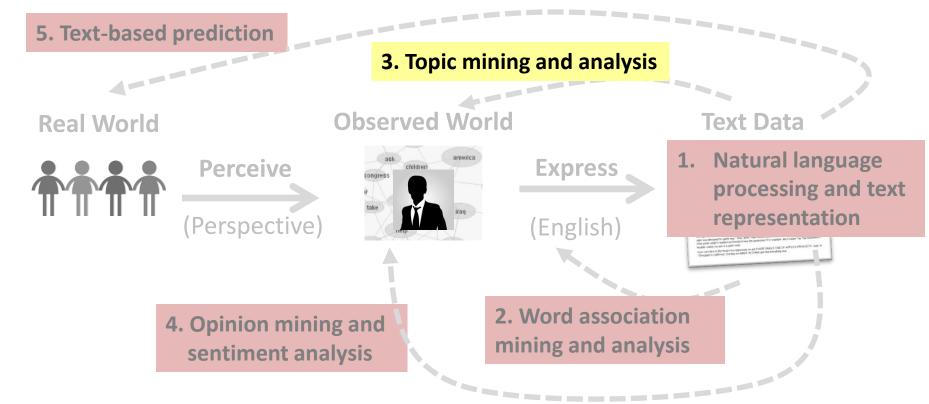
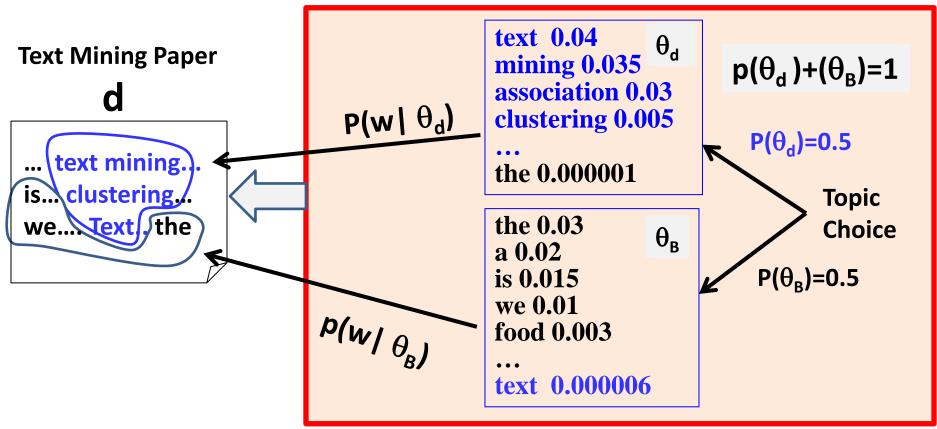
Probabilistic Topic Models: Mixture Model Estimation

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Back to Factoring out Background Words



Estimation of One Topic: $P(w \mid \theta_d)$

Adjust θ_d to maximize $p(d \mid \Lambda)$ text? θ_{d} (all other parameters are known) mining? $p(\theta_d) + (\theta_B) = 1$ association? Would the ML estimate demote clustering? background words in θ_d ? $P(\theta_d)=0.5$ the? **Topic** the 0.03 Choice θ_{B} a 0.02 ... text mining... $P(\theta_B)=0.5$ is 0.015 is... clustering... we 0.01 we.... Text.. the **food 0.003** text 0.000006

Behavior of a Mixture Model

Likelihood:

$$P(\text{"text"}) = p(\theta_d)p(\text{"text"} | \theta_d) + p(\theta_B)p(\text{"text"} | \theta_B)$$

$$= 0.5*p(\text{"text"} | \theta_d) + 0.5*0.1$$

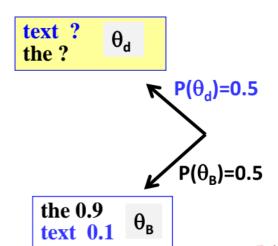
$$P(\text{"the"}) = 0.5*p(\text{"the"} | \theta_d) + 0.5*0.9$$

$$p(d | \Lambda) = p(\text{"text"} | \Lambda) p(\text{"the"} | \Lambda)$$

$$= [0.5*p(\text{"text"} | \theta_d) + 0.5*0.1] x$$

$$[0.5*p(\text{"the"} | \theta_d) + 0.5*0.9]$$

对学现图至4分积线.



How can we set $p(\text{"text"}|\theta_d) \& p(\text{"text"}|\theta_d)$ to maximize it?

Note that $p(\text{"text"} | \theta_d) + p(\text{"the"} | \theta_d) = 1$

tert在OB中把小根外等,要在Od中仍然

"Collaboration" and "Competition" of θ_d and θ_B

```
p(d|\Lambda)=p(\text{"text"}|\Lambda) p(\text{"the"}|\Lambda)
                                                                        d =
                                                                                    text the
           = [0.5*p("text" | \theta_d) + 0.5*0.1] x
             [0.5*p("the" | \theta_d) + 0.5*0.9]
                                                                              text?
                                                                                           \theta_{\text{d}}
                                                                              the?
      Note that p(\text{"text"} | \theta_d) + p(\text{"the"} | \theta_d) = 1
                                                                                                 \mathbb{R} P(\theta_d)=0.5
If x + y = constant, then xy reaches maximum when x = y.
                                                                                                      P(\theta_B)=0.5
0.5*p(\text{"text"} | \theta_d) + 0.5*0.1 = 0.5*p(\text{"the"} | \theta_d) + 0.5*0.9
                                                                                 the 0.9
                                                                                               \theta_{\mathsf{B}}
      \rightarrow p("text" | \theta_d)=0.9 >> p("the" | \theta_d) =0.1!
                                                                                 text 0.1
初省机制
   Behavior 1: if p(w1|\theta_B) > p(w2|\theta_B), then p(w1|\theta_d) < p(w2|\theta_d)
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Response to Data Frequency

```
p(d|\Lambda) = [0.5*p("text"|\theta_d) + 0.5*0.1]
d =
         text the
                                                x [0.5*p("the" | \theta_d) + 0.5*0.9]
                                   \rightarrow p("text" | \theta_d)=0.9 >> p("the" | \theta_d) =0.1!
                                     p(d'|\Lambda) = [0.5*p("text"|\theta_d) + 0.5*0.1]
         text the
                                                x [0.5*p("the" | \theta_d) + 0.5*0.9]
        the the
                                               x [0.5*p("the" | \theta_d) + 0.5*0.9]
                                               x [0.5*p("the" | \theta_d) + 0.5*0.9]
        the ...the
  What if we increase p(\theta_B)?
                                               x [0.5*p("the" | \theta_d) + 0.5*0.9]
 What's the optimal solution now? p("the" | \theta_d) > 0.1? or p("the" | \theta_d) < 0.1?
  Behavior 2: high frequency words get higher p(w|\theta_d)
```

Summary

- General behavior of a mixture model:
 - Every component model attempts to assign high probabilities to highly frequent words in the data (to "collaboratively maximize likelihood")
 - Different component models tend to "bet" high probabilities on different words (to avoid "competition" or "waste of probability")
 - The probability of choosing each component "regulates" the collaboration/competition between the component models
- Fixing one component to a background word distribution (i.e., background language model):
 - Helps "get rid of background words" in other component
 - Is an example of imposing a prior on the model parameters (prior = one model must be exactly the same as the background LM)

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