

Cryptography

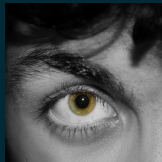
A (nearly) complete overview

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zenhack.it



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Table of Contents

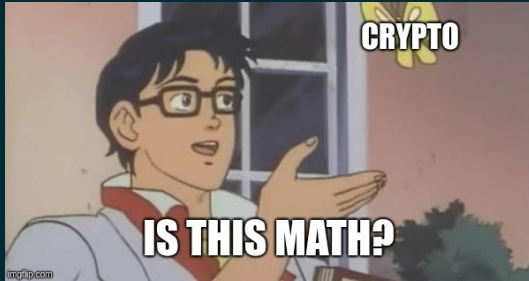
- ▶ 1. Introduction
- ▶ 2. Character encoding
- ▶ 3. Classical cryptography
- ▶ 4. Symmetric-key cryptography
- ▶ 5. Public-key cryptography
- ▶ 6. Key exchange
- ▶ 7. Hash function
- ▶ 8. Steganography

Table of Contents

- ▶ 1. **Introduction**
- ▶ 2. Character encoding
- ▶ 3. Classical cryptography
- ▶ 4. Symmetric-key cryptography
- ▶ 5. Public-key cryptography
- ▶ 6. Key exchange
- ▶ 7. Hash function
- ▶ 8. Steganography

Warning!

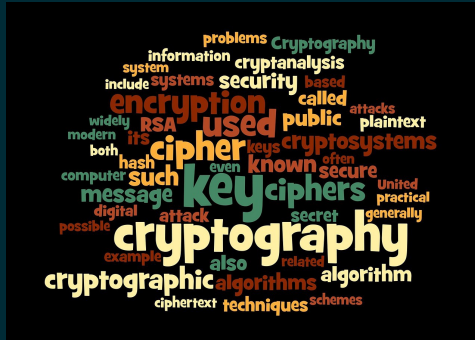
In this lesson we will use *math*!



It wasn't always like that though ...

Why cryptography?

Cryptography (from greek: kryptos "hidden, secret" and graphein, "to write")



The science of secure communication

Cryptography yesterday



(a) Caesar Cipher



(b) Scitala

Cryptography today

The needs, as well as the resources available, have evolved
and today we can divide cryptography into:

(EN|DE)CRYPTION

ASYMMETRIC (RSA, ECC, ...)

SYMMETRIC (DES, AES, ...)

KEY EXCHANGE

RSA, DH, ECDH, ...

AUTHENTICATION

RSA, DSA, ECDSA, ...

HASHING

MD5, SHA-1, SHA-256, ...

Table of Contents

- ▶ 1. Introduction
- ▶ 2. **Character encoding**
- ▶ 3. Classical cryptography
- ▶ 4. Symmetric-key cryptography
- ▶ 5. Public-key cryptography
- ▶ 6. Key exchange
- ▶ 7. Hash function
- ▶ 8. Steganography

What is a message?

A **message** is a sequence of symbols used to communicate

A symbol of the message is called **character**

The set of all the possible characters is called **alphabet**

The set of all the possible (meaningful) messages is called **dictionary**

ASCII encoding

ASCII = American Standard Code for Information Interchange
char encoded in 7 bit + 1 bit for check (parity bit).

ASCII (1977/1986)																
	_0	_1	_2	_3	_4	_5	_6	_7	_8	_9	_A	_B	_C	_D	_E	_F
0 0	NUL 0000	SOH 0001	STX 0002	ETX 0003	EOT 0004	ENQ 0005	ACK 0006	BEL 0007	BS 0008	HT 0009	LF 000A	VT 000B	FF 000C	CR 000D	SO 000E	SI 000F
1 16	DLE 0010	DC1 0011	DC2 0012	DC3 0013	DC4 0014	NAK 0015	SYN 0016	ETB 0017	CAN 0018	EM 0019	SUB 001A	ESC 001B	FS 001C	GS 001D	RS 001E	US 001F
2 32	SP 0020	! 0021	" 0022	# 0023	\$ 0024	% 0025	& 0026	' 0027	(0028) 0029	* 002A	+ 002B	, 002C	- 002D	. 002E	/ 002F
3 48	0 0030	1 0031	2 0032	3 0033	4 0034	5 0035	6 0036	7 0037	8 0038	9 0039	: 003A	; 003B	< 003C	= 003D	> 003E	? 003F
4 64	@ 0040	A 0041	B 0042	C 0043	D 0044	E 0045	F 0046	G 0047	H 0048	I 0049	J 004A	K 004B	L 004C	M 004D	N 004E	O 004F
5 80	P 0050	Q 0051	R 0052	S 0053	T 0054	U 0055	V 0056	W 0057	X 0058	Y 0059	Z 005A	[005B	\ 005C] 005D	^ 005E	_ 005F
6 96	` 0060	a 0061	b 0062	c 0063	d 0064	e 0065	f 0066	g 0067	h 0068	i 0069	j 006A	k 006B	l 006C	m 006D	n 006E	o 006F
7 112	p 0070	q 0071	r 0072	s 0073	t 0074	u 0075	v 0076	w 0077	x 0078	y 0079	z 007A	{ 007B	 007C	} 007D	~ 007E	DEL 007F
<div><div></div> Letter</div> <div><div></div> Number</div> <div><div></div> Punctuation</div> <div><div></div> Symbol</div> <div><div></div> Other</div> <div><div></div> undefined</div> <div><div></div> Changed from 1963 version</div>																

0, ..., 31 + 127 → non-printable chars (null, new line, tab, others)
32, ..., 126 → printable chars (letters, digits, punctuation, others)

Extended ASCII → char encoded in 8 bit (add 128 printable chars to standard ASCII)

Unicode encoding

Obviously 128 (or 256) characters are not enough!
(Chinese, cyrillic, greek alphabets, emojis...)

Different standards: UTF-8, UTF-16, UTF-32 and others

[illegible]

Currently assigned "only" 137993 characters

Morse code

(Audio) character encoding scheme used in (telegraph) telecommunication.

Each character is encoded using a combination of short and long signal.

A	• —	U	• • —
B	— • • •	V	• • • —
C	— • • — •	W	• — —
D	— • •	X	— • • —
E	•	Y	— • — —
F	• • — •	Z	— — • •
G	— — •		
H	• • • •		
I	• •		
J	• — — —		
K	— • — —	1	• — — — —
L	• — • •	2	• • — — —
M	— —	3	• • • — —
N	— •	4	• • • • —
O	— — —	5	• • • • •
P	• — — •	6	— • • • •
Q	— — • • —	7	— — • • •
R	• — •	8	— — — • •
S	• • •	9	— — — — •
T	—	0	— — — — —

Braille code

(Tactile) character encoding scheme used for visually impaired people.
Each character is encoded using a 2×3 rectangle with "raised dots".

a/1	b/2	c/3	d/4	e/5	f/6	g/7	h/8	i/9	j/0
k	l	m	n	o	p	q	r	s	t
u	v	x	y	z					w

Base64

Group message in blocks of 6 bits.

Advantage: encode all the ASCII chars in printable chars

source ASCII (if <128)	M						a						n					
source octets	77 (0x4d)						97 (0x61)						110 (0x6e)					
Bit pattern	0	1	0	0	1	1	0	1	0	1	1	0	0	0	1	0	1	1
Index	19						22						5					
Base64-encoded	T						W						F					
encoded octets	84 (0x54)						87 (0x57)						70 (0x46)					

Valore	ASCII	Valore	ASCII	Valore	ASCII	Valore	ASCII
0	A	16	Q	32	g	48	w
1	B	17	R	33	h	49	x
2	C	18	S	34	i	50	y
3	D	19	T	35	j	51	z
4	E	20	U	36	k	52	0
5	F	21	V	37	l	53	1
6	G	22	M	38	m	54	2
7	H	23	X	39	n	55	3
8	I	24	Y	40	o	56	4
9	J	25	Z	41	p	57	5
10	K	26	a	42	q	58	6
11	L	27	b	43	r	59	7
12	M	28	c	44	s	60	8
13	N	29	d	45	t	61	9
14	O	30	e	46	u	62	+
15	P	31	f	47	v	63	/

Message are padded with = (e.g. *flag* → *ZmxhZwo=*)

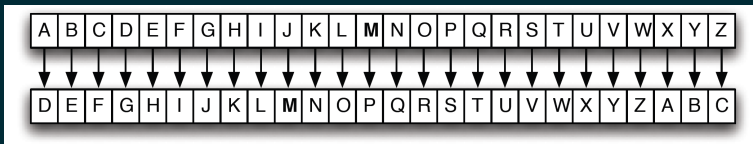
Table of Contents

- ▶ 1. Introduction
- ▶ 2. Character encoding
- ▶ 3. **Classical cryptography**
- ▶ 4. Symmetric-key cryptography
- ▶ 5. Public-key cryptography
- ▶ 6. Key exchange
- ▶ 7. Hash function
- ▶ 8. Steganography

Caesar cipher

Encrypt: right shift each letter of 3 positions

Decrypt: left shift each letter of 3 positions



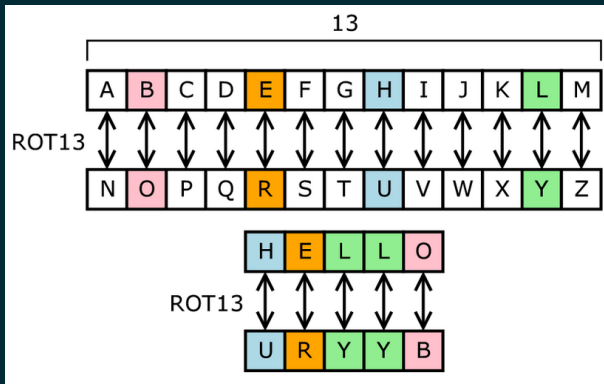
General cipher: shift letter of K positions

Attack: bruteforce all the possible K (only 26...)

ROT{13, 47}

ROT13: Caesar cipher with $K = 13$ on alphabetic dictionary

ROT47: Caesar cipher with $K = 47$ on printable ASCII chars (33 - 126).



Why $K = 13$ (or $K = 47$)? Because Encrypt = Decrypt

Classical ciphers

Substitution ciphers

Monoalphabetic ciphers: $C_{new} = P[C_{old}]$ (Where P is a dictionary permutation)
(ROT-K is a monoalphabetic cipher where P is a cyclic rotation of the alphabet)

Polialphabetic ciphers: multiple substitution alphabets (more than one dictionary permutation)

Transposition ciphers

Encryption systems where the positions held by units of plaintext (characters or groups of characters) are shifted according to a regular system.

E.g. We want to encrypt the message *WE ARE DISCOVERED. FLEE AT ONCE* using the **route cipher**:

Grid:

W	R	I	O	R	F	E	O	E
E	E	S	V	E	L	A	N	J
A	D	C	E	D	E	T	C	X

Cipher text: *EJXCTEDECDAEWRIORFEONALEVSE*

Substitution cipher: XXX

Transposition cipher: XXX

<https://www.dcode.fr/tools-list>



The screenshot displays the dcode.fr website interface. On the left, a search bar contains the text 'e.g. type scrabble' and a 'GO' button. Below it, the 'Results' section shows a list of tools found, including 'CTFCAESARCHIPER', 'PGSPNRFNEPUVCRE', 'NEQNLPLDLCNSTAPC', 'OFROMQEMDOTUBQD', 'EVHECGUCTEJKRGD', 'DUGDBFTBDSIJQFS', 'QHTQOSGOFQVWDSF', and 'RIURPTHGRWXETG'. On the right, the 'CAESAR CIPHER' tool is featured. It includes a 'Sponsored ads' section with a 'Caesar Cipher Decoder' link. Below this, there is a text input field containing 'FWI{fdhvdv_kdshu}'. The 'KNOWING THE SHIFT' section has a '-10' value entered. The 'TEST ALL POSSIBLE SHIFTS (BRUTE-FORCE ATTACK)' section is selected. A 'DECRYPT CAESAR CODE' button is present. The 'ROT Cipher' section is also visible, with a 'Shift Cipher' option selected. The 'With a custom alphabet' section has a text input field containing 'ABCDEFGHIJKLMNOPQRSTUVWXYZ'. The 'USE THE ASCII TABLE AS ALPHABET' checkbox is checked. A 'DECRYPT' button is located at the bottom of the section.

Almost all possible classic ciphers (old and new), encoder/decoder, ...

Cryptanalysis

Often the vulnerability is not in the algorithm but in its application...

- ▶ Bad use of the key (too short, reused, bad generated, ...)
- ▶ Messages use a poorly distributed dictionary
- ▶ We know the message format (e.g.: `FLAG{...}`)

In particular we talk about statistical cryptanalysis when we force the cipher not from algorithmic point of view but from statistical one

For example in english the character E has a frequency of 12.02% while Z only 0.07%

Useful tool (for substitution ciphers): <https://quipqiup.com>

Puzzle:	giuifg cei iprc tpnn du cei qprcni	
0	-0.842	defend the east wall of the castle
1	-0.859	defend the east ball of the castle
2	-0.915	defend the east mall of the castle

Attack models

Classification of cryptographic attacks:

- ▶ **Ciphertext-only** attack: access only to the ciphertext, and has no access to the plaintext
- ▶ **Known-plaintext** attack: access to at least a limited number of pairs of plaintext and the corresponding enciphered text
- ▶ **Chosen plaintext** attack: able to choose a number of plaintexts to be enciphered and have access to the resulting ciphertext (encrypt oracle)
- ▶ **Chosen ciphertext** attack: able to choose arbitrary ciphertext and have access to plaintext decrypted from it (decrypt oracle)
- ▶ **Side-channel** attack: use of other informations to break the cipher (time, sound, power, error, ...).

Table of Contents

- ▶ 1. Introduction
- ▶ 2. Character encoding
- ▶ 3. Classical cryptography
- ▶ 4. **Symmetric-key cryptography**
- ▶ 5. Public-key cryptography
- ▶ 6. Key exchange
- ▶ 7. Hash function
- ▶ 8. Steganography

Symmetric-key cryptography

Symmetric ciphers are those where messages are encrypted and decrypted using the same key, which must be known only and exclusively to the two parties

$\mathcal{C}(m, k) = c$ (encrypt function)

$\mathcal{D}(c, k) = m$ (decrypt function)

Obviously:

$\mathcal{D}(\mathcal{C}(m, k), k) = m$

The original message is not altered during the communication

E.g. In the caesar cipher:

$\mathcal{C}(m, k)$ = right shift of k positions each character

$\mathcal{D}(c, k)$ = left shift of k positions each character

Shannon principle

How to assess whether a cipher is robust enough?

(Where robustness means its probability of being successfully attacked)

Shannon defines two key concepts:

- ▶ **Confusion**: the key must be well distributed in the encrypted message (each bit of the cipher should depend on each bit of the key with probability 50%).
- ▶ **Diffusion**: the message must be well distributed in the encrypted message (each bit of the cipher should depend on each bit of the message with probability 50%).

In the Caesar cipher we have no kind of diffusion and low confusion (why?)

XOR cipher

Consider the XOR (exclusive or) operation \oplus , the following properties are valid:

- ▶ $0 \oplus 0 = 1 \oplus 1 = 0$
- ▶ $0 \oplus 1 = 1 \oplus 0 = 1$
- ▶ $x \oplus y \oplus y = x$

We define the XOR cipher as:

$$\mathcal{C}(m, k) = m \oplus k \quad (m[i] \oplus k[i], 0 \leq i < ||m||)$$

$$\mathcal{D}(c, k) = c \oplus k \quad (c[i] \oplus k[i], 0 \leq i < ||c||)$$

Problem: the key k could be shorter than the message m .

Solution: reuse the key as $k' = k \cdot k \cdot \dots \cdot k$ until $||k'|| \geq ||m||$.

Example:

$m = 01100011 \ 01101001 \ 01100001 \ 01101111$ (ciao in ASCII).

$k = 01111000 \ 01111000 \ 01111000 \ 01111000$ (x in ascii 4 times)

$c = 00011011 \ 00010001 \ 00011001 \ 00010111$ (non printable, GxEZFw== in b64)

One-time pad

The problem with the XOR cipher is that encrypting repeatedly reusing the same key can leak **statistical** informations of the original message

We call Vernam cipher (or one-time pad) a XOR cipher where the key has the same length of the message.

This cipher is called **perfect** because we have that:

$$P(M = m | C = c) = P(M = m)$$

The probability that M is a certain message m knowing that the cipher C is c is equal to the probability that M is a certain message not knowing the cipher (all messages are equiprobable, the encrypted message does not give us any information about the real message).

Nice in theory, but:

- ▶ The key must be exchanged using a secure method (exchange them by *hand*).
- ▶ The key must be generated randomly and not used (otherwise a many-time pad attack is possible).

Many-time pad & XorTool

Nice article: [the many time pad vulnerability](#)

XorTool: tool for statistical analysis of encrypted messages:

```
root@ddos:~/Desktop/xortool/xortool# xortool binary_xored
The most probable key lengths:
 1: 9.6%
 5: 15.0%
10: 21.7%
15: 9.3%
20: 13.6%
25: 6.0%
30: 9.1%
35: 4.2%
40: 6.6%
50: 5.0%
Key-length can be 5*n
Most possible char is needed to guess the key!
```

Knowing the initial part, we can see words in the message:

```
This is clas*****{*
Do not share*****}
{FLG:ch3ck_e*****
```

Going by trial the final flag is reconstructed:

```
This is classified*****
Do not share the s*****
{FLG:ch3ck_em@il}
```

Block vs Stream ciphers

Block ciphers

Stream ciphers

DES

AES

Padding a message (PKCS#5 & PKCS#7)

How to handle messages of length not multiple of the block size?

Idea: append "some chars" to the message (padding string)

PKCS#5:

The padding string PS shall consist of $8 - (||M|| \bmod 8)$ octets all having value $8 - (||M|| \bmod 8)$.

PKCS#7:

For such algorithms, the method shall be to pad the input at the trailing end with $k - (l \bmod k)$ octets all having value $k - (l \bmod k)$, where l is the length of the input.

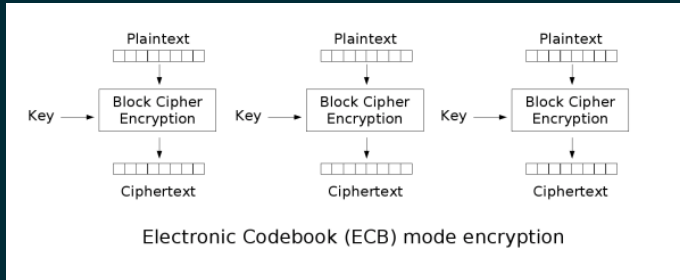
Why $8 - (||M|| \bmod 8)$ and not $(||M|| \bmod 8)$?

Block cipher mode of operation

ECB (Electronic Code Book)

The message is divided into blocks, and each block is encrypted/decrypted separately:

$$C_i = f(M_i, \text{Key})$$
$$M_i = f(C_i, \text{Key})$$

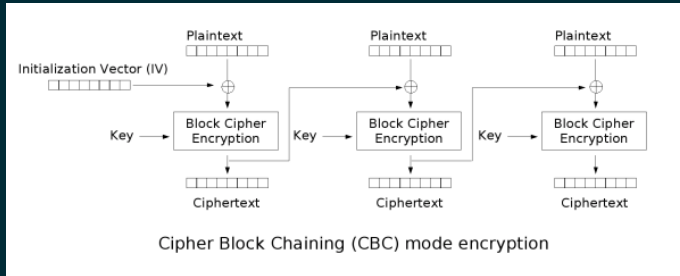


Problem: no diffusion, ECB encrypt same plaintext in same ciphertext

How to break ECB (padding-oracle attack)

CBC (Cipher Block Chaining)

In CBC each block of plaintext is XORed with the previous ciphertext block before being encrypted. An initialization vector is needed for the first block.



$$C_0 = IV$$

$$C_{i+1} = \mathcal{C}(M_i \oplus C_i, \text{Key})$$

$$M_{i+1} = \mathcal{D}(C_{i+1}, \text{Key}) \oplus C_i$$

How to break CBC (bit-flipping attack)

Stream cipher: LFSR

LFSR: Linear-Feedback Shift Registers