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2.3.1 Parsing and typechecking PVS

These two task we leave to PVS native parser and typechecker.

The parser generates objects representing the expressions of the theory.

We only convert a subset of PVS. This subset is defined by a subset of expression objects we can translate. The objective is, of course, to be able to translate the maximum of (if not all) PVS expression objects.

2.3.2 Other translator

- Common Lisp (native) - Clean - Yices

3 Translating PVS Syntax

3.1 PVS Syntax

We describe here the syntax of PVS and the objects system used to represent them in Lisp. Some slots of the classes are voluntarily omitted. For a full description of PVS parser representation, refer to [5].

3.2 Translator architecture

Describe here the Lisp functions and data structures
Skeleton
Expected input
Output objects
Assertions that we (try to) maintain
Main steps :

- Typechecking: The PVS typechecker perform a type analysis on the PVS code to associate a PVS type to each expression. This might generates some proof obligations (TCC).

- Lexical and syntactic analysis: The PVS parser transforms PVS code into a Lisp internal representation.

- Translation: The translator generates a different representation from PVS expressions and functions declarations. Typically, an expression e is translated into a tuple of four elements (t, n, i, d), where t represents a C type used to describe the expression, n is a string representing the expression, i is a list of instructions supposed to be executed prior to using n (initialisation of n) and d is a list of instructions to be executed when n isn't needed anymore (destruction of n).

- Optimizations

Expr	::=	*Number*
	|	*Name*
	|	*Expr* *Arguments*
	|	*Expr* *Binop* *Expr*
	|	*Unaryop* *Expr*
	|	*Expr* ' { *Id* | *Number* }
	|	(*Expr*$^+_,$)
	|	(# *Assignment*$^+_,$ #)
	|	*IfExpr*
	|	LET *LetBinding*$^+_,$ IN *Expr*
	|	*Expr* WHERE *LetBinding*$^+_,$
	|	*Expr* WITH [*Assignment*$^+_,$]
Number	::=	*Digit*$^+$
Id	::=	*Letter* *IdChar*$^+$
IdChar	::=	*Letter* | *Digit*
Letter	::=	A | ... | Z
Digit	::=	O | ... | 9
Arguments	::=	(*Expr*$^+_,$)
IfExpr	::=	IF *Expr* THEN *Expr*
		{ ELSIF *Expr* THEN *Expr* } * ELSE *Expr* ENDIF
Name	::=	true | false | integer?
	|	floor | ceiling | rem | ndiv | even? | odd?
	|	cons | car | cdr | cons? | null | null?
	|	restrict | length | member | nth | append | reverse
Binop	::=	= | \= | OR | \/ | AND | & | /\
	|	IMPLIES | => | WHEN | IFF | <=>
	|	+ | - | * | / | < | <= | > | >=
Unaryop	::=	NOT | -
Assignment	::=	*AssignArg*$^+$ { := | |-> } *Expr*
AssignArg	::=	(*Expr*$^+_,$)
	|	' *Id*
	|	' *Number*
LetBinding	::=	{ *LetBind* | (*LetBind*$^+_,$) } = *Expr*
LetBind	::=	*Id* [: *TypeExpr*]

Figure 1: Syntax of the PVS subset of the translator

expr ⊂ syntax	*[abstract class]*
type the type of the expression	

name ⊂ syntax	*[mixin class]*
id . . . . the identifier	
actuals . . . . a list of actual parameters	
resolutions singleton	

This is a mixin for names, i.e., `name-expr`s, `type-name`s, etc.

name-expr ⊂ name expr	*[class]*

number-expr ⊂ expr	*[class]*
number a nonnegative integer	

tuple-expr ⊂ expr	*[class]*
exprs a list of expressions	

application ⊂ expr	*[class]*
operator an expr	
argument an expr (maybe a tuple-expr)	

field-application ⊂ expr	*[class]*
id . . . . identifier	
actuals . a list of actuals	
argument the argument	

A field application is the internal representation for record extraction, e.g., `r‘a`

record-expr ⊂ expr	*[class]*
assignments a list of assignments	

lambda-expr ⊂ binding-expr	*[class]*

This is the subclass of `binding-expr` used for LAMBDA expressions.

if-expr ⊂ application	*[class]*

When an application has an operator that resolves to the `if_def` it is changed to this class.

update-expr ⊂ expr	*[class]*
expression . an expr	
assignments a list of assignments	

An update expression of the form `e WITH [x := 1, y := 2]`, maps to an `update-expr` instance, where the `expression` is `e`, and the `assignments` slot is set to the list of generated `assigment` instances.

assignment ⊂ syntax	*[class]*
arguments . the list of arguments	
expression the value expression	

Assignments occur in both record-exprs and update-exprs.

The `arguments` form is a list of lists. For example, given the assignment `‘a(x, y)‘1 := 0`, the `arguments` are `((a) (x y) (1))` and the `expression` is `0`.

Figure 2: (Partial) CLOS representation of PVS expressions

- Code generation: C code is generated.

We first define a function T to translate an expression e.

$$T(e) = (\ T^t(e)\ ,\ T^n(e)\ ,\ T^i(e)\ ,\ T^d(e)\ )$$

$$
\begin{aligned}
T(2) \ &= (\ \texttt{int}, "2", [], []) \\
T(4294967296) \ &= (\ \texttt{mpz\_t},\ ?\ , \\
&\quad [\texttt{mpz\_init(?);}\ | \\
&\quad\ \ \texttt{mpz\_set\_str(?, "4294967296");}], \\
&\quad [\texttt{mpz\_clear(?);}]) \\
T(\texttt{lambda(x:below(10)):x}) \ &= (\ \texttt{int*},\ ?\ , \\
&\quad [?\ \ \texttt{= malloc(10 * sizeof(int));}\ | \\
&\quad\ \ \texttt{int i;} | \\
&\quad\ \ \texttt{for(i = 0; i < 10; i++)} \\
&\quad\ \ \ \ \texttt{?[i] = i;}] \\
&\quad [\texttt{free(?);}])
\end{aligned}
$$

Figure 3: Translation examples: number expressions

It may occur that $T^n(e) = ?$. In that case, the symbol ? appearing in $T^i(e)$ and $T^d(e)$ needs to be replaced by a proper variable name.

We then define two other operators:

- R wich take an expression and a type and may add an extra conversion in the instructions to make sure its result has the expected type. Also the result of this function has a proper name.

- S which take an expression, a type and a name. It makes sure that the given variable (type + name) is set to a value representing the expression.

3.3   A few translation rules

Translation rules :

```
number-expr "2"
(C-int, "2", [], [])

number-expr "12315468453213"
(C-mpz, nil,
       [mpz_t ~a; | mpz_t_init("12315468453213"); ],
       [mpz_clear ~a;])

application "f(e1, e2)"
(C-mpz, nil,
      [ instr(e1) | instr(e2)
                  | mpz(~a); | f(~a, e1, e2) ]
      [mpz_clear(~a);]
```

$$
\begin{array}{lll}
\textit{TypeExpr} & ::= & \textit{Name} \\
& | & \textit{EnumerationType} \\
& | & \textit{Subtype} \\
& | & \textit{TypeApplication} \\
& | & \textit{FunctionType} \\
& | & \textit{TupleType} \\
& | & \textit{CotupleType} \\
& | & \textit{RecordType} \\[4pt]
\textit{EnumerationType} & ::= & \texttt{\{ } \textit{IdOps} \texttt{ \}} \\[4pt]
\textit{Subtype} & ::= & \texttt{\{ } \textit{SetBindings} \texttt{ | } \textit{Expr} \texttt{ \}} \\
& | & \texttt{(} \textit{Expr} \texttt{)} \\[4pt]
\textit{TypeApplication} & ::= & \textit{Name Arguments} \\[4pt]
\textit{FunctionType} & ::= & [\,\texttt{FUNCTION} \mid \texttt{ARRAY}\,] \\
& & [\ -[\ \textit{IdOp}\ \texttt{:}\ ]\ \textit{TypeExpr}\ ^{\prime\prime}{}_{;}^{+}\ \texttt{->}\ \textit{TypeExpr}\ ] \\[4pt]
\textit{TupleType} & ::= & [\ -[\ \textit{IdOp}\ \texttt{:}\ ]\ \textit{TypeExpr}\ ^{\prime\prime}{}_{;}^{+}\ ] \\[4pt]
\textit{CotupleType} & ::= & [\ -[\ \textit{IdOp}\ \texttt{:}\ ]\ \textit{TypeExpr}\ ^{\prime\prime}{}_{+}^{+}\ ] \\[4pt]
\textit{RecordType} & ::= & \texttt{[\#}\ \textit{FieldDecls}^{+}_{;}\ \texttt{\#]} \\[4pt]
\textit{FieldDecls} & ::= & \textit{Ids}\ \texttt{:}\ \textit{TypeExpr}
\end{array}
$$

Figure 4: Fragment of the PVS type system

4 Types

4.1 PVS Types

A PVS theory can be typechecked using the emacs interface `M-x typecheck` or with Lisp function (`tc name-theory`). This first runs the PVS parser on the code and generates CLOS objects to represent it. Then, the PVS typechecker is run on this internal representation of the theory and tries to give a type to all expressions generating TCC when needed.

Here we describe how PVS types are represented in Lisp.

4.2 Translating types

PVS types:boolean, number, number_field, real, rational, integer, $A \to B$, restricted types below$(10) :=$ $\{x : \text{int}|0 \le x < 10\}$) enum datatype

This requires a type analysis to decide on the type of a PVS expression. For example the PVS `int` type can be represented by the `int`, `unsigned long` or `mpz_t` C types. In that case, we study the range of the expression to decide which types are allowed to represent it. Then we take the context in which the expression appears to decide. For instance in

```
incr(x:below(10)):int = x+1
```

the `x` expression, result of the function `incr` can always be represented by an `int` or `unsigned long` in C but we choose here to represent it using a `mpz_t`.

Auxiliary type system : C-type with a flag : mutable (meaning that the expression it describes only has one pointer pointing to it.

```
int a = 2;       a : int[mutable]
int* a = malloc( 10 * sizeof(int*) );
```

destructive addition:

```
type-expr ⊂ syntax                                                    [abstract class]
 ................................................................................................
type-name ⊂ type-expr name                                                    [class]
  adt

 ................................................................................................
subtype ⊂ type-expr                                                           [class]
  supertype
  predicate
 ................................................................................................
funtype ⊂ type-expr                                                           [class]
  domain
  range.
 ................................................................................................
tupletype ⊂ type-expr                                                         [class]
  types

 ................................................................................................
recordtype ⊂ type-expr                                                        [class]
  fields

 ................................................................................................
```

Figure 5: (Partial) CLOS representation of PVS types

```
d_add(*mpz_t res, mpz_t[mutable] a, long b) {
  mpz_add(a, a, b);
  (*res) = a;
}
```

Rq : d_add is given a mutable mpz_t, meaning that it can modify it and is responsible for freeing it. It is also responsible for allocating memory for the result. Here it uses the memory to assign res.

Use an auxiliary language :

```
( expr, C-type[mutable] )
```

Conversions and copies create mutables types (at a cost) : a[mutable]_from_b [2]

C types:[3]

```
// integer and floating point types
[unsigned] char, int, long, double
type*  //arrays
char*  // strings
struct types  // structures with fields
enum types
short int, float, union, size_t // etc...
```
Listing 1: C types

Translation rules :
We can only translate a subset of all PVS types. What's missing ?

4.3 Translating PVS syntax

We can only translate a subset of PVS syntax. What's missing ?

7

subrange(a, b)	```int // if small enough```
	```unsigned long // if too big or needed for function call```
	```mpz_t // else```

int	```mpz_t```
rat	```mpq_t```
[below(a) -> Type]	```(Ctype)*```

T : TYPE = [# x_i : t_i #]	```struct CT {```
	``` ...```
	``` Ct_i x_i;```
	``` ...```
	```}; // These types must be declared```

[Range -> Domain]	C closure parameterized by the ```Domain``` return type.

Figure 6: Translation rules for PVS types

4.4 Using a representation of the C language

5 Difficulties and successes

5.1 `if` expressions

Represented by `if-expr`

5.2 Integer, rationnals

In PVS, the `integer` represent the whole set $\mathbb{Z}$ of all relative numbers (and `rational` also describe $\mathbb{Q}$). In C, we have finite types int, long, ...

We need the GMP library which introduces the types `mpz_t` and `mpq_t`. These types are arrays and should be used just as integer (not as pointers except they still need to be freed).

5.3 Update expressions

Update expressions are represented by PVS as `update-expr` objects.

$$E := \texttt{ t with [e1 := e2]}$$

Problem : `t` is an expression typed as a function. Therefore it might be represented in C as an array (if domain type is `below(n)`. We want to know if we can update `t` in place to obtain a C object representing `E` or if we have to make a copy of `t`.

We consider three solutions to this problem.

5.3.1 Pointer counting

A first solution would be to keep track of the number of pointers pointing to an array or a struct. The idea is that if an array is referenced in several portions of the code (nested reference in other data structure, local variable in calling function, ...) then all update must be done non destructively to avoid inconsistency.

We implement a very simple "Reference Counting Garbage Collector" as described in [4].

We maintain a hashtable of pointer counters. Each pointer in the code is a key in the hastable to which we associate an int counter as value.

Pointers only occurs in arrays or struct.

Arrays are created in the code.

Expr	::=	*Number* | *String*
	|	*Variable*
	|	*Function* (*Exprs*)
	|	*Variable* . *Id*
	|	*Variable* [*Expr*]
Variable	::=	(*Type* , *Id*)
Instruction	::=	init(*Variable*)
	|	free(*Variable*)
	|	if (*Expr*) {
		Instructions
		}else {
		Instructions
		}
	|	*MPZFunction* (*Variable* [, *Exprs*])
	|	*Variable* = *Expr*
	|	define_array(*Variable* , *Expr*)
	|	copy(*Variable* , *Variable*)
	|	set(*Variable* , *Variable*)
	|	update(*Variable* , *Variable* , *Variable*)
Exprs	::=	[*Expr* [, *Exprs*]]
Variables	::=	[*Variable* [, *Variables*]]
Instructions	::=	[*Instruction* ; [*Instructions*]]
Function	::=	+ | * | ...
	|	*Id*
MPZFunction	::=	mpz_set_str | mpz_add | ...
FunctionDecl	::=	*Id* (*Variables*) -> *Type*
		Instructions

Figure 7: Syntax of the representation of the target language (subset of the C language)

`T* a = malloc(` `    10 * sizeof(int));`	`T* a = (T*) GC_malloc(10 * sizeof(int));` All memory allocation are handled by the GC to make sure every new reference on the heap is in the reference table and has a pointer counter.
`free(a);`	`GC_free(a);` This will decrement the reference counter on `a` and might free it if this counter is now 0.
`T* a = b;`	`T* a = (T*) GC( b );` The reference count on `b` is incremented to represent that the local variable `a` now also points to the structure `b` points to.

`t[0] = b;`	`GC_free( t[0] );`
	`t[0] = (T*) GC( b );`
	
	This time, we also make sure the reference counter of `t[0]` is decremented and `t[0]` has a chance to be freed if nothing else points to it.

Examples

```
int* f() {
  int* res;
  res = (int*) GC_alloc( 10 * sizeof(int) );
  [... init res...]
  return res; // pointer count = 1
}

void main() {
  int* a = f();  // pointer counter of a = 1
  int** b = (int**) GC_alloc( sizeof( int*) );
  GC_free( b[0] );  // useless
  b[0] = (int*) GC( a );  // pointer counter of a = 2
  printf("f(0) = %s", b[0][0]);
  GC_free(b); // frees b, pointer count of a = 1
  GC_free(a); // frees a
}
```

This requires to build our own C struct (heavy)

```
struct array_int {
  int pointer_count = 1;
  int *data;
};
```

When `A` points to an array (or `struct`) we want to update destructively, we first check if the pointer counter on `A` is 1. If so, we can update in place because only `A` points to the array.

However, we need to be carefull.

$$g(A:\texttt{Array}) : \texttt{ int = f(A, A WITH [(0) := 3])}$$

should not be translated to

```
g(int* A) {
  A[0] = 3;
  return f(A, A);
}
```

for two reasons:

- The variable `A` is updated destructively but it is later used as a reference to the previous value of the array.

- `f` is given twice a pointer to the same data structure. Its reference counter should be incremented.

Instead we could flatten the expression

```
g(int* A) {
  int* arg1 = GC(A);          // A and arg1 now both point to the array
  int* arg2 = update(A, 0, 3); // cannot be done destructively
  int* result = f(arg1, arg2);
  GC_free(A); // A function is responsible for freeing its arguments
              // (this is why we don't free arg1 and arg2)
  return result;
}
```

But again, we are lucky here that `A` is the first argument of `f`. If the updated `A` were the first arguments, the update would have been done destructively. This is why the GC alone is not enoug. We need an analysis of the C code to determine whether a variable is goingto be used later in the code or not. cf 5.3.5 Analysis of the C code.

5.3.2 Pros and cons

Every update require now tests and calls to hashtable functions (small compared to the copy it allows to avoid but no so small compared to a single in place update that could be decided by a code analysis)

Besides, the creation / destruction gets more complicated

Passing argument to function :

```
int* f(int* arg) {
   if ( GC_count(arg) == 1) {
      arg[0] = 3;
      return arg;
   } else {
      int* res;
      res = GC_malloc(10 * sizeof(int));
      int i;
      for(i = 0; i < 10; i++)
         res[i] = GC( arg[i] );
      GC_free(arg);
      res[0] = 3;
      return res;
   }
}
```

This add quite some code compared to the simple :

```
int* f(int* arg) {
   arg[0] = 0;
   return arg;
}
```

5.3.3 Using a different data structure

PVS uses arrays in a very particular way, we might then represent them with an other structure than just only a C array. For example :

```
struct r_list {
    int key;
    int value;
    r_list tl;
};
struct array_int {
    int *data;
    r_list replacement_list;
};
```

Each structure represent the array `data` with the modifications contained in the linked list `r_list_int`

Problems : Just as the previous solution : - add some extra code - add some extra computation (runtime tests, reading the replacement list) - require to create as many structures and associated functions as there are range types fo the manipulated arrays - Very dependent on the GC

5.3.4 Flow analysis on the PVS code

An other optimization would be to perform a analysis on the PVS variables to make sure an udate Pavol [1] suggests three analysis...

5.3.5 Analysis of the C code

Trying to avoid copying arrays by analyzing the C code generated.

Each PVS function is translated into two different C functions: a safe non destructive version which and a destructive version.

The destructive version of a function may have some requirements on the counter of tits arguments. Its arguments may be flagged as **mutable**, meaning that every call to this version of the function must make sure that the arguments passed can be safely destructively updated.

Example (stripped from GC instructions)

```
f(int* A, int* B) {
    if (A[0] == 0) {
        return B;
    } else {
        int* arg1 = copy(B);
        arg1[0] = arg1[0] - 1;
        f(arg1, A);
    }
}

f_d(int* A, int* B) {  // A and B are flagged mutable
    if (A[0] == 0) {
        return B;
    } else {
        int* arg1 = B;     // no need to copy since B is mutable
                           // and never occurs afterwards
        arg1[0] = arg1[0] - 1;
        f_d(arg1, A);
    }
}
```

Algorithm :

Always have a "non destructive" version of any function. A "cautious" version that never modify the arguments in place and always make copies when necessary (when a "mutable" version of an array is necessary (for instance updates)).

In destructive versions of all functions : Flag all array arguments to "mutable". Then for each of these arguments : - If it never occurs destructively, then remove flag (function just read the

arg) - If it occurs destructively, it can never occur at all AFTER. -¿ Need to define the order of evaluation of expression (easy rules on simple expressions) -¿ Need to be able to detect occurences of a name-expr -¿ Otherwise, unflag the arg

A variable V of type array is created in these cases:

- V = λx.e(x) : V has bang type

- update(V, T, key, value) : V has bang type because this is basically a copy and a destructive update.

- f(V,...) = ... : type of V depends on f.

In these case, it has always bang type.Or it can be set to an other referenced object.

- V = $T \rightarrow V$ (should have bang type iff T has !type too and never occurs afterwards). Happens in

- V = T[i] $\rightarrow$ depends on the target type of T.

- V = T.field $\rightarrow$ depends on the type of the field.

At first all updates are non destructive.

First pass : All array variables (actuals and local variables) found in the code are flagged. Local variables are flagged according to the previous rules and actuals are flagged **mutable** in destructive version and **not mutable** in non-destructive versions. In functions returning an array (or record type), the variable result is also flagged.

Other passes : Reading the code backwards, for every occurrence T of a variable flagged **mutable**:

- If it is found in a V = T instruction, then we give the bang type to V and remove bang type from T so that previous occurrences of T won't assume the uniqueness of the reference. This adds a new variable to the set of bang variables, hence the need to make several passes.

- If it is used in a V = copy(T) instruction, then we replace it with a V = T instruction and do as previous.

- If it is found in an update(V, T, i, e, then turn that into V = T; destr_update(V, i, e) .

- If it is a function call

- If we reach the declaration of a variable that is marked **mutable**, this means this variable is never read. In that case, we actually don't need it (unflag it I guess...).

At the end, when we have reached the transitive closure of this definition, if we reach the beginning of the function and some arguments are still bang, this means their bangness is never used, put the flag on that argument to **non mutable** and remove the instructions freeing that variable (reminder : mutable arguments of a functions are freed inside the function or are used in a mutable way and appear somewhere in the result (trapped in closures) or are freed in other function calls.

5.3.6 Algorithm

All variables have three flags: M (mutable), D (duplicated) and T (treated).

Init:All arguments of a destructive function are flagged (M = true, D = false, T = true).All arguments of a non destructive function are flagged (M = false, D = false, T = true).All other variables are flagged (M = false, D = false, T = false).

Rules:When M is changed, T is set to true.When T is true, the flag M can only be set to false. This prevent infinite change of the flag M.The flag D can only be set to true.

Initialization:

We initialize a set M of mutable variables to all array arguments of a function f. We also initialize a set F of variables to free to M since f has the resposnability to free all variables flagged as mutable arguments.

We read the code backwards.T_i refer to variables that are in the set M.S_i refer to variables that are not in the set M.

S = T	$M \leftarrow M \cup \{S\} - \{T\}$ $F \leftarrow F \cup \{S\} - \{T\}$
S = update(S_2, key, value)	$M \leftarrow M \cup \{S\}$ $F \leftarrow F \cup \{S\}$
S = update(T, key, value)	$M \leftarrow M \cup \{S\} - \{T\}$ $F \leftarrow F \cup \{S\}$
S = g(T_i, S_i)	If the arguments of g don't allow g to be called destructively: $M \leftarrow M - \{T_i\}$ $M \leftarrow M \cup \{S\}$ if return type of g is **mutable** $F \leftarrow F \cup \{S\}$
S = g(T_i, S_i)	Otherwise: $\rightarrow S$ = g_d(T_i, S_i $M \leftarrow M \cup \{S\} - \{T\}$ $F \leftarrow F \cup \{S\}$
S = S_2[i]	$M \leftarrow M \cup \{S\} - \{T\}$ $F \leftarrow F \cup \{S\}$

All arguments of the function are flagged **mutable**

What is a destructive occurence :

$$E := \texttt{f(t with [e1 := e2] , t(0))}$$

order of eval : e1 and e2 (t can occur non destr) t (expression of an update : destr) t(0) (occurence of t (even non destr))

`f(x:Arr):int = g( h(t), t)` is destructively translated to

```
1  int f_d(int* t) {    // t has type ! since this is destructive f
2    int* arg1 = h(t); // h can't be called destructively because
3                      // even though t is !, it appears later (line 4)
4    int* arg2 = t;     // t is ! and never appears later => arg2 is !
5    return g( arg1, arg2); // arg2 is ! but g can only be called
6  }                        // destructively if arg1 is
```

Listing 2: Example

if g has type `[Array!  -> ?]` then t can't be destructive

if g has type `[Array -> ?]` then t can be destructive

First algorithm:

Need multiple passes as the flags disappear

update(A, key, value)	A[key] = value;	A must be **mutable**
set(A, *expr*)	A = *expr*;	
declare(A, *expr(i)*)	```A = malloc(l * sizeof(T));int i;for(i = 0; i < l; i++) A[i] = i + 1;```	
copy(A, B)	```A = malloc(l * sizeof(T));int i;for(i = 0; i < l; i++) A[i] = B[i];```	
init(A)	int* A;	
free(A)	free(A);	
base(str, (A, B, ...))	int aux = A[0] + B[1];	A and B are only read.
return	return result;	

Figure 8: C instructions

value(*cste*)	42	
variable(*type*, *name*)	name	
call(f, *exprs*)	f($expr_1$, ..., $expr_n$)	

Figure 9: C expressions

5.3.7 Combination of solutions

We use the C code analysis to write some updates as destructive. However a few updates remain non destructive. For example:

If a function is called but requires its two argument to be **mutable** and only the first is **mutable**. Then the non-destructive version is called and the first argument gets copied even though it was **mutable**.

If we perform an update on T[i], our analysis doesn't tell if T[i] is **mutable** or **non-mutable**.

To prevent that, we also perform a GC check. An update is actually a test wether an object is **mutable** or not and the appropriate update.

6 Conclusion

6.1 What's left to be done ?

Use a C structure to represent a closure

```
struct r_list_int {
   int (*body)(void* env, void* args);
   void* env;
   void* args;
};
```

6.2   My stay at SRI

Besides the conception and implementation of the PVS to C compiler, my stay at SRI International was rich in ??? events.

The first days of my stay were the occasion to discover PVS anc Coq as I started working on a translator Coq to PVS. With Robin, we also wrote as an exercise a basic linear algebra library.

I discovered Lisp the hard way while learning how the back end of PVS worked. I've wrote a Lisp parser to help me see clear in the huge code (classes definitions, inheritances and organization, function dependances, ...)

I also have had the chance to attend to the many interesting seminars SRI hosted every week. The SRI also organized a Summer School to which we were allowed to attend and which was very interesting.

Shankar never hesitated to include us in many project

I've been included in the HACMS project which was very interesting. With other: Correcting translator PVS to SMT-LIB

Draft

Discovering PVS : Translating Coq proofs to PVS PVS library for basic linear algebra

Robin project, HACMS Contest week-end 14-15 June Summer School Parsing Lisp code -¿ generate HTML architecture fileCorrecting translator PVS to SMT-LIB [1]

References

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A   Rules

	B safe	B unsafe

B **mutable**	Replace every occurence of the variable A by the variable B	```c
		A = GC_malloc(...);
		for(i ...) {
		  A[i] = B[i]
		}
		``

B **non-mutable**	```c
	if (GC_count(B) == 1) {
	  A = B;
	} else {
	  A = GC_malloc(...);
	  for(i ...) {
	    A[i] = B[i]
	  }
	}
	``
		``c
		A = GC_malloc(...);
		for(i ...) {
		  A[i] = B[i]
		}
		``

Figure 10: Rules for `copy(A, B)`

	B safe	B unsafe

B **mutable**	Replace every occurence of the variable A by the variable B	```c
		A = GC_malloc(...);
		for(i ...) {
		  A[i] = B[i]
		}
		``

B **non-mutable**	Replace every occurence of the variable A by the variable B	```c
		A = GC(B);
		``

Figure 11: Rules for `set(A, B)`

B Examples

PVS code	Auxiliary language code	C code generated

`f(A:Arr):Arr = A`	```f: ((A, int*)) -> int*```
	 ```set(result, A)```
	 ```return(result)```
		```int* f(int* A) {```
		 ``` return A;```
		 ```}```

`f(A:Arr):Arr =`
 `   let B = A in B`
	```f: ((A, int*)) -> int*```
	 ```set(B, A)```
	 ```set(result, B)```
	 ```return(result)```
		```int* f(int* A) {```
		 ``` return A;```
		 ```}```

`f(A:Arr):Cint =`
 ` let B = A in`
 `  A(0) + B(0)`
	```f: ((A, int*)) -> int```
	 ```set(B, A)```
	 ```set(result, +(A(0), B(0)```
	 ```))```
	 ```return(result)```
		```int* f(int* A) {```
		 ``` int* B = (int*) GC(A);```
		 ``` int result = A[0] + B[0];```
		 ``` GC_free(B);```
		 ``` GC_free(A);```
		 ``` return result;```
		 ```}```

`f(A:Arr):Arr =`
 `   let B = A in`
 `    A WITH [(0) := B(0) ]`
	```f: ((A, int*)) -> int```
	 ```set(B, A)```
	 ```set(L, 0)```
	 ```set(R, B(0))```
	 ```update(result, A, L, R)```
	 ```return(result)```
		```int* f_d(int* A) {```
		 ``` int* B = GC_malloc(...);```
		 ``` for(i ...)```
		 ``` B[i] = A[i];```
		 ``` int L = 0;```
		 ``` int R = B[0];```
		 ``` int* result = GC(A);```
		 ``` result[L] = R;```
		 ``` GC_free(B);```
		 ``` GC_free(A);```
		 ``` return result;```
		 ```}```

Figure 12: Examples of setting variables

PVS code	Auxiliary language code	C code generated
```\nf(A:Arr):Arr =\n A WITH [(0) := 0]\n```	```\nf: ((A, int*)) -> int*\nset(L, 0)\nset(R, 0)\ncopy(result, A)\nupdate(result, L, R)\nreturn(result)\n```	```c\nint* f(int* A) {\n int L = 0, R = 0;\n int* result;\n if(GC_count(A) == 1) {\n result = GC(A);\n } else {\n result = GC_alloc(...);\n for(i ...)\n result[i] = A[i];\n }\n result[L] = R;\n GC_free(A);\n return result;\n}\n\nint* f_d(int* A) {\n int L = 0, R = 0;\n A[L] = R;\n return A;\n}\n```
```\nf(A:Arr):Arr =\n let B = A WITH[(0):=0]\n in A WITH[(0) := B(0)]\n```	```\nf: ((A, int*)) -> int*\nset(L1, 0)\nset(R1, 0)\ncopy(B, A)\nupdate(B, L1, R1)\nset(L2, 0)\nset(R2, B(0))\ncopy(result, A)\nupdate(result, L1, R1)\nreturn(result)\n```	```c\nint* f(int* A) {\n int R1 = 0, L1 = 0;\n B = GC_alloc(...);\n for(i ...)\n B[i] = A[i];\n B[L1] = R1;\n int R2 = 0, L2 = B[0];\n result = GC_alloc(...);\n for(i ...)\n result[i] = A[i];\n result[L2] = R2;\n GC_free(A);\n GC_free(B);\n return result;\n}\n\nint* f_d(int* A) {\n int R1 = 0, L1 = 0;\n B = GC_alloc(...);\n for(i ...)\n B[i] = A[i];\n B[L1] = R1;\n int R2 = 0, L2 = B[0];\n A[L2] = R2;\n GC_free(B);\n return A;\n}\n```

Figure 13: Examples of copying variables