Chance, Machine Learning Algorithms, MVPA, Brains on Trial

Commentary on this assignment:

This assignment revisits concepts from probability and hypothesis testing in assessing accuracy of machine learning algorithms. Then you'll investigate a specific ML algorithm (separate submission). Then you'll apply machine learning to a more complex problem than the 4 brain regions, which will allow you to apply methods to avoid overfitting. Finally, you'll read or watch a video about the use of neuroscience in the courtroom and in lie detection, which raises important questions about how our legal system works.

I provided very rough time estimates just to give you a sense of scale. I expect that there will be lots of variability in how much time people spend on this assignment overall and how much time people spend in each section. I trust you to make the good decisions for your learning goals and the course goals around challenging yourself, engaging your curiosity, and contributing to class.

This document is a bit long, so I've included a linked table of contents and pictures of puppies (puppies only available in this version: https://docs.google.com/document/d/1CmVUOSBBxdDdp-JU8pCzN5pKm6gdCE1sWJtiQXHqv4E/edit?usp=sharing).

The data you need are here: https://drive.google.com/file/d/12cJmNYllwkhTGyHa9NAWpZWJVqPw4hib/view?usp=sharing

Table of Contents

Chance, Machine Learning Algorithms, MVPA, Brains on Trial	1
Understanding "chance" in relation to classification [30 mins]	
Exercise 1a: What is the most probable accuracy?	
Exercise 1b: What is the expected value of the accuracy?	
Exercise 2a: For the training data, what is the probability of getting an accuracy of 50% or worse?	
Exercise 2b: For the training data, what is the probability of getting an accuracy of 50% or worse?	
Exercise 3a: What should I choose as my accuracy threshold for the training data?	
Exercise 3b: What accuracy threshold should I use for my test data?	
Exercise 3c: Are these the same or different? Why?	
Exercise 4: What is the probability that it will perform at chance or worse on the test data?	
Exercise 5: What classification accuracy would we get on the train data if our algorithm just guessed face	
every time?	4
Challenge exercise: If our algorithm is still just a coin flipper, what is the expected value of the accuracy on o	
training data?	
Use external resources to investigate, understand, and explain an algorithm [90 mins]	
Exercise 6: Explain algorithm (separate submission)	
Multi-voxel pattern analysis on fMRI data [90 mins]	
Exercise (BIG ONE): Run multivoxel pattern analysis (machine learning on voxels)	7
Brains on Trial [120 minutes]	. 15

Understanding "chance" in relation to classification [30 mins]

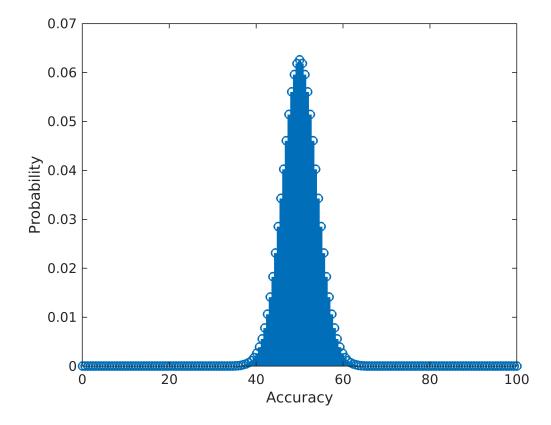
In this section, we're going to explore probability in relation to classification accuracy. We'll use the example from our faces vs houses fMRI data. In the training data, we have 162 total examples and in the test data we have 54 total rows of data. Each is evenly split between faces and houses.

If my algorithm just flips a coin each time ("operates at chance level", p(face)=0.5):

Exercise 1a: What is the most probable accuracy?

I think it should be close to 50, but since we have a discrete sample set, the accuracy might not be exactly 50 if there is an odd number of samples

```
n = 162;
test_n = 54;
b = makedist("Binomial", 'N', n, 'p', 0.5);
x = 0:n; % number of correct predictions
stem(100.*(x./n), b.pdf(x), 'LineWidth', 2);
xlabel('Accuracy');
ylabel('Probability');
```



Exercise 1b: What is the expected value of the accuracy?

Here are some resources about expected values that might be helpful:

https://ocw.mit.edu/courses/mathematics/18-05-introduction-to-probability-and-statistics-spring-2014/readings/MIT18_05S14_Reading4b.pdf

https://www.stat.purdue.edu/~zhanghao/STAT511/handout/Stt511%20Sec3.3.pdf

Expecting around 50, but it can be a non-discrete integer because it is a weighted average

```
expectedValueAccuracy = b.mean/n
expectedValueAccuracy = 0.5000
```

Exercise 2a: For the training data, what is the probability of getting an accuracy of 50% or worse?

```
p = binocdf(n*0.5, n, 0.5) % inclusive of 50%
p = 0.5313
```

Exercise 2b: For the training data, what is the probability of getting an accuracy of 50% or worse?

```
% for testing data
p = binocdf(test_n*0.5, test_n, 0.5) % inclusive of 50% and fewer options so each option
p = 0.5540
```

I want to set a threshold to reject the hypothesis that my algorithm is operating a chance level. Let's say that I feel comfortable being wrong 10% of the time when my algorithm is operating at chance.

Exercise 3a: What should I choose as my accuracy threshold for the training data?

null_hypothesis: my algorithm is operating at chance level

alternative_hypothesis: my algorithm is not operating at chance level

alpha = 0.1

```
b = makedist("Binomial", 'N', n, 'p', 0.5);
100 * icdf(b, 0.9)/n % if 90% were correct, find number correct
```

ans = 54.9383

Exercise 3b: What accuracy threshold should I use for my test data?

```
b = makedist("Binomial", 'N', test_n, 'p', 0.5);
100 * icdf(b, 0.9)/test_n % if 90% were correct, find number correct
ans = 59.2593
```

Exercise 3c: Are these the same or different? Why?

Different because there are a different number of trials in train and test. If there are more trials, we can be more confident in our result and tighten the range.

Now, let's suppose I have an algorithm that is 70% accurate in reality.

Exercise 4: What is the probability that it will perform at chance or worse on the test data?

```
p = 0.7;
binocdf(0.5*test_n, test_n, p)
ans = 0.0016
```

In the questions above, we have been considering a situation where we have an equal number of face and house examples in our data. Now let's think about a situation where that is not the case. Our training data still has 162 total examples, but now 130 of them are faces.

Exercise 5: What classification accuracy would we get on the train data if our algorithm just guessed face every time?

```
100 * 130/162

ans = 80.2469
```

Challenge exercise: If our algorithm is still just a coin flipper, what is the expected value of the accuracy on our training data?

```
p = 0.5;
tp = 130 * p; % number of tp guessed correctly by random chance
tn = (162 - 130) * p; % number of tn guessed correctly by random chance
(tp + tn)./162
ans = 0.5000
```

Used a bayesian tree to draw prior and posterior

.3 / \ .7 .5 / \ .5 \ .5 / \ .5

Use external resources to investigate, understand, and explain an algorithm [90 mins]

Exercise 6: Explain algorithm (separate submission)

Choose one machine learning algorithm that you want to learn more about. Create a short explanation of this algorithm using whatever media you prefer (text, video, slides, whiteboard, audio, stone carving).

Please share any good resources that you find in this mutual document.

https://docs.google.com/document/d/1AC4ULXd8sHEbw2M3u-tdkT0lvJylNvOjN7ojFg1NOQw/edit?usp=sharing

If you are new to machine learning, I recommend "K nearest neighbors" or "linear support vector machines" as good starting algorithms.

How to submit this part: This part of the assignment has a separate submission. This will serve as one of our learning check-offs. Please submit this on time if possible, since we'll probably be doing a peer review between Monday and Wednesday.

Multi-voxel pattern analysis on fMRI data [90 mins]

This is the fMRI data from one person (subject 2 in this study: <u>Haxby, J.V., Gobbini, M.I., Furey, M.L., Ishai, A., Schouten, J.L., Pietrini, P. (2001). Distributed and overlapping representations of faces and objects in ventral temporal cortex. Science, 293(5539):2425-30). There are 162 examples in the training set (these correspond to times where a person saw a house or a face). The labels tell you whether they were looking at a face or a house (same as last assignment). The data are linked at the top of this document.</u>

Think of the voxel values as the potential features. In the train_fmri3d data, the voxels are in a 3 dimensional array (that is 40 x 64 x 64), plus a 4th dimension that is the 162 examples. However, for the classifier, you need to reshape the data to a 2 dimensional array.

fmri2d=	sque	eze(r	eshap	e(tra	ain_fr	mri3d	,1,1,	[],16	2))'				
fmri2d =	162×16	3840 sir	ngle mat	rix									
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	

:

fmri2d has the dimensions of examples x voxels. However, we know that a bunch of these values are outside of the brain (since train_fmri3d is just a cube shape, and fun fact... our brains are not cube shaped).

If we wanted to make a variable that contained every voxel in the brain (but excluded those not in the brain), we can use our brain mask. The brain mask has 1s for voxels in the brain and 0s for voxels not in the brain. We need to reshape this to align with the shape of fmri2d.

Create a variable called brainvals that has the dimensions of (examples x voxels in the brain). Exercise 7: What are the actual dimensions of this variable (numbers)?

```
brainvals = fmri2d.*repmat(brainmask2d, [162 1])
brainvals = 162×163840 single matrix
                                                                                  0 ...
           0
                  0
                        0
                                     0
                                           0
                                                  0
                                                        0
                                                              0
                                                                     0
                                                                           0
     0
           0
                  0
                        0
                              0
                                     0
                                           0
                                                  0
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                                                                     0
                                                                           0
                                                                                  0
     0
           0
                  0
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                              0
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                                                              0
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                              Ω
                                     Ω
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                                                        0
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                                                                           0
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           0
                  0
                        0
                                           0
                                                  0
                                                                           0
                              0
                                     0
                                                        0
                                                              0
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     0
           0
                 0
                        0
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                              0
                                     0
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     0
           Ω
                 Ω
                        0
                              0
                                    0
                                           0
                                                 Ω
                                                        Ω
                                                              Ω
                                                                     Ω
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                                                                                  0
     0
           0
                0
                       0
                              0
                                    0
                                           0
                                                 0
                                                        0
                                                                           0
                                                                                  0
     0
           0
                  0
                       0
                              0
                                     0
                                           0
                                                  0
                                                        0
                                                                                  0
     0
           0
                  0
                                                                                  0
brainvals = brainvals( :, any(brainvals))
brainvals = 162×39912 single matrix
   45.1284 -26.6410 -42.3341 -15.2561 59.0485 -11.6695 -17.1604 -20.3824 ...
   41.1242 - 16.6047 - 36.3399 - 8.2558   63.0427 - 18.6882 - 23.0782 - 6.3803
   39.1200 \quad -22.5684 \quad -26.3456 \quad -1.2556 \quad 62.0368 \quad -20.7068 \quad -20.9959 \quad -12.3783
   39.1159 -15.5321 -31.3513 -10.2553 68.0310 -15.7255 -26.9137 -17.3762
   36.1117 - 24.4957 - 27.3571 - 4.2551 75.0251 - 7.7441 - 22.8314 - 15.3742
   48.1075 \quad -27.4594 \quad -32.3628 \quad -6.2549 \quad 77.0193 \quad -10.7627 \quad -21.7491 \quad -19.3722
   42.1034 -24.4231 -22.3686 0.7454 65.0134 -16.7814 -20.6669 -14.3701
   45.0992 -17.3868 -27.3743 -10.2544 68.0076 -15.8000 -23.5846 -11.3681
   40.0950 \quad -21.3505 \quad -19.3801 \quad -10.2542 \quad \  \  64.0017 \quad -14.8186 \quad -17.5024 \quad -18.3660
   31.9532 - 48.1158 - 42.5753 - 56.2460 \quad 36.8028 - 23.4524 - 26.7056 - 42.2967
```

162 x 39912

Dang, that's a lot of voxels! We could throw all of these voxels into our classifier, with each voxel serving as a feature. I would strongly recommend against this, why?

Think. Then highlight text below for answer

This may lead to overfitting our classifier. We have 162 examples and more than 30k variables.

Also, this will take forever to run and load.

Exercise (BIG ONE): Run multivoxel pattern analysis (machine learning on voxels).

Run classification of faces vs houses using some subset of voxels. Be sure to use cross-validation to help prevent overfitting.

For this part of the assignment, I'm asking you to piece together and extend some of the code that you've seen already. You can look at the brainViewer.mlx for more example code for selecting a subset of voxels from the data. You can look at fmriToFeaturesClassification for tips on how to implement the classifier using only code (though you'll still need to look up how to do cross validation). You are also welcome to use the classificationLearner app if you prefer.

You should explore different aspects of the feature space and document what you try and what you observed. Some things you might try:

- downsample the brain data to a smaller number of voxels randomly
- downsample the brain data to a smaller number of voxels by strategically selecting a brain region (you may still want to downsample within a region if it is big)
- use a dimensionality reduction technique such as PCA or ICA
- create new features that represent and summarize information about groups of voxels (this is like what we did by taking the average activity in each of the 4 regions, but you can get more creative if you want to)

Challenge: Choose some parameter to manipulate (e.g., # of nearest neighbors in KNN algorithm, or how many voxels to include). Generate a plot to represent the relationship between this parameter and a measure of how well your classifier performs (e.g., accuracy). Important tips (feel free to add some here or ask questions)

- As I mentioned in class, the ventral temporal lobe plays an important role in visual processing. One of the 4 regions that we explored before is the ventral temporal lobe.
- If you are using the Classification Learner, only use a table that has a reduced number of features already, otherwise, it will take forever to load the data. (My computer took several minutes to load a table that was 162 x 39913). For computational reasons, you'll probably want max out at around 1000 (but this depends on your computer.)
- Matlab is probably looking for your "predictors" (features) to be in a table. If you need to convert an array to a table, check out: array2table(brainvals).

- If you are using Matlab 2019, you'll need to take one additional step if you want to use the classificationLearner app. You must put the "responses" and the "predictors" in the same table.
- You can do this by following this general format: train_all = [table(train_labels) train_4regions]; In your version, you'll have a different variable than train_4regions.
- Or you can use something like this if you have an array:
- train_table2d = array2table(train_fmri2d); %
- train_table2d.labels = train_labels;

boxplot(region1')

• Other tips from students (you can add a comment here).

```
n = 162;
region1 = fmri2d.*repmat(single(reshape(mask_region1,1,[])), [n 1]);
region1 = region1( :, any(region1))
region1 = 162x334 single matrix
   44.8421 29.0900 88.2853 -23.1248 -0.8906 4.6762 25.0965 -6.1110 ...
   40.9222 27.1457 106.1361 -10.0830 7.1035 4.7111 23.0804 0.8875
   43.0023 \quad 30.2014 \quad 97.9869 \quad -24.0412 \quad -4.9025 \quad 0.7461 \quad 20.0644 \quad -5.1141
   41.0824 25.2571 97.8377 -16.9994 -0.9084 -0.2190 20.0483 -5.1156
   40.1625 26.3128 99.6885 -12.9575
                                                                 4.8159 23.0322
                                                                                        -6.1171
                                                    6.0856

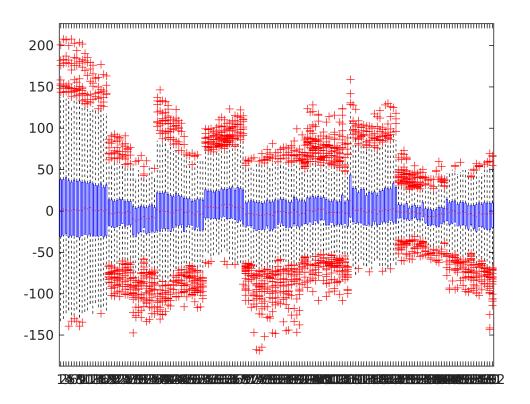
    24.3685
    96.5393
    -18.9157
    2.0796
    2.8509
    19.0162

    26.4242
    82.3901
    -20.8739
    0.0737
    1.8858
    22.0001

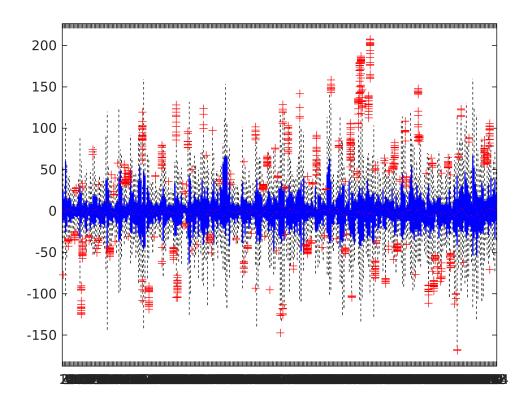
    27.4799
    90.2409
    -20.8321
    -2.9323
    0.9207
    17.9841

    22.5356
    86.0917
    -21.7903
    0.0618
    3.9556
    20.9680

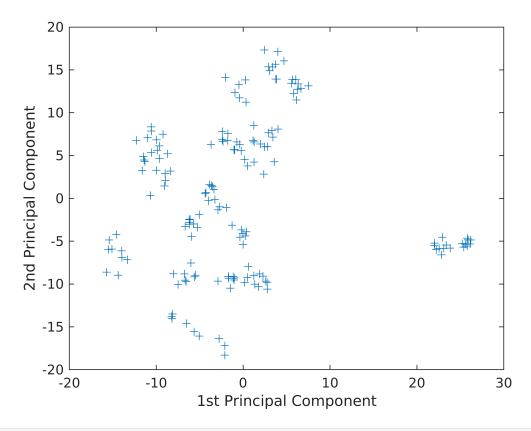
                                                               2.8509 19.0162
   40.2426
                                                                                         -8.1186
   49.3227
                                                                                         -2.1201
   46.4028
                                                                                         -4.1216
   41.4829
                                                                                         -5.1231
   42.2065 26.4295 70.0187 -19.3685 0.8591 1.1433 18.4219 -2.1741
% boxplot by sample
```



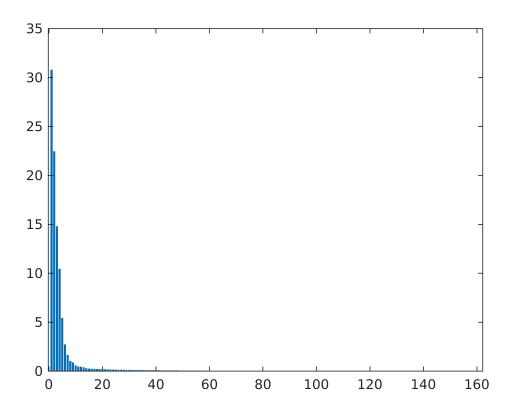
% boxplot by feature boxplot(region1)



```
%corr(region1,region1);
[wcoeff,score,latent,~,explained] = pca(region1,'VariableWeights','variance');
figure()
plot(score(:,1),score(:,2),'+')
xlabel('1st Principal Component')
ylabel('2nd Principal Component')
```



```
figure()
bar(explained)
```



```
region1 = fmri2d.*repmat(single(reshape(mask_region1,1,[])), [n 1]);
region1 = region1( :, any(region1));
region2 = fmri2d.*repmat(single(reshape(mask_region2,1,[])), [n 1]);
region2 = region2( :, any(region2));
region3 = fmri2d.*repmat(single(reshape(mask_region3,1,[])), [n 1]);
region3 = region3( :, any(region3));
region4 = fmri2d.*repmat(single(reshape(mask_region4,1,[])), [n 1]);
region4 = region4( :, any(region4));
[wcoeff1,score1,latent1,~,explained1] = pca(region1);
[wcoeff2,score2,latent2,~,explained2] = pca(region2);
```

Warning: Columns of X are linearly dependent to within machine precision. Using only the first 155 components to compute TSQUARED.

```
[wcoeff3,score3,latent3,~,explained3] = pca(region3);
[wcoeff4,score4,latent4,~,explained4] = pca(region4);
explained1 % first 7
```

```
explained1 = 161×1 single column vector

36.2376

23.9686

15.8495

10.7287

4.2774

1.8731

1.1529

0.7581
```

```
0.5554
   0.4024
explained2 % first 8
explained2 = 161x1 single column vector
  43.1001
  19.9416
   9.8243
   7.8444
   3.7835
   2.1081
   1.6599
   1.2185
   0.7526
   0.5982
explained3 % first 9
explained3 = 161×1 single column vector
  30.9446
  19.2588
  14.2063
   5.7947
   4.4339
   3.8011
   2.8119
   1.3967
   1.0155
   0.9470
explained4 % first 8
explained4 = 31x1 single column vector
  52.1313
  15.8923
  10.1483
   7.3441
   3.6160
   2.2814
   1.6386
   1.3586
   0.9103
   0.7898
region1_10 = score1(:, 1:10)
region1_10 = 162 \times 10 \text{ single matrix}
 882.2699 -249.0720 -17.4099
                               99.1775
                                                                         36.6531 ...
                                           28.8254 -62.8130 -19.3104
 870.9958 -238.3671
                     0.1133 148.2624
                                           38.4298 -62.0343 -25.2092
                                                                         43.2560
 884.9216 -229.5898 22.2092 141.0955
                                           41.0693 -65.1118 -37.8074
                                                                         31.4339
 873.9255 -247.0448 -16.7304 142.4166
                                           22.6208 -67.9866 -21.6513
                                                                         26.2031
```

39.1652 -76.4831 -13.2179

27.8672

855.6765 -251.0692 -18.9221 132.2741

```
876.3199 -230.3638 3.4694 128.8664 34.3494 -67.4803 -25.3893 27.2125
 866.0078 -256.0186 6.7014 100.1808 11.7942 -53.0865 -13.0122 30.2270
 877.5620 -243.5495 -17.7944 103.2499 27.9399 -76.0061 -16.4831 19.0183
 857.6501 -264.7130 -24.1600 118.0704 13.0859 -61.9725 -11.5007
                                                                   23.3495
 809.6169 -261.3054 67.0503 88.7841 25.6060 -41.0882 -6.1224 11.0350
region2 10 = score2(:, 1:10)
region2_10 = 162×10 single matrix
                                                         36.5739 -11.0019 • • •
 500.3787 -17.8039
                   53.0067 -63.0664 -6.9085 -30.1563
 476.8148 -18.8309 38.2953 -64.6518 -12.3547
                                               -7.2812 24.9917 1.2449
 474.8785 -14.6288 43.4600 -61.0633 -21.0159 -10.7514 29.6061 -0.8047
 491.4526 -25.5925 48.6052 -56.0446 -13.0624 -5.6371
                                                        27.1252 -6.8921
 474.1767 -13.9762 48.3750 -63.4748 -13.0364 -5.8352 31.7320 7.9991
                                                        30.9382 -18.9955
 487.9001 -23.4758 43.8801 -59.3961 -15.3894 -26.1054
 490.4452 -26.3618 42.5140 -63.7428 3.0023 -41.1618
                                                        27.9324 -19.6379
 486.4983 -28.6231 48.3556 -61.0351 3.5750 -55.3451
                                                        30.2215 -16.7835
 504.4672 -30.7581 48.3434 -55.0466 -9.9613 -31.1667
                                                         20.1318 -13.8631
 440.9283 -11.7494 18.2610 -34.5127 16.9274 -35.4605
                                                         -2.2187 -16.8447
region3_10 = score3(:, 1:10)
region3_10 = 162 \times 10 single matrix
-602.9750 4.3032 -267.0129
                             -3.7728 \quad -27.3058 \quad -29.2039
                                                         46.4935 51.0825 • • •
-606.9026 16.3646 -247.8228 39.7788 -34.4314 -10.7661
                                                        16.0021
                                                                   4.3593
-597.9197 -5.4570 -248.6415
                                                        44.4269 22.7052
                            19.6119 -34.7483 -12.5068
-600.8988 -15.2894 -242.4704
                              3.1686 -50.0556 -32.8292
                                                        36.7889
                                                                   22.3156
          8.3663 -244.7362
                              10.9536 -52.8146 -28.6015
                                                        41.1013
-610.7221
                                                                   8.9603
-605.3700 -13.4790 -243.7588
                              11.9757 -54.5816 -40.2087
                                                                   3.9702
                                                         64.9597
                              5.8671 -11.7410
 -569.9920
           2.7016 -245.7481
                                               -29.9437
                                                         26.8847
                                                                  18.8572
          -5.5146 -248.1978
 -587.5948
                              27.1901
                                      -25.3469
                                               -60.6531
                                                         52.7184
                                                                  -30.1970
                              24.3634 -29.9500
 -583.7650 -48.5553 -213.8648
                                               -65.3586
                                                          76.7826
                                                                   -1.7185
 -477.6545 -20.4015 -156.0078
                             -1.0636
                                      58.3452 -51.4016 -21.7912
                                                                   35.6059
region4_10 = score4(:, 1:10)
region4_10 = 162 \times 10  single matrix
 -200.7725 -88.9944
                                                                   -5.7794 • • •
                     66.3656
                              30.2970
                                        7.5523
                                                 2.0962
                                                         -5.4538
 -142.5894 -25.5757
                   128.2361
                              46.4931
                                               -10.7303
                                                        -28.3200
                                                                   9.1455
                                       -6.5584
-169.1275
          -21.1523
                   101.0748
                              87.2609 -56.4232
                                                12.0617
                                                          2.9201
                                                                   9.8378
-190.8640
          -79.1459
                    77.3002
                              28.7072
                                       -4.2127
                                                -0.5531
                                                          6.3055
                                                                   -0.1726
-185.5584 -79.0591
                    91.0915
                              35.9461
                                       -4.6241
                                                -1.3296
                                                          8.1930
                                                                   -6.1525
                                                                  -0.2712
-185.4122 -76.7435
                    78.5448
                              24.6691
                                       -6.5634
                                                6.8628
                                                         -1.1384
                             43.4277
                                       -8.1264
-197.2589 -59.4490
                    74.7602
                                                -1.1025 -22.3357
                                                                   6.4737
                                                         1.7366 -11.4634
                              28.4065 -20.0961
-207.4717 -75.2307
                    78.9758
                                                -1.3167
-212.6579 -75.7360
                    71.7959
                              24.7281 -7.0967
                                                -1.8303
                                                         10.4450 -1.5655
 -230.9032 -86.6549
                    53.2212
                             31.3413 -8.3701
                                                 1.6614 -15.4309 10.1136
chosen_features = [region1_10 region2_10 region3_10 region4_10]
```

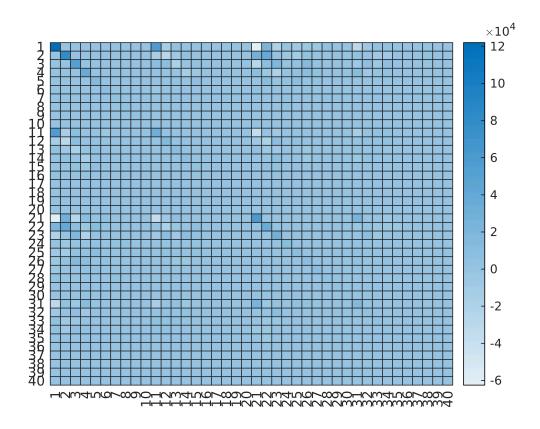
```
chosen_features = 162x40 single matrix
 882.2699 -249.0720 -17.4099
                                 99.1775
                                           28.8254 -62.8130 -19.3104
                                                                          36.6531 • • •
 870.9958 -238.3671
                       0.1133 148.2624
                                           38.4298
                                                    -62.0343 -25.2092
                                                                          43.2560
```

```
884.9216 -229.5898 22.2092 141.0955
                                    41.0693 -65.1118 -37.8074
                                                                31.4339
873.9255 -247.0448 -16.7304 142.4166 22.6208 -67.9866 -21.6513
                                                                26.2031
855.6765 -251.0692 -18.9221 132.2741 39.1652 -76.4831 -13.2179
                                                                27.8672
                 3.4694 128.8664 34.3494 -67.4803 -25.3893
876.3199 -230.3638
                                                                27.2125
866.0078 -256.0186
                 6.7014 100.1808 11.7942 -53.0865 -13.0122
                                                                30.2270
877.5620 -243.5495 -17.7944 103.2499 27.9399 -76.0061 -16.4831
                                                                19.0183
857.6501 -264.7130 -24.1600 118.0704
                                     13.0859 -61.9725 -11.5007
                                                                23.3495
809.6169 -261.3054 67.0503
                           88.7841
                                     25.6060 -41.0882
                                                      -6.1224
                                                                11.0350
```

covmat = cov(chosen_features)

```
covmat = 40 \times 40 \text{ single matrix}
                                                   Rows 27:36 | Columns 1:15
10<sup>5</sup> ×
   -0.0276
             -0.0107
                        0.0130
                                  0.0268
                                              0.0363
                                                        0.0037
                                                                   0.0034
                                                                              0.0002
                       -0.0071
                                  -0.0048
                                                                             -0.0047
    0.0228
             -0.0080
                                             -0.0031
                                                        0.0075
                                                                   0.0177
    0.0054
              0.0144
                        0.0054
                                   0.0026
                                             -0.0097
                                                       -0.0159
                                                                   0.0093
                                                                             0.0036
    0.0097
             -0.0108
                       -0.0100
                                  -0.0027
                                             0.0098
                                                                   0.0036
                                                                             0.0020
                                                        0.0106
   -0.3138
              0.0361
                        -0.0614
                                   0.1048
                                              0.0101
                                                        0.0108
                                                                   0.0049
                                                                             0.0071
   -0.0736
             -0.0181
                         0.0517
                                  -0.0632
                                             -0.0173
                                                        0.0116
                                                                  -0.0071
                                                                             -0.0021
    0.0437
             -0.0746
                       -0.0543
                                   0.0153
                                             -0.0018
                                                       -0.0030
                                                                  -0.0115
                                                                             0.0004
    0.0163
             -0.0638
                         0.0482
                                   0.0387
                                             -0.0093
                                                       -0.0024
                                                                   0.0020
                                                                            -0.0006
             -0.0192
   -0.0061
                       -0.0226
                                   0.0013
                                             -0.0210
                                                        0.0054
                                                                   0.0038
                                                                            -0.0029
   -0.0104
             -0.0005
                        -0.0028
                                  -0.0094
                                             -0.0153
                                                       -0.0013
                                                                  -0.0014
                                                                             0.0054
```

figure(); heatmap(covmat)



After doing PCA and choosing the top 10 features from each region (after the first 10 features the explained variance < 1), I got a reduced feature set of 40 features.

Model	Accuracy
Fine Tree	88.9%
Medium Tree	88.9%
Coarse Tree	89.5%
Fine KNN	98.1% < pretty good training accuracy
Medium KNN	88.9%

Brains on Trial [120 minutes]

Watch this video or read this paper and think about the prompts below.

- Brains on Trial 1 (60 minutes): https://www.youtube.com/watch?v=o0eSqlAmKxU
- Neuroimaging and lie detection paper: https://drive.google.com/open?id=1V9YiLcl82VtDBnQLG_0-LT87tdW2D5tM

Other suggested resources if you want more of this:

- Brains on Trial: Part 2: https://www.youtube.com/watch?v=_cBK_fgTZvk
- Law, Responsibility, and the Brain paper: https://drive.google.com/file/d/1P-AoQPkPbp2EjC6u9LD-IXqgPjoRrChR/view?usp=sharing

Prompt to start thinking about prior to class discussion:

How would you **go about determining** if a future, more accurate, version of brain-based lie detection technology should be permissible in the American justice system and in what situations?

What information would you want? (How realistic is it to obtain this information?) What groups would you need to consider? What measurements of tool effectiveness would you want to see (and under what conditions)? What social and societal implications should you consider?

You should write notes on the video and the prompt. You can either submit them (I would enjoy reading them), or write a note that you did this (what an appropriately themed use of the honor code!).

Gati's Notes

- A jury is like a pooled decision maker
- I would want the data tested and fine-tuned to each individual
- I would want all the jurors and judge to know the short-comings of the technology (how do you make sure they listen and understand?)
- I would want masking techniques and adversarial patterns to be less effective