LISA

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1 Monochromatic Sources

$$\begin{split} \Gamma_{ij} &= \frac{3}{4}S_a(f_0)^{-1} \sum_{\alpha=1:1} \int_{-\infty}^{\infty} \left[\partial_i A_a(t) \partial_j A_a(t) + A_a^2(t) \partial_i \chi_\alpha(t) \partial_j \chi_\alpha(t) \right] \, dt. \\ &A_a(t) &= 2\pi f_0 t + \varphi_0 + \varphi_{2,\alpha}(t) + \varphi_0(t), \\ &\varphi_{p,\alpha}(t) &= \arctan\left(\frac{A_a F_{s,\alpha}(t)}{A_4 F_{s,\alpha}(t)}\right), \\ &\varphi_{p}(t) &= \arctan\left(\frac{A_a F_{s,\alpha}(t)}{A_4 F_{s,\alpha}(t)}\right), \\ &\varphi_{p}(t) &= 2\pi f_0 t^{-1} R \sin \bar{\theta}_3 \cos \left[\bar{\phi}(t) - \bar{\phi}_3\right], \\ &A_4 &= 2\left(1 + [\cos \bar{\theta}_1 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\theta}_5 \cos (\bar{\phi}_1 - \bar{\phi}_5)\right)^2\right\}, \\ &A_4 &= -4e^{\ln A} \left[\cos \bar{\theta}_1 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\theta}_5 \cos (\bar{\phi}_1 - \bar{\phi}_5)\right]^2, \\ &A_5 &= -4e^{\ln A} \left[\cos \bar{\theta}_2 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\phi}_3 \cos 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5, \\ &F_{+,1}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \cos 2\phi_3 \sin 2\phi_5 - \cos \theta_3 \sin 2\phi_5 \cos 2\phi_3 \sin 2\phi_5, \\ &F_{+,11}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \sin 2\phi_5 \cos 2\phi_3 + \cos \theta_3 \sin 2\phi_5 \cos 2\phi_3 \sin 2\phi_5, \\ &F_{+,11}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \sin 2\phi_5 \cos 2\phi_3 \cos 2\phi_3 \cos 2\phi_3 \cos 2\phi_5 \cos$$

2 SMBH MERGERS 2

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$$\begin{split} \Gamma_{ij} &= 4 \sum_{i=1,1} \int_{0}^{f_{min}} \frac{\partial \tilde{h}_{\alpha}^{*}(f) \partial_{i}\tilde{h}_{\alpha}(f)}{S_{\alpha}(f)} \, \mathrm{d}f, \\ \tilde{h}_{\alpha}(f) &= \frac{\sqrt{3}}{2} \Lambda_{\alpha}(t) A f^{-7/8} e^{(\psi(f)-\varphi_{r_{i}}(t)+\pi n(t))}, \\ \Lambda_{\alpha}(t) &= \left[\Lambda_{i}^{2} f_{+,m}^{2}(t) + \Lambda_{x}^{2} f_{x,m}^{2}(t) \right]^{1/2}, \\ \Lambda_{\alpha}(t) &= \left[\Lambda_{i}^{2} f_{+,m}^{2}(t) + \Lambda_{x}^{2} f_{x,m}^{2}(t) \right]^{1/2}, \\ \Lambda &= (5/96)^{1/2} \pi^{-2/3} [M(1+z)]^{-8/3} \left\{ 1 + \frac{20}{9} \left(\frac{733}{336} + \frac{11}{4} \eta \right) [\pi M(1+z) f]^{2/3} - 4 \left(4\pi - \beta \right) [\pi M(1+z) f] \right\}, \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \arctan \left(\frac{A_{x} F_{x,n}(t)}{A_{x} F_{i,\alpha}(t)} \right), \\ \varphi_{p,\alpha}(t) &= \frac{1}{2} (1 + \cos \theta_{t} \cos \bar{\theta}_{t} + \sin \bar{\theta}_{t} \sin \bar{\theta}_{t} \cos (\bar{\phi}_{t} - \bar{\phi}_{t})], \\ \varphi_{p,\alpha}(t) &= \frac{1}{2} (1 + \cos^{2} \theta_{t}) \cos 2\phi_{p} \cos 2\phi_{p} \cos 2\phi_{p} \cos 2\phi_{p} \cos 2\phi_{p}. \\ F_{x,i}(\theta_{s},\phi_{s},\phi_{s}) &= \frac{1}{2} (1 + \cos^{2} \theta_{s}) \cos 2\phi_{s} \sin 2\phi_{s} \cos 2\phi_{s} \sin 2\phi_{s} \cos 2\phi_{s}. \\ F_{x,i}(\theta_{s},\phi_{s},\psi_{s}) &= \frac{1}{2} (1 + \cos^{2} \theta_{s}) \sin 2\phi_{s} \sin 2\phi_{s} \cos 2\phi_{s} \cos 2\phi_{s}. \\ F_{x,i}(\theta_{s},\phi_{s},\psi_{s}) &= \frac{1}{2} (1 + \cos^{2} \theta_{s}) \sin 2\phi_{s} \sin 2\phi_{s} \cos 2\phi_{s} \cos 2\phi_{s}. \\ F_{x,i}(\theta_{s},\phi_{s},\psi_{s}) &= \frac{1}{2} (1 + \cos^{2} \theta_{s}) \sin 2\phi_{s} \sin 2\phi_{s} \cos 2\phi_{s} \cos 2\phi_{s}. \\ F_{x,i}(\theta_{s},\phi_{s},\psi_{s}) &= \frac{1}{2} (1 + \cos^{2} \theta_{s}) \sin 2\phi_{s} \cos 2\phi_{s}. \\ \cos \theta_{s} \sin 2\phi_{s} \cos 2\phi_{s} \cos 2\phi_{s}. \\ \cos \theta_{s} &= \frac{1}{2} \cos \bar{\theta}_{s} - \frac{\sqrt{3}}{2} \sin \bar{\theta}_{s} \cos [\bar{\phi}(t) - \bar{\phi}_{s}] \right\}, \\ \varphi_{s} &= -\alpha_{s} + 2\pi t / T + \arctan \left\{ \sqrt{3} \frac{1}{36} + \frac{1}{4} \eta \right\} [\pi M(1 + z) f]^{2/3} - \frac{8}{5} (4$$