INDIAN INSTITUTE OF TECHNOLOGY GUWAHATI
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ME 543 Computational Fluid Dynamics
Computer Assignment – 2

Solve the following non-dimensional partial differential equation for **Couette Flow** using finite difference method with specified boundary conditions for ***j*=1** to ***j*=101**(M) grid size as shown in Fig. 1. Use **pseudo-transient** solution approach **with initial condition of u-velocity as zero**.

$$\frac{\partial u}{\partial t} = \frac{1}{Re_H}\frac{\partial^2 u}{\partial y^2} \qquad Re_H = \frac{UH}{\nu} \qquad \epsilon = \sqrt{\frac{\sum_{j=1,M}(u^{n+1}-u^n)^2}{M}}$$

1. Explicit method : **FTCS**
2. Implicit method
   a) **BTCS**: Point Gauss-Seidel iterative method
   b) **BTCS**: Line Gauss-Seidel iterative method (TriDiagonal Matrix Algorithm)
   c) **Crank-Nicolson**: Line Gauss-Seidel iterative method (TriDiagonal Matrix Algorithm)

Discretize the above PDE using the discretization schemes mentioned above with uniform grid of M. Take Re_H=100 and $\Delta t = 5 \times 10^{-3}$ for Explicit method and $\Delta t = 10^{-2}$ for Implicit method.

Submit results in terms of velocity profiles at different time* including steady state results as shown in Fig. 2, **convergence history** (**ε vs *t***) for all schemes in a single plot and report on discretized algebraic equation of each discretization scheme, comparison study of number of time iterations and physical time taken to converge up to $\epsilon < 10^{-6}$.

***FTCS:** *t* =0.5, 2.5, 10, 25, converged result and **Crank-Nicolson:** *t*=1, 5, 10, converged result

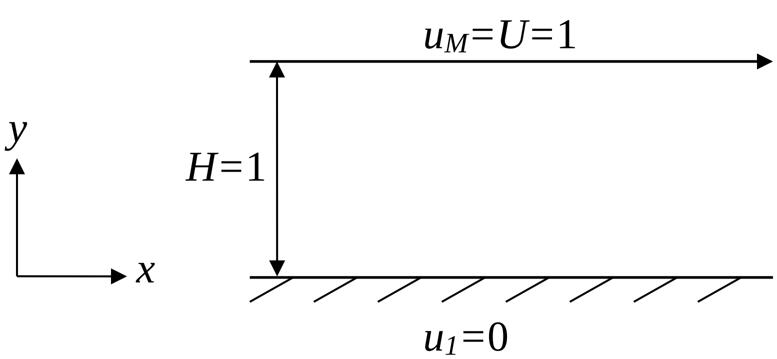

Fig. 1

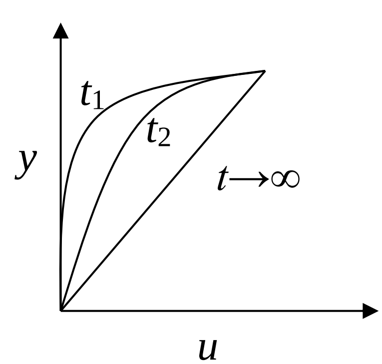

Fig. 2