

# Translating PVS to C

## SRI International

Gaspard Férey

Ecole Polytechnique

September 1st, 2014

# Table of Contents

- 1 Context
- 2 Static analysis
  - The update issue
  - Reference tracking
  - Mutable analysis
- 3 The PVS Translator
  - Architecture
  - Implementation
- 4 Conclusion
  - Demonstration

# Table of Contents

## 1 Context

## 2 Static analysis

- The update issue
- Reference tracking
- Mutable analysis

## 3 The PVS Translator

- Architecture
- Implementation

## 4 Conclusion

- Demonstration

# What is PVS ?

## Prototype Verification System

- A specification language
  - ▶ Expressive syntax
  - ▶ Rich type system
    - ★ uninterpreted types
    - ★ abstract data types
    - ★ predicate subtypes
    - ★ etc
  - ▶ Parameterized theories
- A semi automated theorem prover
  - ▶ Higher order logic
  - ▶ Type system, type-correctness conditions, judgments, ...
  - ▶ Theorems, properties, ...
  - ▶ SMT solvers and other tools integrated
- A functional programming language (?)

# Why translate PVS ?

- To be able to execute PVS
  - ▶ Testing
  - ▶ Debugging
- To integrate high-insurance PVS code into systems

# Table of Contents

- 1 Context
- 2 Static analysis
  - The update issue
  - Reference tracking
  - Mutable analysis
- 3 The PVS Translator
  - Architecture
  - Implementation
- 4 Conclusion
  - Demonstration

# Update expression

- In functional programming languages,

$$E := A \text{ WITH } [(x) := y]$$

$$\text{refers } i \mapsto \begin{cases} A(i) & \text{if } i \neq x \\ y & \text{if } i = x \end{cases}$$

- In imperative languages
  - ▶  $A[x := y]$  a non destructive update using a copy of  $A$ .
  - ▶  $A[x \leftarrow y]$  a destructive, in-place update of the aggregate structure representing  $A$ .

# Two dangers

- Unsafe occurrence

`LET B = A WITH[(0) := 0] IN B(0) + A(0)`

The array represented by A is used later in the code.

- Trapped reference

`LET A = B(0) IN f( A WITH [(0) := 0], B(0) )`

B is affected by a destructive update of the array represented by A.



# Previous analysis

Shankar's analysis relies on sets of *variables*

- $Av$  active variables
- $Ov$  output variables
- $Fv$  free variables
- $Lv$  live variables in an *update context*

Cerny and Shankar's analysis adds *flow analysis*.

# The intermediate language

## Syntax

- Integers, nil pointer
- Variables ( $X, x, y, \dots$ )
- `newArray(x, y)`
- $X[x := y]$
- $X[x \leftarrow y]$
- $X[x]$
- `let  $x = a$  in  $e$`
- `if( $x$ )  $e_1$  else  $e_2$`
- `f( $x_1, \dots, x_n$ )`

## Memory state representation:

- Variables space  $Var$
- Reference space  $\mathcal{R}$
- Value space  $\mathcal{V} := \mathbb{N} \cup \mathcal{R}$
- Store  $R : \mathcal{R} \rightarrow \mathcal{V}$
- Stack  $S : Var \rightarrow \mathcal{V}$

## Evaluation context

- hole  $\{\}$
- `let  $x = \{\}$  in  $e$`
- $E_1\{E_2\}$

# The intermediate language

## Operational semantics

Simple reduction rules:

$$\begin{aligned} \langle x | R, S \rangle &\rightarrow \langle S(x) | R, S \rangle \\ \langle x[y] | R, S \rangle &\rightarrow \langle R(S(x))(S(y)) | R, S \rangle \\ \langle \text{if}(x) \ a \ \text{else} \ b | R, S \rangle &\rightarrow \begin{cases} \langle b | R, S \rangle & \text{if } S(x) = 0 \\ \langle a | R, S \rangle & \text{otherwise} \end{cases} \end{aligned}$$

Introducing variables

$$\begin{aligned} \langle f(x_1, \dots, x_n) | R, S \rangle &\rightarrow \langle \text{pop}([f]) | R, \left( \biguplus_{1 \leq i \leq n} f_i \mapsto S(x_i) \right) :: S \rangle \\ \langle \text{let } x = v \text{ in } e | R, S \rangle &\rightarrow \langle \text{pop}(e) | R, (x \mapsto v) :: S \rangle \\ \langle \text{pop}(v) | R, S \rangle &\rightarrow \langle v | R, \text{pop}(S) \rangle \end{aligned}$$

# The intermediate language

## Operational semantics

### Modifying the store

$$\langle \text{newArray}(x, y) \mid R, S \rangle \rightarrow \langle r \mid R \uplus (r \mapsto (S(y))_{0 \leq i < S(x)}) , S \rangle$$

where  $r$  is a fresh pointer

$$\langle X[x := y] \mid R, S \rangle \rightarrow \langle r \mid R', S \rangle$$

where  $r$  fresh pointer

$$\text{and } R' := R \uplus (r \mapsto A)$$

$$\text{and } A := R(S(X)) \uplus (S(x) \mapsto S(y))$$

$$\langle X[x \leftarrow y] \mid R, S \rangle \rightarrow \langle X \mid R', S \rangle$$

where  $R' := R \uplus (S(X) \mapsto A)$

$$\text{and } A := R(S(X)) \uplus (s(x) \mapsto S(y))$$

# Reference graph

For a context in the body of a function

```
f(A, B) =  
  let C = if(A[0] = 1) then A else B in  
  let D =  
    let E = C in E[0] := 0 in  
  D[0] + A(0)
```

we can define the reference graph  $\mathcal{G}(R)(r)$  as

$$\begin{aligned} r &\in \mathcal{G}(r) \\ \mathcal{R} \cap R(\mathcal{G}(r)) &\subset \mathcal{G}(r) \end{aligned}$$

We are interested in

$$\bigcup_R S^{-1}(\mathcal{G}(R)(S(x)))$$

# Reference graph

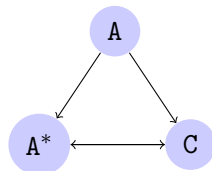
## Definition of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
           else X in  
  let G = F[0 := 0] in  
  let H = if B[0] then G  
           else B in  
  H[0 := B[0]]
```

# Reference graph

```
f(A, B) =  
  let C = A[0]      in  
  let D = { C }     in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
              else X in  
  let G = F[0 := 0] in  
  let H = if B[0] then G  
              else B in  
  H[0 := B[0]]
```

Reference graph



Variables lives in the context

$\{B, D, E, F, G, H, X\}$

Destructive update would impose too many requirements to  $f$ .

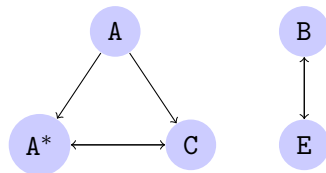
# Reference graph

## Definition of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = { E }     in  
  let F = if X[0] then D  
           else X in  
  let G = F[0 := 0] in  
  let H = if B[0] then G  
           else B in  
  H[0 := B[0]]
```

B is live in the context.

## Reference graph



Variables lives in the context

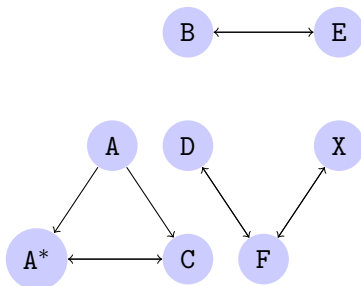
$\{B, C, D, F, G, H, X\}$



# Reference graph

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D else X in  
  
  let G = { F }      in  
  let H = if B[0] then G else B in  
  
  H[0 := B[0]]
```

## Reference graph



Variables lives in the context

$\{B, C, G, H\}$

Destructive update possible.

# Reference graph

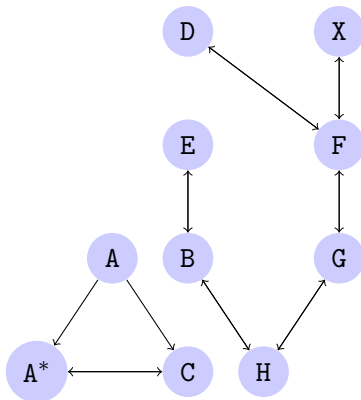
```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
           else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
           else B in  
  { H }
```

Variables lives in the context

{ }

Destructive update possible.

Reference graph



# The flags

We implement an approximation of the analysis using three flags

- **mutable**

- ▶ Variable: Every other variable that may point to that variable is not live.
- ▶ Argument: Variables passed as this argument must be flagged **mutable** and **safe** .
- ▶ Function: The result of a call to that function is "fresh" .

- **dupl**

- ▶ Argument: Possible active variable in a call to this function.
- ▶ Expression: May be active in the return value.

- **safe**

- ▶ Last of occurrence of a variable

# The rules

- Two versions for each function
  - ▶ destructive
  - ▶ non destructive
- Main loop
  - ▶ Flag variables **mutable**
  - ▶ Flag occurrences **safe**
  - ▶ Add destructive update or function calls
- Requirements
  - ▶ Flag arguments **duplicated**
  - ▶ Flag arguments **mutable**
  - ▶ Flag return value **mutable**

# Example

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
          else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
          else B in  
  H[0 <- 0]
```

# Example

C no flags

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
          else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
          else B in  
  H[0 <- 0]
```

# Example

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
          else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
          else B in  
  H[0 <- 0]
```

C no flags

D **mutable**

⇐ non destructive update

# Example

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
          else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
          else B in  
  H[0 <- 0]
```

C no flags

D **mutable**

⇐ non destructive update

E no flags



# Example

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
           else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
           else B in  
  H[0 <- 0]
```

C no flags

D **mutable**

⇐ non destructive update

E no flags

X **mutable**

⇐ non destructive update

# Example

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
           else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
           else B in  
  H[0 <- 0]
```

C no flags

D **mutable**

⇐ non destructive update

E no flags

X **mutable**

⇐ non destructive update

F **mutable** and **safe**

⇐ D and X **safe** and **mutable**

# Example

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
           else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
           else B in  
  H[0 <- 0]
```

C no flags

D **mutable**

⇐ non destructive update

E no flags

X **mutable**

⇐ non destructive update

F **mutable** and **safe**

⇐ D and X **safe** and **mutable**

G **mutable**

⇐ F **safe** and **mutable**

# Example

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
           else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
           else B in  
  H[0 <- 0]
```

C no flags

D **mutable**

⇐ non destructive update

E no flags

X **mutable**

⇐ non destructive update

F **mutable** and **safe**

⇐ D and X **safe** and **mutable**

G **mutable**

⇐ F **safe** and **mutable**

H **mutable** and **safe**

⇐ G and B **safe** and **mutable**

# Example

Destructive version of f

```
f(A, B) =  
  let C = A[0]      in  
  let D = C[0 := 0] in  
  let E = g(B)      in  
  let X = E[0 := 0] in  
  let F = if X[0] then D  
           else X in  
  let G = F[0 <- 0] in  
  let H = if B[0] then G  
           else B in  
  H[0 <- 0]
```

C no flags

D **mutable**

⇐ non destructive update

E no flags

X **mutable**

⇐ non destructive update

F **mutable** and **safe**

⇐ D and X **safe** and **mutable**

G **mutable**

⇐ F **safe** and **mutable**

H **mutable** and **safe**

⇐ G and B **safe** and **mutable**

⇒ Arguments B gets **mutable**

⇒ Return value gets **mutable**

# A reference counting GC

We complete the static analysis with a reference counting garbage collector (GC)

- Easy to implement in C (hashtable of pointers)
- Memory freed soon
- The reference count can allow safe update to be made destructive

# Table of Contents

- 1 Context
- 2 Static analysis
  - The update issue
  - Reference tracking
  - Mutable analysis
- 3 The PVS Translator
  - Architecture
  - Implementation
- 4 Conclusion
  - Demonstration

# Translation steps

- Typechecking: PVS typechecker
  - ▶ TCCs are generated
- Lexical and syntactic analysis: PVS lexer and parser
  - ▶ PVS  $\longrightarrow$  CLOS representation
- Translation:
  - ▶ CLOS representation  $\longrightarrow$  intermediate language



## Translation steps (2)

- Static analysis:
  - ▶ destructive updates added
- Optimizations: Several passes
  - ▶ Choosing C types
  - ▶ Declaring and freeing variables
- Code generation:
  - ▶ intermediate language  $\longrightarrow$  compilable C code

# Implementation details

- In Common Lisp
- Directly integrated to PVS (soon)
- Require the GMP library to run C code

# Table of Contents

- 1 Context
- 2 Static analysis
  - The update issue
  - Reference tracking
  - Mutable analysis
- 3 The PVS Translator
  - Architecture
  - Implementation
- 4 Conclusion
  - Demonstration

- Working compiler
  - ▶ Output C code compilable with gcc, CompCert (?)
  - ▶ Use GMP library to represent PVS big integers
- Promising analysis
- Optimization efficient (for simple programs)
  - ▶ 100 times faster than Ground Evaluator

# Left to be done

- More work on static analysis
  - ▶ Reference counting
  - ▶ Publication
- Less approximate implementation
- Debugging, optimizing Lisp code
- Wider subset of PVS
  - ▶ Closures
  - ▶ More types
  - ▶ ...

# Demonstration

## The program

- We compute the array  $T$

$$T(0) = 9876$$

$$T(i) = (12345 * T(i)) \bmod 59557 \quad \text{for } 0 < i < 10.000$$

- We sort  $T$  it using an insertion sort.

```
insert(A, i, v) =  
  if    i = 0 or v >= A[i-1]  
  then  A[i := v]  
  else  insert( A[i := A[i-1]], i-1, v)
```

```
sort(A, n) =  
  if    n = 100000  
  then  A  
  else  sort( insert(A, A[n], n), n+1 )
```

```
min(A) = sort(A, 0)[0]
```

- Complexity: time  $O(n^2)$  space  $O(n)$

# Questions ?

