The report is based on the "**Heart Failure**" Dataset. The "Heart Failure" Dataset is taken from UCI Machine Learning Repository. The current version of the dataset was elaborated by Davide Chicco (Krembil Research Institute, Toronto, Canada) and donated to the University of California Irvine Machine Learning Repository under the same Attribution 4.0 International (CC BY 4.0) copyright in January 2020. This dataset contains the medical records of 299 patients who had heart failure, collected during their follow-up period, where each patient profile has 13 clinical features. The Dataset Description is as follows:

Data Set characteristics	Multivariate	
Number Of Instances	299	
Area	Life	
Number Of Attributes	13	
Attribute Characteristics	Integer, Real	
Missing Values	N/A	

The description of 13 clinical features (variables) is as follows:

Variable Name	Description	Type	Units
Age	Age of the paitent	Numerical	Years
Anemia	Decrease in the number of blood cells	Categorical	Boolean
High Blood Pressure	Determines whether paitent has hypertension or not	Categorical	Boolean
Creatinine phosphokinase (CPK)	Level of CPK enzyme in blood	Numerical	Mcg/L
Diabetes	Determines whether paitent has diabetes or not	Categorical	Boolean
Ejection fraction	percentage of blood leaving the heart at each contraction	Numerical	Percentage
Platelets	Platelets in blood	Numerical	Kiloplatelets/mL
Sex	Woman or Male	Categorical	Binary
Serum creatinine	Level of serum creatinine in blood	Numerical	Mg/dL
Serum sodium	Level of serum sodium in blood	Numerical	mEq/L
Smoking	Determines whether paitent smokes or not	Categorical	Boolean
Time	Follow Up Period	Numerical	Days
Death Event	Determines whether paitent was deceased during follow up period	Categorical	Boolean

1. Loading Dataset and libraries:

The Data file has a '.csv' extension. We have used the read.csv function to load the dataset into "RStudio". Also, header = True indicates that the first row of values in the .csv is set as header information (column names). We are loading libraries "dplyr", "ggpubr" and "caTOOLs". The detailed information for the following libraries is as follows:

- Dplyr: It is a grammar of data manipulation, providing a consistent set of verbs that help you solve the most common data manipulation challenges.
- Ggpubr: It is a data visualization library which facilitates the creation of beautiful ggplot2-based graphs.
- caTools: It contains several basic utility functions including moving (rolling, running) window statistic functions, read/write for GIF and ENVI binary files, fast calculation of AUC, etc.

2. Accuracy Issues and Missing Values:

"Str" function is being used to check the structure of the dataset.

```
str(df)
'data.frame':
             299 obs. of 13 variables:
                       : num 75 55 65 50 65 90 75 60 65 80 ...
$ age
$ anaemia
                       : int 0001111101...
$ creatinine_phosphokinase: int 582 7861 146 111 160 47 246 315 157 123 ...
                     : int 0000100100...
$ diabetes
: int 20 38 20 20 20 40 15 60 65 35 ...
                      : num 265000 263358 162000 210000 327000 ...
$ platelets
$ serum_creatinine
                       : num 1.9 1.1 1.3 1.9 2.7 2.1 1.2 1.1 1.5 9.4 ...
                       : int 130 136 129 137 116 132 137 131 138 133 ...
: int 1 1 1 1 0 1 1 1 0 1 ...
$ serum_sodium
$ sex
                       : int 0010010101 ...
$ smoking
$ time
                       : int 46778810101010...
$ DEATH_EVENT
                       : int 1111111111...
```

This function provides us a brief overview of the dataset. The structure clearly depicts that we have columns with numeric and integer values in the dataset.

Then, we are using the "summary" function to get the summary of all columns and NA values.

The summary has the following structure:

MIN 1st Quartile Meidian	Mean 3rd Quartile	MAX
--------------------------	-------------------	-----

25% values 75% values

```
creatinine_phosphokinase
                                                                diabetes
                                                                               ejection_fraction
                    anaemia
Min.
       :40.00
                Min.
                        :0.0000
                                  Min.
                                         : 23.0
                                                             Min.
                                                                    :0.0000
                                                                               Min.
                                                                                      :14.00
                                   1st Qu.: 116.5
1st Qu.:51.00
                                                                               1st Qu.:30.00
                1st Qu.:0.0000
                                                             1st Qu.:0.0000
Median:60.00
                Median :0.0000
                                  Median : 250.0
                                                             Median :0.0000
                                                                               Median :38.00
                                         : 581.8
                                                                                      :38.08
       :60.83
                Mean
                        :0.4314
                                   Mean
                                                             Mean
                                                                    :0.4181
                                                                               Mean
3rd Ou.:70.00
                 3rd Qu.:1.0000
                                   3rd Qu.: 582.0
                                                             3rd Qu.:1.0000
                                                                               3rd Qu.:45.00
                                          :7861.0
       :95.00
                Max.
                        :1.0000
                                   Max.
                                                             Max.
                                                                    :1.0000
                                                                               Max.
                                                                                      :80.00
                                                         serum_sodium
high_blood_pressure
                                      serum_creatinine
                       platelets
                                                                               sex
       :0.0000
                     Min.
                            : 25100
                                      Min.
                                              :0.500
                                                        Min.
                                                                :113.0
                                                                         Min.
                                                                                 :0.0000
Min.
1st Qu.:0.0000
                     1st Qu.:212500
                                       1st Qu.:0.900
                                                        1st Qu.:134.0
                                                                         1st Qu.:0.0000
Median :0.0000
                     Median :262000
                                                         Median :137.0
                                                                         Median :1.0000
                                       Median :1.100
Mean
       :0.3512
                     Mean
                            :263358
                                       Mean
                                             :1.394
                                                                :136.6
                                                                         Mean
                                                                                 :0.6488
                                                         Mean
                     3rd Qu.:303500
                                                         3rd Qu.:140.0
3rd Qu.:1.0000
                                       3rd Qu.:1.400
                                                                          3rd Qu.:1.0000
                            :850000
                                              :9.400
                                                                :148.0
Max.
       :1.0000
                     Max.
                                       Max.
                                                         Max.
                                                                         Max.
                                                                                 :1.0000
   smoking
                       time
                                   DEATH_EVENT
Min.
       :0.0000
                 Min.
                         : 4.0
                                   Min.
                                          :0.0000
                 1st Qu.: 73.0
1st Qu.:0.0000
                                   1st Qu.:0.0000
Median :0.0000
                 Median :115.0
                                   Median :0.0000
Mean
       :0.3211
                 Mean
                         :130.3
                                  Mean
                                          :0.3211
3rd Qu.:1.0000
                  3rd Qu.:203.0
                                   3rd Qu.:1.0000
       :1.0000
                                          :1.0000
                         :285.0
Max.
                 Max.
                                  Max.
```

The "head" function gives the first 6 values in each column. If we specify the column name along with the data frame name inside the header function them we'll get the first six values of the specified column.

```
age anaemia creatinine_phosphokinase diabetes ejection_fraction high_blood_pressure platelets
  75
55
             0
                                                     0
                                                                         20
                                        582
                                                                                                        265000
2
3
             0
                                       7861
                                                     0
                                                                         38
                                                                                                  0
                                                                                                        263358
   65
             0
                                        146
                                                     0
                                                                         20
                                                                                                  0
                                                                                                        162000
4
5
6
   50
                                        111
                                                     0
                                                                         20
                                                                                                  0
                                                                                                        210000
             1
   65
             1
                                        160
                                                     1
                                                                         20
                                                                                                        327000
  90
                                                     0
                                                                                                       204000
                                         47
                                                                         40
             1
  serum_creatinine serum_sodium sex smoking time DEATH_EVENT
1
                                130
                                                0
                                                      4
                 1.9
                                       1
2
3
4
5
                                                0
                                136
                 1.1
                                                      6
                                                                    1
                 1.3
                                129
                                                                    1
                                                0
                 1.9
                                137
                                       1
                                                                    1
                                116
                                       0
                                                0
                                                      8
                                132
                                                      8
                 2.1
```

The function "colnames" gives us the name of all columns in the data frame.

The function "colSums(is.na(df))" gives column wise sum of NA values.

3. Converting Numerical Datatype to Categorical Datatype

We have columns with Datatype as "numeric" or "integer". That is why we'll be converting datatypes of columns with binary or boolean values to categorical. In R, the "as.factor" function is used to convert the numeric datatype into factorial datatype. Anaemia, diabetes, high_blood_pressure, sex, smoking, and death_event we'll be converting all the mentioned columns to the categorical data type.

For the age column, we can see that there is one value in decimal. Someone might have included the value by mistake so we'll be rounding off that value to the nearest integer.

```
"48"
 "50"
                                  "53"
                                             "54"
                                                        "55"
                                                                   "56"
                                                                                          "58"
                                                                                                     "59"
                                                                               "66"
                                                        "64"
"60"
                       "61"
                                                                    "65"
                                                                                          "67"
                                                                                                     "68"
                                                                                          "80"
$age<-round(df$age)</pre>
```

4. Significant test (Variance test, Two-sample T-test, Chi-square test)

a. Age

Dividing the dataset into the two samples on the basis of Death_Event and performing t-test on age.

Performing F-test to compare the variance of the two samples.

H₀: Variance of two samples are equal

H_a. Variance of two samples are unequal.

```
p = 0.01
```

- => p < 0.05 (Level of significance)
- => We reject null hypothesis.
- => We conclude that the variance of the two samples are significantly different.

Further for the t-test, we'll be comparing the mean of the two samples.

$$H_0$$
: $\mu 1 = \mu 2$
 H_a : $\mu 1 \neq \mu 2$

** var.equal = F indicates that variance of two samples is not equal**

```
p = 4.708e-05
```

- => p < 0.05 (Level of significance)
- => We reject null hypothesis.
- => We conclude that the mean of the two samples are significantly different.
- => We conclude that age is a significant variable.

b. Creatinine Phosphokinase

Dividing the dataset into the two samples on the basis of Death_Event and performing t-test on **creatinine phosphokinase**.

Performing F-test to compare the variance of the two samples.

H₀: Variance of two samples are equal

H_a. Variance of two samples are unequal.

```
p = 3.354e-11
=> p < 0.05 (Level of significance)
```

- => We reject null hypothesis.
- => We conclude that the variance of the two samples are significantly different.

Further for the t-test, we'll be comparing the mean of the two samples.

```
H_0: \mu 1 = \mu 2
H_a: \mu 1 \neq \mu 2
```

** var.equal = F indicates that variance of two samples is not equal**

```
p = 0.3692
```

- => p > 0.05 (Level of significance)
- => We fail to reject null hypothesis.
- => We conclude that the mean of the two samples are not significantly different.
- => We conclude that **creatinine_phosphokinase** is not a significant variable.

c. Ejection Fraction

Dividing the dataset into the two samples on the basis of Death_Event and performing t-test on ejection_fraction.

Performing F-test to compare the variance of the two samples.

H₀: Variance of two samples are equal

H_a. Variance of two samples are unequal.

```
p = 0.09577
```

- => p > 0.05 (Level of significance)
- => We fail to reject null hypothesis.
- => We conclude that the variance of the two samples are not significantly different.

Further for the t-test, we'll be comparing the mean of the two samples.

```
H_0: \mu 1 = \mu 2
H_a: \mu 1 \neq \mu 2
```

** var.equal = T indicates that variance of two samples is equal**

```
p = 2.453e-06
```

- => p < 0.05 (Level of significance)
- => We reject null hypothesis.
- => We conclude that the mean of the two samples are significantly different.

=> We conclude that ejection fraction is a significant variable.

d. Platelets

Dividing the dataset into the two samples on the basis of Death_Event and performing t-test on platelets .

Performing F-test to compare the variance of the two samples.

H₀: Variance of two samples are equal

H_a. Variance of two samples are unequal.

```
> var.test(no_death_platelets, death_platelets)
     F test to compare two variances

data: no_death_platelets and death_platelets
F = 0.97991, num df = 202, denom df = 95, p-value = 0.8915
alternative hypothesis: true ratio of variances is not equal to 1
95 percent confidence interval:
     0.6854169 1.3706295
sample estimates:
ratio of variances
     0.9799146
```

```
p = 0.8915
```

- => p > 0.05 (Level of significance)
- => We fail to reject null hypothesis.
- => We conclude that the variance of the two samples are not significantly different.

Further for the t-test, we'll be comparing the mean of the two samples.

$$H_0$$
: $\mu 1 = \mu 2$
 H_a : $\mu 1 \neq \mu 2$

^{**} var.equal = T indicates that variance of two samples is equal**

```
p = 0.3692
```

- => p > 0.05 (Level of significance)
- => We fail to reject null hypothesis.
- => We conclude that the mean of the two samples are not significantly different.
- => We conclude that platelets is not a significant variable.

.....

e. Serum Creatinine

Dividing the dataset into the two samples on the basis of Death_Event and performing t-test on serum creatinine.

Performing F-test to compare the variance of the two samples.

H₀: Variance of two samples are equal

H_a. Variance of two samples are unequal.

```
p = 2.2e-16
```

- => p < 0.05 (Level of significance)
- => We reject null hypothesis.
- => We conclude that the variance of the two samples are significantly different.

Further for the t-test, we'll be comparing the mean of the two samples.

$$H_0$$
: $\mu 1 = \mu 2$
 H_a : $\mu 1 \neq \mu 2$

** var.equal = F indicates that variance of two samples is not equal**

```
p = 2.453e-06
```

- => p < 0.05 (Level of significance)
- => We reject null hypothesis.
- => We conclude that the mean of the two samples are significantly different.
- => We conclude that **serum_creatinine** is a significant variable.

f. Serum Sodium

Dividing the dataset into the two samples on the basis of Death_Event and performing t-test on serum sodium.

Performing F-test to compare the variance of the two samples.

H₀: Variance of two samples are equal

H_a. Variance of two samples are unequal.

```
p = 0.007646
```

- => p < 0.05 (Level of significance)
- => We reject null hypothesis.
- => We conclude that the variance of the two samples are significantly different.

Further for the t-test, we'll be comparing the mean of the two samples.

```
H_0: \mu 1 = \mu 2
H_a: \mu 1 \neq \mu 2
```

** var.equal = F indicates that variance of two samples is not equal**

```
p = 0.001872
```

- => p < 0.05 (Level of significance)
- => We reject null hypothesis.
- => We conclude that the mean of the two samples are significantly different.
- => We conclude that serum_sodium is a significant variable.

g. Time

Dividing the dataset into the two samples on the basis of Death_Event and performing t-test on time.

Performing F-test to compare the variance of the two samples.

H₀: Variance of two samples are equal

H_a. Variance of two samples are unequal.

- => p > 0.05 (Level of significance)
- => We fail to reject null hypothesis.
- => We conclude that the variance of the two samples are not significantly different.

Further for the t-test, we'll be comparing the mean of the two samples.

```
H_0: \mu 1 = \mu 2
H_a: \mu 1 \neq \mu 2
```

** var.equal = F indicates that variance of two samples is equal**

```
p = 2.2e-16
```

- => p < 0.05 (Level of significance)
- => We reject null hypothesis.
- => We conclude that the mean of the two samples are significantly different.
- => We conclude that time is a significant variable.

.....

*H***0**: The Death Event is independent of the diabetes *Ha*: The Death Event is not independent of the diabetes

As the p-value 1 is greater than the 0.05 significance level, we fail to reject the null hypothesis that the Death Event is not independent of the diabetes.

.....

H0: The Death Event is independent of the anaemiaHa: The Death Event is not independent of the anaemia

As the p-value 0.3073 is greater than the .05 significance level, we do not reject the null hypothesis that the Death Event is not independent of the anaemia.

H0: The Death Event is independent of the smokingHa: The Death Event is not independent of the smoking

```
> chi_smoking_death <- chisq.test(table(df$DEATH_EVENT, df$smoking))
> chi_smoking_death

Pearson's Chi-squared test with Yates' continuity correction

data: table(df$DEATH_EVENT, df$smoking)
X-squared = 0.0073315, df = 1, p-value = 0.9318
```

As the p-value 0.9318 is greater than the .05 significance level, we do not reject the null hypothesis that the Death Event is independent of smoking.

H0: The Death Event is independent of the high blood pressureHa: The Death Event is not independent of the high blood pressure

As the p-value 0.2141 is greater than the .05 significance level, we do not reject the null hypothesis that the Death Event is not independent of the high blood pressure.

.....

H0: The Death Event is independent of the sexHa: The Death Event is not independent of the sex

```
> chi_sex_death <- chisq.test(table(df$DEATH_EVENT, df$sex))
> chi_sex_death

Pearson's Chi-squared test with Yates' continuity correction
data: table(df$DEATH_EVENT, df$sex)
X-squared = 0, df = 1, p-value = 1
```

As the p-value 1 is greater than the .05 significance level, we do not reject the null hypothesis that the Death Event is not independent of the Sex.

5. Multicollinearity

Multicollinearity occurs when an independent variable is highly correlated with one or more of the other independent variables.

The results parameter estimates are unstable & the standard errors are large.

```
ATH_EVENT~.,family = binomial,data=df)
Call:
glm(formula = DEATH_EVENT ~ ., family = binomial, data = df)
Deviance Residuals:
Min 1Q Median 3Q Max
-2.1849 -0.5705 -0.2399 0.4465 2.6671
Coefficients:
3.004 0.002661 **
                          -1.201e-06
                                                  -0.635 0.525106
3.670 0.000242
                                      1.889e-06
platelets
                          6.661e-01 1.815e-01
-6.698e-02 3.974e-02
serum_creatinine
serum_sodium
                                                  -1.686 0.091882
                          -5.340e-01 4.139e-01
                                                  -1.290 0.197051
                          -1.335e-02 4.127e-01 -0.032 0.974182
-2.105e-02 3.015e-03 -6.982 2.91e-12 ***
smokina1
time
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 375.35 on 298 degrees of freedom
Residual deviance: 219.53 on 286 degrees of freedom AIC: 245.53
Number of Fisher Scoring iterations: 6
```

<pre>> vif_values <-vif(model) > vif_values</pre>			
age	anaemia d	reatinine_phosphokinase	diabetes
1.099757	1.108486	1.087588	1.040799
ejection_fraction	high_blood_pressure	platelets	serum_creatinine
1.174256	1.061194	1.044412	1.080477
serum_sodium	sex	smoking	time
1.058970	1.377590	1.281855	1.133895

The above screenshot clearly depicts that there is ni vif(Variance Inflation Factor) value greater than 5. This clearly indicates that there is no multicollinearity issue. So we are good to go.

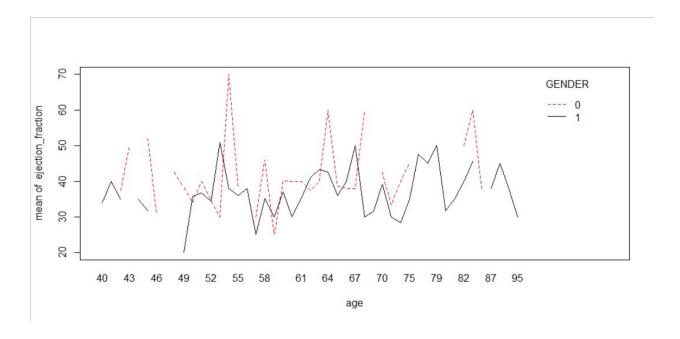
6. Interaction Plot

Interaction plots are used to understand how the value of one variable affects the value of another variable.

Parallel lines - No interaction occurs Non parallel lines - Interaction occurs

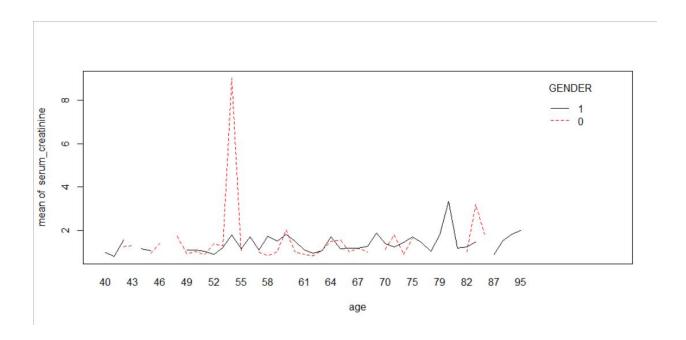
Age VS Ejection Fraction

In this interaction plot, the lines are not parallel. The interaction plot suggests there is an interaction between age and ejection fraction.



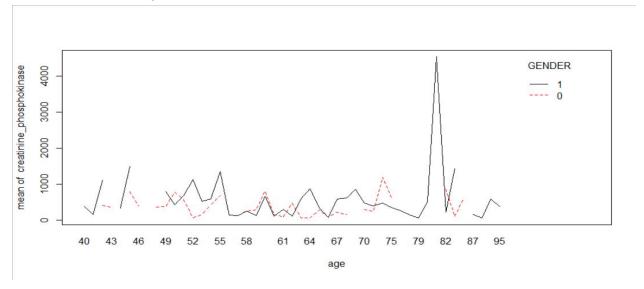
Age VS Serum Creatinine

In this interaction plot, the lines are not parallel. The interaction plot suggests there is an interaction between age and serum creatinine.



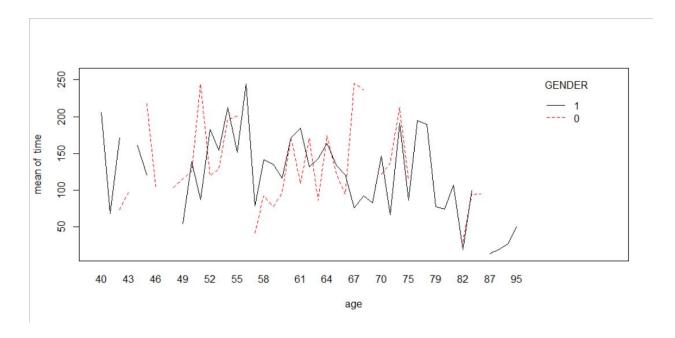
Age VS Creatinine Phosphokinase

In this interaction plot, the lines are not parallel. The interaction plot suggests there is an interaction between age and creatinine phosphokinase.



Age VS Time

In this interaction plot, the lines are not parallel. The interaction plot suggests there is an interaction between age and time.



7. Dividing the Dataset

Partitioning data into training and testing sets helps you to develop highly accurate models that are relevant to data that you collect in the future, not just the data the model was trained on. By training your data and testing it on the holdout set, you get a real sense of how accurate the model's outcomes will be, leading to better decisions and greater confidence in your model's accuracy.

Here we partition our dataset as 70% of values are included in the training set and remaining 30% into the testing set. Training dataset is used to predict the relationship between predictor variables and predicted variables. The training dataset is used to build the model and testing is used to validate the model.

```
set.seed(100)
sample_df<-sample.split(df,SplitRatio = 0.70)
train<-subset(df,sample_df==T)
test<-subset(df,sample_df==F)</pre>
```

So, after splitting our data, below image displays number of observations in training dataset and testing dataset

```
> nrow(train)
[1] 207
> nrow(test)
[1] 92
```

8. Stepwise variable selection technique

In this step, we will use the stepwise regression technique to select explanatory variables which are significant.

We begin by fitting the full model (all predictors used) and then we remove one predictor at a time based on the p-values. We repeat the process until we obtain a model with lowest AIC value and only significant predictors are used to fit the model. Detailed process is explained below.

First, we begin by fighting Full model

```
fit<-glm(DEATH_EVENT~.,family = binomial,data=train)
summary(fit)</pre>
```

Output:

```
> summary(fit)
Call:
glm(formula = factor(DEATH_EVENT) ~ ., family = binomial, data = train)
Deviance Residuals:
   Min
             10
                 Median
                               30
                                      Max
-2.0884 -0.6149 -0.2655 0.5164
                                   2.5094
Coefficients:
                         Estimate Std. Error z value Pr(>|z|)
(Intercept)
                         5.254e+00 6.811e+00 0.771 0.440486
                         4.498e-02 1.843e-02 2.440 0.014683 *
anaemia1
                        -2.836e-01 4.214e-01 -0.673 0.501007
creatinine_phosphokinase 2.739e-04
                                  1.951e-04 1.404 0.160318
diabetes1
                        1.042e-01 4.060e-01 0.257 0.797497
ejection_fraction
                        -6.337e-02 1.834e-02 -3.455 0.000551 ***
                        2.600e-01 4.152e-01 0.626 0.531274
high_blood_pressure1
platelets
                        -1.529e-06 2.199e-06 -0.695 0.487025
serum_creatinine
                        5.736e-01 1.842e-01
                                               3.114 0.001845 **
                        -3.316e-02 4.900e-02 -0.677 0.498608
serum sodium
                        -6.087e-01 4.803e-01 -1.267 0.205101
sex1
smoking1
                        -2.069e-01 5.011e-01 -0.413 0.679721
                        -1.898e-02 3.412e-03 -5.563 2.65e-08 ***
time
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 260.66 on 206 degrees of freedom
Residual deviance: 161.70 on 194 degrees of freedom
AIC: 187.7
```

As we can see, there are 8 predictors which are not significant in this model. Moreover, AIC for this model is 187.7. Model with the lowest AIC is considered the best. Observing the p-values, we conclude that the predictor diabetes is the least significant of all other predictors. Hence, we will remove diabetes and check the model again. We remove predictor one by one until the best model is reached.

Below is the code run to achieve the final model.

```
drop1(fit,test = "Chisq")
#removing diabetes as it has largest p-value=0.79
fit.one <- update(fit,. ~ . - diabetes)
summary(fit.one)
#smoking has largest p value
drop1(fit.one,test = "Chisq")
#again smoking has largest p value</pre>
```

```
fit.two <- update(fit.one,. ~ . - smoking)</pre>
summary(fit.two)
drop1(fit.two,test = "Chisq")
#again high blood presuure has largest p-value
fit.three <- update(fit.two,. ~ . - high blood pressure)</pre>
summary(fit.three)
#removing anaemia
fit.four <- update(fit.three,. ~ . - anaemia)</pre>
summary(fit.four)
#removing platelets
fit.five <- update(fit.four,. ~ . - platelets)</pre>
summary(fit.five)
#removing serium sodium
fit.six <- update(fit.five,. ~ . - serum sodium)</pre>
summary(fit.six) #178.01
#removing creatine phosphokinase
fit.seven <- update(fit.six,. ~ . - creatinine phosphokinase)</pre>
summary(fit.seven)#AIC 178.55
fit.eight <- update(fit.seven,. ~ . - sex)
summary(fit.eight)#AIC 178.27
```

Finally, we see model 'fit.six' has the lowest AIC = 178.01, also it has lower p-values of predictors compared to model 'fit.seven' and 'fit.eight'.Below is the output of model 'fit.six'.

```
> summary(fit.six) #178.01
Call:
glm(formula = factor(DEATH_EVENT) ~ age + creatinine_phosphokinase +
   ejection_fraction + serum_creatinine + sex + time, family = binomial,
   data = train)
Deviance Residuals:
   Min 1Q Median 3Q
-2.1067 -0.6108 -0.2769 0.5370 2.6108
Coefficients:
                       Estimate Std. Error z value Pr(>|z|)
                       0.3445774 1.2842949 0.268 0.788468
(Intercept)
                      0.0446994 0.0178508 2.504 0.012278 *
creatinine_phosphokinase 0.0002687 0.0001863
                                            1.442 0.149197
ejection_fraction -0.0652614 0.0176059 -3.707 0.000210 ***
                      0.5918989 0.1788088 3.310 0.000932 ***
serum_creatinine
                      -0.6419663  0.4181639  -1.535  0.124734
sex1
time
                      Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 260.66 on 206 degrees of freedom
Residual deviance: 164.01 on 200 degrees of freedom
AIC: 178.01
```

Hence, in the end, we conclude that predictors age, creatinine_phosphokinase, ejection_fraction, serum_creatinine, sex and time are significant for our analysis.

9. Comparing model with no interaction vs with interaction term

In this part, we will compare our reduced model with different models having different interaction terms. Also, we will check whether our reduced or full model is better.

Initially, we will start with the variables which were claimed to be significant after running stepwise regression .i.e. age, creatinine_phosphokinase, ejection_fraction, serum_creatinine, sex and time.

```
summary(fit2)
Call:
glm(formula = DEATH_EVENT ~ age + ejection_fraction + serum_creatinine +
   creatinine_phosphokinase + time + sex, family = binomial,
   data = train)
Deviance Residuals:
        1Q Median
                            3Q
   Min
                                   Max
-2.1067 -0.6108 -0.2769 0.5370
                                2.6108
Coefficients:
                       Estimate Std. Error z value Pr(>|z|)
                       0.3445774 1.2842949 0.268 0.788468
(Intercept)
                      0.0446994
                                0.0178508 2.504 0.012278 * 0.0176059 -3.707 0.000210 ***
                      -0.0652614
ejection_fraction
sex1
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
Null deviance: 260.66 on 206 degrees of freedom
Residual deviance: 164.01 on 200 degrees of freedom
AIC: 178.01
Number of Fisher Scoring iterations: 5
```

Fit 2 is our reduced model.

Now, we will create a full model with the interaction terms. The interaction terms are as follow:

- 1. age*ejection fraction
- 2. age*serum_creatinine
- 3. age*creatinine_phosphokinase
- 4. age*time

As shown in the screenshot below, the fit3 is our full model which includes all the interaction terms.

```
> summary(fit3)
glm(formula = DEATH_EVENT ~ age + ejection_fraction + serum_creatinine +
    creatinine_phosphokinase + time + sex + age * ejection_fraction +
    age * serum_creatinine + age * creatinine_phosphokinase +
    age * time, family = binomial, data = train)
Deviance Residuals:
   Min
             10 Median
                                30
                                        Max
-2.2044
         -0.5917
                 -0.2782
                            0.4431
                                     2.5982
Coefficients:
                              Estimate Std. Error z value Pr(>|z|)
(Intercept)
                             -3.059e+00 4.466e+00
                                                   -0.685
                                                              0.493
                              1.044e-01
                                        7.643e-02
                                                    1 366
                                                              0.172
age
ejection_fraction
                             -1.010e-01
                                        1.099e-01
                                                    -0.918
                                                              0.358
                              1.550e+00
                                        1.273e+00
serum_creatinine
                                                    1.218
                                                              0.223
                              9.802e-04
creatinine_phosphokinase
                                         7.545e-04
                                                     1.299
                                                              0.194
                                                    0.401
                                                              0.688
                              7.010e-03
                                         1.747e-02
time
                             -6.876e-01
                                         4.235e-01
                                                    -1.624
                                                              0.104
age:ejection_fraction
                                         1.771e-03
                              5.082e-04
                                                    0.287
                                                              0.774
age:serum_creatinine
                             -1.650e-02
                                         2.118e-02
                                                    -0.779
                                                              0.436
                                                   -0.988
                                         1.190e-05
                                                              0.323
age:creatinine_phosphokinase -1.176e-05
                             -4.177e-04 2.864e-04 -1.458
                                                              0.145
age:time
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 260.66 on 206
                                   degrees of freedom
Residual deviance: 160.46 on 196 degrees of freedom
AIC: 182.46
Number of Fisher Scoring iterations: 5
```

Now, we'll be comparing the above two models (fit2 and fit3) using anova and likelihood ratio test.

H0: Reduced model suits best Ha: Full model suits better

```
P-value = 0.4713
=> p < 0.05 (Level of significance)
=> We accept the null hypothesis.
```

Hence, we conclude that the Reduced model suits better than the full model.

Hence, now that we know that the full model with interaction terms has been rejected. So we'll be comparing reduced model by adding interaction terms to it.

Here, we are taking interaction term age*ejection_fraction along with the reduced model. We'll be calling this model as fit4.

```
fit4<-glm(DEATH_EVENT~age+ejection_fraction+serum_creatinine+creatinine_phosphokinase+
 summary(fit4)
Call:
glm(formula = DEATH_EVENT ~ age + ejection_fraction + serum_creatinine +
    creatinine_phosphokinase + time + sex + age * ejection_fraction,
    family = binomial, data = train)
Deviance Residuals:
Min 1Q Median 3Q
-2.0920 -0.6148 -0.2761 0.5316
                                        Max
                                     2.6349
Coefficients:
                         Estimate Std. Error z value Pr(>|z|)
(Intercept)
                        1.0988732 3.8117162
                                               0.288 0.773126
                         0.0319151 0.0632365
                                               0.505 0.613773
age
ejection_fraction
                        -0.0868175 0.1042571
                                               -0.833 0.405000
                                                3.310 0.000934 ***
                         0.5960733 0.1800935
serum_creatinine
                                                1.438 0.150466
creatinine_phosphokinase 0.0002680 0.0001864
                         -0.0185527 0.0032467
-0.6369121 0.4190075
                                                -5.714 1.1e-08 ***
time
                                               -1.520 0.128499
sex1
age:ejection_fraction
                         0.0003536 0.0016815
                                                0.210 0.833467
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 260.66 on 206 degrees of freedom
Residual deviance: 163.96 on 199 degrees of freedom
AIC: 179.96
Number of Fisher Scoring iterations: 5
```

Now, we'll be comparing the above model with reduced model (fit2 and fit4) using anova and likelihood ratio test.

H0: Reduced model suits best

Ha: Reduced model with interaction term age*ejection_fraction suits better

```
P-value = 0.8325
=> p < 0.05 (Level of significance)
=> We accept the null hypothesis.
```

Hence, we conclude that the Reduced model suits better than the Reduced model with interaction term age*ejection_fraction.

Hence, now as we know that the reduced model with interaction term age*ejection_fraction has been rejected. Next we'll be considering Reduced model with interaction term age*serum creatinine. We'll name this model as fit 5.

```
fit5<-glm(DEATH_EVENT~age+ejection_fraction+serum_creatinine+creatinine_phosphokinase+
              time+sex+ age*serum_creatinine,family = binomial,data=train)
  summary(fit5)
Call:
glm(formula = DEATH_EVENT ~ age + ejection_fraction + serum_creatinine +
    creatinine_phosphokinase + time + sex + age * serum_creatinine,
    family = binomial, data = train)
Deviance Residuals:
    Min 1Q Median
                               3Q
                                       Max
         -0.5985 -0.2727
                           0.5326
                                    2.6544
 -2.1279
Coefficients:
                          Estimate Std. Error z value Pr(>|z|)
                        -0.5758366 2.1548112 -0.267 0.789290
(Intercept)
                        0.0613191 0.0360595
                                              1.700 0.089037
age
                       -0.0663851 0.0178163 -3.726 0.000194 ***
ejection_fraction
serum_creatinine 1.2344768 1.2146712
creatinine_phosphokinase 0.0002708 0.0001880
                                              1.016 0.309484
                                               1.440 0.149888
                        time
sex1
                        -0.6390909 0.4190718 -1.525 0.127255
age:serum_creatinine
                        -0.0108135 0.0201113 -0.538 0.590796
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 260.66 on 206 degrees of freedom
Residual deviance: 163.73 on 199 degrees of freedom
AIC: 179.73
Number of Fisher Scoring iterations: 5
```

Now, we'll be comparing the above model with the reduced model (fit2 and fit5) using anova and likelihood ratio test.

H0: Reduced model suits best

Ha: Reduced model with interaction term age*serum_creatinine suits better

```
P-value = 0.5999
=> p < 0.05 (Level of significance)
=> We accept the null hypothesis.
```

Hence, we conclude that the Reduced model suits better than the Reduced model with interaction term age*serum_creatinine.

Hence, now as we know that the reduced model with interaction term age*serum_creatinine. has been rejected. Next we'll be considering a Reduced model with interaction term age*creatinine phosphokinase. We'll name this model as fit 6.

Now, we'll be comparing the above model with the reduced model (fit2 and fit6) using anova and likelihood ratio test.

H0: Reduced model suits best

Ha: Reduced model with interaction term age*creatinine_phosphokinase suits better

```
P-value = 0.4008
=> p < 0.05 (Level of significance)
=> We accept the null hypothesis.
```

Hence, we conclude that the Reduced model suits better than the Reduced model with interaction term age*creatinine phosphokinase.

Hence, now as we know that the reduced model with interaction term age*creatinine_phosphokinase has been rejected. Next we'll be considering a Reduced model with interaction term age*time. We'll name this model as fit 7.

```
Call:
glm(formula = DEATH\_EVENT \sim age + ejection\_fraction + serum\_creatinine +
    creatinine_phosphokinase + time + sex + age * time, family = binomial,
    data = train)
Deviance Residuals:
 Min 1Q Median 3Q
-2.1735 -0.6056 -0.2848 0.4369
                                       2.4815
Coefficients:
                            Estimate Std. Error z value Pr(>|z|)
                          -2.1035982
                                      2.1317829
(Intercept)
                                                 -0.987 0.323751
                           0.0863878
                                      0.0351310
                                                   2.459 0.013932 *
age
ejection_fraction
                                                  -3.757 0.000172 ***
                          -0.0674875
                                      0.0179651
                                                   3.228 0.001247 **
                           0.5743814
                                      0.1779414
serum_creatinine
creatinine_phosphokinase 0.0002874
                                                   1.555 0.119940
                                      0.0001848
                                                  0.414 0.678898
-1.604 0.108754
time
                           0.0072154
                                      0.0174297
sex1
                           -0.6727552
                                       0.4194713
                          -0.0004216 0.0002883
age:time
                                                  -1.462 0.143616
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 260.66 on 206 degrees of freedom
Residual deviance: 161.76 on 199 degrees of freedom AIC: 177.76
Number of Fisher Scoring iterations: 5
```

Now, we'll be comparing the above model with the reduced model (fit2 and fit7) using anova and likelihood ratio test.

H0: Reduced model suits best

Ha: Reduced model with interaction term age*time suits better

```
P-value = 0.1342
=> p < 0.05 (Level of significance)
=> We accept the null hypothesis.
```

Hence, we conclude that the Reduced model suits better than the Reduced model with interaction term age*time.

Hence, after comparing the Reduce Model with the Model with all the interaction terms we finally conclude that our Reduce Model with variables age, creatinine_phosphokinase, ejection_fraction, serum_creatinine, sex and time is best than other ones.

10. Sensitivity ,Specificity And ROC: -

Sensitivity: - Sensitivity is defined as the ability of modal to identify correctly the patients with disease.

Mathematically it is given as: -

$$P(T^{+}|D^{+}) = TP / (TP+FN).$$

Where, **TP**- true positives **FN**-false negatives

True Positives is defined as the patients who were tested with a disease and the modal predicted them having the disease.

Similarly, False negatives is defined as patients who do not have the disease, and the modal classified it not having the disease.

Specificity: - The ability of a test to correctly identify people without disease.

Mathematically, it is given as: -

$$P(T|D) = TN / (TN + FP).$$

where **TN-** True Negative

FP- false positives: - False positive is when the modal test positive for the disease, and the disease is actually not present.

```
> sum(diag(table_mat))/sum(table_mat)
[1] 0.9130435
> 1-sum(diag(table_mat))/sum(table_mat)
[1] 0.08695652
```

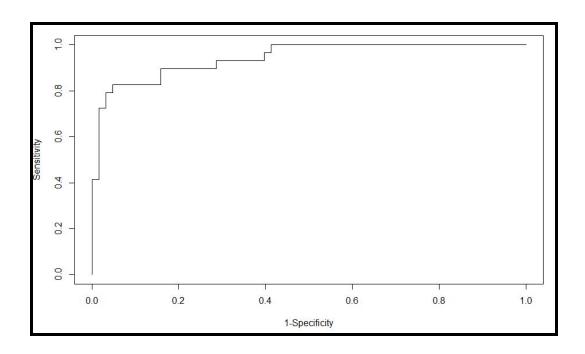
Accuracy:-

Accuracy is defined as the ability of the modal to correctly identify the class of the response variable on the hidden data i.e the test data. The accuracy for the data in the dataset was found out to be 91% which is extremely good.

ROC curve :-

ROC curve describes the trade off between the sensitivity and the specificity of the modal. Classifier with top left corner describes a better performance as the one close to the diagonal which is at 45 degree angle.

As seen from the figure above, the ROC curve is fairly good.



11. Hosmer and Lemeshow Test