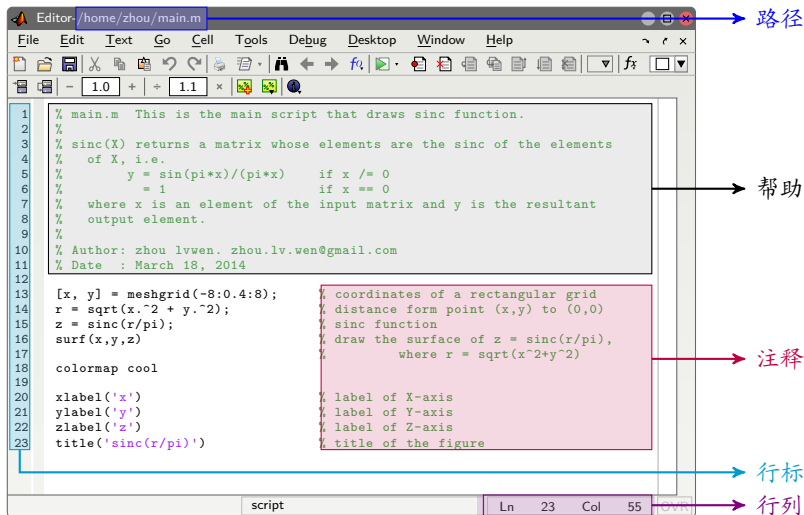
脚本窗口



脚本窗口



脚本窗口



脚本窗口

Editor: /home/zhou/main.m

File Edit Text Go Cell Tools Debug Desktop Window Help

1.0 1.1 x

```
1 % main.m This is the main script that draws sinc function.
2 %
3 % sinc(X) returns a matrix whose elements are the sinc of the elements
4 % of X, i.e.
5 %     y = sin(pi*x)/(pi*x)    if x /= 0
6 %     = 1                    if x == 0
7 % where x is an element of the input matrix and y is the resultant
8 % output element.
9 %
10 % Author: zhou lvwen. zhou.lv.wen@gmail.com
11 % Date : March 18, 2014
12
13 [x, y] = meshgrid(-8:0.4:8);
14 r = sqrt(x.^2 + y.^2);
15 z = sinc(r/pi);
16 surf(x,y,z)
17
18 colormap cool
19
20 xlabel('x')
21 ylabel('y')
22 zlabel('z')
23 title('sinc(r/pi)')
```

script Ln 23 Col 55

路径

调试

运行

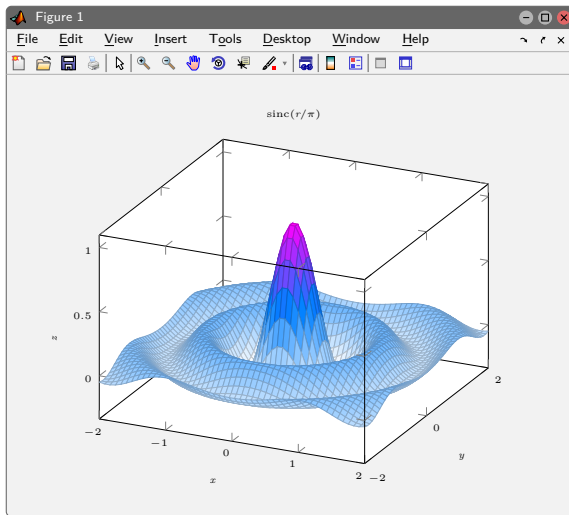
帮助

注释

行标

行列

图形窗口



获得帮助

帮助文档

- 如果你知道一个函数名, 想了解它的用法, 你可以用 `'help'` 命令得到它的帮助文档:
`>> help functionname`
- 如果你了解含某个关键词的函数, 你可以用 `'lookfor'` 命令得到相关的函数:
`>> lookfor keyword`

网络资源

- Mathworks 文件交流中心: [▶ Mathworks](#)
- Github 代码托管网站: [▶ Github](#)

实数, 复数, 行向量, 列向量, 矩阵的赋值



实数, 复数, 行向量, 列向量, 矩阵的赋值

```
Command Window
>> x = 5
```



实数, 复数, 行向量, 列向量, 矩阵的赋值

```
Command Window
>> x = 5
x =
    5
fx>>
```

实数, 复数, 行向量, 列向量, 矩阵的赋值

Command Window

```
>> x = 5
```

```
x =
```

```
5
```

```
>> x = [1 2 3]
```

实数, 复数, 行向量, 列向量, 矩阵的赋值

```
Command Window
>> x = 5
x =
    5
>> x = [1 2 3]
x =
    1     2     3
fx>>
```

实数, 复数, 行向量, 列向量, 矩阵的赋值

Command Window

```
>> x = 5
```

```
x =
```

```
5
```

```
>> x = [1 2 3]
```

```
x =
```

```
1    2    3
```

```
>> x = [1;2;3]
```

实数, 复数, 行向量, 列向量, 矩阵的赋值

```
Command Window

>> x = 5

x =

    5

>> x = [1 2 3]

x =

    1    2    3

>> x = [1;2;3]

x =

    1
    2
    3

fx >>
```

实数, 复数, 行向量, 列向量, 矩阵的赋值

Command Window

```
>> x = 5  
  
x =  
  
    5  
  
>> x = [1 2 3]  
  
x =  
  
    1    2    3  
  
>> x = [1;2;3]  
  
x =  
  
    1  
    2  
    3  
  
>> clc
```

实数, 复数, 行向量, 列向量, 矩阵的赋值



实数, 复数, 行向量, 列向量, 矩阵的赋值

Command Window

```
>> x = [1 2 3; 4 5 6; 7 8 9]
```



实数, 复数, 行向量, 列向量, 矩阵的赋值

```
Command Window
>> x = [1 2 3; 4 5 6; 7 8 9]
x =
     1     2     3
     4     5     6
     7     8     9
fx>>
```



实数, 复数, 行向量, 列向量, 矩阵的赋值

Command Window

```
>> x = [1 2 3; 4 5 6; 7 8 9]
```

```
x =
```

```
    1    2    3  
    4    5    6  
    7    8    9
```

```
>> y = [1 2 3  
        4 5 6]
```

实数, 复数, 行向量, 列向量, 矩阵的赋值

```
Command Window
>> x = [1 2 3; 4 5 6; 7 8 9]
x =
     1     2     3
     4     5     6
     7     8     9
>> y = [1 2 3
        4 5 6]
y =
     1     2     3
     4     5     6
 $f_x$  >>
```

向量的一般赋值方法



向量的一般赋值方法

```
Command Window
>> x = [0:2]
```

向量的一般赋值方法

```
Command Window
>> x = [0:2]

x =

    0.00    1.00    2.00

 $f_x$  >>
```



向量的一般赋值方法

Command Window

```
>> x = [0:2]
```

```
x =
```

```
    0.00    1.00    2.00
```

```
>> x = [0:2]'
```

向量的一般赋值方法

```
Command Window
>> x = [0:2]
x =
    0.00    1.00    2.00
>> x = [0:2] '
x =
    0.00
    1.00
    2.00
 $f_x$  >>
```


向量的一般赋值方法

Command Window

```
>> x = [0:2]
```

```
x =
```

```
0.00    1.00    2.00
```

```
>> x = [0:2]'
```

```
x =
```

```
0.00
```

```
1.00
```

```
2.00
```

```
>> x = [0:0.5:2]
```

向量的一般赋值方法

```
Command Window
>> x = [0:2]
x =
    0.00    1.00    2.00
>> x = [0:2] '
x =
    0.00
    1.00
    2.00
>> x = [0:0.5:2]
x =
    0.00    0.50    1.00    1.50    2.00
fx >>
```

向量的一般赋值方法

Command Window

```
>> x = [0:2]
```

```
x =
```

```
0.00    1.00    2.00
```

```
>> x = [0:2]'
```

```
x =
```

```
0.00
```

```
1.00
```

```
2.00
```

```
>> x = [0:0.5:2]
```

```
x =
```

```
0.00    0.50    1.00    1.50    2.00
```

```
>> x = linspace(0, 2, 5)
```

向量的一般赋值方法

```
Command Window
>> x = [0:2]
x =
    0.00    1.00    2.00
>> x = [0:2] '
x =
    0.00
    1.00
    2.00
>> x = [0:0.5:2]
x =
    0.00    0.50    1.00    1.50    2.00
>> x = linspace(0, 2, 5)
x =
    0.00    0.50    1.00    1.50    2.00
fx >>
```

常用矩阵



常用矩阵

Command Window

```
>> x = zeros(2,3)
```

常用矩阵

```
Command Window
>> x = zeros(2,3)

x =

    0.00    0.00    0.00
    0.00    0.00    0.00

fx >>
```



常用矩阵

Command Window

```
>> x = zeros(2,3)
```

```
x =
```

```
    0.00    0.00    0.00
```

```
    0.00    0.00    0.00
```

```
>> y = ones(2)
```


常用矩阵

Command Window

```
>> x = zeros(2,3)
```

```
x =
```

```
    0.00    0.00    0.00  
    0.00    0.00    0.00
```

```
>> y = ones(2)
```

```
x =
```

```
    1.00    1.00  
    1.00    1.00
```

f_x >>

常用矩阵

Command Window

```
>> x = zeros(2,3)
```

```
x =
```

```
    0.00    0.00    0.00  
    0.00    0.00    0.00
```

```
>> y = ones(2)
```

```
x =
```

```
    1.00    1.00  
    1.00    1.00
```

```
>> x = eye(2)
```

常用矩阵

```
Command Window

>> x = zeros(2,3)

x =

    0.00    0.00    0.00
    0.00    0.00    0.00

>> y = ones(2)

x =

    1.00    1.00
    1.00    1.00

>> x = eye(2)

x =

    1.00    0.00
    0.00    1.00

 $f_x$  >>
```



固定变量



固定变量

```
Command Window
>> pi
```



固定变量

```
Command Window
>> pi
ans =
    3.1416
 $f_x$  >>
```

固定变量

```
Command Window
>> pi
ans =
    3.1416
>> z = i
```



固定变量

```
Command Window
>> pi
ans =
    3.1416
>> z = i
z =
    0.00 + 1.00i
 $f_x$  >>
```


固定变量

Command Window

```
>> pi
```

```
ans =
```

```
3.1416
```

```
>> z = i
```

```
z =
```

```
0.00 + 1.00i
```

```
>> x = 1/0
```

固定变量

```
Command Window
>> pi
ans =
    3.1416
>> z = i
z =
    0.00 + 1.00i
>> x = 1/0
x =
    Inf
 $f_x$  >>
```



固定变量

```
Command Window
>> pi
ans =
    3.1416
>> z = i
z =
    0.00 + 1.00i
>> x = 1/0
x =
    Inf
>> 0/0
```



固定变量

```
Command Window

>> pi
ans =
    3.1416

>> z = i
z =
    0.00 + 1.00i

>> x = 1/0
x =
    Inf

>> 0/0
ans =
    NaN

 $f_x$  >>
```



矩阵运算和数组运算



矩阵运算和数组运算

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
fx>>
```



矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
fx>>
```

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> C = A + B
```


矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> C = A + B
```

C =

```
     2     5     8  
    10    14     6  
     9    12    15
```

f_x >>

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> C = A + B  
  
C =  
     2     5     8  
    10    14     6  
     9    12    15  
  
>> D = A - B
```

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> C = A + B
```

C =

2	5	8
10	14	6
9	12	15

```
>> D = A - B
```

D =

0	-1	-2
-2	-4	6
5	4	03

f_x >>

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> C = A + B  
  
C =  
     2     5     8  
    10    14     6  
     9    12    15  
  
>> D = A - B  
  
D =  
     0    -1    -2  
    -2    -4     6  
     5     4    03  
  
>> clc
```

矩阵运算和数组运算



矩阵运算和数组运算

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
fx>>
```



矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
 $f_x$  >>
```

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> E = A * B
```


矩阵运算和数组运算

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> B = [1 3 5; 6 9 0; 2 4 6];
>> E = A * B

E =

    19    33    23
    46    81    56
    73   129    89

fx >>
```



矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> E = A * B  
  
E =  
  
    19    33    23  
    46    81    56  
    73   129    89  
  
>> F = A.* B
```

矩阵运算和数组运算

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> B = [1 3 5; 6 9 0; 2 4 6];
>> E = A * B

E =

    19    33    23
    46    81    56
    73   129    89

>> F = A.* B

F =

     1     6    15
    24    45     0
    14    32    54

f_x >>
```



矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> E = A * B  
  
E =  
  
    19    33    23  
    46    81    56  
    73   129    89  
  
>> F = A.* B  
  
F =  
  
     1     6    15  
    24    45     0  
    14    32    54  
  
>> clc
```



矩阵运算和数组运算



矩阵运算和数组运算

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
fx>>
```

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
fx>>
```

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> G = A / B
```



矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> G = A / B
```

G =

```
      0      0  0.50  
-3.00  0.00  3.50  
-6.00  0.00  6.50
```

f_x >>

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> G = A / B  
  
G =  
  
         0         0    0.50  
   -3.00    0.00    3.50  
   -6.00    0.00    6.50  
  
>> H = A ./ B
```

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> G = A / B
```

G =

```
      0      0  0.50  
-3.00  0.00  3.50  
-6.00  0.00  6.50
```

```
>> H = A ./ B
```

H =

```
 1.00  0.67  0.60  
 0.67  0.56  inf  
 3.50  2.00  1.50
```

f_x >>

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> G = A / B  
  
G =  
  
         0         0    0.50  
   -3.00    0.00    3.50  
   -6.00    0.00    6.50  
  
>> H = A ./ B  
  
H =  
  
    1.00    0.67    0.60  
    0.67    0.56    inf  
    3.50    2.00    1.50  
  
>> clc
```

矩阵运算和数组运算



矩阵运算和数组运算

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
fx>>
```

矩阵运算和数组运算

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> B = [1 3 5; 6 9 0; 2 4 6];
fx>>
```

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> I = A ^ 2
```


矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> I = A ^ 2
```

I =

30	36	42
66	81	96
102	126	150

f_x >>

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> I = A ^ 2  
  
I =  
  
    30    36    42  
    66    81    96  
   102   126   150  
  
>> J = A.^ 2
```

矩阵运算和数组运算

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> B = [1 3 5; 6 9 0; 2 4 6];
>> I = A ^ 2

I =

    30    36    42
    66    81    96
   102   126   150

>> J = A.^ 2

J =

     1     4     9
    16    25    36
    49    64    81

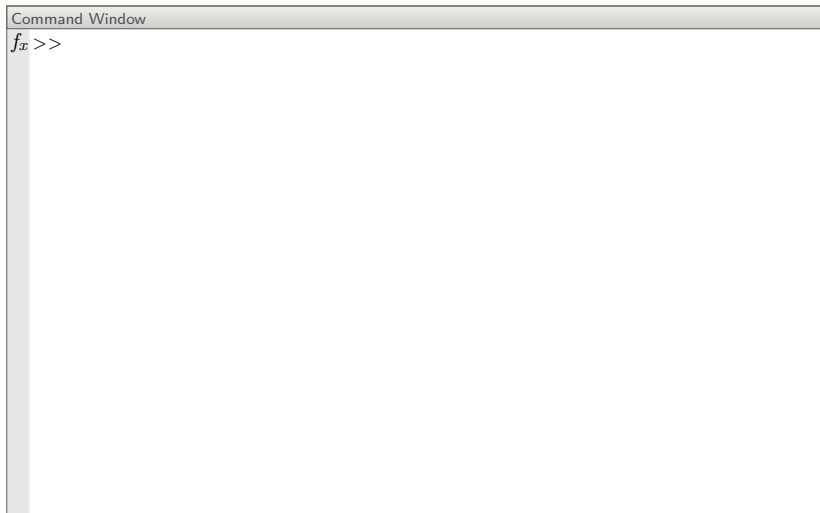
f_x>>
```

矩阵运算和数组运算

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = [1 3 5; 6 9 0; 2 4 6];  
>> I = A ^ 2  
  
I =  
  
    30    36    42  
    66    81    96  
   102   126   150  
  
>> J = A.^ 2  
  
J =  
  
     1     4     9  
    16    25    36  
    49    64    81  
  
>> clc
```

数组和数组行列块操作: 取值



数组和数组行列块操作: 取值

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
 $f_x$  >>
```

数组和数组行列块操作: 取值

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> x = A(1, 3)
```

数组和数组行列块操作: 取值

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> x = A(1, 3)

x =

    3

fx>>
```


数组和数组行列块操作: 取值

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> x = A(1, 3)  
  
x =  
  
    3  
  
>> y = A(2, :)
```

数组和数组行列块操作: 取值

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> x = A(1, 3)

x =

    3

>> y = A(2, :)

y =

    4    5    6

 $f_x$  >>
```

数组和数组行列块操作: 取值

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> x = A(1, 3)  
  
x =  
  
3  
  
>> y = A(2, :)  
  
y =  
  
4     5     6  
  
>> z = A(1:2, 1:3)
```

数组和数组行列块操作: 取值

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> x = A(1, 3)

x =

    3

>> y = A(2, :)

y =

    4    5    6

>> z = A(1:2, 1:3)

z =

    1    2    3
    4    5    6

f_x>>
```

数组和数组行列块操作: 赋值



数组和数组行列块操作: 赋值

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
 $f_x$  >>
```

数组和数组行列块操作: 赋值

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> A(1, 3) = 0
```

数组和数组行列块操作: 赋值

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> A(1, 3) = 0

A =

     1     2     0
     4     5     6
     7     8     9

fx>>
```


数组和数组行列块操作: 赋值

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];
```

```
>> A(1, 3) = 0
```

```
A =
```

```
    1    2    0  
    4    5    6  
    7    8    9
```

```
>> A(2, :) = [6 5 4]
```

数组和数组行列块操作: 赋值

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];
```

```
>> A(1, 3) = 0
```

A =

1	2	0
4	5	6
7	8	9

```
>> A(2, :) = [6 5 4]
```

A =

1	2	0
6	5	4
7	8	9

f_x >>

数组和数组行列块操作: 赋值

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> A(1, 3) = 0  
  
A =  
  
     1     2     0  
     4     5     6  
     7     8     9  
  
>> A(2, :) = [6 5 4]  
  
A =  
  
     1     2     0  
     6     5     4  
     7     8     9  
  
>> A(1:2, 1:2) = [-1 -2; -3 -4]
```

数组和数组行列块操作: 赋值

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];
```

```
>> A(1, 3) = 0
```

A =

1	2	0
4	5	6
7	8	9

```
>> A(2, :) = [6 5 4]
```

A =

1	2	0
6	5	4
7	8	9

```
>> A(1:2, 1:2) = [-1 -2; -3 -4]
```

A =

-1	-2	0
-3	-4	4
7	8	9

比较和逻辑运算



比较和逻辑运算

```
Command Window
>> x = [1 2 3 4 5 6 7 8 9];
fx>>
```

比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
 $f_x$  >>
```

比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
>> eq = (x==y)
```


比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
>> eq = (x==y)
```

eq =

1 0 1 0 0 0 1 0 1

f_x >>

比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
>> eq = (x==y)
```

```
eq =
```

```
1 0 1 0 0 0 1 0 1
```

```
>> xy = (x>5)&(y<7)
```

比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
>> eq = (x==y)
```

```
eq =
```

```
      1      0      1      0      0      0      1      0      1
```

```
>> xy = (x>5)&(y<7)
```

```
xy =
```

```
      0      0      0      0      0      1      0      1      0
```

f_x >>

比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
>> eq = (x==y)
```

eq =

```
1 0 1 0 0 0 1 0 1
```

```
>> xy = (x>5)&(y<7)
```

xy =

```
0 0 0 0 0 1 0 1 0
```

```
>> xoy = (x>5)|(y<7)
```

比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
>> eq = (x==y)
```

eq =

```
1 0 1 0 0 0 1 0 1
```

```
>> xy = (x>5)&(y<7)
```

xy =

```
0 0 0 0 0 1 0 1 0
```

```
>> xoy = (x>5)|(y<7)
```

xoy =

```
1 1 1 0 1 1 1 1 1
```

 f_x >>

比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
>> eq = (x==y)  
eq =  
      1      0      1      0      0      0      1      0      1  
>> xy = (x>5)&(y<7)  
xy =  
      0      0      0      0      0      1      0      1      0  
>> xoy = (x>5)|(y<7)  
xoy =  
      1      1      1      0      1      1      1      1      1  
>> xory = xor(x>5,y<7)
```



比较和逻辑运算

Command Window

```
>> x = [1 2 3 4 5 6 7 8 9];  
>> y = [1 4 3 8 6 5 7 2 9];  
>> eq = (x==y)  
eq =  
      1      0      1      0      0      0      1      0      1  
>> xy = (x>5)&(y<7)  
xy =  
      0      0      0      0      0      1      0      1      0  
>> xoy = (x>5)|(y<7)  
xoy =  
      1      1      1      0      1      1      1      1      1  
>> xory = xor(x>5,y<7)  
xory =  
      1      1      1      0      1      0      1      0      1
```

 f_x >>

比较和逻辑运算



比较和逻辑运算

```
Command Window
>> x = [1 -2 3 -4 5 -6 7 -8 9];
fx>>
```

比较和逻辑运算

Command Window

```
>> x = [1 -2 3 -4 5 -6 7 -8 9];  
>> x(x<0) = 0
```

比较和逻辑运算

```
Command Window
>> x = [1 -2 3 -4 5 -6 7 -8 9];
>> x(x<0) = 0
x =
    1     0     3     0     5     0     7     0     9
fx>>
```



比较和逻辑运算

Command Window

```
>> x = [1 -2 3 -4 5 -6 7 -8 9];
```

```
>> x(x<0) = 0
```

```
x =
```

```
1    0    3    0    5    0    7    0    9
```

```
>> y = [1 2 3;-4 5 6; 7 8 9];
```

f_x >>

比较和逻辑运算

Command Window

```
>> x = [1 -2 3 -4 5 -6 7 -8 9];
```

```
>> x(x<0) = 0
```

```
x =
```

```
1    0    3    0    5    0    7    0    9
```

```
>> y = [1 2 3;-4 5 6; 7 8 9];
```

```
>> y(y(:,1)<0,:) = 0
```

比较和逻辑运算

Command Window

```
>> x = [1 -2 3 -4 5 -6 7 -8 9];
```

```
>> x(x<0) = 0
```

```
x =
```

```
1    0    3    0    5    0    7    0    9
```

```
>> y = [1 2 3;-4 5 6; 7 8 9];
```

```
>> y(y(:,1)<0,:) = 0
```

```
y =
```

```
1    2    3
```

```
0    0    0
```

```
7    8    9
```

f_x >>

数组操作函数: flipud, fliplr, rot90



数组操作函数: flipud, fliplr, rot90

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
fx>>
```



数组操作函数: flipud, fliplr, rot90

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];  
>> B = flipud(A)
```

数组操作函数: flipud, fliplr, rot90

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];
```

```
>> B = flipud(A)
```

A =

7	8	9
4	5	6
1	2	3

f_x >>

数组操作函数: flipud, fliplr, rot90

Command Window

```
>> A = [1 2 3; 4 5 6; 7 8 9];
```

```
>> B = flipud(A)
```

```
A =
```

```
    7    8    9  
    4    5    6  
    1    2    3
```

```
>> C = rot90(A)
```



数组操作函数: flipud,fliplr, rot90

```
Command Window
>> A = [1 2 3; 4 5 6; 7 8 9];
>> B = flipud(A)

A =

     7     8     9
     4     5     6
     1     2     3

>> C = rot90(A)

C =

     3     6     9
     2     5     8
     1     4     7

 $f_x$  >>
```

数组操作函数: sum



数组操作函数: sum

```
Command Window
>> A = [1 2 3];
 $f_x$  >>
```

数组操作函数: sum

Command Window

```
>> A = [1 2 3];  
>> sum(A)
```

数组操作函数: sum

```
Command Window
>> A = [1 2 3];
>> sum(A)

ans =

    6

fx>>
```


数组操作函数: sum

```
Command Window
>> A = [1 2 3];
>> sum(A)

ans =

    6

>> B = [1 2 3; 4 5 6; 7 8 9];
fx >>
```



数组操作函数: sum

Command Window

```
>> A = [1 2 3];  
>> sum(A)  
  
ans =  
  
        6  
  
>> B = [1 2 3; 4 5 6; 7 8 9];  
>> sum(B)
```

数组操作函数: sum

```
Command Window
>> A = [1 2 3];
>> sum(A)

ans =

     6

>> B = [1 2 3; 4 5 6; 7 8 9];
>> sum(B)

ans =

    12    15    18

 $f_x$  >>
```

数组操作函数: sum

Command Window

```
>> A = [1 2 3];  
>> sum(A)  
  
ans =  
  
        6  
  
>> B = [1 2 3; 4 5 6; 7 8 9];  
>> sum(B)  
  
ans =  
  
    12    15    18  
  
>> sum(B,2)
```

数组操作函数: sum

```
Command Window
>> A = [1 2 3];
>> sum(A)

ans =

     6

>> B = [1 2 3; 4 5 6; 7 8 9];
>> sum(B)

ans =

    12    15    18

>> sum(B,2)

ans =

     6
    15
    25

fx>>
```

数组操作函数: max, min



数组操作函数: max, min

```
Command Window
>> A = [1 2 3];
fx>>
```

数组操作函数: max, min

Command Window

```
>> A = [1 2 3];  
>> max(A)
```


数组操作函数: max, min

```
Command Window
>> A = [1 2 3];
>> max(A)

ans =

    3

fx>>
```

数组操作函数: max, min

Command Window

```
>> A = [1 2 3];  
>> max(A)  
  
ans =  
  
     3  
>> max(A,2)
```

数组操作函数: max, min

```
Command Window
>> A = [1 2 3];
>> max(A)

ans =

     3

>> max(A,2)

ans =

     2     2     3

 $f_x$  >>
```

数组操作函数: max, min

```
Command Window
>> A = [1 2 3];
>> max(A)

ans =

     3

>> max(A,2)

ans =

     2     2     3

>> B = [1 3 9; 4 8 6];
fx>>
```

数组操作函数: max, min

Command Window

```
>> A = [1 2 3];  
>> max(A)  
  
ans =  
  
3  
  
>> max(A,2)  
  
ans =  
  
2 2 3  
  
>> B = [1 3 9; 4 8 6];  
>> max(B)
```

数组操作函数: max, min

```
Command Window
>> A = [1 2 3];
>> max(A)

ans =

     3

>> max(A,2)

ans =

     2     2     3

>> B = [1 3 9; 4 8 6];
>> max(B)

ans =

     4     8     9

 $f_x$  >>
```

数组操作函数: max, min

Command Window

```
>> A = [1 2 3];  
>> max(A)  
  
ans =  
  
3  
  
>> max(A,2)  
  
ans =  
  
2    2    3  
  
>> B = [1 3 9; 4 8 6];  
>> max(B)  
  
ans =  
  
4    8    9  
  
>> max(B, [], 2)
```

数组操作函数: max, min

Command Window

```
>> A = [1 2 3];  
>> max(A)  
  
ans =  
  
3  
  
>> max(A,2)  
  
ans =  
  
2    2    3  
  
>> B = [1 3 9; 4 8 6];  
>> max(B)  
  
ans =  
  
4    8    9  
  
>> max(B, [], 2)  
  
ans =  
  
9  
8
```


常用数学函数: sin, cos, tan, cot, asin, acos, atan, acot



常用数学函数: \sin , \cos , \tan , \cot , \arcsin , \arccos , \arctan , arccot

Command Window

```
>> x = 0:pi/6:pi;
```

常用数学函数: sin, cos, tan, cot, asin, acos, atan, acot

Command Window

```
>> x = 0:pi/6:pi;
```

```
x =
```

```
0.00 0.52 1.05 1.57 2.09 2.62 3.14
```

```
 $f_x$  >>
```

常用数学函数: sin, cos, tan, cot, asin, acos, atan, acot

Command Window

```
>> x = 0:pi/6:pi;
```

```
x =
```

```
0.00 0.52 1.05 1.57 2.09 2.62 3.14
```

```
>> y = sin(x)
```

常用数学函数: sin, cos, tan, cot, asin, acos, atan, acot

Command Window

>> x = 0:pi/6:pi;

x =

0.00 0.52 1.05 1.57 2.09 2.62 3.14

>> y = sin(x)

y =

0.00 0.50 0.87 1.00 0.87 0.50 0.00

 f_x >>

常用数学函数: sin, cos, tan, cot, asin, acos, atan, acot

Command Window

```
>> x = 0:pi/6:pi;  
x =  
    0.00    0.52    1.05    1.57    2.09    2.62    3.14  
>> y = sin(x)  
y =  
    0.00    0.50    0.87    1.00    0.87    0.50    0.00  
>> z = asin(y)
```

常用数学函数: sin, cos, tan, cot, asin, acos, atan, acot

Command Window

>> x = 0:pi/6:pi;

x =

0.00 0.52 1.05 1.57 2.09 2.62 3.14

>> y = sin(x)

y =

0.00 0.50 0.87 1.00 0.87 0.50 0.00

>> z = asin(y)

z =

0.00 0.52 1.05 1.57 2.09 2.62 3.14

 f_x >>

常用数学函数: abs, sqrt



常用数学函数: abs, sqrt

Command Window

```
>> x = [-4 9 -16 25];
```

常用数学函数: abs, sqrt

```
Command Window
>> x = [-4 9 -16 25];
x =
    -4     9   -16    25
fx >>
```

常用数学函数: abs, sqrt

Command Window

```
>> x = [-4 9 -16 25];
```

```
x =
```

```
    -4     9   -16    25
```

```
>> y = abs(x)
```

常用数学函数: abs, sqrt

```
Command Window
>> x = [-4 9 -16 25];
x =
    -4     9   -16    25
>> y = abs(x)
y =
     4     9    16    25
 $f_x$  >>
```

常用数学函数: abs, sqrt

Command Window

```
>> x = [-4 9 -16 25];
```

```
x =
```

```
    -4     9   -16    25
```

```
>> y = abs(x)
```

```
y =
```

```
     4     9    16    25
```

```
>> z = sqrt(y)
```

常用数学函数: abs, sqrt

Command Window

```
>> x = [-4 9 -16 25];
```

```
x =
```

```
    -4     9    -16    25
```

```
>> y = abs(x)
```

```
y =
```

```
     4     9    16    25
```

```
>> z = sqrt(y)
```

```
z =
```

```
     1     3     4     5
```

f_x >>

常用数学函数: ceil, fix, floor, round



常用数学函数: ceil, fix, floor, round

```
Command Window
>> x = [-1.6 -0.2 1.2 0.6];
fx>>
```


常用数学函数: ceil, fix, floor, round

Command Window

```
>> x = [-1.6 -0.2 1.2 0.6];  
>> y = ceil(x)
```

常用数学函数: ceil, fix, floor, round

Command Window

```
>> x = [-1.6 -0.2 1.2 0.6];
```

```
>> y = ceil(x)
```

```
y =
```

```
    -1     0     2     1
```

f_x >>

常用数学函数: ceil, fix, floor, round

Command Window

```
>> x = [-1.6 -0.2 1.2 0.6];  
>> y = ceil(x)  
y =  
    -1     0     2     1  
>> z = floor(x)
```

常用数学函数: ceil, fix, floor, round

Command Window

```
>> x = [-1.6 -0.2 1.2 0.6];
```

```
>> y = ceil(x)
```

```
y =
```

```
    -1     0     2     1
```

```
>> z = floor(x)
```

```
z =
```

```
    -2    -1     1     0
```

f_x >>

常用数学函数: ceil, fix, floor, round

Command Window

```
>> x = [-1.6 -0.2 1.2 0.6];  
>> y = ceil(x)  
y =  
    -1     0     2     1  
>> z = floor(x)  
z =  
    -2    -1     1     0  
>> g = fix(x)
```

常用数学函数: ceil, fix, floor, round

Command Window

```
>> x = [-1.6 -0.2 1.2 0.6];
```

```
>> y = ceil(x)
```

```
y =
```

```
    -1     0     2     1
```

```
>> z = floor(x)
```

```
z =
```

```
    -2    -1     1     0
```

```
>> g = fix(x)
```

```
g =
```

```
    -1     0     1     0
```

f_x >>

常用数学函数: ceil, fix, floor, round

Command Window

```
>> x = [-1.6 -0.2 1.2 0.6];  
>> y = ceil(x)  
y =  
    -1     0     2     1  
>> z = floor(x)  
z =  
    -2    -1     1     0  
>> g = fix(x)  
g =  
    -1     0     1     0  
>> f = round(x)
```

常用数学函数: ceil, fix, floor, round

Command Window

```
>> x = [-1.6 -0.2 1.2 0.6];
```

```
>> y = ceil(x)
```

```
y =
```

```
    -1     0     2     1
```

```
>> z = floor(x)
```

```
z =
```

```
    -2    -1     1     0
```

```
>> g = fix(x)
```

```
g =
```

```
    -1     0     1     0
```

```
>> f = round(x)
```

```
f =
```

```
    -2     0     1     1
```

f_x >>

基本语句

基本语句

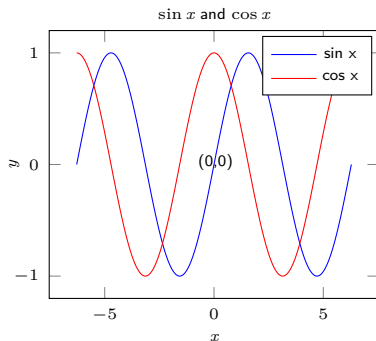
- `for .. end`
- `if .. else .. end`
- `while .. end`
- `switch .. case .. end`

举例: 求 1-10 以内的奇数和

```
1 % sum of the odd numbers between 1 and 10
2 x = 0;
3 for i = 1:10
4     if mod(i,2)
5         x = x + i;
6     end
7 end
```

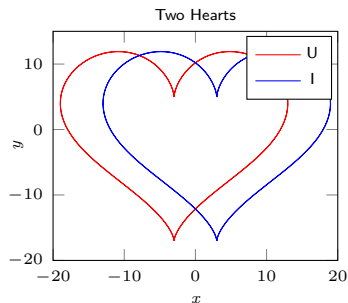
简单作图

```
1 x = -2*pi:0.1:2*pi;  
2 y1 = sin(x);  
3 y2 = cos(x);  
4 plot(x, y1, '-b');  
5 hold on  
6 plot(x, y2, '-r');  
7 xlabel('x')  
8 ylabel('y')  
9 text(0,0, '(0,0)')  
10 legend('sin x', 'cos x')
```



简单作图

```
1  t = 0:pi/180:4*pi;  
2  x = 16*sin(t).^3;  
3  y = 13*cos(t)-5*cos(2*t)...  
4      -2*cos(3*t)-cos(4*t);  
5  plot(x-3,y,'-r', x+3,y,'-b');  
6  xlabel('x');  
7  ylabel('y');  
8  axis([-20, 20, -20, 15]);  
9  title('Two Heart')  
10 legend('U', 'I')
```



简单作图

● 曲线图 plot: plot(x,y); plot(x,y,s), plot(x1,y1,s1,x2,y2,s2,...)

1	b	blue	.	point	-	solid
2	g	green	o	circle	:	dotted
3	r	red	x	x-mark	-.	dashdot
4	c	cyan	+	plus	--	dashed
5	m	magenta	*	star	(none)	no line
6	y	yellow	s	square		
7	k	black	d	diamond		
8	w	white	v	triangle (down)		
9			^	triangle (up)		
10			<	triangle (left)		
11			>	triangle (right)		
12			p	pentagram		
13			h	hexagram		



简单控制语句

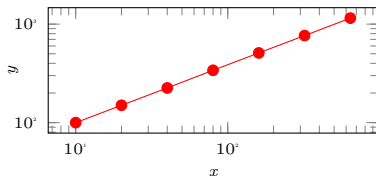
- title(图形名称)
- xlabel(x 轴说明); ylabel(y 轴说明)
- text(x,y, 图形说明)
- legend(图例 1, 图例 2, ...)
- grid on / grid off / grid minor
- axis([xmin xmax ymin ymax]), xlim([xmin, xmax])



其它坐标系

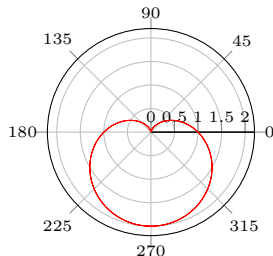
对数坐标: loglog, semilogx

```
1 x = 10*2.^[0:6];  
2 y = [100 150 225 340 ...  
3      510 765 1150];  
4 loglog(x,y,'.-r')  
5 xlim([0.5e1,0.8e3])  
6 ylim([0.8e2,1.4e3])  
7 xlabel('x'); ylabel('y')
```



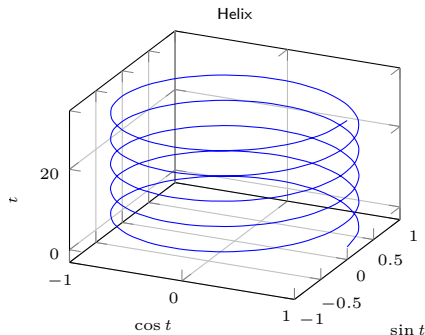
极坐标: polar

```
1 theta=0:pi/180:4*pi;  
2 r=1-sin(theta);  
3 polar(theta,r,'-r');
```



三维曲线图

```
1  t=0:pi/50:10*pi;  
2  x = sin(t);  
3  y = cos(t);  
4  z = t;  
5  plot3(x,y,z)  
6  title('Helix')  
7  xlabel('sin t')  
8  ylabel('cos t')  
9  zlabel('t')  
10 grid on
```



三维曲面图: 补充函数 meshgrid

Command Window

$f_x >>$

(1, 1)	(2, 1)	(3, 1)
(1, 2)	(2, 2)	(3, 2)
(1, 3)	(2, 3)	(3, 3)

2	1	2
1	0	1
2	1	2

$\sqrt{2}$	1	$\sqrt{2}$
1	0	1
$\sqrt{2}$	1	$\sqrt{2}$

三维曲面图: 补充函数 meshgrid

Command Window

```
>> [x, y] = meshgrid(1:3, 1:3)
```

x =

```
1 2 3
1 2 3
1 2 3
```

y =

```
1 1 1
2 2 2
3 3 3
```

f_x >>

(1, 1)	(2, 1)	(3, 1)
(1, 2)	(2, 2)	(3, 2)
(1, 3)	(2, 3)	(3, 3)

2	1	2
1	0	1
2	1	2

$\sqrt{2}$	1	$\sqrt{2}$
1	0	1
$\sqrt{2}$	1	$\sqrt{2}$

三维曲面图: 补充函数 meshgrid

Command Window

```
>> [x, y] = meshgrid(1:3, 1:3)
```

x =

```
1 2 3
1 2 3
1 2 3
```

y =

```
1 1 1
2 2 2
3 3 3
```

```
>> rsq = (x-2).^2 + (x-2).^2
```

rsq =

```
2 1 2
1 0 1
2 1 2
```

f_x >>

(1,1)	(2,1)	(3,1)
(1,2)	(2,2)	(3,2)
(1,3)	(2,3)	(3,3)

2	1	2
1	0	1
2	1	2

$\sqrt{2}$	1	$\sqrt{2}$
1	0	1
$\sqrt{2}$	1	$\sqrt{2}$

三维曲面图: 补充函数 meshgrid

Command Window

```
>> [x, y] = meshgrid(1:3, 1:3)
```

```
x =
```

```
1 2 3
1 2 3
1 2 3
```

```
y =
```

```
1 1 1
2 2 2
3 3 3
```

```
>> rsq = (x-2).^2 + (x-2).^2
```

```
rsq =
```

```
2 1 2
1 0 1
2 1 2
```

```
>> r = sqrt(rsq)
```

```
r =
```

```
1.4142 1.0000 1.4142
1.0000 0 1.0000
1.4142 1.0000 1.4142
```

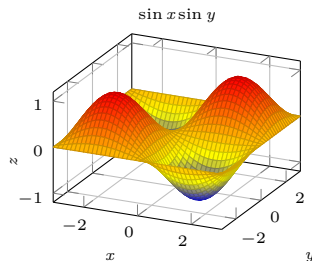
(1,1)	(2,1)	(3,1)
(1,2)	(2,2)	(3,2)
(1,3)	(2,3)	(3,3)

2	1	2
1	0	1
2	1	2

$\sqrt{2}$	1	$\sqrt{2}$
1	0	1
$\sqrt{2}$	1	$\sqrt{2}$

三维曲面图

```
1 [x,y] = meshgrid(-pi:0.1:pi);  
2 z = sin(x).*cos(y);  
3 mesh(x,y,z) % meshc(x,y,z)  
4 surf(x,y,z) % surfc(x,y,z)  
5 xlabel('x')  
6 ylabel('y')  
7 zlabel('z')  
8 title('sin x sin y')
```



M 函数格式

M 函数格式

```
1 function [output 1, ..] = functionname(input1, ..)
2 % comment of this function
3
4 MatLab command 1;
5 MatLab command 2;
```

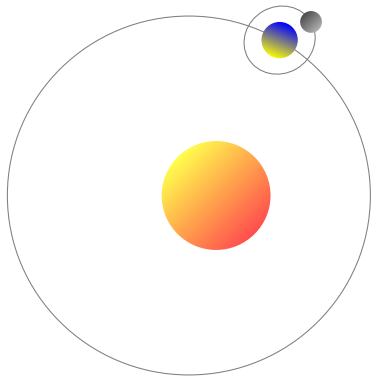
举例: 求矩形面积

```
1 function area = rectarea(L, W)
2 % rectarea Area of a rectangle
3 %
4 % rectarea(l, w) calculate the area of a rectangle
5 % with a length of L and a width of W
6
7 area = L .* W
```

Part II

MatLab 编程实例

多体问题



考虑多个天体的系统 (比如“日地月”三天体系统), 求各个天体的运动规律.

- 天体间的距离远大于天体的尺寸, 所有天体都视为质点.
- 每个天体有固定质量, 并给出初始位置和初始速度.
- 任意两天体之间只有万有引力的作用.

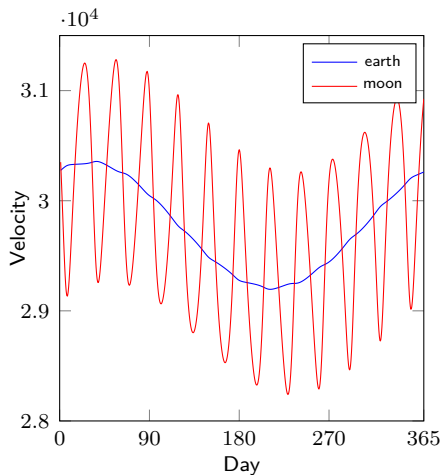
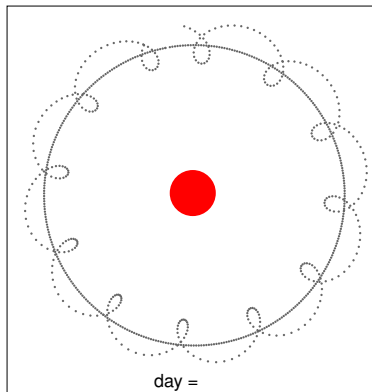
$$\mathbf{F}_{ij} = \frac{Gm_i m_j}{r_{ij}^2} \hat{\mathbf{r}}_{ij}$$

多体问题模拟程序

Matlab 程序: main.m

```
01 G = 6.67e-11; dt = 24*3600; N = 3;
02 M = [sun.mass      ; earth.mass      ; moon.mass      ];% N X 1
03 R = [sun.position; earth.position; moon.position];% N X 3
04 V = [sun.velocity; earth.velocity; moon.velocity];% N X 3
05 for t = 1:365
06     F = zeros(N,3);           % F(i,:) = [fx, fy, fz]
07     for i = 1 : N
08         mi = M(i); ri = R(i,:); % 第i个天体的质量和位置
09         for j = (i+1):N;
10             mj = M(j); rj = R(j,:);% 第j个天体的质量和位置
11             rij = rj - ri;
12             fij = G*mi*mj./(norm(rij).^3).*rij;% 万有引力
13             F([i,j],:) = F([i,j],:) + [fij; -fij];
14         end
15     end
16     V = V + F./repmat(M,1,3)*dt; % v(t+dt)=v(t)+a(t+dt)dt
17     R = R + V*dt;                % r(t+dt)=r(t)+v(t+dt)dt
18 end
```


多体问题模拟结果



Thank You!!!