

# Ayudamemoria

My room is random Sorted

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## 1 Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 #define forr(i, a, b) for (int i = int(a); i < int(b); i++)
5 #define forn(i, n) forr(i,0,n)
6 #define dforr(i, a, b) for (int i = int(b)-1; i >= int(a); i--)
7 #define dforn(i, n) dforr(i,0,n)
8 #define all(v) begin(v),end(v)
9 #define sz(v) (int(size(v)))
10 #define pb push_back
11 #define fst first
12 #define snd second
13 #define mp make_pair
14 #define endl '\n'
15 #define dprint(v) cout << #v " = " << v << endl
16
```

```

17 typedef long long ll;
18 typedef pair<int, int> pii;
19
20 int main() {
21     ios::sync_with_stdio(0); cin.tie(0);
22 }

```

### 1.1 run.sh

```

1 clear
2 make -s $1 && ./ $1 < $2

```

### 1.2 comp.sh

```

1 clear
2 make -s $1 2>&1 | head -$2

```

### 1.3 Makefile

```

1 CXXFLAGS = -std=gnu++2a -O2 -g -Wall -Wextra -Wshadow -Wconversion
  \
2 -fsanitize=address -fsanitize=undefined

```

## 2 Estructuras de datos

### 2.1 Sparse Table

```

1 #define oper min
2 int st[K][1<<K]; int n; // K such that 2^K > n
3 void st_init(vector<int> a){
4     forn(i,n) st[0][i]=a[i];
5     forr(k,1,K) forn(i,n-(1<<k)+1)
6         st[k][i]=oper(st[k-1][i], st[k-1][i+(1<<(k-1))]);
7 }
8 int st_query(int s, int e){
9     int k=31-__builtin_clz(e-s);
10    return oper(st[k][s], st[k][e-(1<<k)]);
11 }

```

### 2.2 Segment Tree

```

1 // Dado un array y una operacion asociativa con neutro, get(i, j)
  opera en [i, j)
2 #define MAXN 100000
3 #define oper(x, y) max(x, y)
4 const int neutro=0;
5 struct RMQ{
6     int sz;
7     tipo t[4*MAXN];
8     tipo &operator[](int p){return t[sz+p];}
9     void init(int n){ // O(n lg n)
10         sz = 1 << (32-__builtin_clz(n));
11         forn(i, 2*sz) t[i]=neutro;
12     }
13     void updall(){dforn(i, sz) t[i]=oper(t[2*i], t[2*i+1]);} //
      O(N)
14     tipo get(int i, int j){return get(i, j, 1, 0, sz);}
15     tipo get(int i, int j, int n, int a, int b){ // O(lg n)
16         if(j<=a || i>=b) return neutro;
17         if(i<=a && b<=j) return t[n];
18         int c=(a+b)/2;
19         return oper(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
20     }
21     void set(int p, tipo val){ // O(lg n)
22         for(p+=sz; p>0 && t[p]!=val;){
23             t[p]=val;
24             p/=2;
25             val=oper(t[p*2], t[p*2+1]);
26         }
27     }
28 }rmq;
29 // Usage:
30 cin >> n; rmq.init(n); forn(i, n) cin >> rmq[i]; rmq.updall();

```

### 2.3 Segment Tree Lazy

```

1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j)
  opera sobre el rango [i, j).
2 typedef int Elem; //Elem de los elementos del arreglo
3 typedef int Alt; //Elem de la alteracion
4 #define operacion(x,y) x+y

```

```

5  const Elem neutro=0; const Alt neutro2=0;
6  #define MAXN 100000
7  struct RMQ{
8      int sz;
9      Elem t[4*MAXN];
10     Alt dirty[4*MAXN];//las alteraciones pueden ser de distinto
        Elem
11     Elem &operator[](int p){return t[sz+p];}
12     void init(int n){//O(nlgn)
13         sz = 1 << (32-__builtin_clz(n));
14         forn(i, 2*sz) t[i]=neutro;
15         forn(i, 2*sz) dirty[i]=neutro2;
16     }
17     void push(int n, int a, int b){//propaga el dirty a sus hijos
18         if(dirty[n]!=0){
19             t[n]+=dirty[n]*(b-a);//altera el nodo
20             if(n<sz){
21                 dirty[2*n]+=dirty[n];
22                 dirty[2*n+1]+=dirty[n];
23             }
24             dirty[n]=0;
25         }
26     }
27     Elem get(int i, int j, int n, int a, int b){//O(lgn)
28         if(j<=a || i>=b) return neutro;
29         push(n, a, b);//corrige el valor antes de usarlo
30         if(i<=a && b<=j) return t[n];
31         int c=(a+b)/2;
32         return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c,
33             b));
34     }
35     Elem get(int i, int j){return get(i,j,1,0,sz);}
36     //altera los valores en [i, j) con una alteracion de val
37     void alterar(Alt val, int i, int j, int n, int a, int
38         b){//O(lgn)
39         push(n, a, b);
40         if(j<=a || i>=b) return;
41         if(i<=a && b<=j){
42             dirty[n]+=val;
43             push(n, a, b);

```

```

42         return;
43     }
44     int c=(a+b)/2;
45     alterar(val, i, j, 2*n, a, c), alterar(val, i, j, 2*n+1, c,
46         b);
47     t[n]=operacion(t[2*n], t[2*n+1]);//por esto es el push de
        arriba
48     }
49     void alterar(Alt val, int i, int j){alterar(val,i,j,1,0,sz);}
50 }rmq;

```

## 2.4 Fenwick Tree

```

1  struct Fenwick{
2      static const int sz=1<<K;
3      ll t[sz]={};
4      void adjust(int p, ll v){
5          for(int i=p+1;i<sz;i+=(i&-i)) t[i]+=v;
6      }
7      ll sum(int p){ // suma [0,p)
8          ll s = 0;
9          for(int i=p;i;i=(i&-i)) s+=t[i];
10         return s;
11     }
12     ll sum(int a, int b){return sum(b)-sum(a);} // suma [a,b)
13
14     //funciona solo con valores no negativos en el fenwick
15     //longitud del minimo prefijo t.q. suma <= x
16     //para el maximo v+1 y restar 1 al resultado
17     int pref(ll v){
18         int x = 0;
19         for(int d = 1<<(K-1); d; d>>=1){
20             if( t[x|d] < v ) x |= d, v -= t[x];
21         }
22         return x+1;
23     }
24 };
25
26 struct RangeFT { // 0-indexed, query [0, i), update [l, r)
27     Fenwick rate, err;

```

```

28 void adjust(int l, int r, int x) { // range update
29     rate.adjust(l, x); rate.adjust(r, -x);
30     err.adjust(l, -x*1); err.adjust(r, x*r);
31 }
32 ll sum(int i) { return rate.sum(i) * i + err.sum(i); }
33 }; // prefix query
34
35
36 struct Fenwick2D{
37     ll t[N][M]={};
38     void adjust(int p, int q, ll v){
39         for(int i=p+1;i<N;i+=(i&-i))
40             for(int j= q+1; j<M; j+=(j&-j))
41                 t[i][j]+=v;
42     }
43     ll sum(int p,int q){ // suma [0,p)
44         ll s = 0;
45         for(int i=p;i;i--=(i&-i))
46             for(int j=q;j;j--=(j&-j))
47                 s+=t[i][j];
48         return s;
49     }
50     ll sum(int x1, int y1, int x2, int y2){
51         return sum(x2,y2)-sum(x1,y2)-sum(x2,y1)+sum(x1,y1);
52     } // suma [a,b)
53 };

```

## 2.5 Tabla Aditiva

```

1 // Tablita aditiva 2D
2 forn (dim, 2) {
3     forn (i, N) {
4         forn (j, M) {
5             int pi = i-(dim==0), pj = j-(dim==1);
6             if (pi >= 0 && pj >= 0) {
7                 dp[i][j] += dp[pi][pj];
8             }
9         }
10     }
11 }

```

```

12 // Generalizacion a 32 dimensiones para mascarar de bits
13 forn (i, 32) {
14     forn (mask, 1<<32) {
15         if ((mask>>i)&1) {
16             dp[mask] += dp[mask - (1<<i)];
17         }
18     }
19 }

```

## 2.6 Union Find

```

1 vector<int> uf(MAXN, -1);
2 int uf_find(int x) { return uf[x]<0 ? x : uf[x] = uf_find(uf[x]); }
3 bool uf_join(int x, int y){ // True sii x e y estan en !=
    componentes
4     x = uf_find(x); y = uf_find(y);
5     if(x == y) return false;
6     if(uf[x] > uf[y]) swap(x, y);
7     uf[x] += uf[y]; uf[y] = x; return true;
8 }

```

## 3 Matemática

### 3.1 Criba Lineal

```

1 const int N = 10'000'000;
2 vector<int> lp(N+1);
3 vector<int> pr;
4 for (int i=2; i <= N; ++i) {
5     if (lp[i] == 0) lp[i] = i, pr.push_back(i);
6     for (int j = 0; i * pr[j] <= N; ++j) {
7         lp[i * pr[j]] = pr[j];
8         if (pr[j] == lp[i]) break;
9     }
10 }

```

### 3.2 Phollard's Rho

```

1 ll mulmod(ll a, ll b, ll m) { return ll(__int128(a) * b % m); }
2
3 ll expmod(ll b, ll e, ll m) { // O(log b)

```

```

4     if (!e) return 1;
5     ll q=expmod(b,e/2,m); q=mulmod(q,q,m);
6     return e%2 ? mulmod(b,q,m) : q;
7 }
8
9 bool es_primo_prob(ll n, int a) {
10    if (n == a) return true;
11    ll s = 0, d = n-1;
12    while (d%2 == 0) s++, d/=2;
13    ll x = expmod(a,d,n);
14    if ((x == 1) || (x+1 == n)) return true;
15    forn(i,s-1){
16        x = mulmod(x,x,n);
17        if (x == 1) return false;
18        if (x+1 == n) return true;
19    }
20    return false;
21 }
22
23 bool rabin(ll n) { // devuelve true sii n es primo
24     if (n == 1) return false;
25     const int ar[] = {2,3,5,7,11,13,17,19,23};
26     forn(j,9) if (!es_primo_prob(n,ar[j])) return false;
27     return true;
28 }
29
30 ll rho(ll n) {
31     if ((n & 1) == 0) return 2;
32     ll x = 2, y = 2, d = 1;
33     ll c = rand() % n + 1;
34     while (d == 1) {
35         x = (mulmod(x,x,n)+c)%n;
36         y = (mulmod(y,y,n)+c)%n;
37         y = (mulmod(y,y,n)+c)%n;
38         d=gcd(x-y,n);
39     }
40     return d==n ? rho(n) : d;
41 }
42
43 void factRho(map<ll,ll>&prim, ll n){ //O (lg n)^3. un solo numero

```

```

44     if (n == 1) return;
45     if (rabin(n)) { prim[n]++; return; }
46     ll factor = rho(n);
47     factRho(factor); factRho(n/factor);
48 }
49 auto factRho(ll n){
50     map<ll,ll>prim;
51     factRho(prim,n);
52     return prim;
53 }

```

### 3.3 Divisores

```

1 // Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
2 void divisores(const map<ll,ll> &f, vector<ll> &divs, auto it, ll
    n=1){
3     if (it==f.begin()) divs.clear();
4     if (it==f.end()) { divs.pb(n); return; }
5     ll p=it->fst, k=it->snd; ++it;
6     forn(_, k+1) divisores(f,divs,it,n), n*=p;
7 }

```

### 3.4 Inversos Modulares

```

1 pair<ll,ll> extended_euclid(ll a, ll b) {
2     if (b == 0) return {1, 0};
3     auto [y, x] = extended_euclid(b, a%b);
4     y -= (a/b)*x;
5     if (a*x + b*y < 0) x = -x, y = -y;
6     return {x, y}; // a*x + b*y = gcd(a,b)
7 }

1 constexpr ll MOD = 1000000007; // tmb es comun 998'244'353
2 ll invmod[MAXN]; // inversos mdulo MOD hasta MAXN
3 void invmods() { // todo entero en [2,MAXN] debe ser coprimo con
    MOD
4     inv[1] = 1;
5     forr(i, 2, MAXN) inv[i] = MOD - MOD/i*inv[MOD%i]%MOD;
6 }
7
8 // si MAXN es demasiado grande o MOD no es fijo:

```

```

9 // versin corta, m debe ser primo. O(log(m))
10 ll invmod(ll a, ll m) { return expmod(a,m-2,m); }
11 // versin larga, a y m deben ser coprimos. O(log(a)), en general
    ms rpido
12 ll invmod(ll a, ll m) { return (extended_euclid(a,m).fst % m + m)
    % m; }

```

## 4 Geometria

```

1 struct Point
2 {
3     double x, y;
4     double Point::operator*(const Point &o) const {
5         return x * o.x + y * o.y; }
6     double Point::operator^(const Point &o) const {
7         return x * o.y - y * o.x; }
8     Point Point::operator-(const Point &o) const {
9         return {x - o.x, y - o.y}; }
10    Point Point::operator+(const Point &o) const {
11        return {x + o.x, y + o.y}; }
12    Point Point::operator*(const double &u) const {
13        return {x * u, y * u}; }
14    Point Point::operator/(const double &u) const {
15        return {x / u, y / u}; }
16    double Point::norm_sq() const {
17        return x * x + y * y; }
18    double Point::norm() const {
19        return sqrt(x * x + y * y); }
20 };
21
22 struct Comp {
23     Vector o, v;
24     Comp(Vector _o, Vector _v) : o(_o), v(_v) {}
25     bool half(Vector p) {
26         assert(!(p.x == 0 && p.y == 0));
27         return (v ^ p) < 0 || ((v ^ p) == 0 && (v * p) < 0);
28     }
29     bool operator()(Vector a, Vector b) {
30         return mp(half(a - o), 0ll) < mp(half(b - o), ((a - o) ^ (b
            - o)));

```

```

31     }
32 };
33
34 struct Segment {
35     Vector a, b;
36     long double eval() const
37     { // funcion auxiliar para ordenar segmentos
38         assert(a.x != b.x || a.y != b.y);
39         Vector a1 = a, b1 = b;
40         if (a1.x > b1.x)
41             swap(a1, b1);
42         assert(x >= a1.x && x <= b1.x);
43         if (x == a1.x)
44             return a1.y;
45         if (x == b1.x)
46             return b1.y;
47         Vector ab = b1 - a1;
48         return a1.y + (x - a1.x) * (ab.y / ab.x);
49     }
50     bool operator<(Segment o) const
51     { // orden de segmentos en un punto (x=cte)
52         return (eval() - o.eval()) < -1e-13;
53     }
54 };
55
56 bool ccw(const Point &a, const Point &m, const Point &b) {
57     return ((a - m) ^ (b - m)) > EPS; }
58
59 bool collinear(const Point &a, const Point &b, const Point &c) {
60     return fabs((b - a) ^ (c - a)) < EPS; }
61
62 double dist_sq(const Point &a, const Point &b) {
63     return (a - b).norm_sq(); }
64
65 double dist(const Point &a, const Point &b) {
66     return (a - b).norm(); }
67
68 bool in_segment(const Point &p, const Point &b, const Point &c) {
69     return fabs(dist_sq(p, b) + dist_sq(p, c) - dist_sq(b, c)) <
        EPS; }

```

```

70
71 double angle(const Point &a, const Point &m, const Point &b) {
72     Point ma = a - m, mb = b - m;
73     return atan2(ma ^ mb, ma * mb);} //atan2l
74
75 void sweep_space() {
76     vector<Event> eventos; // puntos, segmentos, ...
77     sort(eventos);        // sort por x, y, ...
78     set<Info> estado;     // mantener la informacion ordenada
79     forn(i, sz(eventos)) {
80         Event &e = eventos[i];
81         process(e, estado); // procesar un evento cambia el estado
82         ans = actualizar(ans);
83     } }
84
85 vector<pt> minkowski_sum(vector<pt> p, vector<pt> q){
86     int n=sz(p),m=sz(q),x=0,y=0;
87     fore(i,0,n) if(p[i]<p[x]) x=i;
88     fore(i,0,m) if(q[i]<q[y]) y=i;
89     vector<pt> ans={p[x]+q[y]};
90     fore(it,1,n+m){
91         pt a=p[(x+1)%n]+q[y];
92         pt b=p[x]+q[(y+1)%m];
93         if(b.left(ans.back(),a)) ans.pb(b), y=(y+1)%m;
94         else ans.pb(a), x=(x+1)%n;
95     }
96     return ans; }

```

## 4.1 Lower Envelope

```

1  const ll is_query = -(1LL<<62);
2  struct Line {
3      ll m, b;
4      mutable multiset<Line>::iterator it;
5      const Line *succ(multiset<Line>::iterator it) const;
6      bool operator<(const Line & rhs) const {
7          if (rhs.b != is_query) return m < rhs.m;
8          const Line *s = succ(it);
9          if (!s) return 0;
10         ll x = rhs.m;

```

```

11         return b - s->b > (s->m - m) * x;
12     }
13 };
14 struct HullDynamic : public multiset<Line> {
15     bool bad(iterator y) {
16         iterator z = next(y);
17         if (y == begin()) {
18             if (z == end()) return 0;
19             return y->m == z->m && y->b >= z->b;
20         }
21         iterator x = prev(y);
22         if (z == end()) return y->m == x->m && y->b >= x->b;
23         return (x->m-z->m)*(z->b-y->b) >= (z->b-x->b)*(y->m-z->m);
24     }
25     iterator next(iterator y) {return ++y;}
26     iterator prev(iterator y) {return --y;}
27     void insert_line(ll m, ll b) {
28         iterator y = insert((Line) {m, b});
29         y->it = y;
30         if (bad(y)) {erase(y); return;}
31         while (next(y) != end() && bad(next(y))) erase(next(y));
32         while (y != begin() && bad(prev(y))) erase(prev(y));
33     }
34     ll eval(ll x) {
35         Line l = *lower_bound((Line) {x, is_query});
36         return l.m * x + l.b;
37     }
38 } h;
39 const Line *Line::succ(multiset<Line>::iterator it) const {
40     return (++it==h.end() ? NULL : &*it); }

```

## 5 Strings

### 5.1 Hashing

```

1  struct StrHash { // Hash polinomial con exponentes decrecientes.
2      static constexpr ll ms[] = {1'000'000'007, 1'000'000'403};
3      static constexpr ll b = 500'000'000;
4      vector<ll> hs[2], bs[2];
5      StrHash(string const& s) {

```

```

6     int n = sz(s);
7     forn(k, 2) {
8         hs[k].resize(n+1), bs[k].resize(n+1, 1);
9         forn(i, n) {
10             hs[k][i+1] = (hs[k][i] * b + s[i]) % ms[k];
11             bs[k][i+1] = bs[k][i] * b % ms[k];
12         }
13     }
14 }
15 ll get(int idx, int len) const { // Hashes en 's[idx,
16     // idx+len)'
17     ll h[2];
18     forn(k, 2) {
19         h[k] = hs[k][idx+len] - hs[k][idx] * bs[k][len] % ms[k];
20         if (h[k] < 0) h[k] += ms[k];
21     }
22     return (h[0] << 32) | h[1];
23 }

```

## 5.2 Suffix Array

```

1 #define RB(x) ((x) < n ? r[x] : 0)
2 void csort(vector<int>& sa, vector<int>& r, int k) {
3     int n = sz(sa);
4     vector<int> f(max(255, n)), t(n);
5     forn(i, n) ++f[RB(i+k)];
6     int sum = 0;
7     forn(i, max(255, n)) f[i] = (sum += f[i]) - f[i];
8     forn(i, n) t[f[RB(sa[i]+k)]]++ = sa[i];
9     sa = t;
10 }
11 vector<int> compute_sa(string& s){ // O(n*log2(n))
12     int n = sz(s) + 1, rank;
13     vector<int> sa(n), r(n), t(n);
14     iota(all(sa), 0);
15     forn(i, n) r[i] = s[i];
16     for (int k = 1; k < n; k *= 2) {
17         csort(sa, r, k), csort(sa, r, 0);
18         t[sa[0]] = rank = 0;

```

```

19         forr(i, 1, n) {
20             if(r[sa[i]] != r[sa[i-1]] || RB(sa[i]+k) !=
21                 RB(sa[i-1]+k)) ++rank;
22             t[sa[i]] = rank;
23         }
24         r = t;
25         if (r[sa[n-1]] == n-1) break;
26     }
27     return sa; // sa[i] = i-th suffix of s in lexicographical order
28 }
29 vector<int> compute_lcp(string& s, vector<int>& sa){
30     int n = sz(s) + 1, L = 0;
31     vector<int> lcp(n), plcp(n), phi(n);
32     phi[sa[0]] = -1;
33     forn(i, 1, n) phi[sa[i]] = sa[i-1];
34     forn(i, n) {
35         if (phi[i] < 0) { plcp[i] = 0; continue; }
36         while(s[i+L] == s[phi[i]+L]) ++L;
37         plcp[i] = L;
38         L = max(L - 1, 0);
39     }
40     forn(i, n) lcp[i] = plcp[sa[i]];
41     return lcp; // lcp[i] = longest common prefix between sa[i-1]
42         // and sa[i]

```

## 5.3 Kmp

```

1 template<class Char=char>struct Kmp {
2     using str = basic_string<Char>;
3     vector<int> pi; str pat;
4     Kmp(str const& _pat): pi(move(pfun(_pat))), pat(_pat) {}
5     vector<int> matches(str const& txt) const {
6         if (sz(pat) > sz(txt)) {return {};}
7         vector<int> occs; int m = sz(pat), n = sz(txt);
8         if (m == 0) {occs.push_back(0);}
9         int j = 0;
10        forn(i, n) {
11            while (j != 0 && txt[i] != pat[j]) {j = pi[j-1];}
12            if (txt[i] == pat[j]) {++j;}

```



```

13         if (j == m) {occs.push_back(i - j + 1);}
14     }
15     return occs;
16 }
17 };

```

## 5.4 Manacher

```

1 struct Manacher {
2     vector<int> p;
3     Manacher(string const& s) {
4         int n = sz(s), m = 2*n+1, l = -1, r = 1;
5         vector<char> t(m); forn(i, n) t[2*i+1] = s[i];
6         p.resize(m); forr(i, 1, m) {
7             if (i < r) p[i] = min(r-i, p[l+r-i]);
8             while (p[i] <= i && i < m-p[i] && t[i-p[i]] ==
9                 t[i+p[i]]) ++p[i];
10            if (i+p[i] > r) l = i-p[i], r = i+p[i];
11        }
12    } // Retorna palindromos de la forma {comienzo, largo}.
13    pii at(int i) const {int k = p[i]-1; return pair{i/2-k/2, k};}
14    pii odd(int i) const {return at(2*i+1);} // Mayor centrado en
15        s[i].
16    pii even(int i) const {return at(2*i);} // Mayor centrado en
17        s[i-1, i].
18 };

```

## 5.5 String Functions

```

1 template<class Char=char>vector<int> pfun(basic_string<Char>const&
2     w) {
3     int n = sz(w), j = 0; vector<int> pi(n);
4     forr(i, 1, n) {
5         while (j != 0 && w[i] != w[j]) {j = pi[j - 1];}
6         if (w[i] == w[j]) {++j;}
7         pi[i] = j;
8     } // pi[i] = lengh of longest proper suffix of w[0..i] that is
9         also prefix
10    return pi;
11 }

```

```

10 template<class Char=char>vector<int> zfun(const
11     basic_string<Char>& w) {
12     int n = sz(w), l = 0, r = 0; vector<int> z(n);
13     forr(i, 1, n) {
14         if (i <= r) {z[i] = min(r - i + 1, z[i - l]);}
15         while (i + z[i] < n && w[z[i]] == w[i + z[i]]) {++z[i];}
16         if (i + z[i] - 1 > r) {l = i, r = i + z[i] - 1;}
17     } // z[i] = lengh of longest prefix of w that also begins at
18         index i
19     return z;
20 }

```

## 6 Grafos

### 6.1 Dijkstra

```

1 vector<pair<int,int>> g[MAXN]; // u->[(v,cost)]
2 ll dist[MAXN];
3 void dijkstra(int x){
4     memset(dist,-1,sizeof(dist));
5     priority_queue<pair<ll,int> > q;
6     dist[x]=0;q.push({0,x});
7     while(!q.empty()){
8         x=q.top().snd;ll c=-q.top().fst;q.pop();
9         if(dist[x]!=c)continue;
10        forn(i,g[x].size()){
11            int y=g[x][i].fst; ll c=g[x][i].snd;
12            if(dist[y]<0||dist[x]+c<dist[y])
13                dist[y]=dist[x]+c,q.push({-dist[y],y});
14        }
15    }
16 }

```

### 6.2 LCA

```

1 vector<int> g[1<<K]; int n; // K such that 2^K>=n
2 int F[K][1<<K], D[1<<K];
3 void lca_dfs(int x){
4     forn(i, sz(g[x])){
5         int y = g[x][i]; if(y==F[0][x]) continue;

```

```

6      F[0][y]=x; D[y]=D[x]+1;lca_dfs(y);
7  }
8  }
9  void lca_init(){
10     D[0]=0;F[0][0]=-1;
11     lca_dfs(0);
12     forr(k,1,K)forn(x,n)
13         if(F[k-1][x]<0)F[k][x]=-1;
14         else F[k][x]=F[k-1][F[k-1][x]];
15 }
16
17 int lca(int x, int y){
18     if(D[x]<D[y])swap(x,y);
19     for(int k = K-1;k>=0;--k) if(D[x]-(1<<k) >=D[y])x=F[k][x];
20     if(x==y)return x;
21     for(int k=K-1;k>=0;--k)if(F[k][x]!=F[k][y])x=F[k][x],y=F[k][y];
22     return F[0][x];
23 }
24
25 int dist(int x, int y){
26     return D[x] + D[y] - 2*D[lca(x,y)];
27 }

```

### 6.3 Toposort

```

1  vector<int> g[MAXN];int n;
2  vector<int> tsort(){ // lexicographically smallest topological sort
3      vector<int> r;priority_queue<int> q;
4      vector<int> d(2*n,0);
5      forn(i,n)forn(j,g[i].size())d[g[i][j]]++;
6      forn(i,n)if(!d[i])q.push(-i);
7      while(!q.empty()){
8          int x=-q.top();q.pop();r.pb(x);
9          forn(i,sz(g[x])){
10              d[g[x][i]]--;
11              if(!d[g[x][i]])q.push(-g[x][i]);
12          }
13      }
14      return r; // if not DAG it will have less than n elements
15 }

```

## 7 Flujo

### 7.1 Dinic

```

1  struct Dinic{
2      int nodes,src,dst;
3      vector<int> dist,q,work;
4      struct edge {int to,rev;ll f,cap;};
5      vector<vector<edge>> g;
6      Dinic(int x):nodes(x),g(x),dist(x),q(x),work(x){}
7      void add_edge(int s, int t, ll cap){
8          g[s].pb((edge){t,sz(g[t]),0,cap});
9          g[t].pb((edge){s,sz(g[s])-1,0,0});
10     }
11     bool dinic_bfs(){
12         fill(all(dist),-1);dist[src]=0;
13         int qt=0;q[qt++]=src;
14         for(int qh=0;qh<qt;qh++){
15             int u=q[qh];
16             forn(i,sz(g[u])){
17                 edge &e=g[u][i];int v=g[u][i].to;
18                 if(dist[v]<0&&e.f<e.cap)dist[v]=dist[u]+1,q[qt++]=v;
19             }
20         }
21         return dist[dst]>=0;
22     }
23     ll dinic_dfs(int u, ll f){
24         if(u==dst)return f;
25         for(int &i=work[u];i<sz(g[u]);i++){
26             edge &e=g[u][i];
27             if(e.cap<=e.f)continue;
28             int v=e.to;
29             if(dist[v]==dist[u]+1){
30                 ll df=dinic_dfs(v,min(f,e.cap-e.f));
31                 if(df>0){e.f+=df;g[v][e.rev].f-=df;return df;}
32             }
33         }
34         return 0;
35     }
36     ll max_flow(int _src, int _dst){

```

```

37     src=_src;dst=_dst;
38     ll result=0;
39     while(dinic_bfs()){
40         fill(all(work),0);
41         while(ll delta=dinic_dfs(src,INF))result+=delta;
42     }
43     return result;
44 }
45 };

```

## 7.2 Kuhn

```

1  vector<int> g[MAXN];
2  vector<bool> vis;
3  vector<int> match;
4
5  bool kuhn_dfs(int u){
6      if (vis[u]) return false;
7      vis[u] = true;
8      for (int v : g[u]) if (match[v] == -1 || kuhn_dfs(match[v])) {
9          match[v] = u;
10         return true;
11     } return false;
12 }
13
14 vector<int> kuhn(int n) {
15     match.resize(n, -1);
16     vis.resize(n);
17     forn(u, n) {
18         vis.assign(n, false);
19         kuhn_dfs(u);
20     }
21     return match;
22 } //n: cant de nodos devuelve un vector con -1 si no matchea y
    sino su match

```

# 8 Optimización

## 8.1 Ternary Search

```

1  // mnimo entero de f en (l,r)
2  ll ternary(auto f, ll l, ll r) {
3      for (ll d = r-l; d > 2; d = r-l) {
4          ll a = l+d/3, b = r-d/3;
5          if (f(a) > f(b)) l = a; else r = b;
6      }
7      return l+1; // retorna un punto, no un resultado de evaluar f
8  }
9
10 // mnimo real de f en (l,r)
11 // para error < EPS, usar iters = log((r-l)/EPS)/log(1.618)
12 double golden(auto f, double l, double r, int iters) {
13     constexpr double ratio = (3-sqrt(5))/2;
14     double x1 = l+(r-l)*ratio, f1 = f(x1);
15     double x2 = r-(r-l)*ratio, f2 = f(x2);
16     while (iters--) {
17         if (f1 > f2) l=x1, x1=x2, f1=f2, x2=r-(r-l)*ratio, f2=f(x2);
18         else      r=x2, x2=x1, f2=f1, x1=l+(r-l)*ratio, f1=f(x1);
19     }
20     return (l+r)/2; // retorna un punto, no un resultado de
        evaluar f
21 }

```

## 8.2 Longest Increasing Subsequence

```

1  int lis(vector<int> const& a) {
2      int n = a.size();
3      const int INF = 1e9;
4      vector<int> d(n+1, INF);
5      d[0] = -INF;
6      forn(i,n){
7          int l = upper_bound(all(d), a[i]) - d.begin();
8          if (d[l-1] < a[i] && a[i] < d[l])
9              d[l] = a[i];
10     }
11     int ans = 0;
12     for (int l = 0; l <= n; l++) {
13         if (d[l] < INF)
14             ans = l;
15     }

```

```

16     return ans;
17 }

```

## 9 Otros

### 9.1 Mo

```

1  int n,sq,nq; // array size, sqrt(array size), #queries
2  struct qu{int l,r,id;};
3  qu qs[MAXN];
4  ll ans[MAXN]; // ans[i] = answer to ith query
5  bool qcomp(const qu &a, const qu &b){
6      if(a.l/sq!=b.l/sq) return a.l<b.l;
7      return (a.l/sq)&1?a.r<b.r:a.r>b.r;
8  }
9  void mos(){
10     forn(i,nq)qs[i].id=i;
11     sq=sqrt(n)+.5;
12     sort(qs,qs+nq,qcomp);
13     int l=0,r=0;
14     init();
15     forn(i,nq){
16         qu q=qs[i];
17         while(l>q.l)add(--l);
18         while(r<q.r)add(r++);
19         while(l<q.l)remove(l++);
20         while(r>q.r)remove(--r);
21         ans[q.id]=get_ans();
22     }
23 }

```

### 9.2 Fijar el numero de decimales

```

1 // antes de imprimir decimales, con una sola vez basta
2 cout << fixed << setprecision(DECIMAL_DIG);

```

### 9.3 Hash Table (Unordered Map/ Unordered Set)

```

1 #include <ext/pb_ds/assoc_container.hpp>
2 using namespace __gnu_pbds;

```

```

3 template<class Key,class Val=null_type>using
    htable=gp_hash_table<Key,Val>;
4 // como unordered_map (o unordered_set si Val es vacio), pero sin
    metodo count

```

### 9.4 Indexed Set

```

1 #include <ext/pb_ds/assoc_container.hpp>
2 using namespace __gnu_pbds;
3 template<class Key, class Val=null_type>
4 using indexed_set = tree<Key, Val, less<Key>, rb_tree_tag,
5                        tree_order_statistics_node_update>;
6 // indexed_set<char> s;
7 // char val = *s.find_by_order(0); // acceso por indice
8 // int idx = s.order_of_key('a'); // busca indice del valor

```