

Formula File

Thursday, 3 October, 2024

04:41 PM

$$E[X] = \sum p_i * \text{Face_value}(\text{bond})$$

$$\text{Var} = E[X^2] - E[X]^2$$

$$P_0(1+r)^T = P_1$$

Special Case:

$$FV/(1+r) + FV/(1+r)^2 + FV/(1+r)^3 \dots = FV/r[1-1/(1+r)^T]$$

$$FV = (1+r/n)^{nT}$$

Choice Sets (m is income, c is consumption, p is price)

$$\text{slope} = -p_1(\text{Horizontal/x-axis})/p_2(\text{vertical/y-axis})$$

$$c_2 = m_2 + (1+r)(m_1 - c_1)$$

$$P_1 = P_0 e^{rT} \text{ (If return is continuous)}$$

Perpetuities

$$PV = C/r - \text{From next year return}$$

$$PV = C + C/r - \text{From current year return}$$

$$PV = C/r - g - \text{For growth, g, on investment on every time period}$$

Annuities

$$PV = C/r[1-1/(1+r)^T]$$

$$FV = C * ((1+r)^T - 1)/r$$

$$PV = \frac{C}{r-g} \left[1 - \left(\frac{1+g}{1+r} \right)^T \right]$$

Arbitrage Opportunity

$$1+r > p_1/p_0$$

$$1+r = p_1/p_0 - \text{No arbitrage condition}$$

Loan and Balance Payment

$$B_m = P * ((1+r)^n - (1+r)^m) / ((1+r)^n - 1)$$

$$EMI = P * r / [1 - 1/(1+r)^T], \quad r = \text{Monthly interest rate}, T = \text{years} * 12$$

Forward- Looking Dividend Yield

$$\text{Dividends } D \text{ Next Year} / \text{Stock Price } P \text{ today} = r - g$$

$$\text{Profitability Index} = NPV / - \text{payout}$$

Maturity and Duration

$$Duration = \frac{\sum C_t t}{\sum C_t}$$

$$Macauley's Duration = \frac{\sum C_t t}{\sum C_t}, C_t = NPV$$

CPI and Inflation

CPI = cost of basket in current year / cost of basket in base year * 100

Inflation = Year to year change in CPI starting from base year.

Nominal and Real GDP

Nominal GDP = \sum cost * quantity, cost and quantity from current year

Real GDP = \sum cost * quantity, cost from base year and quantity from current year

GDP Deflator = Nominal GDP / Real GDP

Interest Rates

$$r_t = P_t(1+i_t)/P_{t+1} - 1$$

$$r_t = (1+i_t)/(1+\pi_{t+1}) - 1 \quad i_t : \text{Nominal interest rate}, \pi_{t+1} : \text{Inflation}$$

$$r_t \approx i_t - \pi_{t+1}$$

$$\text{Holding rate of return} = (1+r)^T - 1$$