LISA

GasinAn

2022年1月18日

1 Monochromatic Sources

$$\begin{split} \Gamma_{ij} &= \frac{3}{4}S_a(f_0)^{-1} \sum_{\alpha=1:1} \int_{-\infty}^{\infty} \left[\partial_i A_a(t) \partial_j A_a(t) + A_a^2(t) \partial_i \chi_\alpha(t) \partial_j \chi_\alpha(t) \right] \, dt. \\ &A_a(t) &= 2\pi f_0 t + \varphi_0 + \varphi_{2,\alpha}(t) + \varphi_0(t), \\ &\varphi_{p,\alpha}(t) &= \arctan\left(\frac{A_a F_{s,\alpha}(t)}{A_4 F_{s,\alpha}(t)}\right), \\ &\varphi_{p}(t) &= \arctan\left(\frac{A_a F_{s,\alpha}(t)}{A_4 F_{s,\alpha}(t)}\right), \\ &\varphi_{p}(t) &= 2\pi f_0 t^{-1} R \sin \bar{\theta}_3 \cos \left[\bar{\phi}(t) - \bar{\phi}_3\right], \\ &A_4 &= 2\left(1 + [\cos \bar{\theta}_1 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\theta}_5 \cos (\bar{\phi}_1 - \bar{\phi}_5)\right)^2\right\}, \\ &A_4 &= -4e^{\ln A} \left[\cos \bar{\theta}_1 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\theta}_5 \cos (\bar{\phi}_1 - \bar{\phi}_5)\right]^2, \\ &A_5 &= -4e^{\ln A} \left[\cos \bar{\theta}_2 \cos \bar{\theta}_3 + \sin \bar{\theta}_5 \sin \bar{\phi}_3 \cos 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5 \sin 2\phi_5, \\ &F_{+,1}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \cos 2\phi_3 \sin 2\phi_5 - \cos \theta_3 \sin 2\phi_5 \cos 2\phi_3 \sin 2\phi_5, \\ &F_{+,11}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \sin 2\phi_5 \cos 2\phi_3 + \cos \theta_3 \sin 2\phi_5 \cos 2\phi_3 \sin 2\phi_5, \\ &F_{+,11}(\theta_3, \phi_3, \psi_3) &= \frac{1}{2}(1 + \cos^2 \theta_3) \sin 2\phi_5 \cos 2\phi_3 \cos 2\phi_3 \cos 2\phi_3 \cos 2\phi_5 \cos$$

2 SMBH MERGERS 2

2 SMBH Mergers

$$\begin{split} \Gamma_{ij} &= 4 \sum_{\alpha = 1,1} \int_{0}^{f_{max}} \frac{\partial \tilde{h}_{\alpha}(f) \partial_{\beta} \tilde{h}_{\alpha}(f)}{S_{\alpha}(f)} \, \mathrm{d}f, \\ \tilde{h}_{\alpha}(f) &= \frac{\sqrt{3}}{2} \Lambda_{\alpha}(t) A f^{-7/6} e^{4\beta (f) - \varphi_{\alpha} + (c) + \varphi_{\alpha}(t)}, \\ \Lambda_{\alpha}(t) &= [\Lambda_{+}^{2} F_{+,\alpha}^{2}(t) + \Lambda_{+}^{2} F_{+,\alpha}^{2}(c)]^{1/2}, \\ A_{\alpha}(t) &= [\Lambda_{+}^{2} F_{+,\alpha}^{2}(t) - \Lambda_{+}^{2} F_{+,\alpha}^{2}(c)]^{1/2}, \\ A_{\alpha}(t) &= [\Lambda_{+}^{2} F_{+,\alpha}^{2}(t) - \Lambda_{+}^{2} F_{+,\alpha}^{2}(c)]^{1/2}, \\ A_{\alpha}(t) &= 2\pi f t_{\alpha} + \frac{\pi}{4} \frac{3}{4} (8\pi f)^{-8/3} [M(1+z)]^{-8/3} \left\{ 1 + \frac{20}{9} \left(\frac{743}{336} + \frac{11}{4} \eta \right) [\pi M(1+z) f]^{2/3} - 4 \left(4\pi - \beta \right) [\pi M(1+z) f] \right\}, \\ \varphi_{\alpha}(t) &= \arctan \left(-\frac{\Lambda_{+} F_{+,\alpha}(t)}{2} \right), \\ \varphi_{\alpha}(t) &= 2\pi f t^{-1} R \sin \theta_{8} \cos (\tilde{\theta}_{t} t) - \tilde{\theta}_{8} \right], \\ \Lambda_{+} &= 1 + \left[\cos \tilde{\theta}_{t} \cos \tilde{\theta}_{8} + \sin \tilde{\theta}_{t} \sin \tilde{\theta}_{8} \cos (\tilde{\theta}_{t} t - \tilde{\theta}_{8})]^{2}, \\ \Lambda_{+} &= -2 \left[\cos \tilde{\theta}_{t} \cos \tilde{\theta}_{8} + \sin \tilde{\theta}_{t} \sin \tilde{\theta}_{8} \cos (\tilde{\theta}_{t} t - \tilde{\theta}_{8})]^{2}, \\ \Lambda_{+} &= -2 \left[\cos \tilde{\theta}_{t} \cos \tilde{\theta}_{8} + \sin \tilde{\theta}_{t} \sin \tilde{\theta}_{8} \cos (\tilde{\theta}_{t} t - \tilde{\theta}_{8})] \right], \\ F_{+,1}(\theta_{3}, \phi_{8}, \psi_{8}) &= \frac{1}{2} \left(1 + \cos^{2} \theta_{8} \right) \cos 2\phi_{8} \sin 2\phi_{8} - \cos \theta_{8} \sin 2\phi_{8} \sin 2\phi_{8} \cos 2\phi_{8}. \\ F_{+,11}(\theta_{3}, \phi_{8}, \psi_{8}) &= \frac{1}{2} \left(1 + \cos^{2} \theta_{8} \right) \sin 2\phi_{8} \cos 2\psi_{8} - \cos \theta_{8} \cos 2\phi_{8} \sin 2\psi_{8}. \\ F_{+,11}(\theta_{5}, \phi_{8}, \psi_{8}) &= \frac{1}{2} \left(1 + \cos^{2} \theta_{8} \right) \sin 2\phi_{8} \sin 2\phi_{8} - \cos \theta_{5} \cos 2\phi_{8} \sin 2\psi_{8}. \\ F_{+,11}(\theta_{5}, \phi_{5}, \psi_{8}) &= \frac{1}{2} \left(1 + \cos^{2} \theta_{8} \right) \sin 2\phi_{8} \sin 2\phi_{8} - \cos \theta_{5} \cos 2\phi_{8} \sin 2\psi_{8}. \\ F_{+,11}(\theta_{5}, \phi_{5}, \psi_{8}) &= \frac{1}{2} \left(1 + \cos^{2} \theta_{8} \right) \sin 2\phi_{8} \sin 2\phi_{8} - \cos \theta_{5} \cos 2\phi_{8} \sin 2\phi_{8}. \\ \cos \theta_{5} &= \frac{1}{2} \cos \theta_{5} - \frac{\sqrt{3}}{2} \sin \theta_{5} \cos \left[\tilde{\phi}(t) - \tilde{\phi}_{8}\right], \\ \phi_{8} &= \alpha_{9} + 2\pi t / T + \arctan \left\{ \frac{\sqrt{3} \cos \theta_{8} + \sin \theta_{8} \cos \left[\tilde{\phi}(t) - \tilde{\phi}_{8}\right]}{2 \sin \theta_{8} \sin \tilde{\theta}_{8} \sin \tilde{\theta}_{8} \sin \tilde{\phi}_{8} - \cos \theta_{8} \sin \tilde{\theta}_{8} \sin \tilde{\theta}_{8} \cos (\tilde{\phi}(t) - \tilde{\phi}_{8}) \right], \\ \phi_{8} &= \frac{1}{2} \cos \theta_{5} - \frac{\sqrt{3}}{2} \sin \tilde{\theta}_{8} \cos \tilde{\phi}_{8} - \cos \theta_{8} \sin \tilde{\theta}_{8} \sin \tilde{\phi}_{8} - \cos \theta_{8} \sin \tilde{\theta}_{8} \cos \tilde{\phi}(t) - \frac{\sqrt{3}}{2} (\cos \tilde{\theta}_{8} \sin \tilde{\theta}_{8} \cos \tilde{\phi}_{8}) \sin \tilde{\phi}_{8} - \cos \theta_{8} \sin \tilde{\phi}_{8} \cos \tilde{\phi}_{8}(t) - \frac{\sqrt{3}}{2} \left($$