

# Ayudamemoria

My room is random Sorted

October 10, 2024

## Contents

### 1 Template

### 2 Estructuras de datos

- 2.1 Fenwick Tree . . . . .
- 2.2 Tabla Aditiva . . . . .

### 3 Matemática

- 3.1 Criba Lineal . . . . .
- 3.2 Phollard's Rho . . . . .

### 4 Geometria

- 4.1 Lower Envelope . . . . .

### 5 Otros

- 5.1 Fijar el numero de decimales . . . . .

## 1 Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define dprint(v) cout << #v " = " << v << endl //;
4 #define forr(i, a, b) for (int i = (a); i < (b); i++)
5 #define forn(i, n) forr(i, 0, n)
6 #define dforn(i, n) for (int i = n - 1; i >= 0; i--)
7 #define forall(it, v) for (auto it = v.begin(); it != v.end();
    ++it)
8 #define sz(c) ((int)c.size())
9 #define zero(v) memset(v, 0, sizeof(v))
```

```
10 #define pb push_back
11 #define fst first
12 #define snd second
13 #define mp make_pair
14 #define all(v) begin(v),end(v)
15 #define endl '\n'
16 typedef long long ll;
17 typedef pair<int, int> ii;
18 typedef vector<int> vi;
19
20 int main(int argc, char **argv){
21     ios::sync_with_stdio(0); cin.tie(0); cout.tie(0);
22     if(argc == 2) freopen(argv[1], "r", stdin);
23
24 }
```

### 2 1.1 run.sh

```
1 clear
2 make -s $1 && ./ $1 $2
```

### 3 1.2 comp.sh

```
1 clear
2 make -s $1 2>&1 | head -$2
```

### 5 1.3 Makefile

```
1 CC = g++
2 CXXFLAGS = -Wall -g \
3 -fsanitize=undefined -fsanitize=bounds \
4 -std=c++2a -O2
```

## 2 Estructuras de datos

### 2.1 Fenwick Tree

```
1 struct Fenwick {
2     static const int sz = 1<<11;
3     ll t[sz];
4     void adjust(ll v, int p) {
```

```

5         for (int i=p; i<sz; i+=(i&-i)) t[i]+=v; }
6     ll sum(int p){
7         ll s=0;
8         for(int i=p; i; i==(i&-i)) s+=t[i];
9         return s;
10    }
11    ll sum(int a, int b) {return sum(b)-sum(a-1);}
12 };
13
14 struct RangeFenwick {
15     Fenwick add;
16     Fenwick sub;
17     void adjust(ll v, int a, int b) {
18         add.adjust(v,a);
19         add.adjust(-v,b+1);
20         sub.adjust((a-1)*v,a);
21         sub.adjust(-b*v,b+1);
22     }
23     ll sum(int p) {
24         return 1ll * p * add.sum(p) - sub.sum(p);
25     }
26     ll sum(int a, int b) {
27         return sum(b) - sum(a-1);
28     }
29 };
30
31 struct Fenwick2D {
32     static const int sz=(1<<10);
33     Fenwick t[sz];
34     void adjust(int x, int y, ll v) {
35         for (int i=x; i<sz; i+=(i&-i)) t[i].adjust(y,v);}
36     ll sum(int x, int y) {
37         ll s=0;
38         for (int i=x; i; i==(i&-i)) s += t[i].sum(y);
39         return s;
40     }
41     ll sum(int x1, int y1, int x2, int y2) {
42         ll s = sum(x2,y2)
43             + ((x1>1) ? -sum(x1-1,y2) : 0)
44             + ((y1>1) ? -sum(x2,y1-1) : 0)

```

```

45         + ((x1>1&&y1>1) ? sum(x1-1,y1-1) : 0);
46         return s;
47     }
48 };

```

## 2.2 Tabla Aditiva

```

1 // Tablita aditiva 2D
2 forn (dim, 2) {
3     forn (i, N) {
4         forn (j, M) {
5             int pi = i-(dim==0), pj = j-(dim==1);
6             if (pi >= 0 && pj >= 0) {
7                 dp[i][j] += dp[pi][pj];
8             }
9         }
10    }
11 }
12 // Generalizacion a 32 dimensiones para mascarar de bits
13 forn (i, 32) {
14     forn (mask, 1<<32) {
15         if ((mask>>i)&1) {
16             dp[mask] += dp[mask - (1<<i)];
17         }
18     }
19 }

```

## 3 Matemática

### 3.1 Criba Lineal

```

1 const int N = 10000000;
2 vector<int> lp(N+1);
3 vector<int> pr;
4
5 for (int i=2; i <= N; ++i) {
6     if (lp[i] == 0) {
7         lp[i] = i;
8         pr.push_back(i);
9     }

```

```

10     for (int j = 0; i * pr[j] <= N; ++j) {
11         lp[i * pr[j]] = pr[j];
12         if (pr[j] == lp[i]) {
13             break;
14         }
15     }
16 }

```

### 3.2 Phollard's Rho

```

1 ll gcd(ll a, ll b){return a?gcd(b %a, a):b;}
2
3
4 ll mulmod(ll a, ll b, ll m) {
5     return ll(__int128(a) * b % m);
6 }
7
8 ll expmod (ll b, ll e, ll m){//O(log b)
9     if(!e) return 1;
10    ll q= expmod(b,e/2,m); q=mulmod(q,q,m);
11    return e%2? mulmod(b,q,m) : q;
12 }
13
14 bool es_primo_prob (ll n, int a)
15 {
16     if (n == a) return true;
17     ll s = 0,d = n-1;
18     while (d % 2 == 0) s++,d/=2;
19
20     ll x = expmod(a,d,n);
21     if ((x == 1) || (x+1 == n)) return true;
22
23     forn (i, s-1){
24         x = mulmod(x, x, n);
25         if (x == 1) return false;
26         if (x+1 == n) return true;
27     }
28     return false;
29 }
30

```

```

31 bool rabin (ll n){ //devuelve true si n es primo
32     if (n == 1) return false;
33     const int ar[] = {2,3,5,7,11,13,17,19,23};
34     forn (j,9)
35         if (!es_primo_prob(n,ar[j]))
36             return false;
37     return true;
38 }
39
40 ll rho(ll n){
41     if( (n & 1) == 0 ) return 2;
42     ll x = 2 , y = 2 , d = 1;
43     ll c = rand() % n + 1;
44     while( d == 1 ){
45         x = (mulmod( x , x , n ) + c)%n;
46         y = (mulmod( y , y , n ) + c)%n;
47         y = (mulmod( y , y , n ) + c)%n;
48         if( x - y >= 0 ) d = gcd( x - y , n );
49         else d = gcd( y - x , n );
50     }
51     return d==n? rho(n):d;
52 }
53
54 map<ll,ll> prim;
55 void factRho (ll n){ //O (lg n)^3. un solo numero
56     if (n == 1) return;
57     if (rabin(n)){
58         prim[n]++;
59         return;
60     }
61     ll factor = rho(n);
62     factRho(factor);
63     factRho(n/factor);
64 }

```

## 4 Geometria

```

1 struct Point
2 {
3     double x, y;

```

```

4     double Point::operator*(const Point &o) const {
5         return x * o.x + y * o.y; }
6     double Point::operator^(const Point &o) const {
7         return x * o.y - y * o.x; }
8     Point Point::operator-(const Point &o) const {
9         return {x - o.x, y - o.y}; }
10    Point Point::operator+(const Point &o) const {
11        return {x + o.x, y + o.y}; }
12    Point Point::operator*(const double &u) const {
13        return {x * u, y * u}; }
14    Point Point::operator/(const double &u) const {
15        return {x / u, y / u}; }
16    double Point::norm_sq() const {
17        return x * x + y * y; }
18    double Point::norm() const {
19        return sqrt(x * x + y * y); }
20 };
21
22 struct Comp {
23     Vector o, v;
24     Comp(Vector _o, Vector _v) : o(_o), v(_v) {}
25     bool half(Vector p) {
26         assert(!(p.x == 0 && p.y == 0));
27         return (v ^ p) < 0 || ((v ^ p) == 0 && (v * p) < 0);
28     }
29     bool operator()(Vector a, Vector b) {
30         return mp(half(a - o), 0ll) < mp(half(b - o), ((a - o) ^ (b
31             - o)));
32     }
33 };
34 struct Segment {
35     Vector a, b;
36     long double eval() const
37     { // funcion auxiliar para ordenar segmentos
38         assert(a.x != b.x || a.y != b.y);
39         Vector a1 = a, b1 = b;
40         if (a1.x > b1.x)
41             swap(a1, b1);
42         assert(x >= a1.x && x <= b1.x);

```

```

43         if (x == a1.x)
44             return a1.y;
45         if (x == b1.x)
46             return b1.y;
47         Vector ab = b1 - a1;
48         return a1.y + (x - a1.x) * (ab.y / ab.x);
49     }
50     bool operator<(Segment o) const
51     { // orden de segmentos en un punto (x=cte)
52         return (eval() - o.eval()) < -1e-13;
53     }
54 };
55
56 bool ccw(const Point &a, const Point &m, const Point &b) {
57     return ((a - m) ^ (b - m)) > EPS; }
58
59 bool collinear(const Point &a, const Point &b, const Point &c) {
60     return fabs((b - a) ^ (c - a)) < EPS; }
61
62 double dist_sq(const Point &a, const Point &b) {
63     return (a - b).norm_sq(); }
64
65 double dist(const Point &a, const Point &b) {
66     return (a - b).norm(); }
67
68 bool in_segment(const Point &p, const Point &b, const Point &c) {
69     return fabs(dist_sq(p, b) + dist_sq(p, c) - dist_sq(b, c)) <
70         EPS; }
71
72 double angle(const Point &a, const Point &m, const Point &b) {
73     Point ma = a - m, mb = b - m;
74     return atan2(ma ^ mb, ma * mb);} //atan2l
75
76 void sweep_space() {
77     vector<Event> eventos; // puntos, segmentos, ...
78     sort(eventos); // sort por x, y, ...
79     set<Info> estado; // mantener la informacion ordenada
80     forn(i, sz(eventos)) {
81         Event &e = eventos[i];
82         process(e, estado); // procesar un evento cambia el estado

```

```

82     ans = actualizar(ans);
83 } }
84
85 vector<pt> minkowski_sum(vector<pt> p, vector<pt> q){
86     int n=SZ(p),m=SZ(q),x=0,y=0;
87     fore(i,0,n) if(p[i]<p[x]) x=i;
88     fore(i,0,m) if(q[i]<q[y]) y=i;
89     vector<pt> ans={p[x]+q[y]};
90     fore(it,1,n+m){
91         pt a=p[(x+1)%n]+q[y];
92         pt b=p[x]+q[(y+1)%m];
93         if(b.left(ans.back(),a)) ans.pb(b), y=(y+1)%m;
94         else ans.pb(a), x=(x+1)%n;
95     }
96     return ans; }

```

## 4.1 Lower Envelope

```

1  const ll is_query = -(1LL<<62);
2  struct Line {
3      ll m, b;
4      mutable multiset<Line>::iterator it;
5      const Line *succ(multiset<Line>::iterator it) const;
6      bool operator<(const Line & rhs) const {
7          if (rhs.b != is_query) return m < rhs.m;
8          const Line *s = succ(it);
9          if (!s) return 0;
10         ll x = rhs.m;
11         return b - s->b > (s->m - m) * x;
12     }
13 };
14 struct HullDynamic : public multiset<Line> {
15     bool bad(iterator y) {
16         iterator z = next(y);
17         if (y == begin()) {
18             if (z == end()) return 0;
19             return y->m == z->m && y->b >= z->b;
20         }
21         iterator x = prev(y);
22         if (z == end()) return y->m == x->m && y->b >= x->b;

```

```

23         return (x->m-z->m)*(z->b-y->b) >= (z->b-x->b)*(y->m-z->m);
24     }
25     iterator next(iterator y) {return ++y;}
26     iterator prev(iterator y) {return --y;}
27     void insert_line(ll m, ll b) {
28         iterator y = insert((Line) {m, b});
29         y->it = y;
30         if (bad(y)) {erase(y); return;}
31         while (next(y) != end() && bad(next(y))) erase(next(y));
32         while (y != begin() && bad(prev(y))) erase(prev(y));
33     }
34     ll eval(ll x) {
35         Line l = *lower_bound((Line) {x, is_query});
36         return l.m * x + l.b;
37     }
38 } h;
39 const Line *Line::succ(multiset<Line>::iterator it) const {
40     return (++it==h.end() ? NULL : &*it); }

```

## 5 Otros

### 5.1 Fijar el numero de decimales

```

1  cout.precision(7); fixed(cout);
2  cout << x << " " << y;
3  // otra forma
4  cout.precision(7);
5  cout << fixed << x << " " << fixed << y;

```