

Lecture 2:



Wiss example:

$n = 124$

$80 : R$

x_1, \dots, x_n

$$x_i = \begin{cases} 1 \\ 0 \end{cases}$$

ith couple
turn right
o.w.

$$\frac{80}{124} = 0.695$$

$x_i \stackrel{\text{iid}}{\sim} \text{Ber}(p)$

$$\frac{x_1 + \dots + x_n}{n} = \bar{x}_n$$

Let's assume $p = 1/2$.

$$\begin{aligned} P(\bar{x}_n \geq 0.695) &= P\left(\sum x_i \geq 0.695 \cdot n\right) \\ &\sim \text{Bin}(n, p) \end{aligned}$$

Use CLT (Central Limit Thm) \rightarrow need to know μ & σ .

$$x_i = \begin{cases} 1 \text{ w/ prob } p \\ 0 \text{ w/ prob } 1-p \end{cases}$$

$$\mathbb{E}[\bar{x}_n] = p$$

$$\mathbb{V}[\bar{x}_n] = \frac{\mathbb{V}[x_i]}{n} = \frac{p(1-p)}{n}$$

$$\frac{\bar{x}_n - \mu}{\sigma/\sqrt{n}} \rightsquigarrow N(0, 1)$$

$\sqrt{V(x)}$

$$P(\bar{x}_n \geq 0.695) = P(\bar{x}_n - \mu \geq 0.695 - \mu)$$

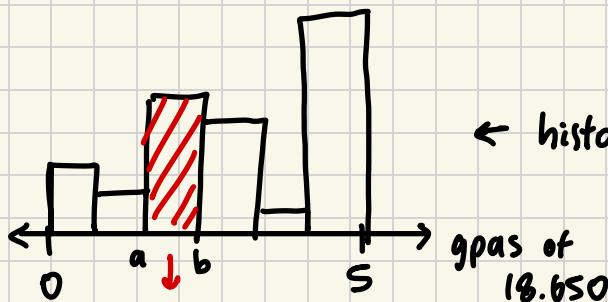
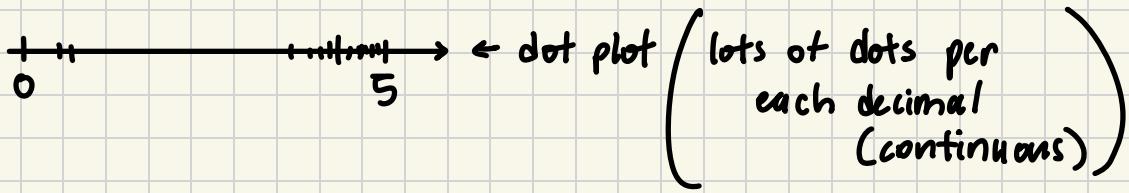
$$= P\left(\frac{\bar{x}_n - \mu}{\sigma/\sqrt{n}} \geq \frac{0.695 - \mu}{\sigma/\sqrt{n}}\right) = P\left(Z > \frac{0.695 - \mu}{\sigma/\sqrt{n}}\right)$$

where $Z \sim N(0, 1)$.

$$= 0.003.$$

p score.

X_1, \dots, X_{233}



area

= proportion of data that is in the bin.

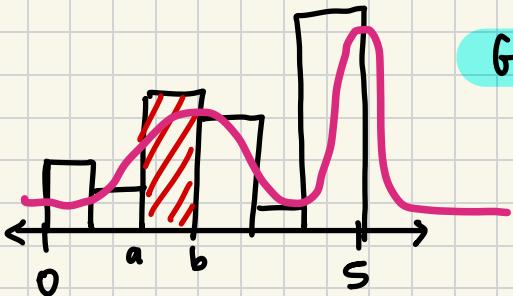
$$\text{area} = \frac{1}{n} \sum_{i=1}^n \mathbb{1}(\alpha \leq x_i < \beta) \rightarrow \begin{array}{l} (b-a) \text{ height} = \text{prop.} \\ h = \frac{\text{prop.}}{b-a} \end{array}$$

↓
add if in range

* histogram readability depends on def. of intervals.

Gaussian = getting curve out of histogram.

KDE

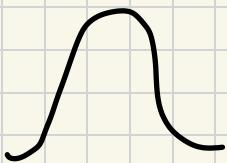
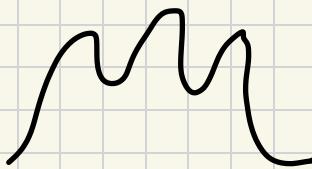
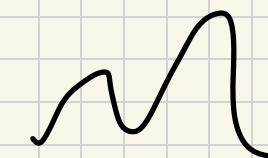
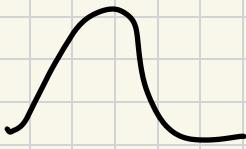


Analyzing graphs:

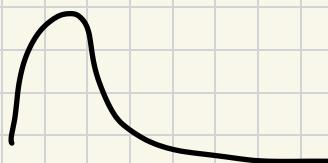
unimodal

bimodal

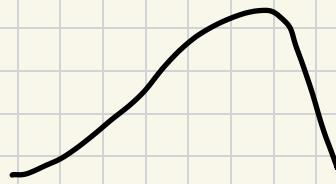
multi modal



symmetric



right-skewed
(prior of houses,
income)



left-skewed
(gpa, hopefully)

* mean (average, μ)

* standard deviation (std, σ)

* median $\rightarrow \frac{1}{n} \sum \mathbb{1} (x_i \leq \text{median}) = \frac{1}{2}$

* range

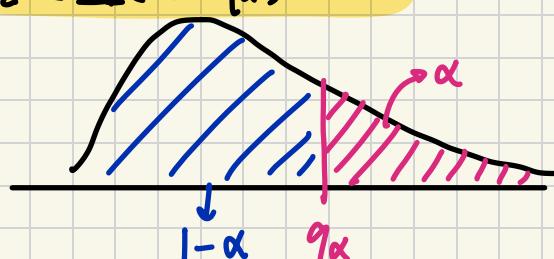
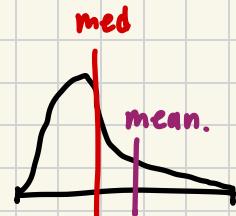
* quantiles : $q_\alpha = (1-\alpha)$ quantile = $100(1-\alpha)$ percentile

$$\frac{1}{2} \sum \mathbb{1} (x_i \leq q_\alpha) = 1-\alpha$$

$$1^{\text{st}} \text{ quartile} = q_{3/4}$$

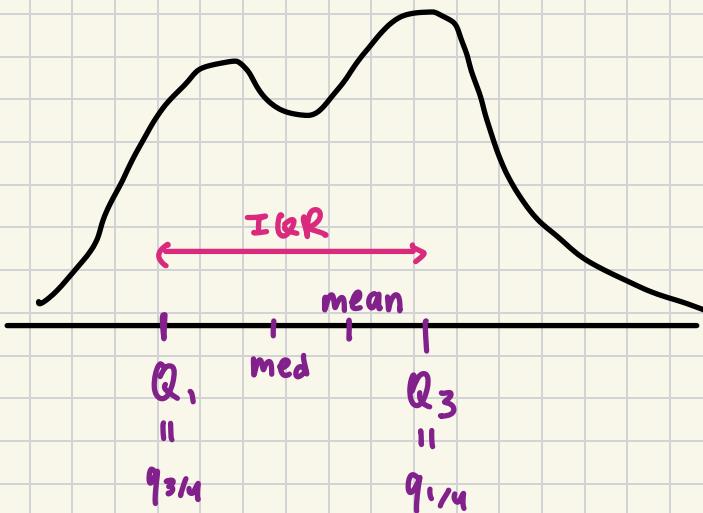
$$\text{third quartile} = q_{1/4}$$

$$\text{IQR} = Q_3 - Q_1, \quad (\text{interquartile range})$$



Mean vs med.

- mean is not robust bc 1 bad pt. can ruin whole mean.
- med, Q_1 , Q_3 , IQR are more robust bc they are not impeded by outliers



x_i is outlier if $x_i > Q_3 + 1.5 \text{ IQR}$
or $x_i < Q_1 - 1.5 \text{ IQR}$