LISA

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1 Monochromatic Sources

$$\begin{split} \Gamma_{ij} &= \frac{3}{4}S_a(f_0)^{-1} \sum_{\alpha=1:1} \int_{-\infty}^{\infty} \left[\partial_i A_a(t) \partial_j A_a(t) + A_a^2(t) \partial_i \chi_\alpha(t) \partial_j \chi_\alpha(t) \right] \, dt. \\ &A_a(t) &= 2\pi f_0 t + \varphi_0 + \varphi_{2,\alpha}(t) + \varphi_0(t), \\ &\varphi_{p,\alpha}(t) &= \arctan\left(\frac{A_a F_{s,\alpha}(t)}{A_4 F_{s,\alpha}(t)}\right), \\ &\varphi_{p}(t) &= \arctan\left(\frac{A_a F_{s,\alpha}(t)}{A_4 F_{s,\alpha}(t)}\right), \\ &\varphi_{p}(t) &= 2\pi f_0 t^{-1} R \sin \bar{\theta}_3 \cos \left[\bar{\phi}(t) - \bar{\phi}_3\right], \\ &A_4 &= 2\left(1 + [\cos \bar{\theta}_1 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\theta}_5 \cos (\bar{\phi}_1 - \bar{\phi}_5)\right)^2\right\}, \\ &A_4 &= -4e^{\ln A} \left[\cos \bar{\theta}_1 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\theta}_5 \cos (\bar{\phi}_1 - \bar{\phi}_5)\right]^2, \\ &A_5 &= -4e^{\ln A} \left[\cos \bar{\theta}_2 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\phi}_3 \cos 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5, \\ &F_{+,1}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \cos 2\phi_3 \sin 2\phi_5 - \cos \theta_3 \sin 2\phi_5 \cos 2\phi_3 \sin 2\phi_5, \\ &F_{+,11}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \sin 2\phi_5 \cos 2\phi_3 + \cos \theta_3 \sin 2\phi_5 \cos 2\phi_3 \sin 2\phi_5, \\ &F_{+,11}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \sin 2\phi_5 \cos 2\phi_3 \cos 2\phi_3 \cos 2\phi_3 \cos 2\phi_5 \cos$$

2 SMBH MERGERS 2

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$$\begin{split} \Gamma_{ij} &= 4 \sum_{n=1/3} \int_{0}^{1} \frac{\partial \tilde{h}_{ij}(f) \tilde{h}_{ij}(f)}{S_{ij}(f)} \, df, \\ \tilde{h}_{ij}(f) &= \frac{\sqrt{3}}{2} \lambda_{ij}(f) A f^{-1} u_{i}^{2} \theta^{2}(f) - \sigma_{ij} u_{i}^{2}(f) + \sigma_{ij}^{2}(f) - \sigma_{ij}^{2}(f), \\ \tilde{h}_{ij}(f) &= \frac{\sqrt{3}}{2} \lambda_{ij}(f) A f^{-1} u_{i}^{2} \theta^{2}(f) - \sigma_{ij}^{2}(f) + \delta_{ij}^{2} R_{ij}^{2}(f) - \delta_{ij}^{2}(f), \\ \tilde{h}_{ij}(f) &= 2\pi f h_{ii} - \phi_{ij} - \frac{\pi}{4} + \frac{3}{4} (8\pi f)^{-5/3} [M(1+z)]^{-5/3} \left\{ 1 + \frac{90}{2} \left(\frac{313}{36} + \frac{11}{4} v \right) [\pi M(1+z) f]^{2/3} - 4 (4\pi - \beta) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= 2\pi f h_{ii} - \phi_{ij} - \frac{\pi}{4} + \frac{3}{4} (8\pi f)^{-5/3} [M(1+z)]^{-5/3} \left\{ 1 + \frac{90}{2} \left(\frac{313}{36} + \frac{11}{4} v \right) [\pi M(1+z) f]^{2/3} - 4 (4\pi - \beta) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= 2\pi f h_{ii} - \phi_{ij} - \frac{\pi}{4} + \frac{3}{4} (8\pi f)^{-5/3} [M(1+z)]^{-5/3} \left\{ 1 + \frac{90}{2} \left(\frac{313}{36} + \frac{11}{4} v \right) [\pi M(1+z) f]^{2/3} - 4 (4\pi - \beta) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= 2\pi f h_{ii} - \phi_{ij} - \frac{\pi}{4} + \frac{3}{4} (8\pi f)^{-5/3} [M(1+z)]^{-5/3} \left\{ 1 + \frac{90}{2} \left(\frac{313}{36} + \frac{11}{4} v \right) [\pi M(1+z) f]^{2/3} - 4 (4\pi - \beta) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= 2\pi f h_{ii} - \phi_{ij} - \frac{\pi}{4} + \frac{3}{4} (8\pi f)^{-5/3} [M(1+z) f]^{-5/3} \left\{ 1 + \frac{3}{2} \left(\frac{31}{4} + \frac{11}{4} u \right) [\pi M(1+z) f]^{2/3} - 4 (4\pi - \beta) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= 2\pi f h_{ij} - \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-5/3} \left\{ 1 + \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-5/3} - 4 (4\pi - \beta) [\pi M(1+z) f] \right\}, \\ \psi_{ij}(f) &= \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-5/3} \left\{ 1 + \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-5/3} - \frac{\pi}{5} \left(\frac{\pi}{4} - \beta \right) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-2/3} - \frac{\pi}{5} \left(\frac{\pi}{4} - \beta \right) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-2/3} - \frac{\pi}{5} \left(\frac{\pi}{4} - \beta \right) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-2/3} + \left(\frac{\pi}{4} - \beta \right) [\pi M(1+z) f] \right\}, \\ \varphi_{ij}(f) &= \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-2/3} + \frac{\pi}{4} \left(\frac{\pi}{4} + \frac{\pi}{4} \right) [\pi M(1+z) f]^{-2/3} + \frac{\pi}{4} \left(\frac{\pi$$