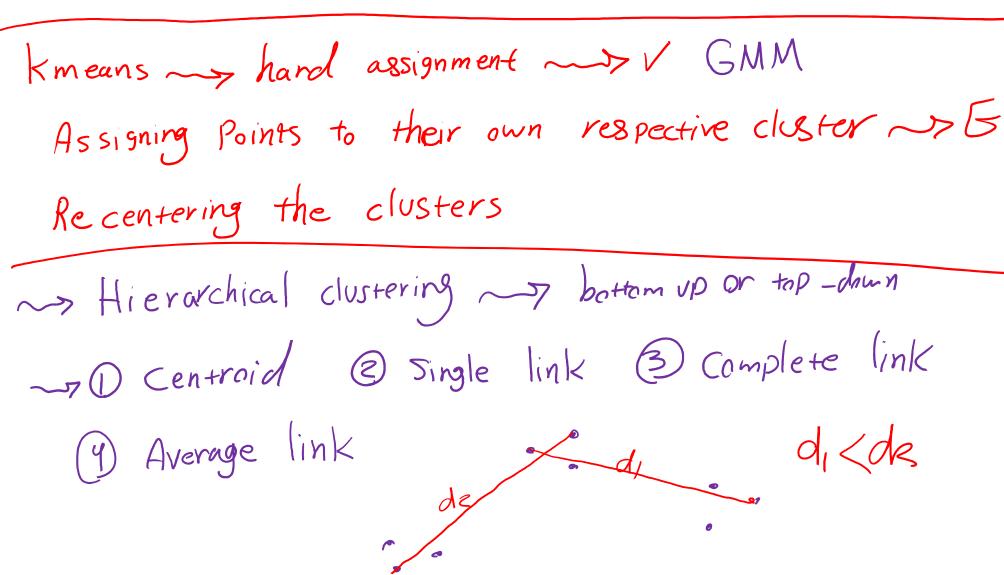
Inline-style:

![alt text](https://github.com/adam-p/markdown-here/raw/master/src/common/images/icon48.png)







Lecture 08 Density-Based Clustering

Mahdi Roozbahani Georgia Tech

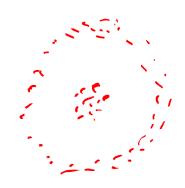
when you're a constant and you see d/dx



Outline

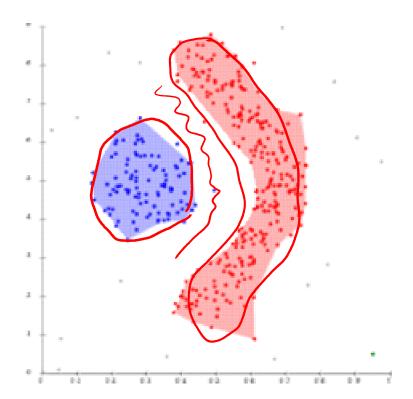
- Overview
- Basic Concepts
- The DBSCAN Algorithm
- Analysis of DBSCAN

Density-Based Clustering



Basic Idea

- Clusters are dense regions in the data space, separated by regions of lower density
- A cluster is defined as a maximal set of density-connected points
- Detect arbitrarily shaped clusters



Method

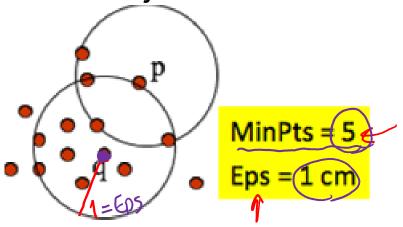
DBSCAN (<u>Density-Based Spatial</u>
 <u>Clustering of Applications with Noise</u>)

Outline

- Overview
- Basic Concepts
- The DBSCAN Algorithm
- Analysis of DBSCAN

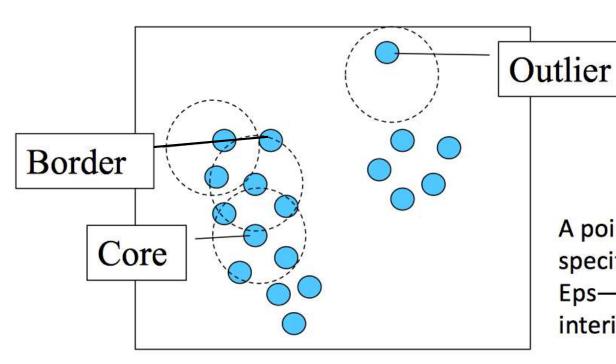
High Density v.s. Low Density

- Two parameters
 - _δ Eps (ε): Maximum radius of the neighborhood
 - MinPts: Minimum number of points in the Eps-neighborhood of a point
- High density: ε-Neighborhood of an object contains at least MinPts of objects



Density of **p** is low Density of **q** is high

Core Points, Border Points, and Outliers



 $\varepsilon = 1$ unit, MinPts = 5

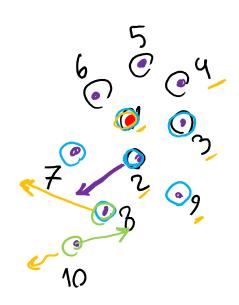
Given ε and MinPts, categorize the objects into three exclusive groups.

A point is a core point if it has more than a specified number of points (MinPts) within Eps—These are points that are at the interior of a cluster.

A border point has fewer than MinPts within Eps, but is in the neighborhood of a core point.

A noise point is any point that is not a core point nor a border point.

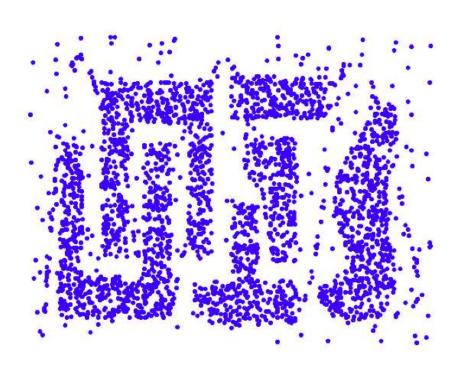
MinPts = 5 Eps = 1

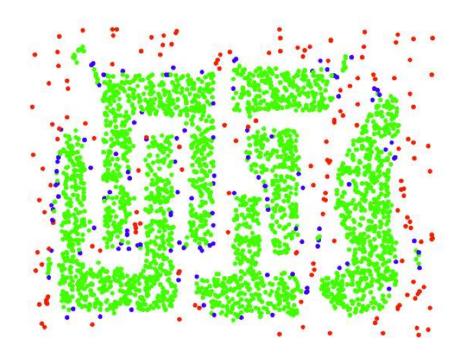


1: as a core Point

- (2) is a core Print
- (B) a border Point
- 8) is a cove Paint

Examples





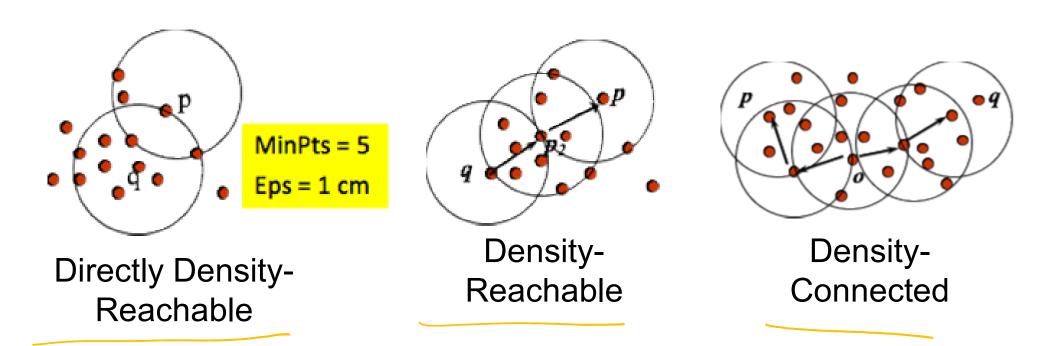
Original Points

Point types: core, border and outliers

 ε = 10, MinPts = 4

Density-based related points

- Direct density reachability:
 - An object p is directly density-reachable from object q if (1) q is a core object; and (2) p is in q's ε-neighborhood

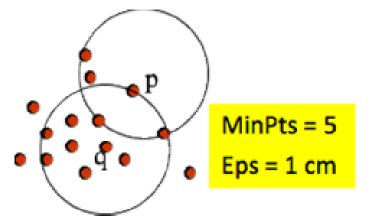


Density-based related points

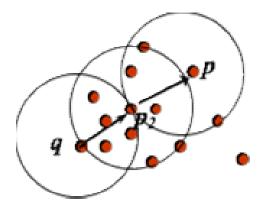
Density reachability:

A point p is density-reachable from a point q if there is a chain of points $p_1, ..., p_n, p_1 = q, p_n = p$ such that p_{i+1} is directly density-reachable from p_i

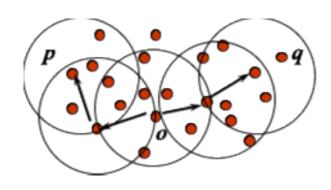
$$p_1 = q \rightarrow p_2 \rightarrow \dots \rightarrow p_n = q$$



Directly Density-Reachable



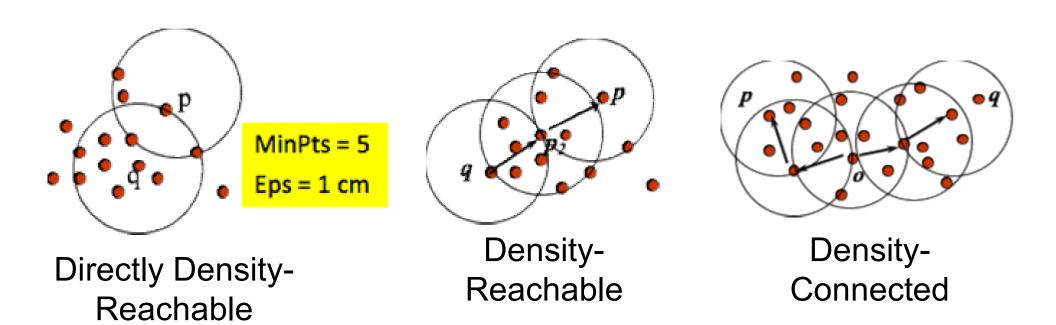
Density-Reachable



Density-Connected

Density-based related points

- Density connectivity:
 - A point p is density-connected to a point q if there is a point o such that both p and q are density-reachable from o

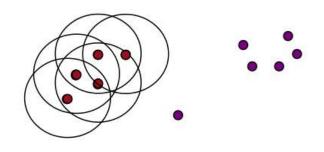


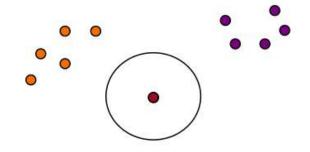
Outline

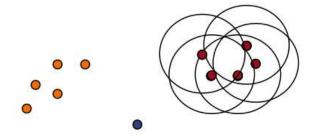
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The DBSCAN Algorithm

```
DBSCAN(D, eps, MinPts)
C = 0
for each unvisited point P in dataset D
     mark P as visited
     NeighborPts = regionQuery(P, eps)
     if sizeof(NeighborPts) < MinPts
          mark P as NOISE
     else
          C = next cluster
          expandCluster(P, NeighborPts, C, eps, MinPts)
expandCluster(P, NeighborPts, C, eps, MinPts)
     add P to cluster C
     for each point P' in NeighborPts
          if P' is not visited
               mark P' as visited
               NeighborPts' = regionQuery(P', eps)
               if sizeof(NeighborPts') >= MinPts
                    NeighborPts = NeighborPts joined with NeighborPts'
          if P' is not yet member of any cluster
               add P' to cluster C
```







regionQuery(P, eps) return all points within P's eps-neighborhood (including P)

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DBSCAN is Sensitive to Parameters

Figure 8. DBScan results for DS1 with MinPts at 4 and Eps at (a) 0.5 and (b) 0.4.

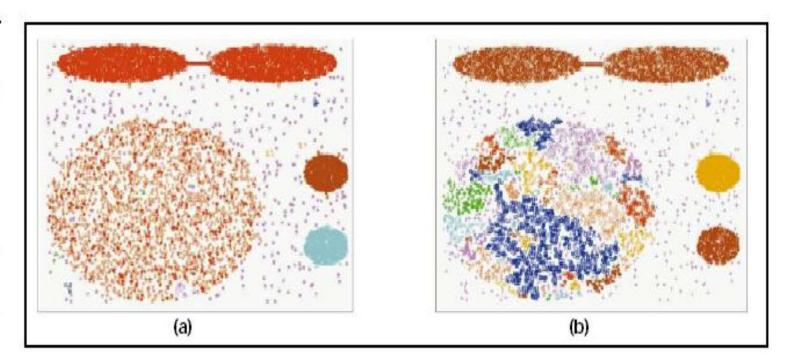


Figure 9. DBScan results for DS2 with MinPts at 4 and Eps at (a) 5.0, (b) 3.5, and (c) 3.0.

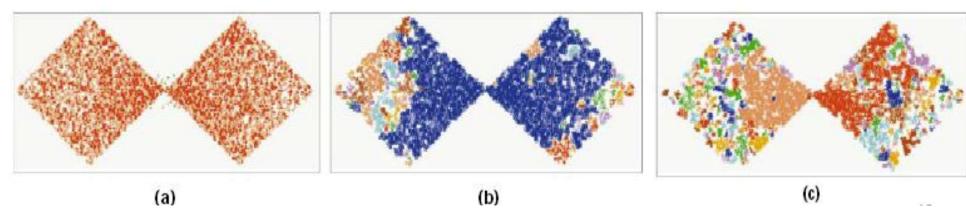
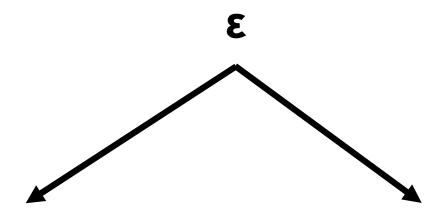


Image Credit: George Karypis.



High value (what will happen?)

Low value (what will happen?)

Clusters will merge and the majority of data points will be in the same cluster

A large part of data won't be clustered and considered as outliers. Because, they won't satisfy the number of pints to create a dense region

Do we need to define the number of clusters in DBSCAN?

Nope

Minimum number of Points (MinPts)

Every point will be a cluster on its own, Why?

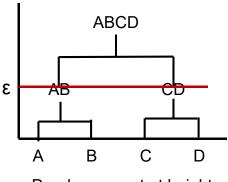
MinPts = 1?

Don't forget, in DBSCAN, a core point is counted as the number of neighboring points

MinPts = 2?







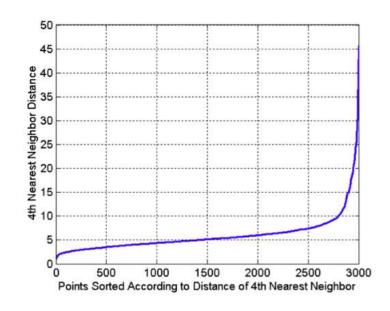
Dendogram cut at height ε

So, MinPts should be at least 3

Rule of thumb, MinPts >= D+1; For noisy data => MinPts = 2*D (yield more significant clusters)

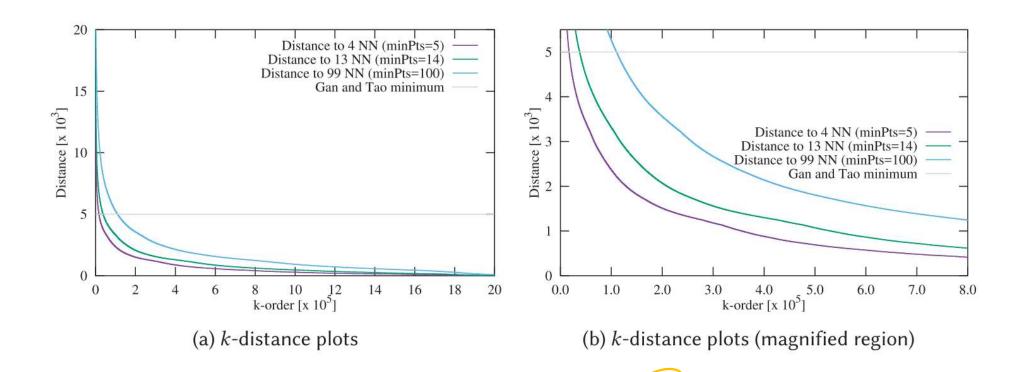
How about Eps? (Elbow effect)

- Idea is that for points in a cluster, their kth nearest neighbors are at roughly the same distance
- Noise points have the kth nearest neighbor at farther distance
- So, plot sorted distance of every point to its kth nearest neighbor



Here we have 3000 points and x-axis shows just a point index. Point indices are sorted in ascending order based on their 4th nearest neighbor distance

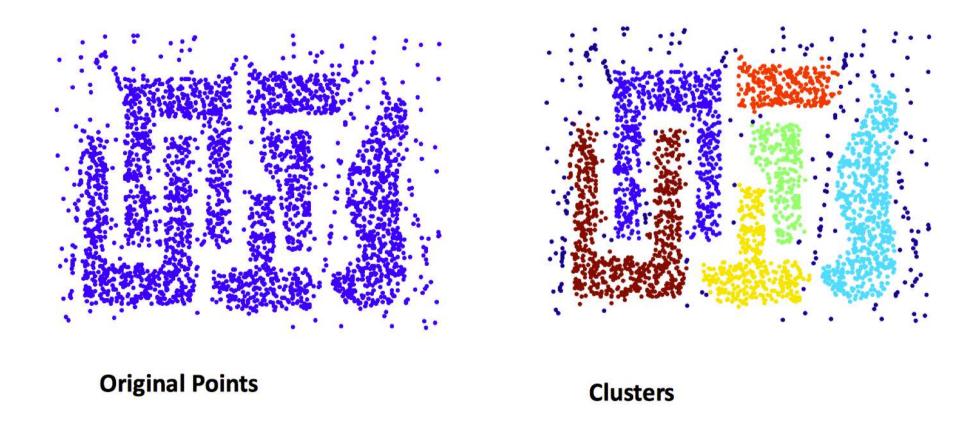
Elbow effect another example



minPts often does have a significant impact on the clustering results

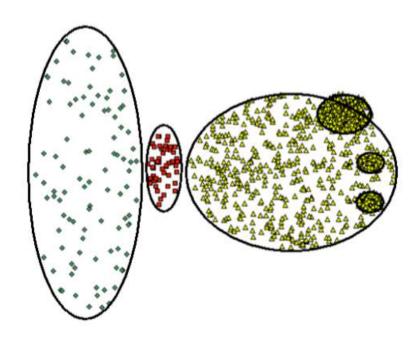
When DBSCAN Works Well

- Robust to noise
- Can detect arbitrarily-shaped clusters

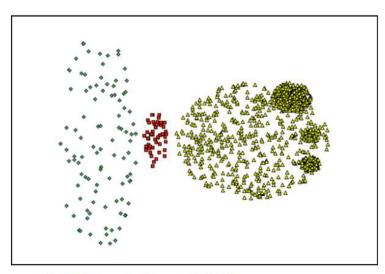


When DBSCAN Does NOT Work Well

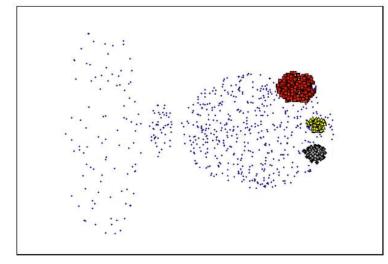
- Cannot handle varying densities
- Sensitive to noise (parameters) hard to determine the best setting of parameters



Original Points



(MinPts=4, Eps=9.92).



(MinPts=4, Eps=9.75)

Take-Home Messages

- The basic idea of density-based clustering
- The two important parameters and the definitions of neighborhood and density in DBSCAN
- Core, border and outlier points
- DBSCAN algorithm
- DBSCAN's pros and cons