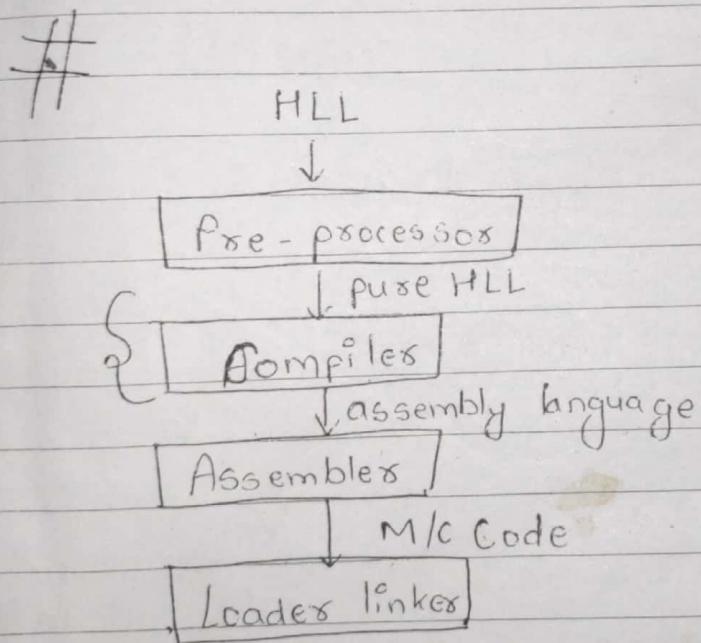
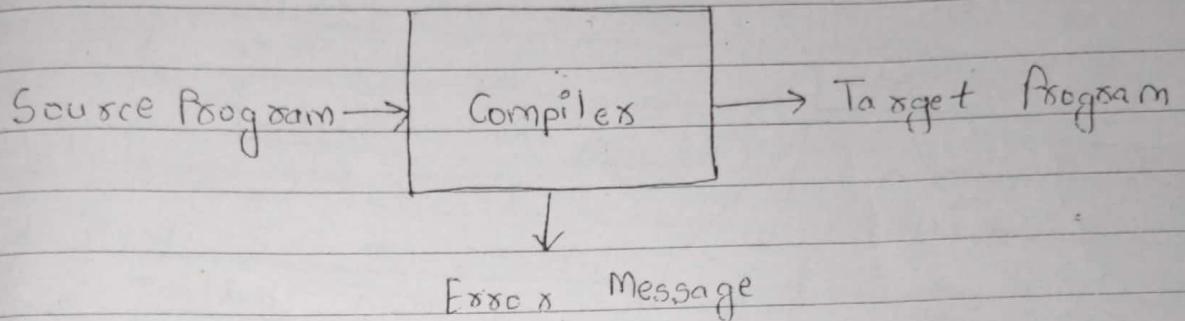


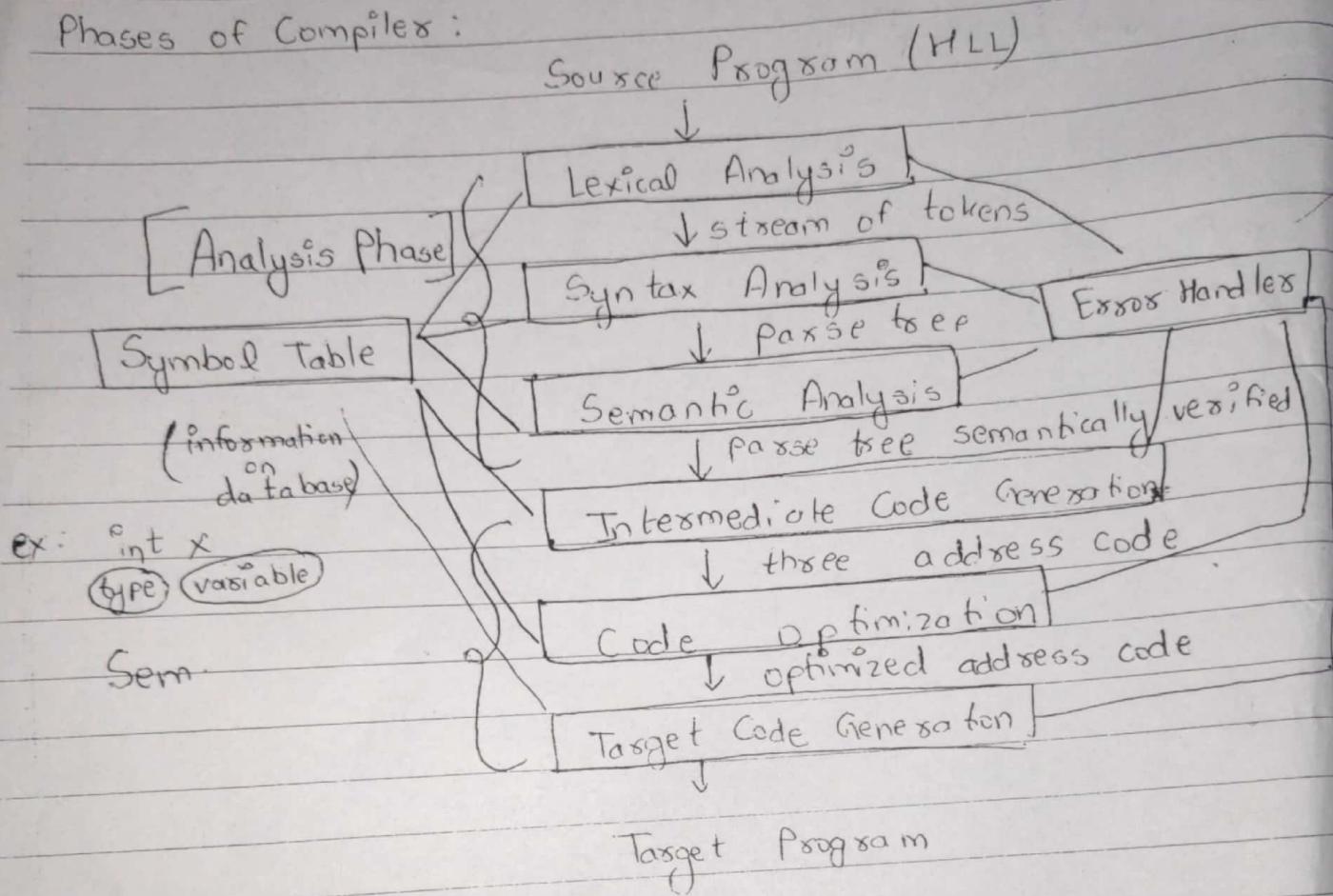
Q 4) what is compiler?

↪ A compiler is a program that takes a program written in a source language and translates it into an equivalent program in a target language.



V.V.V. Imp

Phases of Compiler:



Useless Grammars

Context-free Grammars: $V \cap P \subseteq S$

Defⁿ: CFG consisting of a finite set of grammars rules P is a quadruple (V, T, P, S)

variable terminal Production Start

where,

ex: $S \rightarrow OSO \quad | \quad 1S1$

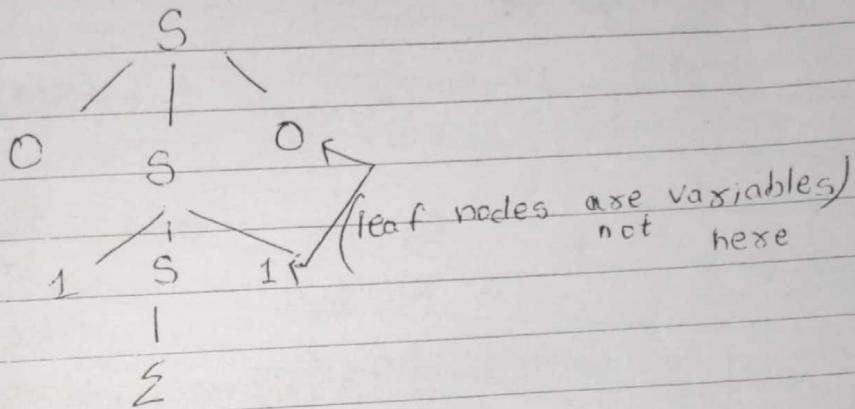
$\rightarrow O1S1O \quad | \quad$ $V = \text{variable}$

$\rightarrow O11O \quad | \quad T = \text{set of terminals}$

$S = \text{start symbol}$

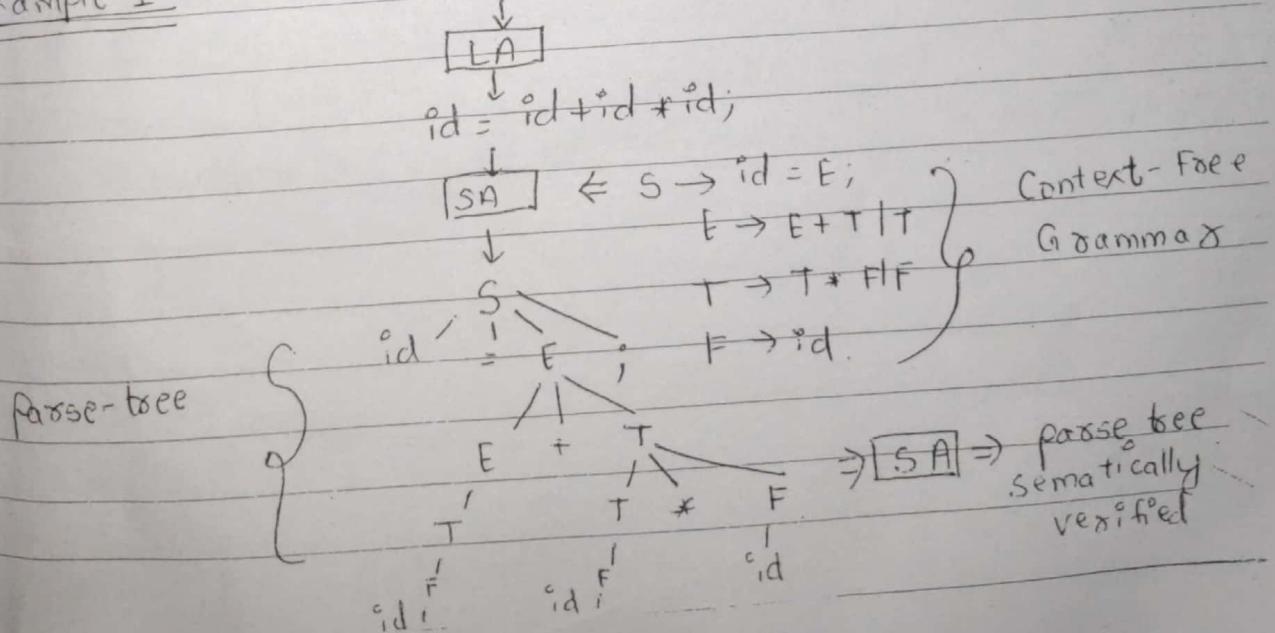
$P = \text{set of rules, left side of production}$

Parse Tree:



Example 1:

$$H = a + b * c;$$



I CG

$$t_3 = b * c;$$

$$t_2 = a + t_1;$$

$$x = t_2;$$

Preference

o/e / *

+ -

Code Optimization



$$t_1 = b * c;$$

$$x \cancel{=} t_1 = a + t_1;$$



T CG

(Target code Generation)



mul R₁, R₂ as; a → R₀

add R₀, R₂

b → R₁ [Registers]

mov R₂, X

c → R₂

(memory address)

Symbol Table :

A symbol table stores information about keywords and tokens found during Lexical Analysis.

The symbol table is consulted on almost all phases of compilation.

For ex : `insert ("dist", id);`

// insert a symbol table entry associating the string "dist" with token type - id.

`look up ("dist");`

// an occurrence of the string "dist" can be looked up in the symbol table. If found, a reference to its token type is returned. Else, look up returns zero.

Error Handling :

1. Errors may encounter at any phase of compilation.

The objective of Error Handling is to go as far as possible in the compilation whenever an error is encountered.

For ex : ① Handling missing symbols during Lexical Analysis by inserting Symbols.
(preference for symbolic errors)

② Automatic type conversion during Semantic Analysis

CHAPTER - 2

(Space — isn't used as a token)

Lexical Analysis

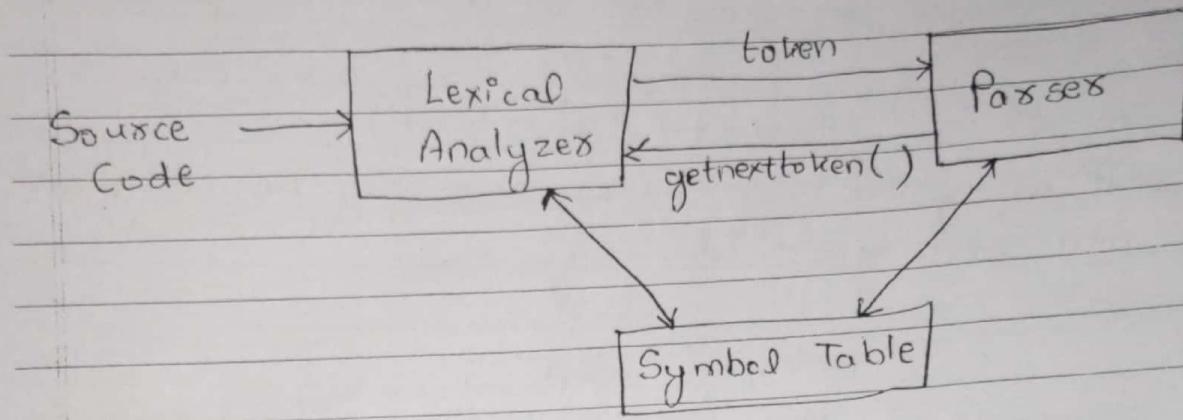
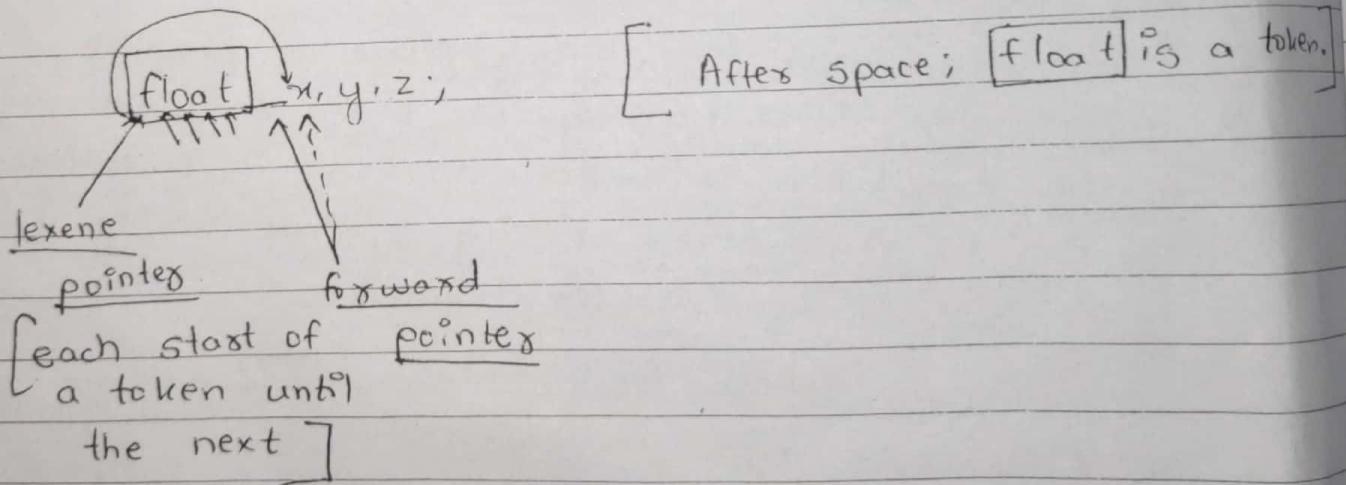


Fig : Interaction of Lexical Analyzer with parser

Look ahead and Buffering



Specification of Tokens:

1) Alphabets : A finite set of symbols (a, b, c...z)

2) String : A finite set of alphabets.

$$\Sigma^* = \{a, \dots z\}$$

$$L = \{bba, abb, can, dog, \dots\}$$

3) Kleen Closure :

$$\Sigma = \{a, b\}$$

$$\hookrightarrow \Sigma^* = \{\epsilon, a, b, aa, ab, ba, bb, \dots\}$$

4) Language : Collection of string
(selected strings from Kleen closure)

$$L \subseteq \Sigma^*$$

5) Regular Expression:-

$$\Sigma = \{0, 1\}$$

① Starting with zero; ending with 1:

$$0(1+0)^*1$$

or;

$$0 \Sigma^* 1$$

[Regular Language are accepted by Finite Automata]
(Regular Language are accepted by Finite Automata)
and
are Expressed by Regular Expression.

• Binary numbers multiple of 2:

$$[2, 4, 6, 8, 10 \dots]$$

$$\{10, 110, 100, 1000, \dots\}$$

i.e. $\Sigma^* 0$ → Must be 0 at the end and ahead of 0 any amount of number can be.

(Regular Expressions)

Q. R.E that gives binary strings having at most two 1's.

$$\Sigma = \{0, 1\}$$

$$0^*(1+0) \ 0^*(1+0) \ 0^*$$

$$L = \{0, 1, 11, 01, 10, 010, 001, 100, 0100, 1000, 01001, 010100, \dots\}$$

$$\boxed{L \rightarrow (0^* + 0^* 1 0^* + 0^* 1 0^* 1 0^*)}$$

$$\text{as; } 0^* = \{\epsilon, 0, 00, 000, \dots\}$$

Language

Q. R.E for string containing single 1.

$$\boxed{0^* 1 0^*}$$

L = collection of strings

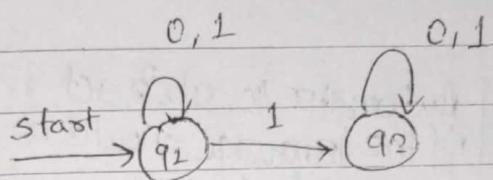
$$= \{1, 01, 10, 010, 0001, 000100000, \dots\}$$

Q. R.E string containing at least single 1.

$$L = \{ 1, 001, 010, 0110, 011100, \dots \}$$

$$0^* 1 0^* + 0^* 1^* 0^* \quad \times$$

$$\hookrightarrow [\Sigma^* 1 \Sigma^*] \quad \checkmark$$



Q. Contains the string 001 as substring:

$$\Sigma^* 001 \Sigma^*$$

Q. String with exactly 3 ones:

$$0^* \underline{1} 0^* \underline{1} 0^* \underline{1} 0^*$$

Q. String that have substring either 001 or 100

$$\Sigma^* 001 \Sigma^* + \Sigma^* 100 \Sigma^*$$

$$\hookrightarrow \Sigma^* (001 + 100) \Sigma^*$$

Q. R.E for the string ending with 11.

$\Sigma^* 11$

Q. R.E for identifying C identifiers :
denoting identifiers

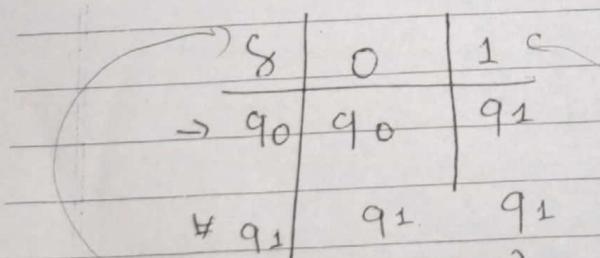
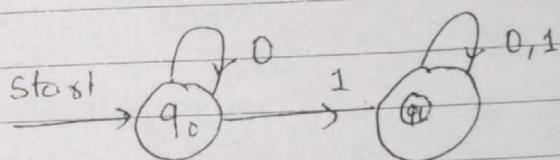
$$(\text{Alphabet} + _) (\text{Alphabet} + \text{digit} + _)^*$$

\downarrow

a-z
A-Z

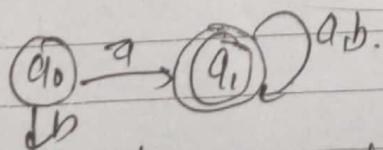
Finite Automata [Automata is abstract model that tells if the language should be accepted or not]

1) D.F.A (Deterministic Finite Automata)



DFA: on applying certain string one state goes to any other particular state.

2) start with a/b or $\Sigma(a/b)$

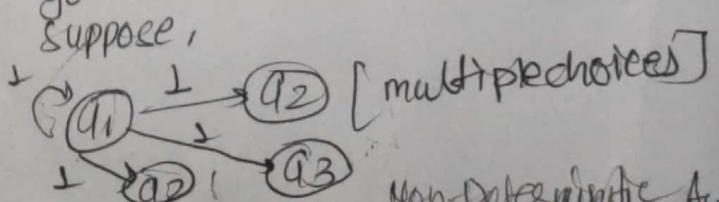


(q1) a/b → this is dead state so that we don't

① → set of finite states
 Σ → set of alphabets (0,1)
 δ → transition
 q_0 → start
 f → set of final states

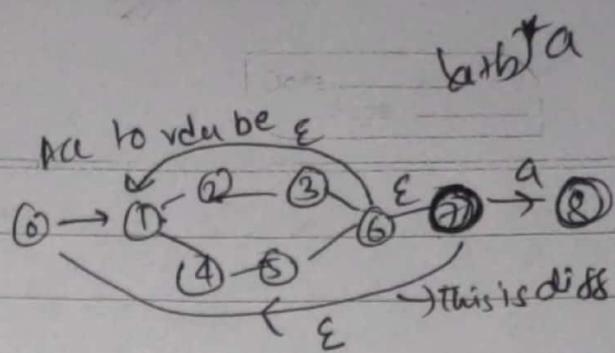
Σ	0	a	b
q_0	q_1	q_2 (dead state)	
q_1	q_1	q_1	
q_2	q_2		q_2

NFA: on applying string on state it may go to one or multiple state.



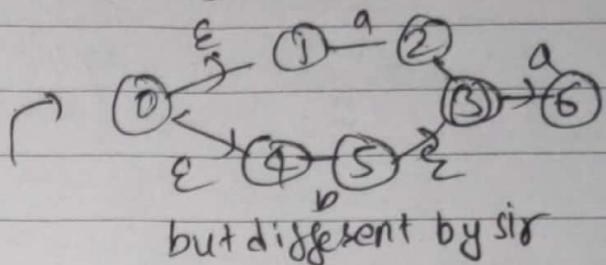
Non-Deterministic Automata

Reducibility



- 1) NFA to DFA
- 2) RE to NFA
- 3) RE to DFA

acc to geekforgeeks.
 $(a+b)^*$ a is

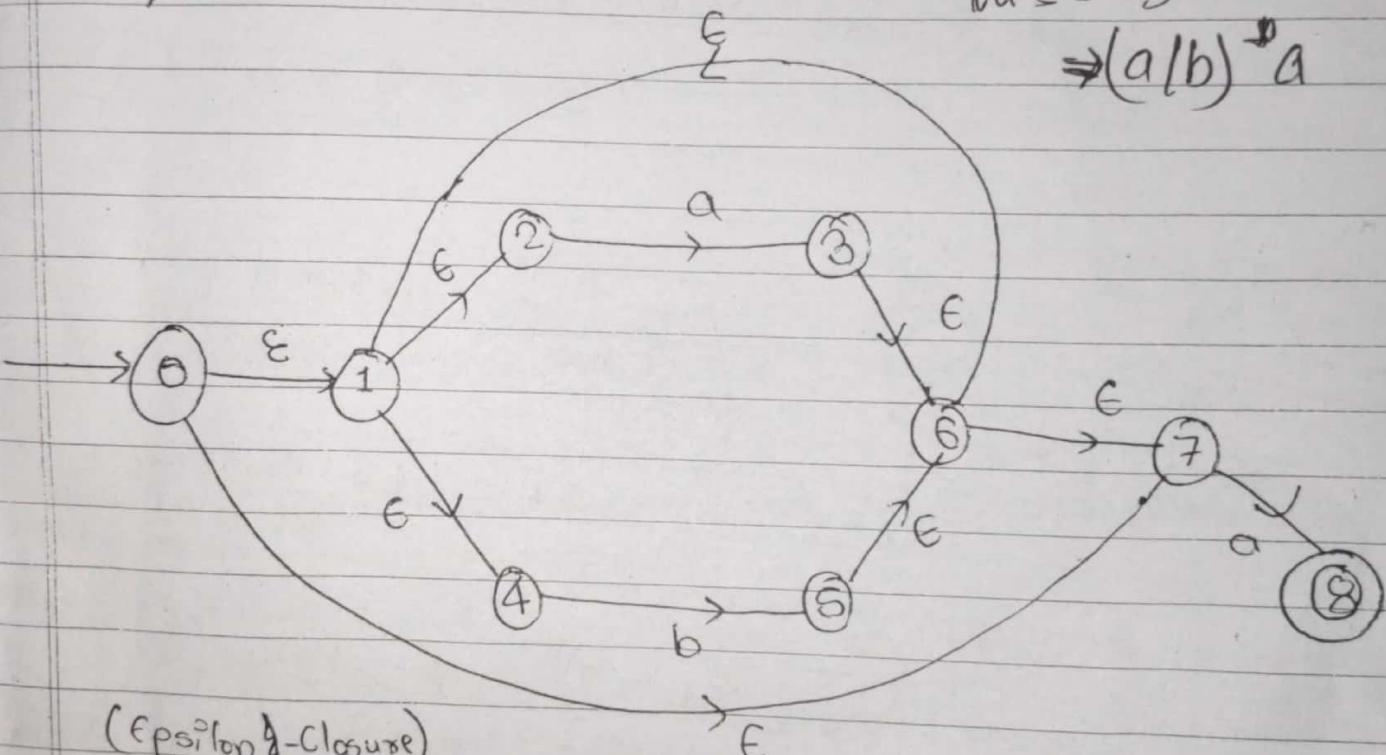


- 1) N.F.A to D.F.A (subset construction)

\Rightarrow

this is reg expression for a figure

$$\Rightarrow (a/b)^* a$$



(ϵ -closure)

ϵ -closure of state 1 = {1, 2, 4}

ϵ -closure of state 0 = {0, 1, 2, 4, 7}

ϵ -closure of state 2 = {2, 3}

→ 1) N.F.A to D.F.A (subset construction)

⇒ From above fig:

$$S_0 = \epsilon\text{-closure}(\{0\}) = \{0, 1, 2, 4, 7\}$$

Mark S₀

$$\epsilon\text{-closure}(\text{move}(S_0, a)) = \epsilon\text{-closure}(3, 8)$$

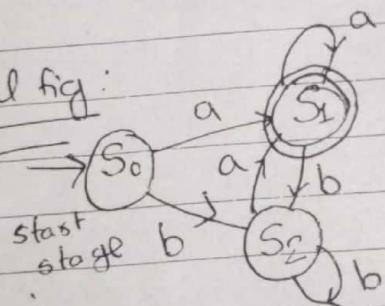
$$= \{3, 6, 7, 1, 2, 4, 8\} - a \rightarrow ?$$

$$= S_1$$

$$\epsilon\text{-closure}(\text{move}(S_0, b)) = \epsilon\text{-closure}(5)$$

$$= \{5, 6, 7, 1, 2, 4\} = S_2$$

Final fig:



(Brief version of above figure)

If bba then we can get to the final state

Mark S₁

$$\epsilon\text{-closure}(\text{move}(S_1, a)) = \epsilon\text{-closure}(8, 3)$$

$$= S_1$$

$$\epsilon\text{-closure}(\text{move}(S_1, b)) = \epsilon\text{-closure}(5)$$

$$= S_2$$

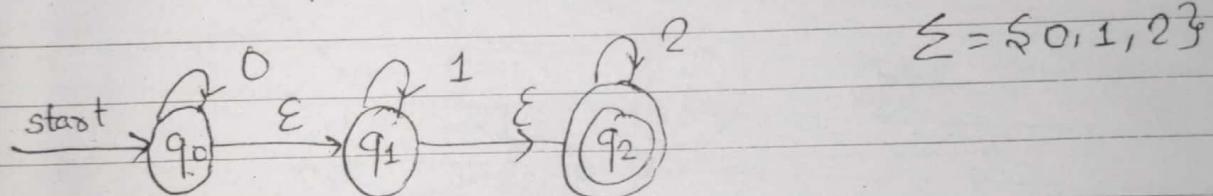
Mark S2

$$\begin{aligned}\epsilon\text{-closure}(\text{move}(S_2, a)) &= \epsilon\text{-closure}(q_3) \\ &= S_1\end{aligned}$$

$$\begin{aligned}\epsilon\text{-closure}(\text{move}(S_2, b)) &= \epsilon\text{-closure}(q_5) \\ &= S_2\end{aligned}$$

↳ Those which have \textcircled{B} are final states: $S_1 = \{q_3, q_7, q_1, q_2, q_8\}$

Start state $\rightarrow \textcircled{0} \quad S_0; \quad S_0 \#$



$$S_0 = \epsilon\text{-closure}(\{q_0\}) = \{q_0, q_1, q_2\}$$

Mark S0:

$$\begin{aligned}\epsilon\text{-closure}(\text{move}(S_0, 1)) &= \epsilon\{q_1\} = S_2 = \{q_1, q_2\} \\ \epsilon\text{-closure}(\text{move}(S_0, 0)) &= \epsilon\{q_0\} = S_0 = \{q_0, q_1, q_2\} \\ \epsilon\text{-closure}(\text{move}(S_0, 2)) &= \epsilon\{q_2\} = S_3 = \{q_2\}\end{aligned}$$

Mark S1:

$$\begin{aligned}\epsilon\text{-closure}(\text{move}(S_1, 0)) &= \epsilon\{q_0\} = S_0 = \{q_0, q_1, q_2\} \\ \epsilon\text{-closure}(\text{move}(S_1, 1)) &= \{q_3\} / \emptyset \\ \epsilon\text{-closure}(\text{move}(S_1, 2)) &= \{q_3\} / \emptyset\end{aligned}$$

Mark S_0 :

$$\epsilon\text{-closure } (\text{move}(S_2, 0)) = \emptyset$$

$$\epsilon\text{-closure } (\text{move}(S_2, 1)) = \epsilon \{q_1\} = S_2 = \{q_1\}$$

$$\epsilon\text{-closure } (\text{move}(S_2, 2)) = \emptyset$$

Mark S_3 :

$$\epsilon\text{-closure } (\text{move}(S_3, 0)) = \emptyset$$

$$\epsilon\text{-closure } (\text{move}(S_3, 1)) = \emptyset$$

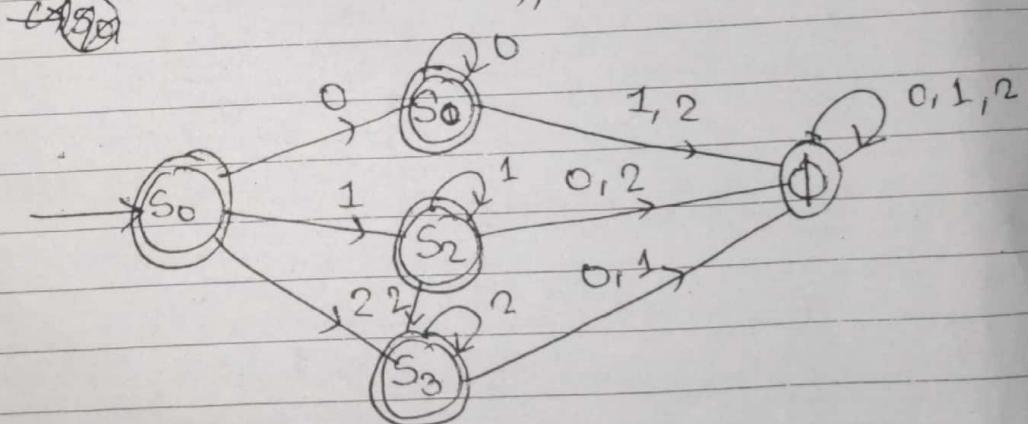
$$\epsilon\text{-closure } (\text{move}(S_3, 2)) = \epsilon \{q_2\} = S_3 = \{q_2\}$$

Mark \emptyset :

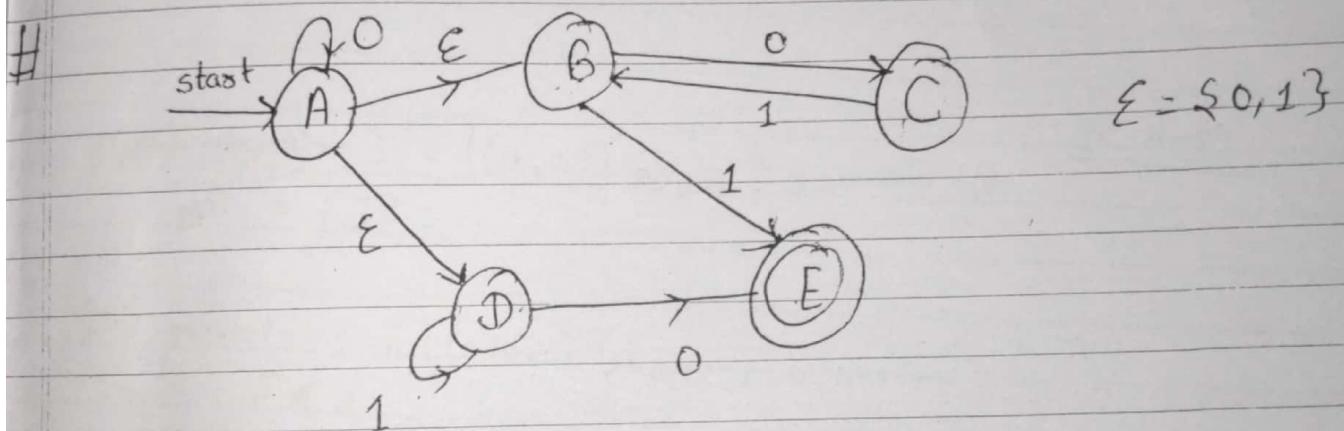
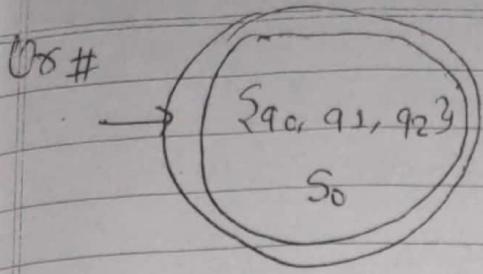
$$\epsilon\text{-closure } (\text{move}(\emptyset, \underline{0}, \underline{1}, \underline{2})) = \emptyset$$

"

"



Final state consists $\circled{q_2}$: S_3 and S_0



$\# S_0 = \epsilon\text{-closure } (\{A\}) = \{A, B, D\}$

Mark S_0

$$\begin{aligned}\epsilon\text{-closure } (\text{move } (S_0, 0)) &= \epsilon\text{-closure } (A, C, E) \\ &= \{A, B, D, C, E\} \\ &= S_1\end{aligned}$$

$$\begin{aligned}\epsilon\text{-closure } (\text{move } (S_0, 1)) &= \epsilon\text{-closure } (E, D) \\ &= \{E, D\} \\ &= S_2\end{aligned}$$

Mark S₁:

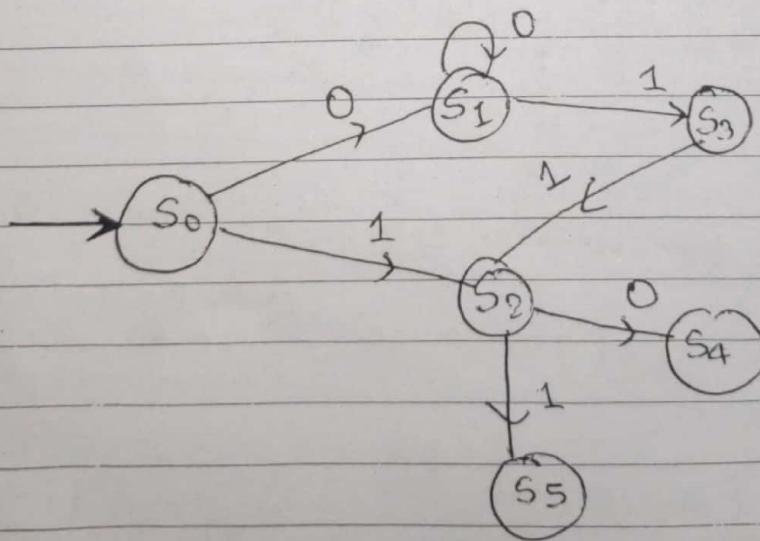
$$\begin{aligned}\epsilon\text{-closure}(\text{move}(S_1, 0)) &= \epsilon\text{-closure}(A, C, E) \\ &= \{A, B, C, D, E\} \\ &= S_1\end{aligned}$$

$$\begin{aligned}\epsilon\text{-closure}(\text{move}(S_1, 1)) &= \epsilon\text{-closure}(B, E, D) \\ &= \{B, E, D\} \\ &= S_2\end{aligned}$$

Mark S₂:

$$\begin{aligned}\epsilon\text{-closure}(\text{move}(S_2, 0)) &= \epsilon\text{-closure}(E) \\ &= \{E\} = S_4\end{aligned}$$

$$\begin{aligned}\epsilon\text{-closure}(\text{move}(S_2, 1)) &= \epsilon\text{-closure}(D) \\ &= \{D\} = S_5\end{aligned}$$



Mark S3:

$$\epsilon\text{-closure } (\text{move}(S_3, 0)) = \epsilon\text{-closure}(C, E)$$

$$= \{ C, E \}$$

$$\epsilon\text{-closure } (\text{move}(S_3, 1)) = \epsilon\text{-closure}(F, D)$$

$$= \{ F, D \}$$

$$= S_2$$

Mark S4:Mark S5:

$$S_0 = \{A, B, D\}$$

	0	1
$\rightarrow \{A, B, D\}$	$\{A, B, C, D, E\}$ including youself	$\{E, D\}$
* $\{A, B, C, D, E\}$	$\{A, B, C, D, E\}$	$\{B, D, E\}$
* $\{D, E\}$		
* $\{B, D, E\}$		
* $\{E\}$		
$\{D\}$		
* $\{C, E\}$		
$\{B\}$		
$\{C\}$		
\emptyset		

These cannot be more than 5 final-states when the states are $\{A, B, C, D, E\}$

NFA \Rightarrow DFA $\text{H} \text{ लात् ट्रॉप } (\emptyset) \text{ state chahinxa}$

Yehi NFA \Rightarrow nai DFA xa

that means $\text{DFA} \xrightarrow{\text{to}} \text{DFA}$; no trap state needed

2) RE to NFA (Thomson's Construction)

Input \Rightarrow RE, Σ over alphabet A

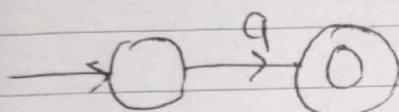
Output \Rightarrow ϵ -NFA accepting $L(\Sigma)$

Eg : $\delta = a(a+b)^*b$
 (Starting with a , ending with b)
 [Regular expression]

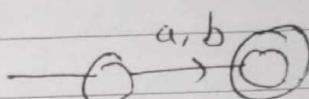
$$L(\delta) = \{ab, aab, abbb, aabbbb\}$$

[Language of regular expression \rightarrow Collection of strings generated by Regular Language.]

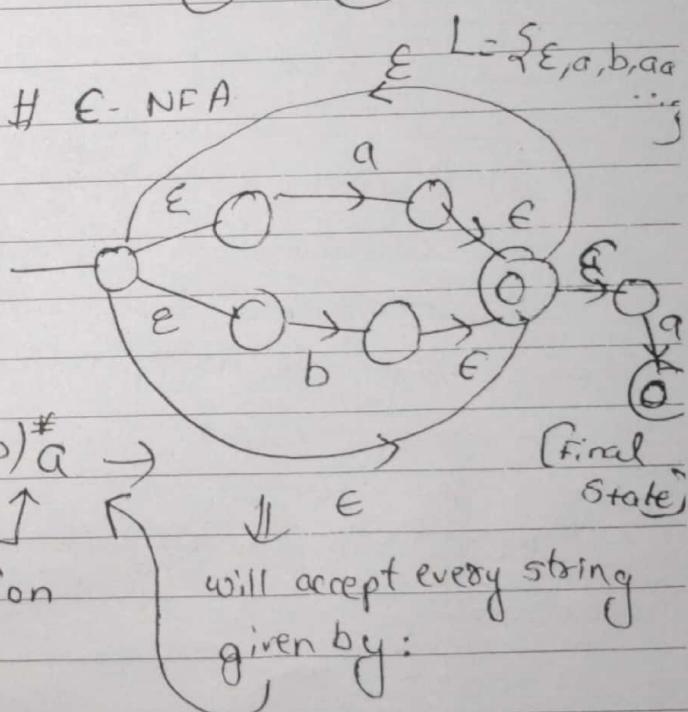
$\delta = a$



$\delta = a+b$



ϵ -NFA



① R.E to D.F.A

↳ 1) Convert the given expression to augmented expression by concatenating with hash.
i.e. $(\gamma)\#$

$$\text{Ex: } \gamma = (a+b)^*abb \text{ or } (a|b)^*abb$$

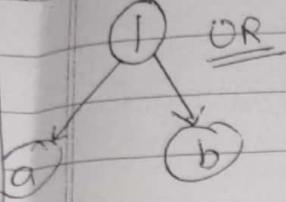
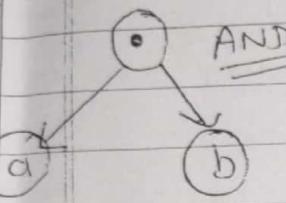
$$\hookrightarrow \gamma = (a+b)^*abb\#\#$$

2) Construct the syntax-tree of this augmented R.E.
In this tree, all the operators will be inner-node
and all the alphabets, symbols including $\#$ will be
leaves. (leaf nodes)

3) Number each leaves.

4) Traverse tree to construct nullable, firstpos, lastpos
and followpos.

Note Rule to evaluate nullable firstpos and lastpos.

Node - n	Nullable (n)	firstpos (n)	lastpos(n)
leaf labelled ϵ	True	$\{ \}$	$\{ \}$
non null leaf position p	False	$\{ \}^*$	$\{ \}^*$
	nullable (a) or nullable (b)	firstpos(a) \cup firstpos(b)	last pos(a) \cup lastpos(b)
	nullable(a) and nullable(b)	if nullable(a) is true then; firstpos(a) \cup firstpos(b) else firstpos(a)	If nullable (b) is True then; last pos(a) \cup lastpos(b) else lastpos(b)
	True	firstpos(a)	lastpos(a)

Q. Convert the R.E $(a+b)^*ab^*$ into D.F.A directly.

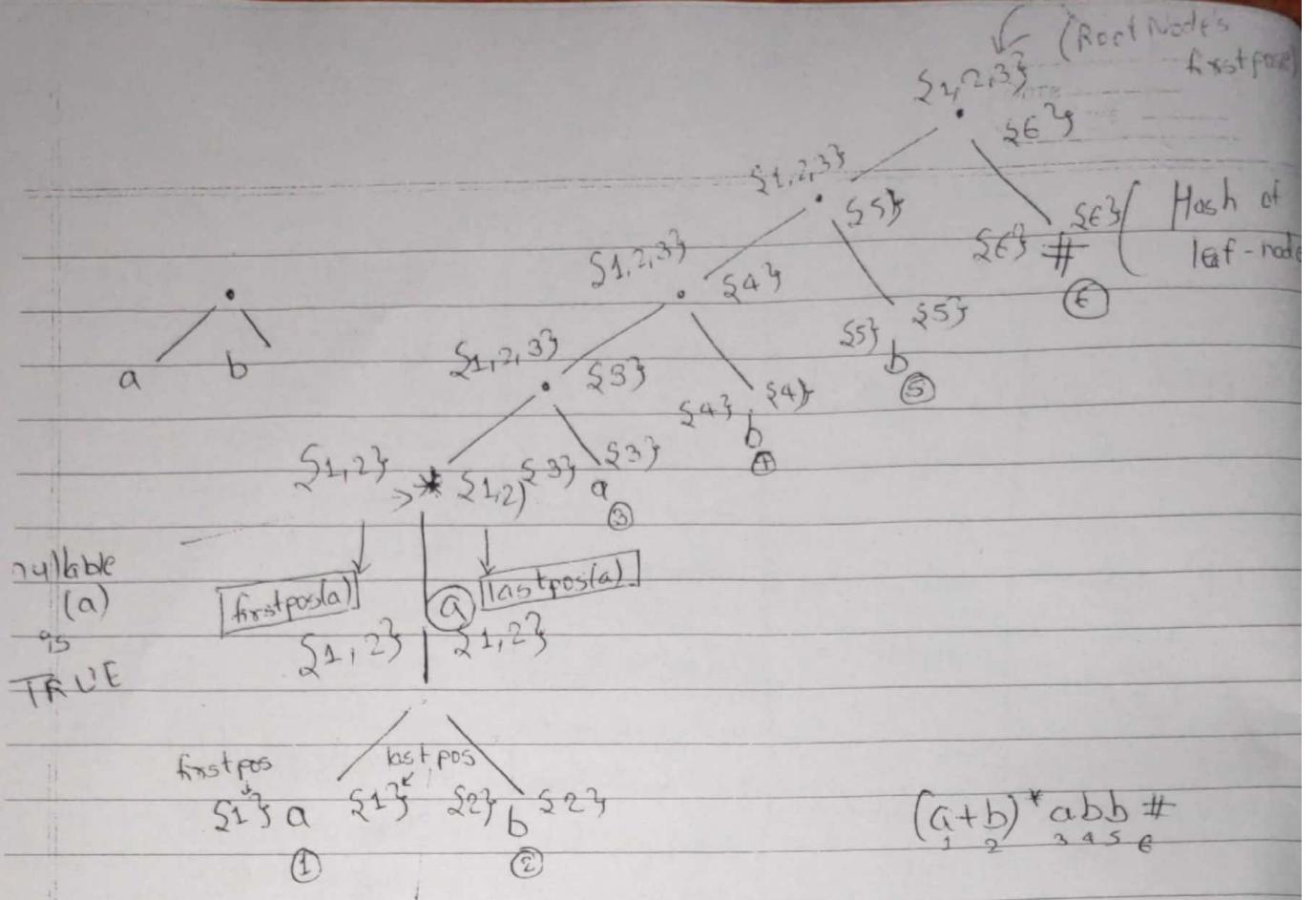
Soln;

1. Augmenting the regular expression; we get:

$$(a+b)^*ab^*\#$$

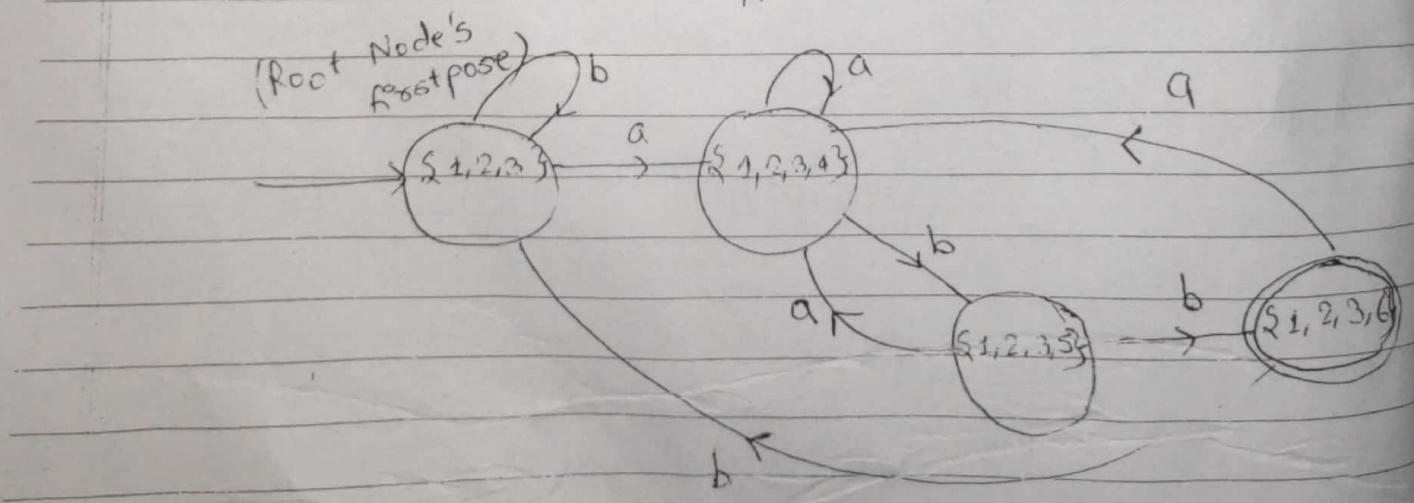
2.

(P.T.O)



only star and concat(•) nodes will be considered!!!

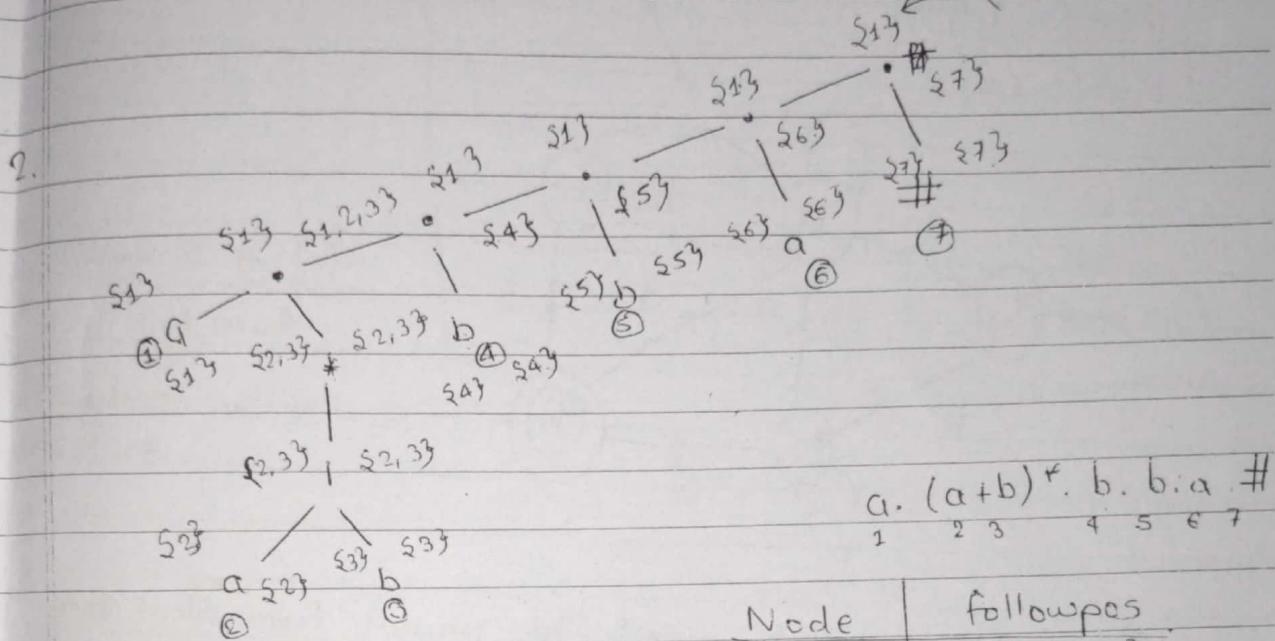
Node	follow pos
a 1	S1,2,3}
b 2	S1,2,3}
a 3	S43
b 4	S53
b 5	S63
# 6	-



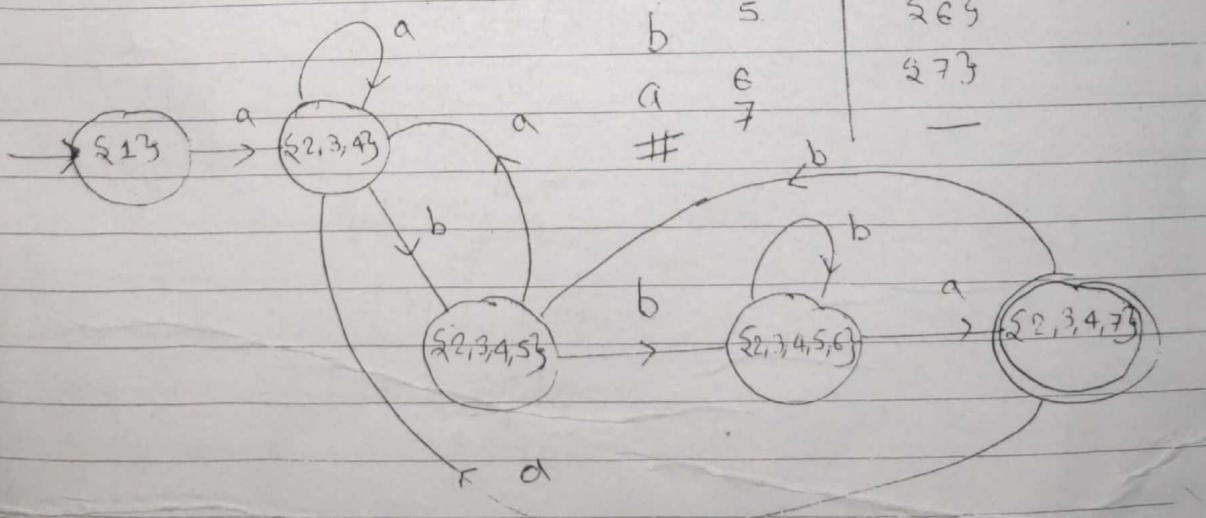
2. Convert the R.E $a.(a+b)^* \cdot b.b.a$ into D.F.A directly.

Soln:

1. Augmenting the regular expression; we get.
 $a \cdot (a+b)^* \cdot b \cdot b \cdot a \cdot \#$



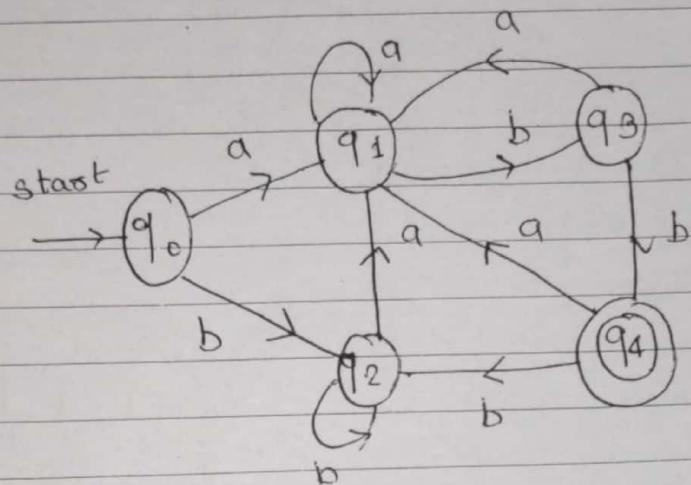
Node	followpos
1	$\{2, 3, 4\}$
2	$\{2, 3, 4\}$
3	$\{2, 3, 4\}$
4	$\{5\}$
5	$\{6\}$
6	$\{7\}$
7	—



⑥ State Minimization in D.F.A

↳ Reducing the number of states from D.F.A.

[Language must be same]



(q4) is reachable

from (q0)

So, it is Reachable state.

Those states which cannot be reached from start state
is called Unreachable State.

$$\delta(p, a) \in F$$

$$\delta(q, a) \in F$$

$p \& q$ are equivalent even in:

$$\delta(p, a) \notin F$$

$$\delta(q, a) \notin F$$

O-equivalent States:

Non-final & Final

$$[q_0, q_1, q_2, q_3] [q_4]$$

States
Grouping

δ	a	b
q_0	q_1	q_2
q_1	q_1	q_3
q_2	q_1	q_2
q_3	q_1	q_4
q_4	q_1	q_2

Does q_0 and q_1 belong
in same group?

Equivalent for 'a'

$$\delta(q_0, a) \rightarrow q_1$$

$$\delta(q_1, a) \rightarrow q_1$$

q_0 and q_1 on 'b'

go to $\{q_2\}$ and $q_3\}$

which is on same group

i.e. $[q_0, q_1, q_2, q_3]$

and not on final group.

$[q_4]$

Equivalent for 'b'

1-equivalent

$[q_0, q_1, q_2] [q_3] [q_4]$

can be composed
with anyone
of these three

q_3 and q_2 on b

goes to

q_4 and q_2

Not on same
states

So; not-equivalent
at all.

0-eq: $[q_0, q_1, q_2, q_3] [q_4]$

1-eq: $[q_0, q_1, q_2] [q_3] [q_4]$

2-equivalence:

Compare q_0 and q_1 :

q_0 on $b \rightarrow q_2$

q_1 on $b \rightarrow q_3$ (different state)

[Not 2-equivalence]

↳ 1-eq. $[q_0, q_1, q_2]$

2-eq: $\begin{matrix} ? \\ [q_0, q_e] \end{matrix} [q_1] [q_3] [q_4]$

s	a	b
q_0	q_1	q_2
q_1	q_1	q_3
q_2	q_1	q_2

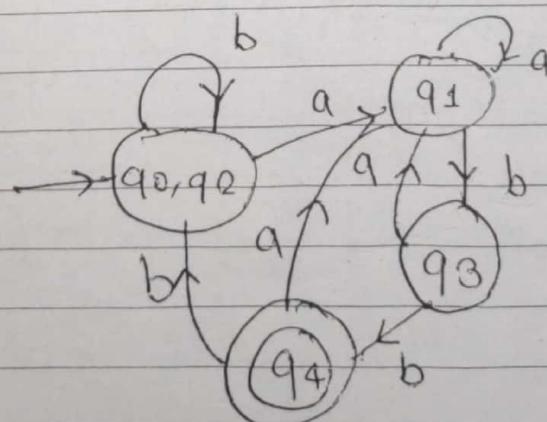
equivalent

3-eq: $[q_0, q_2] [q_1] [q_3] [q_4]$

as;

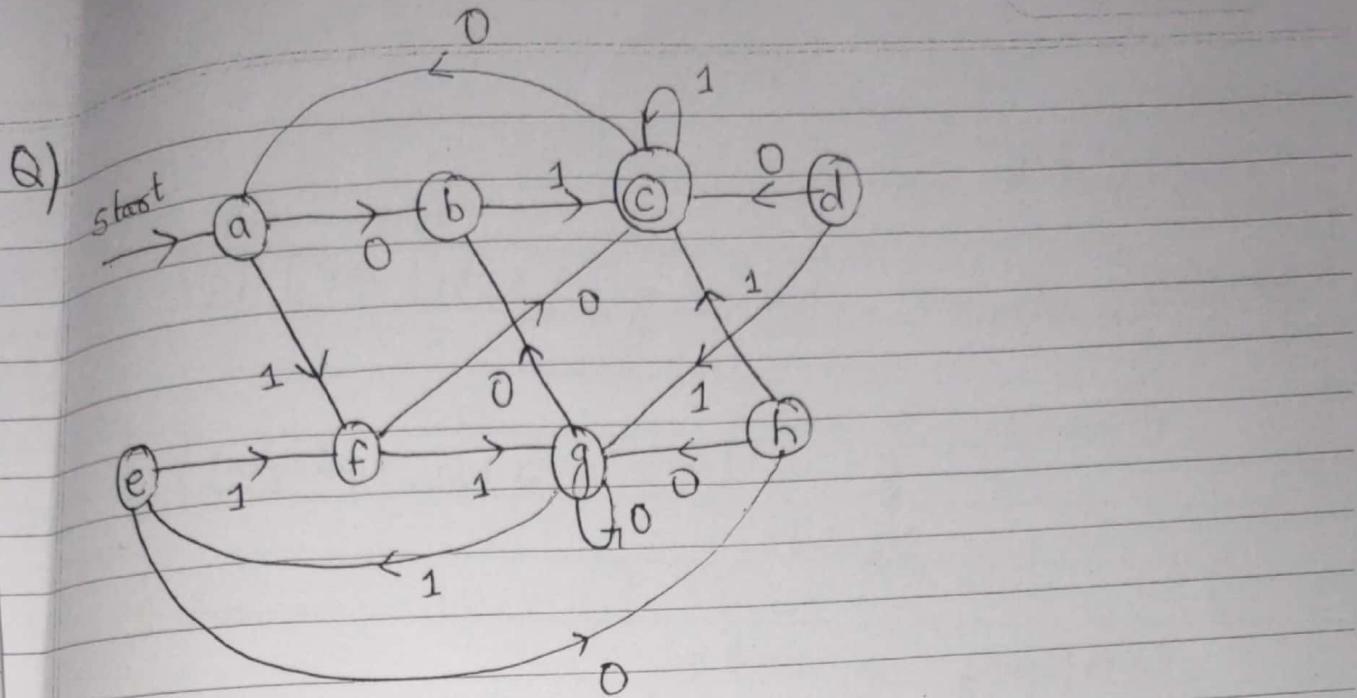
$\delta(q_0, a) \notin F$

$\delta(q_2, a) \notin F$] So equiv



STOP!

This is called
DFA State
Minimization



Since (d) is an Unreachable state

#0-equivalence : $[a, b, e, f, g, h] \quad [c]$
Non-Final and Final States

δ	0	1	
a	b	f	a and b are not equivalent as: $\delta(a, 1) \rightarrow f \leftarrow$ different states $\delta(b, 1) \rightarrow c \leftarrow$ states
b		c	
e	h	f	a and e are equivalent
f	c	g	e and g are equivalent
g	b, g	e	
h	g	c	
c	a	c	

b and h are Equivalent.

1-equivalence: $[a, e, g] [b, h] [f] [c]$

Comparing b and h
 \downarrow
No state { Not equivalent }

Comparing a and e

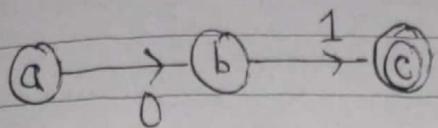
$a \xrightarrow{o} b$] Same state
 $e \xrightarrow{o} h$

Comparing e and g

$e \xrightarrow{1} f$] Different states
 $g \xrightarrow{1} e$

2-equivalence: $[a, e] [g] [b] [h] [f] [c]$

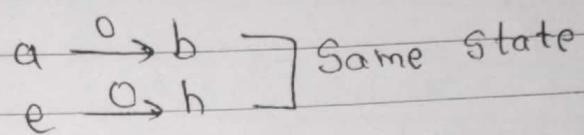
3-equivalence: $[a] [e] [g] [b] [h] [f] [c]$
(As a and e gives different states)



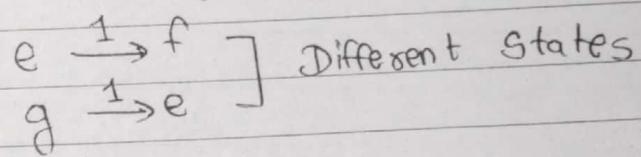
b and h are Equivalent.

1-equivalence: $[a, e, g]$ $[b, h]$ $[f]$ $[c]$

Composing a and e



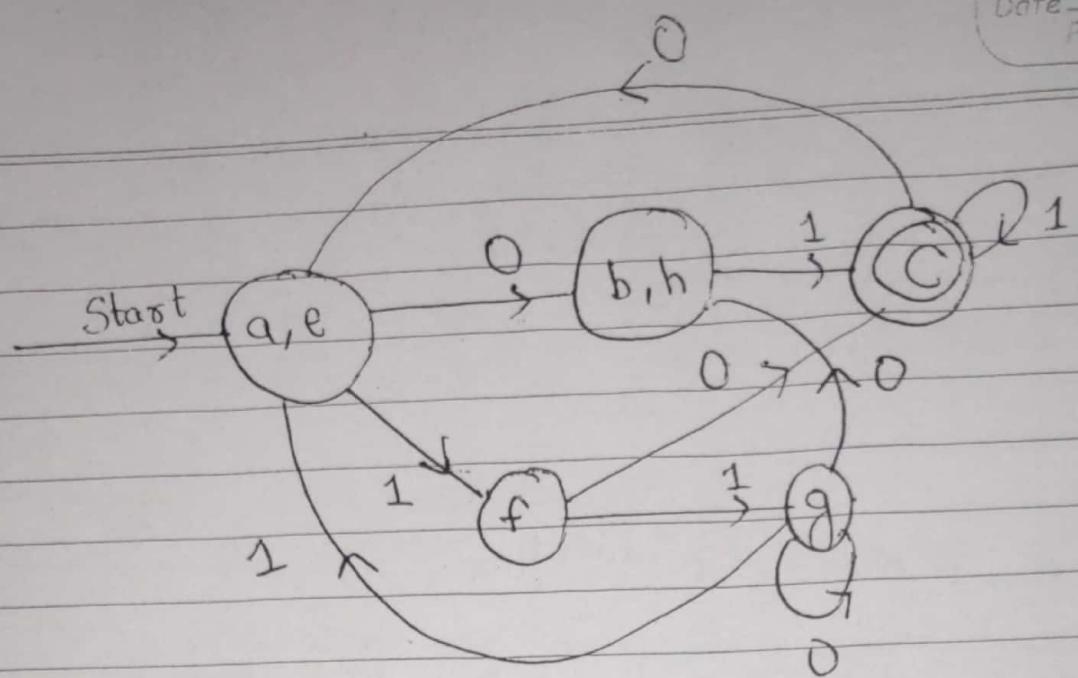
Composing e and g



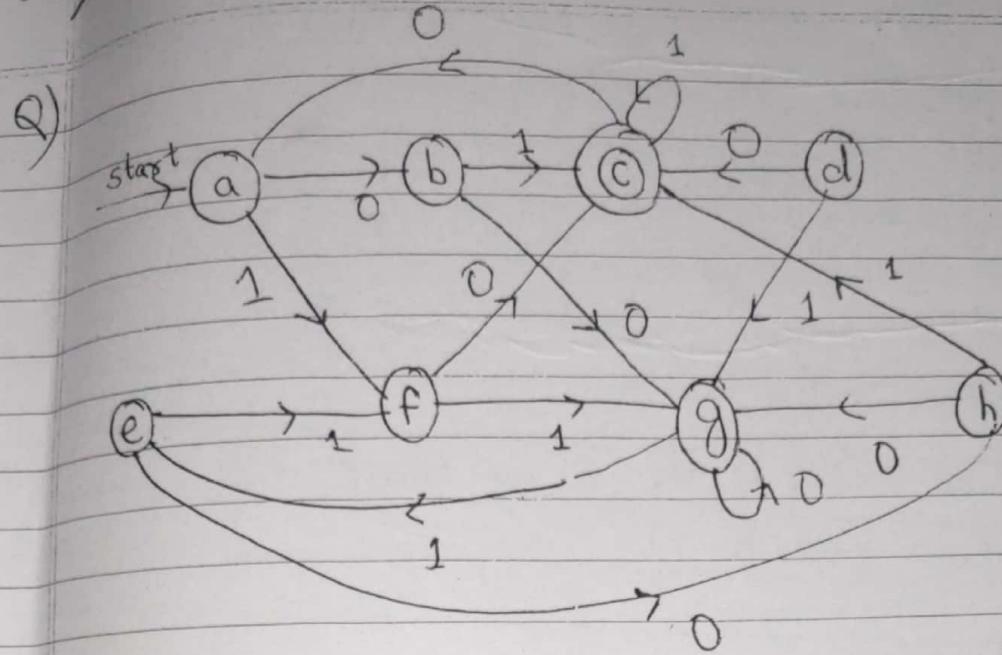
2-equivalence: $[a, e]$ $[g]$ $[b, h]$ $[f]$ $[c]$

3-equivalence: $[a, e]$ $[g]$ $[b, h]$ $[f]$ $[c]$

P. T. O



Minimization D.F.A



Since \textcircled{d} is an Unreachable State

0-equivalence : $[a, b, e, f, g, h] \quad [c]$

Non-Final & Final States

s	0	1
a	b	f
b	g	c
e	h	f
f	c	g
g	g	e
h	g	c
c	a	c

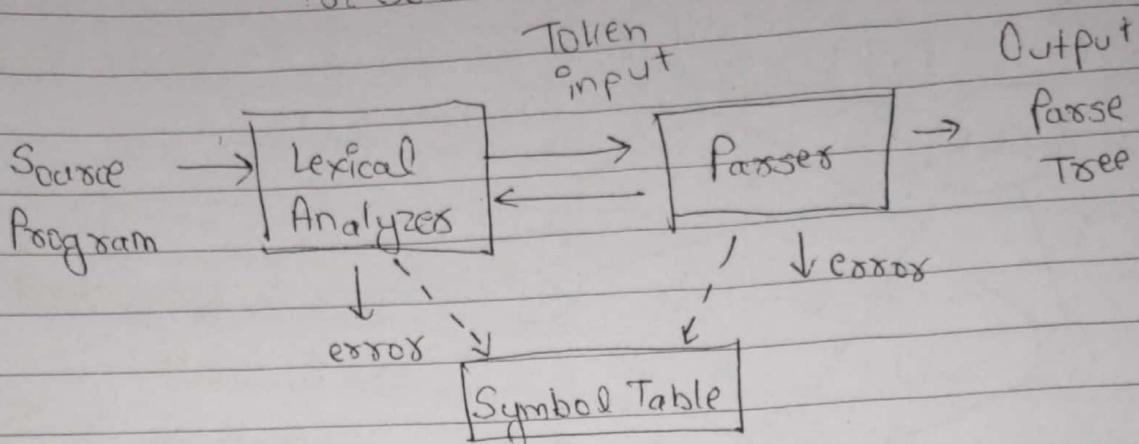
a and b are not equivalent
as:

$s(a, 1) \rightarrow f$] different states
 $s(b, 1) \rightarrow c$] states

a and e are equivalent
e and g are equivalent

b and h are equivalent

Parser



Syntax analyzer is also called the parser. Its job is to analyze the source program based on the definition of its syntax.

It works in back-step with lexical Analyzer and is responsible for creating the parse-tree.

→ It implements a Context-Free Grammar.



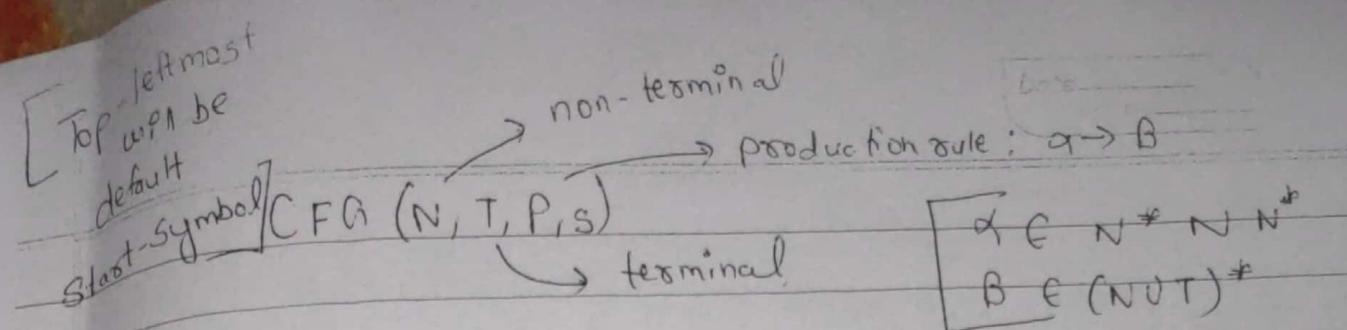
- Gives a precise syntactic specification of a programming language.

Top-Down Parser

→ the parse tree is created top-to-bottom, starting from the root.

Bottom-Up Parser

→ the parse is created bottom to top; starting from the leaves.



$S \in N$ is a designated start symbol.

α and β can be both terminals and non-terminals

CFG: Derivations

$$\begin{aligned} E &\rightarrow E + F \\ &\rightarrow id + F \\ &\rightarrow id + id \end{aligned}$$

$L(G) \rightarrow$ Language of Grammar

\hookrightarrow A sentence of $L(G)$ is a string of terminal symbols of G .

If S is the start symbol of G then
 w is a sentence of $L(G)$ iff $S \Rightarrow^* w$
 where w is a string of terminals of G .

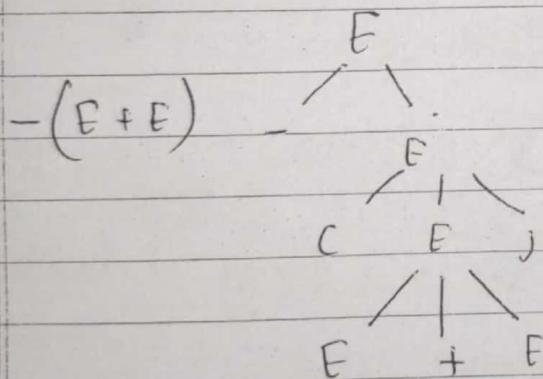
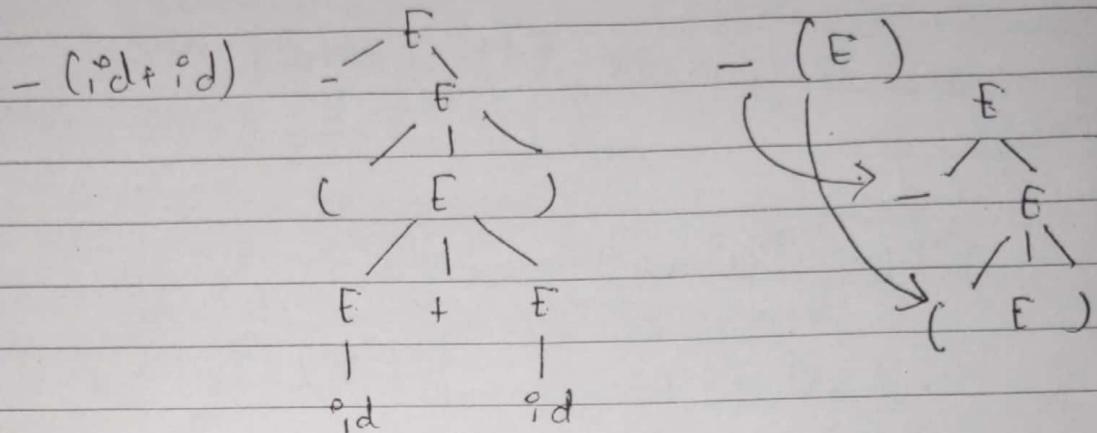
#rm → Right Most Derivation:

we replace rightmost variable first.

(hidden step) $\xrightarrow{*}$ derives in 0 or more than 1 step.

A Parse-tree is a graphical representation of a CFG derivation.

Inner nodes are non-terminal symbols.



Ambiguity:

↳ A grammar produces more than one parse-tree for a sentence is called an ambiguous grammar.

Compiler Design

Class Work

1) ans:

Parsing is a technique where a token string is taken as input and with the help of existing grammar, converted to Parsing Tree / Parse Tree. [Syntax Analyzers]

Types of Parsing :

• Top- Down Parser :

↳ This type generates parse for the given input string with the help of grammar's productions by expanding the non-terminals i.e. starts from start symbol and ends on terminals; using leftmost derivation.

i) Recursive descent parser / Backtracking / Brute force

Parser : Generates parse tree using Brute force.

ii) Non-recursive descent parser: Predictive parser

without backtracking / dynamic parser using parse table to generate parse tree.

• Bottom- Up Parser :

↳ It generates parse tree for the given input string with the help of grammar's productions by compressing the non-terminals. It starts from non-terminals and ends on start symbol; uses reverse of the rightmost derivation.

i) LR parser: Generates parse-tree for the given string by using unambiguous grammar.

ii) Operator precedence parser: Generates parse tree from given grammar and string where 2 consecutive non-terminals and epsilon never appear on the right-hand side of any production.

~~iii) A parser that reads and understands operator precedence grammar. It is bottom-up parser that interprets operator grammar. Ambiguous grammar are not allowed in any grammar except operator precedence parser.~~

2) ans:

CFA consisting of a finite set of grammar rules is a quaduple (N, Σ, P, S) .

Types of derivations in C.F. A:

i) Leftmost derivation: It is obtained by applying production to the leftmost variable in each successive step.

$$S \Rightarrow AaSS$$

$$A \Rightarrow a$$

$$S \Rightarrow AaSS$$

$$\Rightarrow aaSS$$

$$\Rightarrow aaAaSS \text{ and so on.}$$

ii) Rightmost derivation: It is obtained by applying production to the rightmost variable in each step.

~~$S \rightarrow aSS$~~
 ~~$A \rightarrow b$~~
 ~~$S \Rightarrow aSS$~~
 $\Rightarrow qaSS b$

~~$E \rightarrow EE$~~
 ~~$E \rightarrow E^*$~~
 ~~$E \rightarrow id$~~

$E \rightarrow EE$ $E \rightarrow E^*$ $E \rightarrow id$
 right most derivation.

The right most derivation for the string 'atafa' may be-

$$X \rightarrow X^* X \rightarrow X^* a \rightarrow \begin{matrix} X + X^* a \\ \sqcup \\ \text{added later} \end{matrix} \rightarrow a + a^* a$$

iii) Mixed derivation: It is obtained by applying products to the leftmost and rightmost variable simultaneously as per the requirement in each successive step.

$$\begin{aligned} S &\Rightarrow aSS \\ &\Rightarrow aSb \\ &\Rightarrow aaSSb \\ &\Rightarrow aabSb \\ &\Rightarrow aabbSSb \\ &\Rightarrow aababSbb \\ &\Rightarrow aababbhb \end{aligned}$$

3) ans:

A CFG is said to be ambiguous if there exists more

than one derivation tree for the given input string i.e., more than one Left Most Derivation Tree (LMDT) or Right Most Derivation Tree (RMDT).

Defn $\hookrightarrow G = (V, T, P)$ is a CFG is said to be ambiguous if and only if there exists a string in T^* that has more than one parse tree.

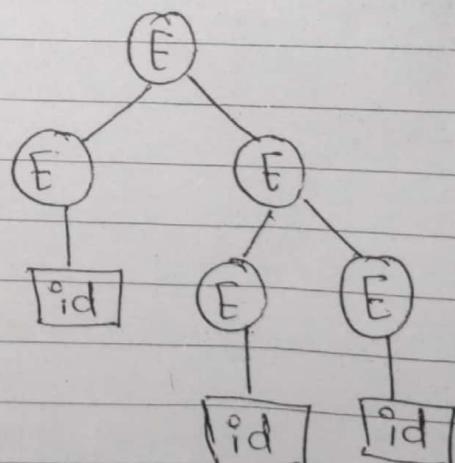
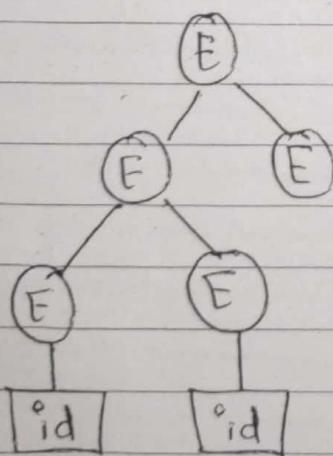
$$A \rightarrow \alpha$$

where; $\alpha \in (V \cup T)^* S$
(Start Symbol)

For Example:

$$E \rightarrow E + E \mid id$$

We can create 2 parse tree from this grammar to obtain
 $id = id + id$



4) ans:

A grammar $G(V, T, P, S)$ is left recursive if it has a production in the form:

$$A \rightarrow A\alpha|\beta$$

↳ Above grammar is left recursive because the left of production is occurring at a first position on the right side of production. It can eliminate left recursion by replacing a pair of production with

$$A \rightarrow BA'$$

$$A \rightarrow \alpha A' |\epsilon$$

Elimination of Left Recursion

Left Recursion can be eliminated by introducing new non-terminal A' such that,

$$A \rightarrow A\alpha|\beta$$

Left Recursive Grammar

$$A \rightarrow BA'$$

$$A' \rightarrow \alpha A' |\epsilon$$

Removal of Left Recursion

This type of Recursion is also called Immediate Left Recursion.

Example: Removal of left-recursion from the grammar:

$$E \rightarrow E(T) | T$$

$$T \rightarrow T(F) | F$$

$$F \rightarrow id$$

Solution:

Eliminating immediate left-recursion among all $A \alpha$ production, we obtain:

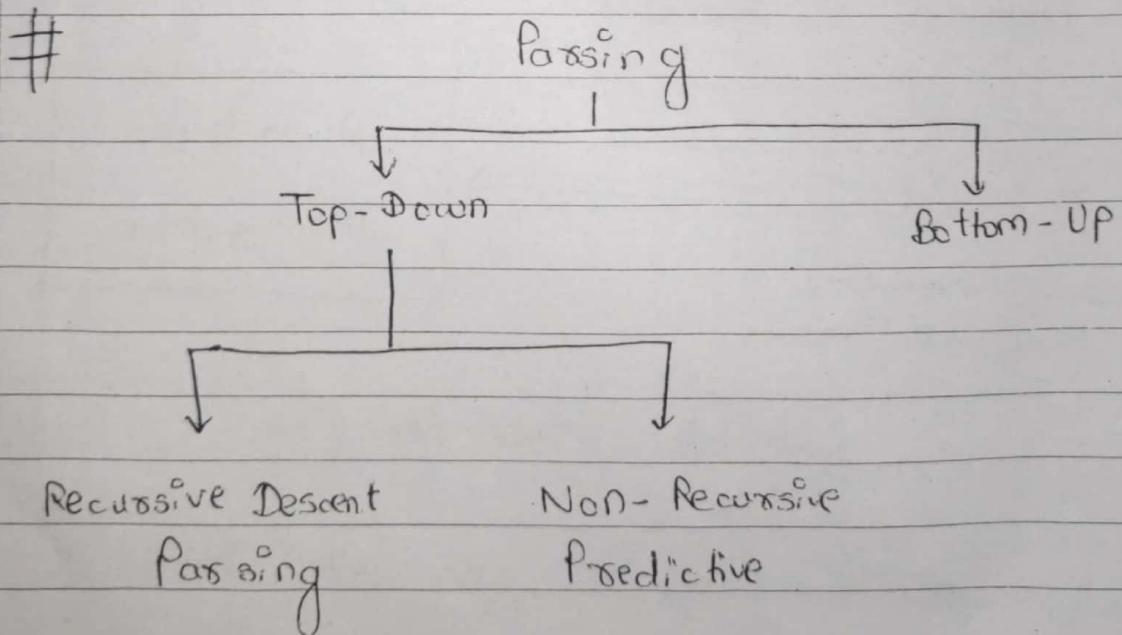
$$E \rightarrow TE'$$

$$E' \rightarrow (T)E' | \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow (F)T' | \epsilon$$

$$F \rightarrow id$$



1) Recursive Descent Parsing:

Rules

- 1) Use 2 pointers $iptr$ for pointing the input symbol to be read and $optr$ for pointing the symbol of output string i.e initially start symbol : S.
- 2) If the symbol pointed by $optr$ is non-terminal ; use the first production rule for expansion.
- 3) While the symbol pointed by $iptr$ and $optr$ is same, increment both pointers.
- 4) The loop at the above step terminates when
 - a) A non-terminal at the output is, (case A)
 - b) The end of the input is, (case B)
 - c) On matching terminal symbols pointed by $iptr$ and $optr$ is same is, (case C)
- 5) If (A) is true ; expand the non-terminal using the first rule and go to step 2).
- 6) If (B) is true ; terminate with success.
- 7) If (C) is true ; decrement both the pointers to the place of last non-terminal expansion, and use the next production rule for the non-terminal.

8) If there is no more production and (B) is not done; report errors.

Example: Consider the Grammar

$$S \rightarrow cAd$$

$$A \rightarrow ab/a$$

Input string is "cad"

Production Rules:

Rule 1	
Rule 2	Rule 3

[Algorithm Rules]

Input.

(^{opt}s)cad

(^{opt}s)cad

ement
nters
→ c(^{opt}s)ad

Output.

(^{opt}s)S

(^{opt}s)cAd

c(^{opt}s)Ad

↑
the non-terminal
at the output

Rules Fixed ↓

[Rule 1, Try $S \rightarrow cAd$]

[Rule 3, Match c]

[Rule 5, Try $A \rightarrow ab$]

c(^{opt}s)ad

Ca(^{opt}s)d

c(^{opt}s)a₁b₁d

c a(^{opt}s)b₁d

[Rule 3, Match a]

[Rule 7, deadend,

backtrack]

.. c (^{opt}s) ad c (^{opt}s) Ad [Rule 5, Try $A \rightarrow a$]

c (^{opt}s) ad c (^{opt}s) ad [Rule 3, Match a]

ca (^{opt}s) d ca (^{opt}s) d [Rule 3, Match d]

cad (^{opt}s)

cad (^{opt}s)

[Rule 6, Terminate with success.]

However;

[caa is not produced by this grammar]

Left Recursion:

Example: $A \rightarrow A\alpha$
 \downarrow
 same

Eg: $E \rightarrow E+E \mid E*E \mid id$
(Terminal)

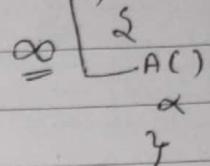
Top-Down Parsing
 Method cannot handle

Non-immediate left recursion:

$$\begin{array}{l} S \rightarrow Aabb \\ A \rightarrow Sc \mid c \end{array} \quad \Rightarrow \quad S \rightarrow \underline{S}cab$$

Left-recursive Grammar

as $\hookrightarrow A()$



① Removing Left Recursion:

$$\begin{array}{l} A \rightarrow A(\alpha) \mid \beta \\ \Downarrow \\ \left\{ \begin{array}{l} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array} \right. \end{array} \quad \text{Then: we have: } \quad A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \dots \mid A\alpha_n \mid \beta_1 \mid \beta_2 \mid \dots \mid \beta_m$$

(where β does not
 start with
 Non-terminal symbol)

[General Form:]

$$A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \alpha_3 A' \mid \dots \mid \alpha_n A' \mid \epsilon$$

$$\begin{array}{l} \boxed{E \rightarrow E+E} \mid id \\ \boxed{E \rightarrow E*E} \\ \boxed{E \rightarrow id} \\ \boxed{E' \rightarrow +EE'} \\ \boxed{E' \rightarrow *EE'} \\ \boxed{E' \rightarrow idE'} \\ \boxed{E' \rightarrow +EE' \mid \epsilon} \end{array}$$

$E \rightarrow \text{id} E'$
$E' \rightarrow + E E' \epsilon$
$E \rightarrow \text{id} E''$
$E'' \rightarrow * E E'' \epsilon$
$E \rightarrow \text{id}$

$$E \rightarrow E + E | E * E | \text{id}$$

2) Non-Recursive Predictive Parsing (Table Driven Parsing)

Consider the grammar:

$$S \rightarrow aB\alpha$$

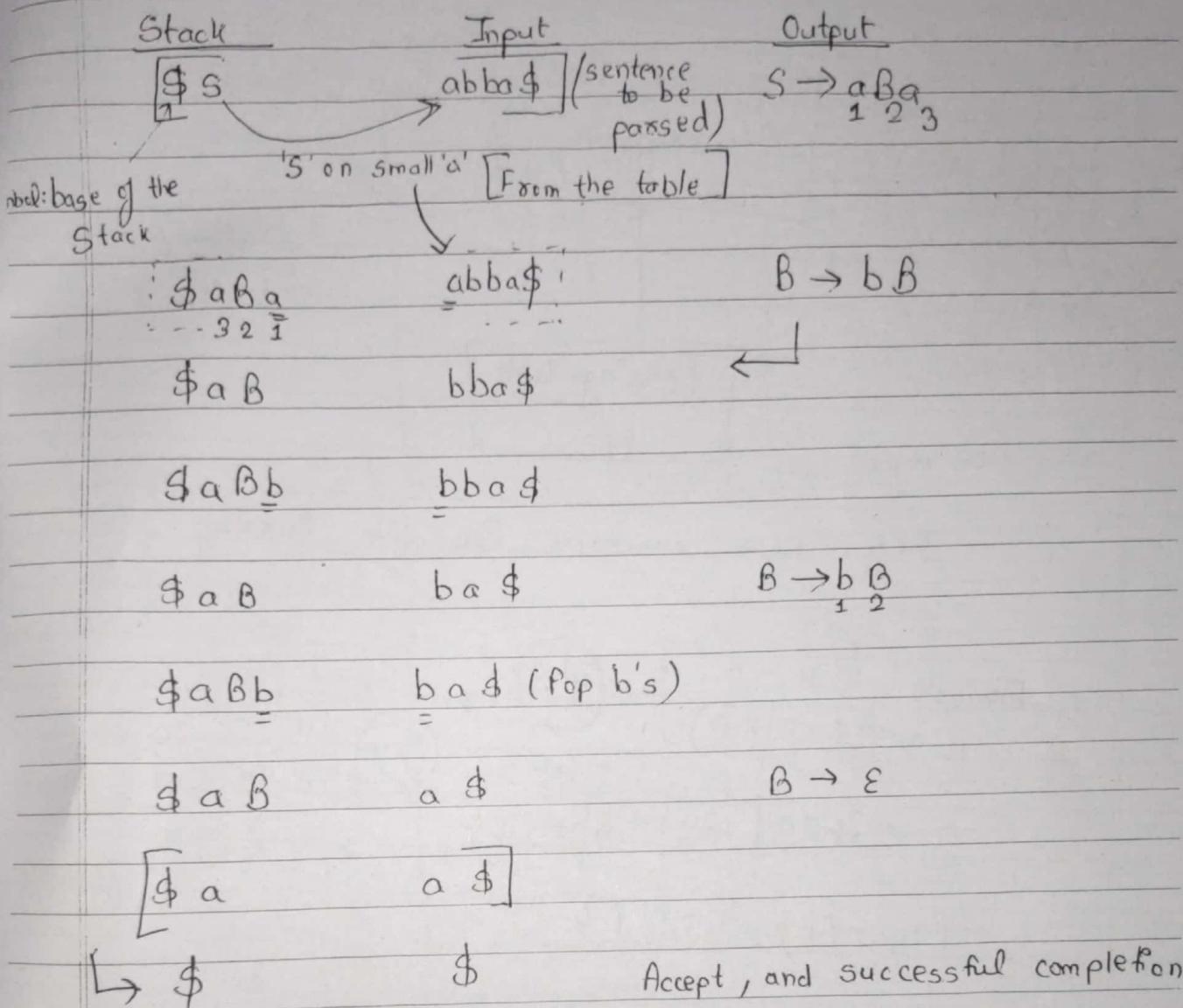
$$B \rightarrow bB | \epsilon$$

Parsing Table is :

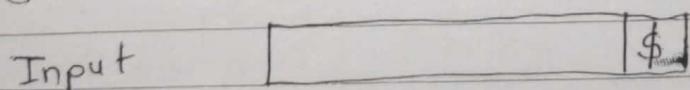
	a	b	\$
S	$S \rightarrow aB\alpha$		
B	$B \rightarrow \epsilon$	$B \rightarrow bB$	

Table :- LL(1) Parsing Table

Given String $w = abba$



Defn / Theory:



[P.T.O.]

0x //

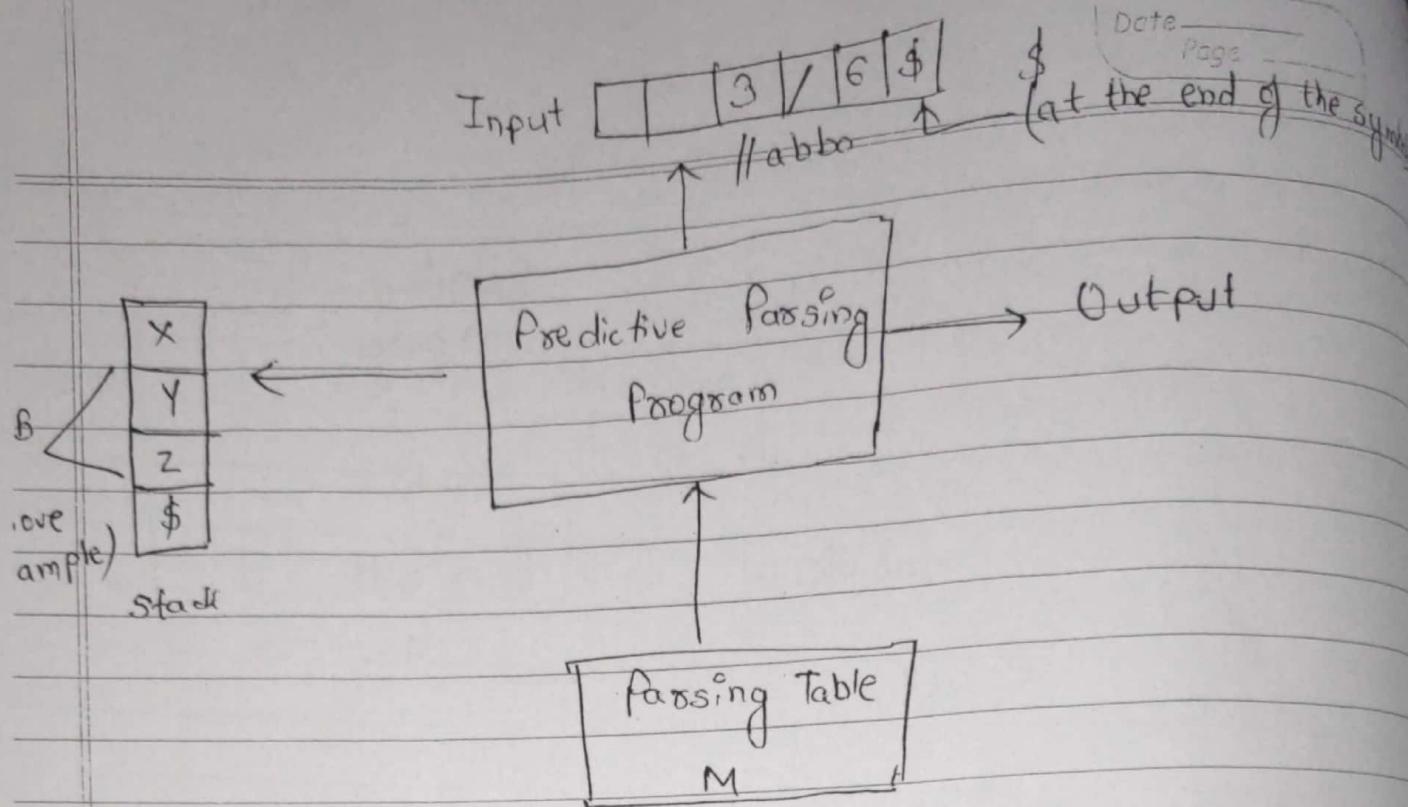


Fig: Non-recursive Predictive Parsing

\therefore Example

$$R \rightarrow id\ S \mid (R)\ S$$

$\underline{id\ S}$ or $\underline{(R)\ S}$

$$S \rightarrow +\ R\ S \mid .\ R\ S \mid *S \mid \epsilon \quad \{ +, ., *, \epsilon \}$$

$$FIRST(R) = \{ id, (\}$$

$$FIRST(S) = \{ +, ., * \}$$

first of
A follows B

$$S \rightarrow A|B|C|D|E$$

$$A \rightarrow a|e$$

$$B \rightarrow b|e$$

$$C \rightarrow c$$

$$D \rightarrow d|e$$

$$E \rightarrow e|e$$

FIRST $\{a, b, c\}$

also {No capital letters}

First of A

$\{a, e\}$

$\{b, e\}$

$\{c\}$

$\{d, e\}$

$\{e\}$

FOLLOW

$\{\$\}$

$\{b, c\}$

$\{c\}$

$\{d, e, \$\}$

$\{e, \$\}$

$\{\$\}$

$\{c\}$

$\{d\}$

$\{e\}$

$\{c\}$

$\{d\}$

$\{e\}$

$\{\$\}$

$\{b\}$

$\{d\}$

$\{e\}$

$\{c\}$

$\{d\}$

$\{e\}$

$\{\$\}$

$\{c\}$

$\{d\}$

$\{e\}</$

		FIRST	FOLLOW
$S \rightarrow A^e C^e B^e$	$C b B B a$	$\{d, g, h, \epsilon, b, a\}$	$\{\$, \$\}$
$A \rightarrow d a$	$B^e C^e$	$\{d, g, h, \epsilon\}$	$\{h, g, \$\}$
$(\text{Follow } A)$			
$B \rightarrow g$	ϵ	$\{g, \epsilon\}$	$\{\$, a, h\}$
$C \rightarrow h$	ϵ	$\{h, \epsilon\}$	$\{g, \$, a\}$
			b^3

$\hookrightarrow \text{FOLLOW}(A) = \{ \text{set of terminals} \text{ that can immediately follow non-terminal } A \}$

$B \rightarrow * A \beta \rightarrow \text{IF } \beta = \epsilon$
 otherwise; then $\text{Follow of } A = \text{Follow of } B$

everything in $\text{FIRST}(\beta)$ except ϵ is placed in $\text{Follow}(A)$

	FIRST	FOLLOW
$S \rightarrow A^e B^e$	$\{b, a, c\}$	$\{\$\}$
$A \rightarrow C a \epsilon$	$\{b, \epsilon\}$	$\{c, b, \$, a\}$
$B \rightarrow B a A C c$	$\{c\}$	$\{\$\}, a\}$
$C \rightarrow b \epsilon$	$\{b, \epsilon\}$	$\{\$\}, a\}$

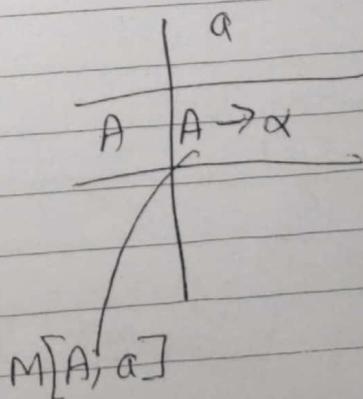
After removing Left Recursion:
So, the new Grammar is

$S \rightarrow AB$	$FIRST$	$FOLLOW$
$P_1 \quad S \rightarrow A B$ <small>follow of A is First of B</small>	$\{b, a, c\}$	$\{\$\}$
$P_2 \quad P_3 \quad A \rightarrow C a \epsilon$	$\{b, a, c\} \text{ (for } \epsilon\}$	$\{c, b, a, \$\}$
$P_4 \quad B \rightarrow c B' $ <small>follow of A is First of C</small>	$\{c\}$	$\{\$\}$
$P_5 \quad P_6 \quad B' \rightarrow a A \& B' \epsilon$	$\{a, \epsilon\}$	$\{\$\}$
$P_7 \quad P_8 \quad C \rightarrow b \epsilon$ <small>Follow</small>	$\{b, \epsilon\}$	$\{a, \$\}$

Now, Parsing Table (consists of variables and terminals).

	a	b	c	\$
S	$S \rightarrow AB \text{ (1)}$	$S \rightarrow AB \text{ (1)}$	$S \rightarrow AB \text{ (1)}$	
A	(2)	(2)	(3)	(3)
B				
B'	(5)	(7)		(6)
C	(9)			(8)

of LR(0) =
Double entry;
meaning the
grammar is
not L.L(1) #



#	$S \rightarrow aSbS$	$\{a\}$	$\{a, b, \$\}$
	$/ bSas$	$\{b\}$	
	$\sqcap \epsilon$	$\{\epsilon\}$	

Passing Table:

Variables / N.T	Terminals		
	\rightarrow	a	b
S			
	(1)	$S \rightarrow aSbS$	$S \rightarrow bSas$
		$S \rightarrow \epsilon$	$S \rightarrow \epsilon$
	(2)		$S \rightarrow \epsilon$

Not \times L.L(1)

	FIRST	FOLLOW
	$\{a\}$	
$S \rightarrow aA B b$	$\{c, \epsilon\}$	$\{d, b\}$
$A \rightarrow c / \epsilon$		
$B \rightarrow d / \epsilon$	$\{d, \epsilon\}$	$\{b\}$

Passing Table:

	a	b	c	d	\$
S	$S \rightarrow aA B b$				
A			$A \rightarrow c$	$A \rightarrow \epsilon$	
B			$B \rightarrow \epsilon$	$B \rightarrow d$	

It is
L.L(1)
program

		<u>FIRST</u>	<u follow<="" u=""></u>
$\hookrightarrow \# S \rightarrow aB \epsilon$		$\{a, \epsilon\}$	$\{\$\}$
$B \rightarrow b C \epsilon$		$\{b, \epsilon\}$	$\{\$\}$
$C \rightarrow c S \epsilon$		$\{c, \epsilon\}$	$\{\$\}$

Passing Table:

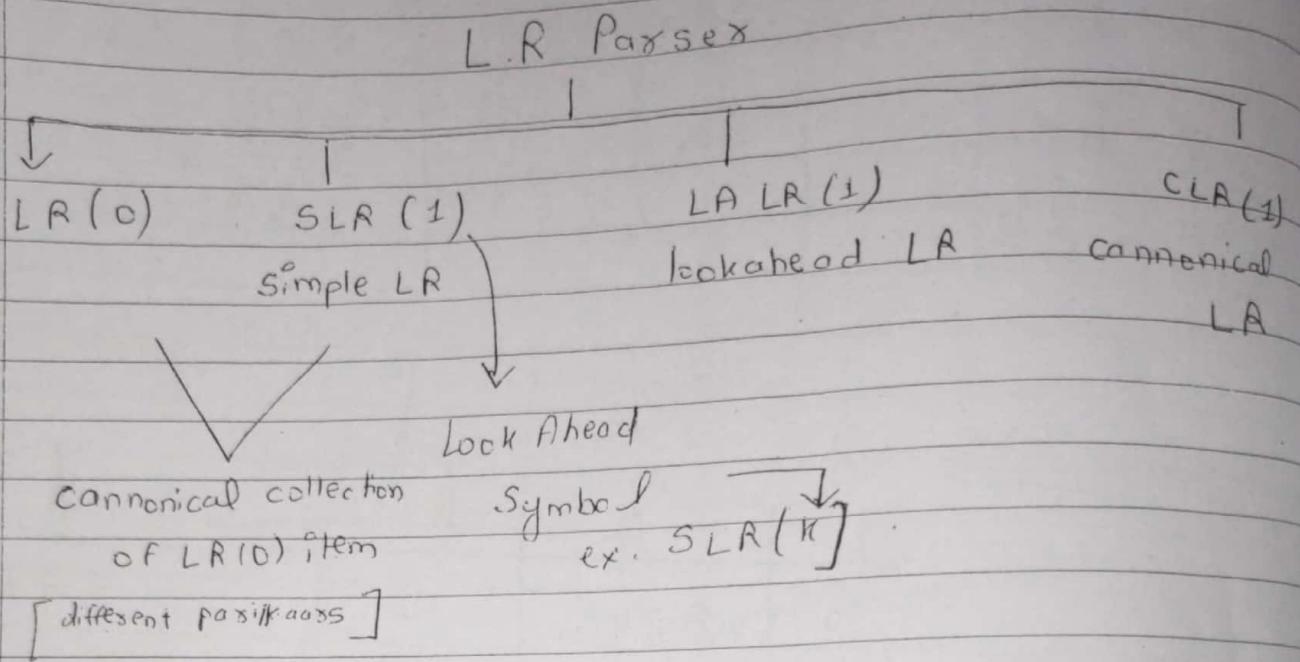
	a	b	c	\$
S	$S \rightarrow aB$			$S \rightarrow \epsilon$
L. L. (1) B		$B \rightarrow bC$		$B \rightarrow \epsilon$
C			$C \rightarrow cS$	$C \rightarrow \epsilon$

	<u>FIRST</u>	<u follow<="" u=""></u>
$\hookrightarrow \# S \rightarrow aSA \epsilon$	$\{a, \epsilon\}$	$\{\$, c\}$
$A \rightarrow c \epsilon$	$\{c, \epsilon\}$	$\{\$\}$

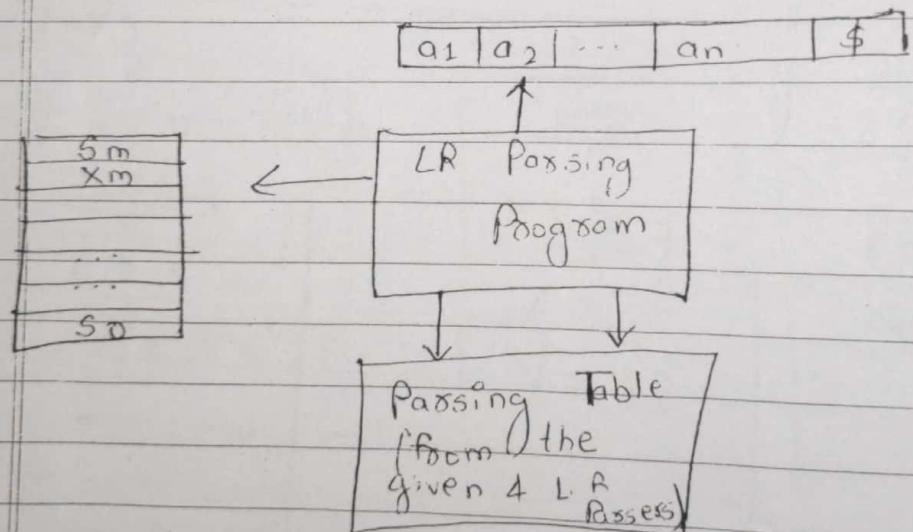
Passing Table:

	a	c	\$
S	$S \rightarrow aSA$	$S \rightarrow \epsilon$	$S \rightarrow \epsilon$
A		$A \rightarrow c$ $A \rightarrow \epsilon$	$A \rightarrow \epsilon$

[Bottom-up Parsing]

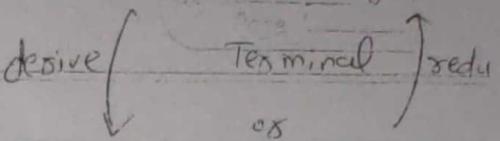


Structure of L.R Passes



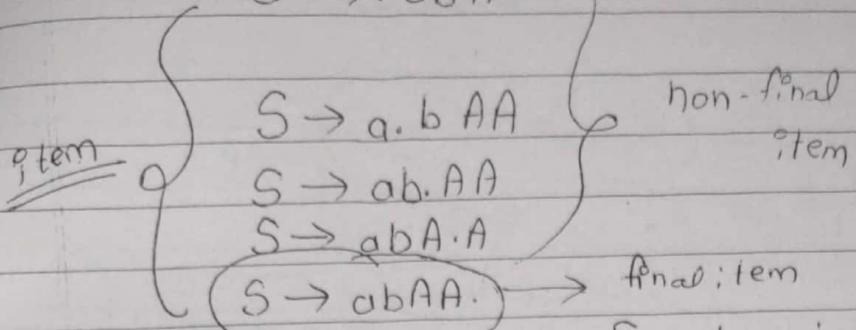
- For the construction of LR(0) and SLR(1); we have to construct the canonical collection of LR(0) item.

From start string to



$$S \rightarrow .abAA$$

[vice-versa]



[If there is dot(.) on the Rightmost side]

Reduction : abAA can be replaced by S

as : $S \rightarrow abAA$
Leftmost side replaced by S

Consider a grammar :

$$\begin{aligned} S &\rightarrow Af \\ A &\rightarrow aA \quad | \quad b \end{aligned}$$

Augmented the given grammar:

$$S' \rightarrow S$$

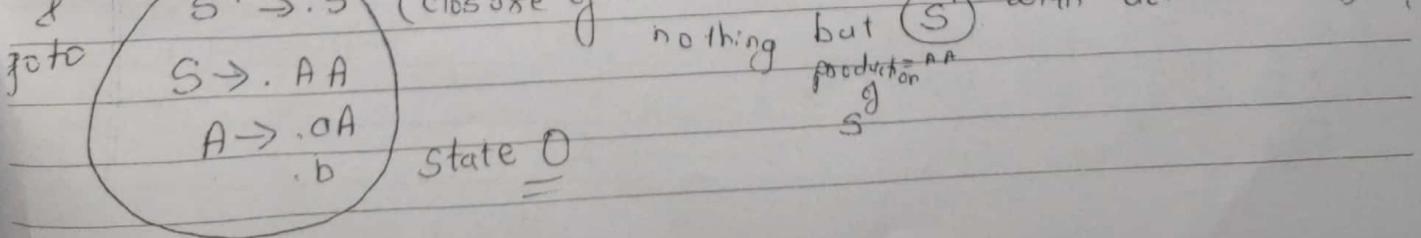
$$S \rightarrow AA$$

$$A \rightarrow aA \quad | \quad b$$

DFA

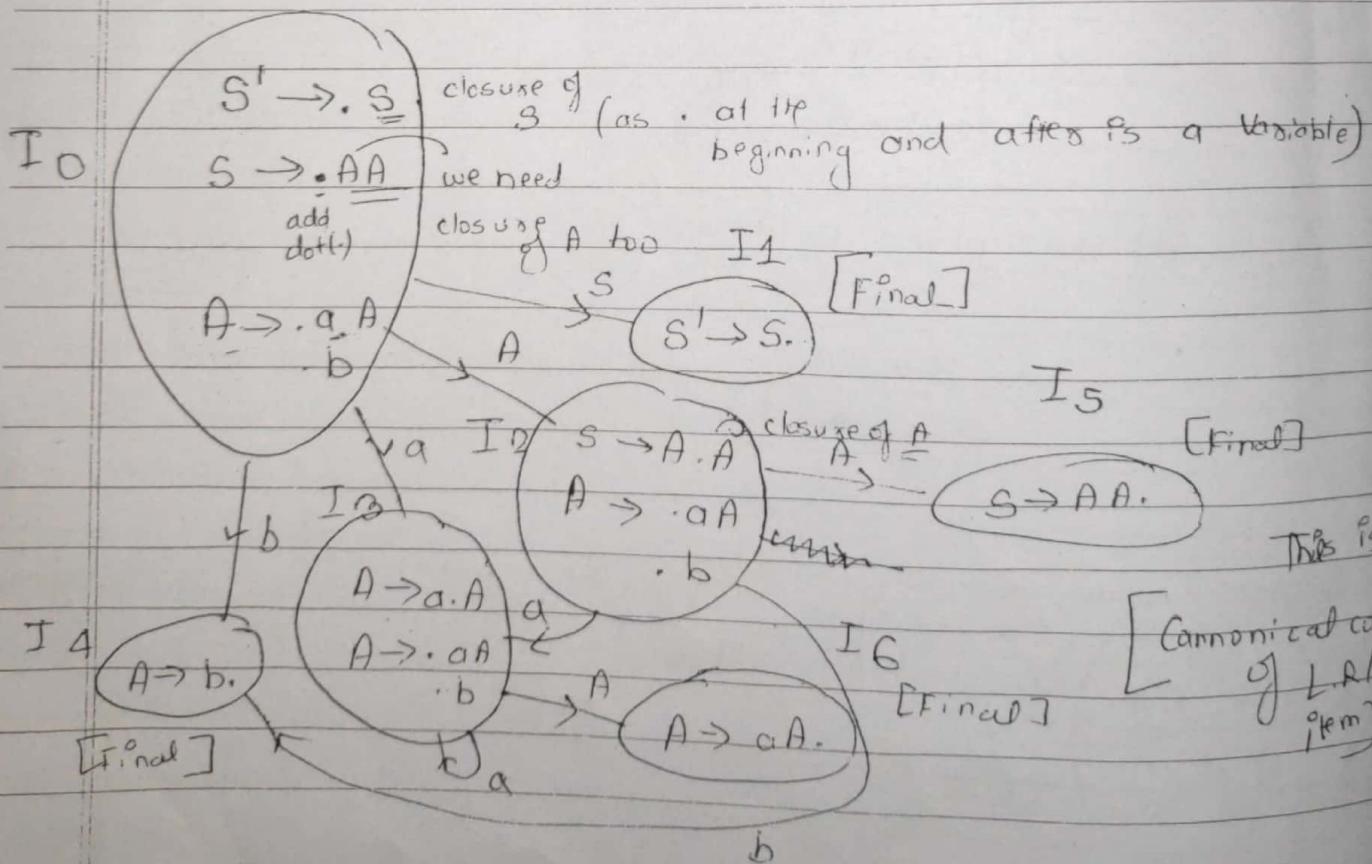
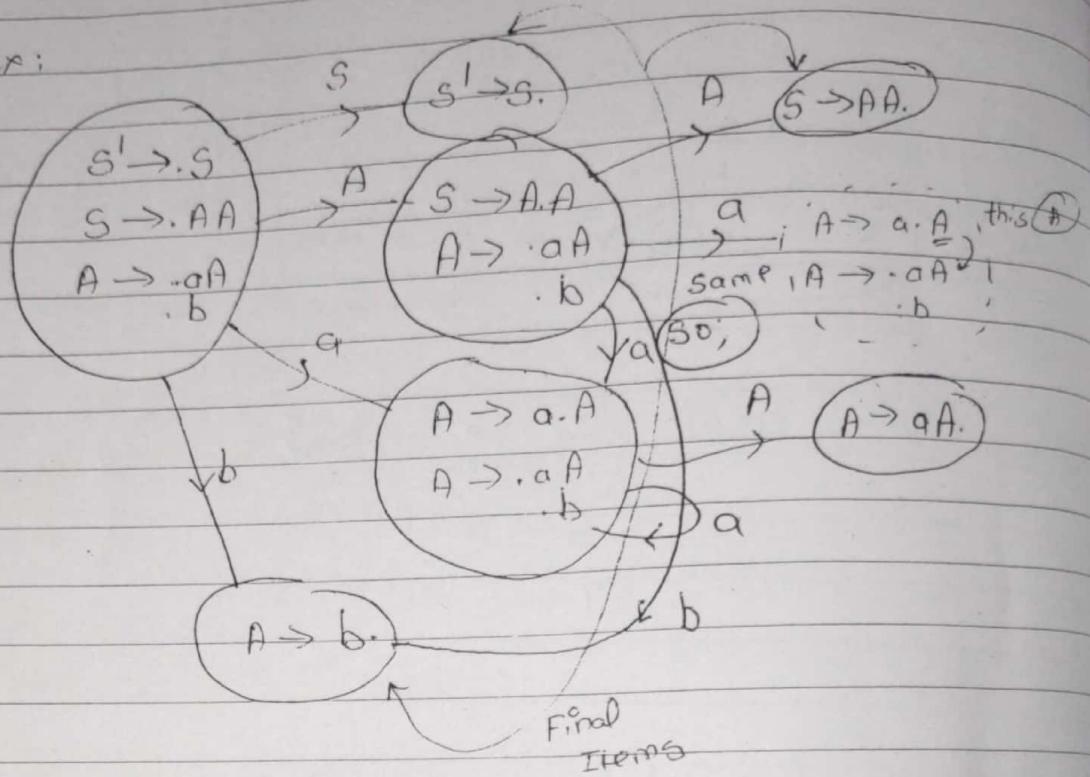
closure (closure)

$$S' \rightarrow S$$



goto (go from one state to beginning)

For ex:



→ Parsing Table consists of 2 parts: → Action Part
→ Goto Part

Construction of Parsing Table → consists of terminal symbols like a, b, \$

	Action			Goto		consists of Variables (Non-Terminal)
	a	b	\$	S	A	[no need to write \$]
0	s_3	s_4				
1						Accept
2	s_3	s_4				
3	s_3	s_4				
4						Accept at $s^1 \rightarrow s_1 s_1$
5	s_1	s_1	s_1			
6	s_2	s_2	s_2			

Timing
conventions]

Action Part/
non-terminals:

we use
any key + β
any numbers

we have;

$$s^1 \rightarrow s$$

$$s \rightarrow A A (s_1)$$

$$A \rightarrow a A \quad | \cdot b \quad = (s_3) \quad \text{reduction numbers}$$

Note $S \rightarrow a A B$

Final item at last:

$s \rightarrow a A B$ = ready for
reduction

We have;

$$S \rightarrow A A \text{ gives } \underline{\underline{abb}}$$

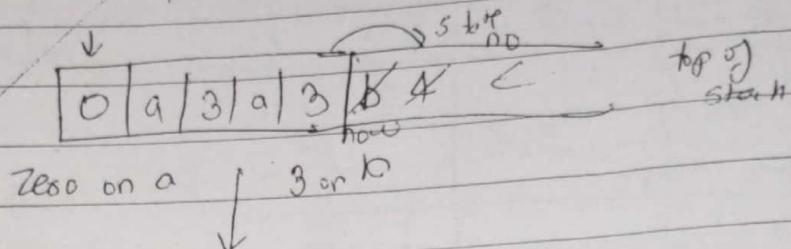
$$\rightarrow a A A$$

$$\rightarrow a a A$$

$$\rightarrow a A b A$$

$$\rightarrow a abb$$

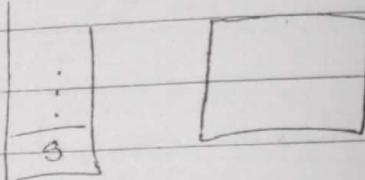
$\alphaabb\$\nmid$



we have

$a_1 a_2 \mid \$$

\downarrow
 $\boxed{0 \mid a \mid 3 \mid a \mid 3 \mid A \mid 6 \mid}$,
 replace 4 of them
 $A \Rightarrow aA$ (2)
 by
 $A \#$



Passing Table consulting w/ L.R(0)

$\boxed{0 \mid a \mid 3 \mid A \mid 6 \mid \mid \mid}$,
 # on 6 $\Rightarrow 2$

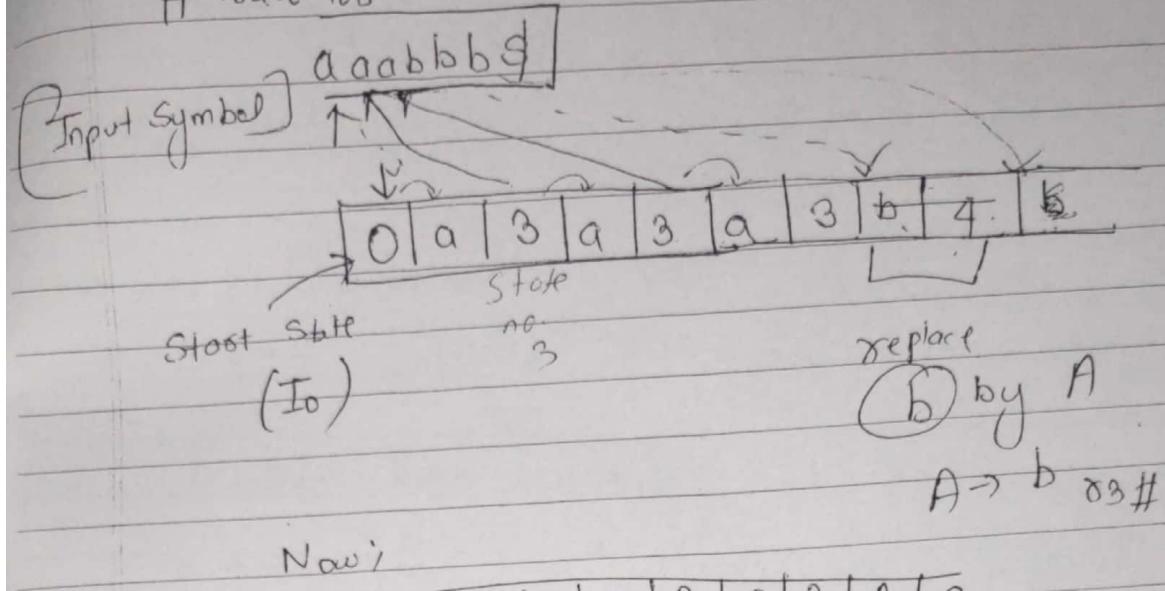
[Storage]

on
 $\$$]
 \downarrow
 $\boxed{0 \mid A \mid 2 \mid b \mid 4 \mid}$,

$\boxed{0 \mid s \mid 1 \mid}$,
 Accept

$\boxed{0 \mid A \mid 2 \mid A \mid 5 \mid}$,

Trace for :



SLR(1) Parsing Table

		Action	Note	
		a	b	\$
		s ₃	s ₃	s ₃
0				Accept
1				
2		s ₃	s ₄	
3		s ₃	s ₄	
4		γ ₃	γ ₃	γ ₃
5				γ ₁
6		γ ₂	γ ₂	γ ₂

(Hijo entire row γ_1 कैसा जाएगी।)

following L.H.S		First	Follow
$S \rightarrow AA$	(S1)	{a, b}	{\$}
$A \rightarrow aA \mid b$	(S2)	{a, b}	{a, b, \$}

Note: In SLR(1) Parsing Table; reduction (δ) is only done for Follow of Left Hand Side (L.H.S).

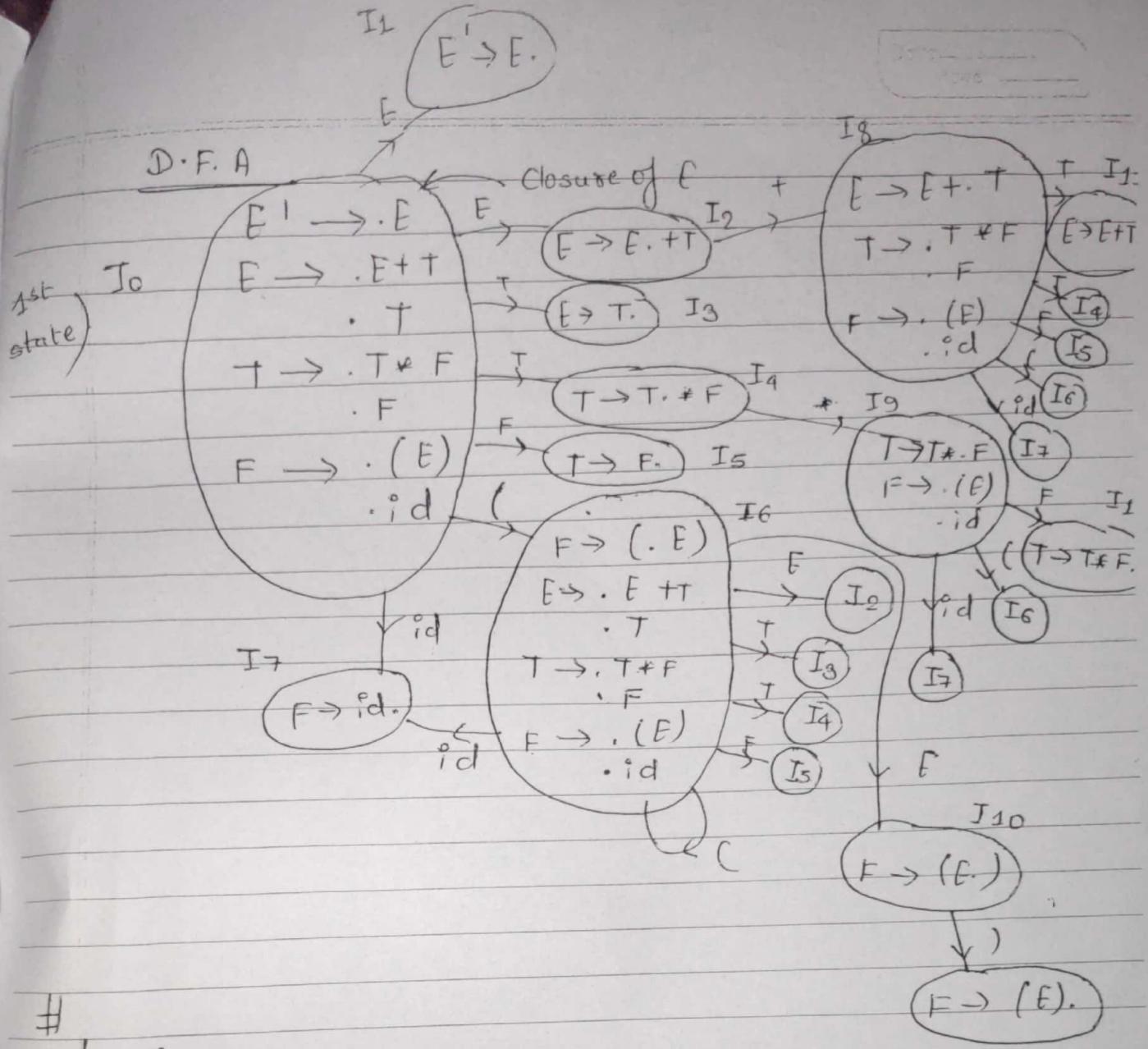
↳ Everything is same for L.R(0) and SLR(1) Parsing Table; except for (δ_x)/reduction ↳ follow of L.H.S //

Q. Construct L.R(0) and S.L.R(1) Parsing Table for the Grammar given below:

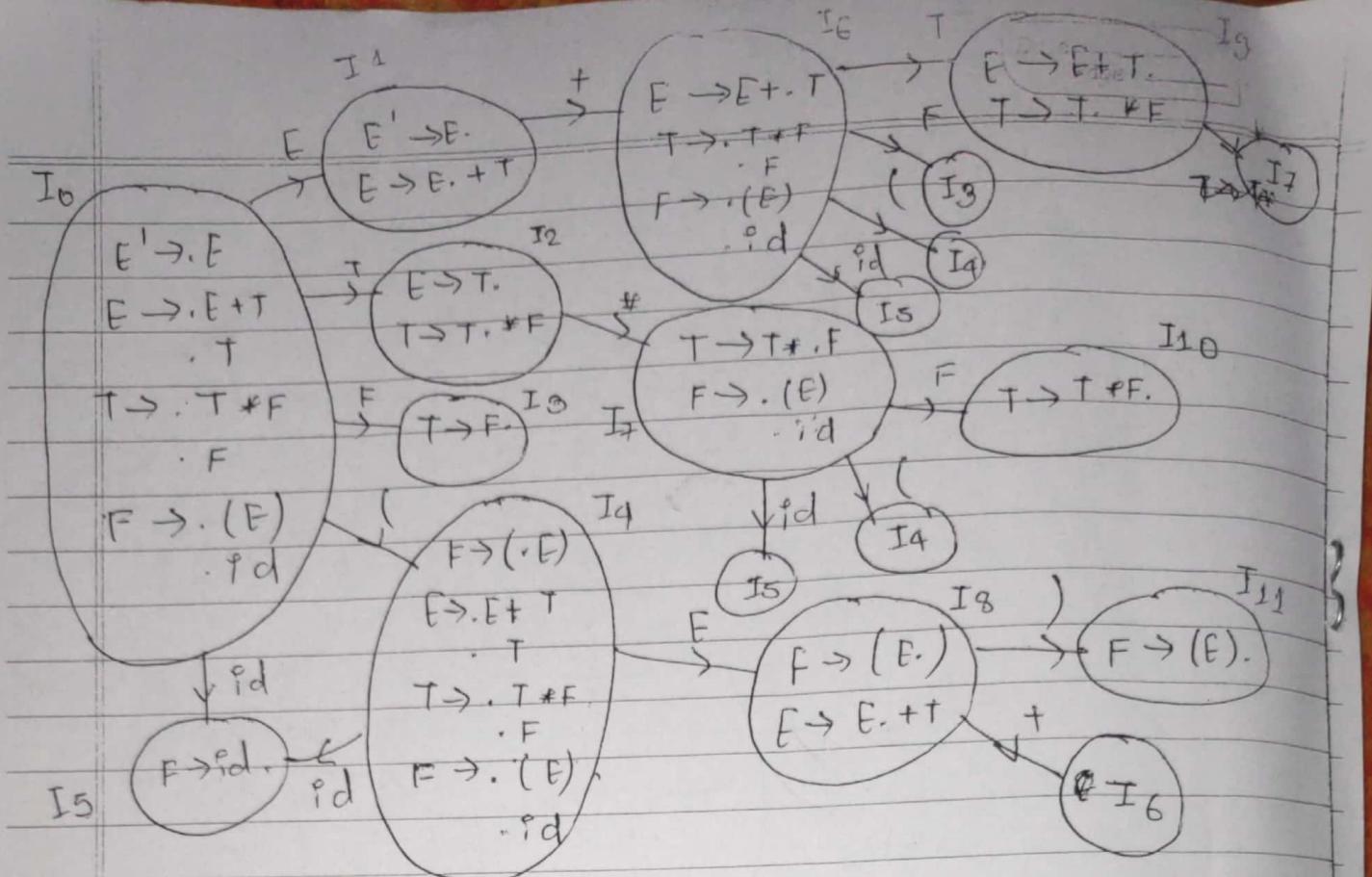
$$\begin{aligned} E &\longrightarrow E + T \mid T \\ T &\longrightarrow T * F \mid F \\ F &\longrightarrow (E) \mid id \end{aligned}$$

Soln: Augmenting the given grammar; we have:

$E' \rightarrow E$
$E \rightarrow E + T \mid T$
$T \rightarrow T * F \mid F$
$F \rightarrow (E) \mid id$



#	Action	E	T	F	(don't worry E^1 here)
0	$\text{id} + * () \$$	S7	S6		
1					
2					
3					
4					
5					
6					
7					
8					
9					
10					
11					
12					
13					



Action

	E	T	F
fd	1	2	3
+	55		
*			
(
)			
\$			

1 56

2 57

3 Final Item

	E	T	F
4	8	2	3

5

6

7

8

9

10

11

Goto